

Constraint Satisfaction Problem (CSP)

→ CSP consists of three components
 V, D, C

→ V is the set of variable
 $\{v_1, v_2, \dots, v_n\}$

→ D is the set of Domains one for
 $\{D_1, D_2, \dots, D_n\}$ each variable

→ C is the set of constraints that
allowable combination of values

$C_i = (\text{scope}, \text{relation}) \quad \{C_1, C_2, C_3\}$

where

↳ Scope is the set of variables
that participate in the constraint

↳ Relation is the relation that
defines the values that variable
can take

$$C_1 = (V_1, V_2)$$

rel:

$$V_1 \neq V_2$$

$(1, 2) \quad (2, 4)$

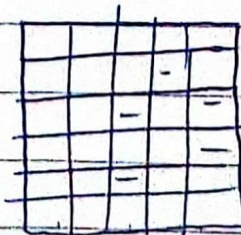
↓

$$C_1 = ((V_1, V_2), (V_1 \neq V_2))$$

$$C_1 = ((V_1, V_2), (1, 2), (1, 4), (2, 4))$$

Summary

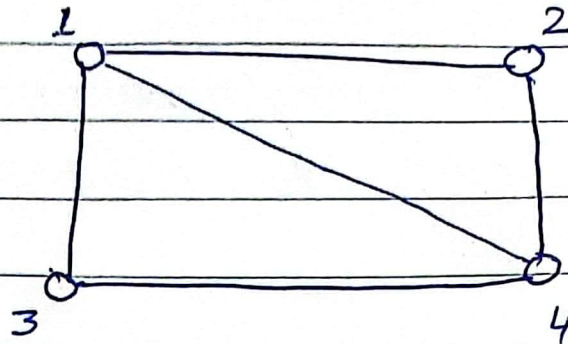
A CSP is a type of problem
in AI where:



"You have to assign values to variables
without breaking any rule (constraints)"

How CSP Algorithm works? NO Date

Backtracking (Intelligent)

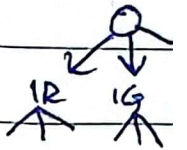


Constraint Graph

$$V = \{1, 2, 3, 4\}$$

$$D = \{Red, Green, Blue\}$$

$$C = \{1 \neq 2, 1 \neq 3, 1 \neq 4, 2 \neq 4, 3 \neq 4\}$$



		1	2	3	4
	Initial Domain	RGB	RGB	RGB	RGB
Forward checking	1 = R	R	GB	GB	GB
Constraint propagation	2 = G	R	G	GB	B
	3 = G	R	G	G	B
Inference ↳ thinking ahead					

It is a time efficient

Real world Examples of CSP

→ sudoku

→ Timetable scheduling

→ Map coloring

Local search in CSP

Instead of trying all combinations (like backtracking), local search starts with a random guess, then keeps changing it slightly to reduce rule violations (conflicts).

Min-Conflicts Heuristic

A smart rule for local search:

Always pick the value for a variable that causes the fewest problems (conflicts)

How it works?

1. Choose a variable that's in conflict
2. Try all possible values
3. Pick one with minimum conflict.

Super fast practice for many CSPs.

Constraint Weighting

When solving CSPs, some constraints are harder to satisfy.

So give them "weights" or importance score.

How it works:

- i) Start with equal weights.
- ii) Everytime a constraint is violated, increase its weight.
- iii) The solver will pay more attention to solving this in future moves.