# Finding the Next NBA Superstar: How to Predict a Player's Performance?

## Hongyu Zhang

What factors determine an excellent basketball player? This is an interesting and significant question that concerns coaches, basketball managers, as well as many basketball fans. For instance, Michael Jordan, the well-known NBA superstar, had 6 NBA Championships and was selected to All Star 14 times<sup>1</sup>. In his career, he scored average 30.1 points per game<sup>2</sup> and was considered to be one of the greatest players in NBA history<sup>3</sup>. Similarly, Kobe Bryant, with 25.0 average points per game, won 5 NBA Championships and was selected to All Star 18 times<sup>4</sup>. Can we find any similarities between these two players that made them superstars in NBA history? Inspired by this intriguing problem, I want to find out whether there is a way to predict a player's performance using a variety of factors. The goal of this study is to construct a statistical model that uses players' statistics to explain his performance in game. Solving this particular problem will give us a clue about the question stated at the beginning: for basketball players, what factors influence their performance?

#### Introduction

The easiest way to evaluate a player's performance is to see how many points in average he scored per game. The higher his average points are, the better the player is. There are only 2 ways to score points in a game: free throw and field goal. Free throws result from a foul in opposing team. In a free throw, a player attempts to score points behind the free throw line without opposed interference<sup>5</sup>. A field goal is "a basket scored on any shot or tap other than a free throw". There are also many other moves in a basketball game, like rebounds, steals, blocks and so on. All of these data are purely numerical and objective, and they can be easily found from the official website of NBA or other sources. My plan is to construct a linear regression model to explain players' average points scored by using players' data like height, weight, field goal scored, free throw scored and so on. I plan to first construct a relatively simple model that fits using few regressors. Then I hope to find the best model from many variables using stepwise search.

## **Data Collection**

I was able to find this dataset online from Cengage<sup>7</sup>. This dataset referred *The official NBA basketball Encyclopedia*, Villard Books, which is an official book that records all NBA players' statistics. The dataset contains 54 players' data in 5 categories: column 1 is **height** (in feet), column 2 is **weight** (in pounds), column 3 is **field** (percent of successful field goals out of 100 attempted), column 4 is **free** (percent of successful free throws out of 100 attempted) and column 5 is **points** (average points scored per game). Here, the response variable is **points**, since it is the variable that I want to predict. I can read the data and extract some useful information about this dataset. Below are the first 6 rows of this dataset and basic summary statistics of these 5 variables.

	> summar	y(points)		
	Min.	1st Qu. Median	Mean 3rd Qu.	Max.
	2.80	8.15 10.75	11.79 13.60	27.40
	> summar	y(height)		
	Min.	1st Qu. Median	Mean 3rd Qu.	Max.
TT 2019(C) 61920 1 0 2019(C) 51936	5.700	6.225 6.650	6.587 6.900	7.600
X1 X2 X3 X4	X5 > summar	y(weight)		
1 6.8 225 0.442 0.672	9.2 Min.	1st Qu. Median	Mean 3rd Qu.	Max.
2 6.3 180 0.435 0.797 1	105 0	185.0 212.5	209.9 235.0	263.0
	> summar	y(field)		
3 6.4 190 0.456 0.761 1	15.8 Min.	1st Qu. Median	Mean 3rd Qu.	Max.
4 6.2 180 0.416 0.651	8.6 0.2910	0.4153 0.4435	0.4491 0.4835	0.5990
5 6.9 205 0.449 0.900 2	> summar	y(free)		
	Min.	1st Qu. Median	Mean 3rd Qu.	Max.
6 6.4 225 0.431 0.780 2	27.4 0.2440	0.7130 0.7535	0.7419 0.7953	0.9000

## **Simple Approach**

First, I need to make sure this model does not have multicollinearity issue. In the design matrix  $\mathbf{X}$ , the first column is column vector 1, and the second column is the percent of successful field goals, and the third column is the percent of successful free throws. Using the eigen function in  $\mathbf{R}$ , I calculate eigenvalues of  $\mathbf{X}^T\mathbf{X}$ :

The condition number of  $X^TX$  is:

$$K = \frac{\lambda_{max}}{\lambda_{min}} = \frac{94.7953878}{0.1344273} = 705.1798$$

This condition number is not very large, which indicates that it is numerically stable to calculate the inverse of  $X^TX$ . I also calculate the result of  $X^TX * (X^TX)^{-1}$ :

$$\begin{bmatrix} 1.000000e^{+00} & 1.199041e^{-14} & 0 \\ 7.105427e^{-15} & 1.000000e^{+00} & 0 \\ 7.105427e^{-15} & -7.327472e^{-15} & 1 \end{bmatrix}$$

We can see that  $X^TX * (X^TX)^{-1}$  is very close to the identity matrix. These evidences show that our design matrix does not have multicollinearity issue. We can then start build the model.

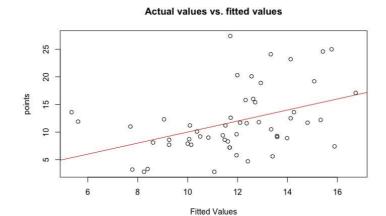
The model can be described as  $\mathbf{y} = \beta_0 + \beta_1 \mathbf{x}_1 + \beta_2 \mathbf{x}_2 + \epsilon$ , where y is the average points scored,  $\mathbf{x}_1$  is the percent of successful field goals, and  $\mathbf{x}_2$  is the percent of successful free throws. In matrix notation, we have:  $\mathbf{y} = \mathbf{X}\boldsymbol{\beta} + \epsilon$ , where y has dimension  $54 \times 1$ , X has dimension  $54 \times 3$ ,  $\boldsymbol{\beta}$  has dimension  $3 \times 1$ , and  $\epsilon$  has dimension  $54 \times 1$ . Using R, I obtain  $\boldsymbol{\beta}$ :

and SS<sub>res</sub> is 1516.422 and  $\widehat{\sigma^2}$  (also MS<sub>res</sub>) is 29.16196. The fitting model becomes:  $\hat{y}=-15.277+35.825x_1+14.799x_2.$ 

The next step is to conduct hypothesis tests about our estimated coefficients. Using R, the p-value for the hypothesis test of  $\beta_1$  being 0 is 0.008606811, and the p-value for the hypothesis test of  $\beta_2$  being 0 is 0.0509969. Because both p-values are relatively small, we do not have enough statistical evidence to support the

null hypotheses. Therefore, we reject the claims that  $\beta_1$  is 0 and  $\beta_2$  is 0, and these two estimated coefficients are statistically significant.

Currently, my model is  $\hat{y} = -15.277 + 35.825x_1 + 14.799x_2$ . To find out whether this model fits the dataset well, we can plot the actual values vs. fitted values graph and add a straight fit line for reference:



In this plot, we observe that roughly most of the points are near around the straight fit line, which indicates that our model fits the dataset well in general. However, some points deviate from the straight fit line very much, and this provides evidence that this model is probably not the best model to fit our data. In the next step, I plan to use the stepwise approach to obtain the best model from these variables.

## **Stepwise Search to Find the Best Model**

Given our dataset, there are 4 possible regressors: **height**, **weight**, **field** (percent of successful field goals) and **free** (percent of successful free throws).

In order to find the best set of variables, we can use the stepwise search approach.

To obtain the best set of variables, we can use forward selection based on Bayesian Information Criterion (BIC). The reason I use BIC is that I want to obtain the best fitting model using fewest variables. BIC is defined by:

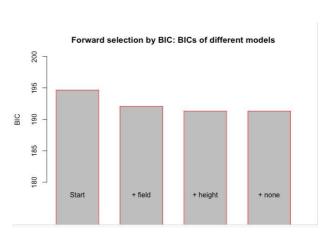
$$BIC = -2logL(\theta B) + Klogn.$$

Compared to Akaike's Information Criterion (AIC) which penalizes the complexity of model by a factor of 2, BIC penalizes the complexity of the model by a factor of *logn*, where n is the sample size. Using R, I do the forward selection process and graph the bar plot of the BICs of different models:

+ weight 1

```
Start: AIC=194.66
points ~ 1
         Df Sum of Sq
                         RSS
+ field 1 211.668 1632.8 192.07
<none>
                      1844.5 194.66
         1 110.580 1733.9 195.31
+ free
+ height 1
              8.758 1835.7 198.39
+ weight 1
                0.179 1844.3 198.65
Step: AIC=192.07
points ~ field
        Df Sum of Sq
                        RSS
                                ATC
+ height 1 137.066 1495.7 191.32
+ free 1 116.375 1516.4 192.06
                      1632.8 192.07
+ weight 1 85.725 1547.1 193.14
Step: AIC=191.32
points ~ field + height
         Df Sum of Sq RSS
               1495.7 191.32
59.978 1435.8 193.10
<none>
+ free
```

0.060 1495.7 195.31



From the forward selection result on the left and the bar plot on the right, we can see that first I start with regressor 1 and the model has BIC 194.66. Then I find out that adding the variable **field** can reduce the BIC to 192.07, so I add **field** to the model. Then I find out that adding the variable **height** can reduce the BIC to 191.32, so I add **height** to the model. In the end, I find out that there is no way to reduce the BIC further by adding more variables, so forward selection ends and the final model I obtain has 2 regressors: **height** and **field**. Our final model is:  $y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \epsilon$ , where y is points,  $x_1$  is height, and  $x_2$  is field.

# **Analysis of Final Model**

In matrix notation, our final model is:  $\mathbf{y} = \mathbf{X}\boldsymbol{\beta} + \boldsymbol{\epsilon}$ , where  $\mathbf{y}$  has dimension  $54 \times 1$ ,  $\mathbf{X}$  has dimension  $54 \times 3$ ,  $\boldsymbol{\beta}$  has dimension  $3 \times 1$ , and  $\boldsymbol{\epsilon}$  has dimension  $54 \times 1$ .

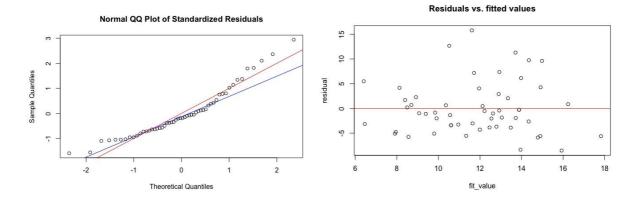
First, I check that  $X^TX$  is not a singular matrix. The result of  $X^TX * (X^TX)^{-1}$ :

$$\begin{bmatrix} 1.000000e^{+00} & 7.105427e^{-15} & -2.842171e^{-14} \\ -2.842171e^{-14} & 1.000000e^{+00} & 0.0000000e^{+00} \\ -6.217249e^{-15} & -5.329071e^{-15} & 1.0000000e^{+00} \end{bmatrix}$$

We can see that  $X^TX * (X^TX)^{-1}$  is very close to the identity matrix. This shows that our design matrix does not have multicollinearity issue. We can start to construct the model. Using R, I obtain  $\beta$ :

and  $SS_{res}$  is 1495.732 and  $\widehat{\sigma^2}$  (also  $MS_{res}$ ) is 28.76407. The fitting model becomes:  $\hat{v}=15.210-4.035x_1+51.562x_2$ .

In order to investigate the normal assumption and homogeneous variance assumption, I plot the normal QQ plot of standardized residues and the residuals vs. fitted values graph:



From the QQ plot, we observe that the blue line (straight line of standardized residuals) is relatively close to the red line (reference line). This indicates that our normal assumption is good. In the residuals vs. fitted values graph, we observe a random scatter of points around the horizontal axis. Therefore, our homogeneity assumption is good. Since the normal assumption and the homogeneity assumption both holds, our final model is valid.

After obtaining the final model, this question arises: Are there any differences in average points scored for players who have the same percent of successful field goals?

To answer this, we can conduct hypothesis tests about our estimated coefficients. Question is equivalent to test whether  $\beta_1$  is 0. Hypothesis testing:  $H_0$ :  $\beta_1 = 0$ ,  $H_1$ :  $\beta_1 \neq 0$ . Using R, the p-value for the hypothesis test of  $\beta_1$  being 0 is 0.03357903. Because the p-value is small (< 0.05), we reject the null hypothesis that  $\beta_1 = 0$ . Therefore, we have statistical evidence to support that there are differences in average points scored for players with the same successful field goal rates.

Using Im function, I can verify my results:

```
> m2 <- lm(points~height+field)
> summary(m2)
Call:
lm(formula = points ~ height + field)
Residuals:
  Min
          1Q Median
                         30
                               Max
-8.527 -3.621 -1.002 2.222 15.789
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
                         10.727
(Intercept)
             15.210
                                 1.418
                                          0.1623
              -4.035
                                          0.0353
height
                         1.866 -2.162
                                          0.0013 **
              51.562
field
                         15.144
                                 3.405
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
Residual standard error: 5.416 on 51 degrees of freedom
Multiple R-squared: 0.1891,
                               Adjusted R-squared: 0.1573
F-statistic: 5.945 on 2 and 51 DF, p-value: 0.004776
```

My results and the results obtained by lm function are almost the same, considering rounding errors. In the summary, we see that the overall F-test for this model is highly statistically significant with p-value 0.004776.

## **Summary & Discussion**

In this project, I first construct a multiple linear regression model of **points** and **field** and **free**. Then, in order to find the best fitting model, I use stepwise search technique to find the final model, which has 2 regressors: **height** and **field**. The final model is:  $\hat{y} = 15.210 - 4.035x_1 + 51.562x_2$ . The mean square error of the final model is 28.76407, which is smaller than the previous model. And the sum of square residuals is 1495.732, which is also smaller than the previous model. These evidences show that the final model is better than the previous model. The forward selection based on BIC also show that this final model is the best fitting model. According to the final model, if player A is 6.3 feet tall and has 45% successful field goals, then his predicted average points scored is approximately 12.99466. If player B is 6.4 feet tall and has 46% successful field goals, then his predicted average points scored is approximately 13.10682. Basketball manager and team coach will probably choose player B instead of player A. This final model provides predictive power so that given a player's statistics, we can predict his average points scored per game.

## References

- 1: Michael Jordan career statistics: https://www.basketballreference.com/players/j/jordami 01.html
- 2: Michael Jordan career statistics: https://www.basketball-reference.com/players/j/jordami01. html
- 3: Fox sports ranking: https://www.foxsports.com/nba/ga llery/ ranking-the-25-greatest-players-innba-history-100716
- 4: Kobe Bryant career statistics: https://www.basketball-reference.com/players/b/bryanko0 1.html
- 5: Free throw definition: https://en.wikipedia.org/wiki/Free\_throw
- 6: Field goal definition: https://en.wikipedia.org/wiki/Field \_goal\_(basketball) 7: Dataset source:
- http://college.cengage.com/mathe matics/brase/understandable\_statis tics/

 $7e/students/datasets/mlr/frames/ml\\r09.html$