

Benchmark results : The boundary sine-Gorden model

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$$\hat{H}_{bsG} = -E_J \cos\left(\frac{\hat{\phi}(0)}{\sqrt{\alpha}}\right) + \hat{H}_T LL : \text{boundary sine Gordon model}$$

- ① $\alpha = 1$ → : transition
- ② $\alpha > 1$ → E_J : irrelevant
- ③ $\alpha < 1$ → E_J : renormalizes to $z=0$

$$\begin{aligned} \text{dc phase mobility} : \mu &\equiv \frac{\alpha}{2\pi} \lim_{\omega \rightarrow +0} \omega \langle \psi \psi \rangle_{\omega} \\ \text{dc phase mobility in transformed frame} : \mu &= \lim_{\omega \rightarrow +0} \sum_{n=0}^{\infty} \omega_{n0} \mu_{n0} \delta(\omega - \omega_{n0}) \end{aligned}$$

$$\begin{aligned} \omega_{n0} &: \text{nth excitation freq.} \\ \mu_{n0} &\equiv \alpha |\langle 0 | \hat{\Xi} | n \rangle|^2 : \text{mobility matrix element (nth energy eigenstate)} \end{aligned}$$

For mobility, :

- ① $\mu \rightarrow 0$, SC Phase , $\alpha > \alpha_c$
- ② $\mu \neq 0$, insulator Phase, $\alpha < \alpha_c$

wilson parameter? (what is this?), critical value : $\alpha_c(\Lambda)$,
Crossover scale $N(\alpha)$,
 $N(\alpha) \propto (\alpha - \alpha_c)^{-1}$
 $\Lambda \rightarrow 1$: locate transition point.

NRG result : consistent with the analytical value $\alpha_c = 1$, in the scaling limit $\epsilon_J = \frac{E_J}{\hbar W} \rightarrow 0$

previous study : Vertical phase boundary : $\alpha_c = 1$, ν is irrelevant.
UV Theory : Large capacitance term, $\nu \gg 1$, low-energy theory may go beyond perturbative regimes, $\nu \rightarrow$ (fixed point)