1 Introduction

1.1 Beamsplitter

$$\begin{split} \hat{c} &= \hat{a}\sqrt{r} + \hat{b}\sqrt{1-r} \\ \hat{d} &= \hat{a}\sqrt{1-r} - \hat{b}\sqrt{r} \\ \hat{a}_H^\dagger \hat{b}_V^\dagger \left| 0 \right\rangle &\to \frac{1}{2} (\hat{c}_H^\dagger \hat{c}_V^\dagger - \hat{c}_H^\dagger \hat{d}_V^\dagger + \hat{d}_H^\dagger \hat{c}_V^\dagger - \hat{d}_H^\dagger \hat{d}_V^\dagger) \left| 0 \right\rangle \\ \hat{a}^\dagger \hat{b}^\dagger \left| 0 \right\rangle &\to \frac{1}{\sqrt{2}} (\left| 2 \right\rangle_c - \left| 2 \right\rangle_d) \end{split}$$

1.2 two-photon interference

$$\begin{split} |\psi\rangle_{in} &= |1\rangle_{a,H} \, |1\rangle_{b,V} = |H\rangle_a \, |V\rangle_b = \hat{a}_H^\dagger \hat{b}_V^\dagger \, |0\rangle \\ & \left|\Psi^+\right\rangle_{ab} \rightarrow (\hat{c}_H^\dagger \hat{c}_V^\dagger - \hat{d}_H^\dagger \hat{d}_V^\dagger) \, |0\rangle \\ & \left|\Psi^-\right\rangle_{ab} \rightarrow (\hat{c}_H^\dagger \hat{d}_V^\dagger - \hat{d}_H^\dagger \hat{c}_V^\dagger) \, |0\rangle \\ & \left|\Phi^\pm\right\rangle_{ab} \rightarrow ((\hat{c}_H^\dagger)^2 \pm (\hat{c}_V^\dagger)^2 - (\hat{d}_H^\dagger)^2 \mp (\hat{d}_V^\dagger)^2) \, |0\rangle \end{split}$$

1.3 time measurement

$$N_c = C(T^2 + R^2)(1 - \frac{2RT}{R^2 + T^2}e^{-(\Delta\omega\delta\tau)^2})$$

2 Application

$$\begin{split} \left|\Psi^{+}\right\rangle_{ab} &\rightarrow \frac{1}{\sqrt{2}}(\left|1\right\rangle_{c,H}\left|1\right\rangle_{c,V} - \left|1\right\rangle_{d,H}\left|1\right\rangle_{d,V}) \\ \left|\Psi^{-}\right\rangle_{ab} &\rightarrow \frac{1}{\sqrt{2}}(\left|1\right\rangle_{c,H}\left|1\right\rangle_{d,V} - \left|1\right\rangle_{d,H}\left|1\right\rangle_{c,V}) \\ \left|\Phi^{\pm}\right\rangle_{ab} &\rightarrow \frac{1}{2}(\left|2\right\rangle_{c,H} \pm \left|2\right\rangle_{c,V} - \left|2\right\rangle_{d,H} \pm \left|2\right\rangle_{d,V}) \\ \left|\psi\right\rangle &= \alpha \left|0\right\rangle + \beta \left|1\right\rangle + \gamma \left|2\right\rangle \\ &\rightarrow \left|\psi'\right\rangle = \alpha \left|0\right\rangle + \beta \left|1\right\rangle - \gamma \left|2\right\rangle \end{split}$$