

# Assignment 2

## Written : Understanding Word2vec

**a.**

–  $\sum_{w \in Vocab} y_w \cdot \log(y_w^{hat}) = -\log(y_0^{hat})$  because  $y_w$  is indeed one-hot coding vector.

**b.**

**i.**

Compute the partial derivative of  $J$  with respect to  $v_c$

$$J_{naive-softmax}(v_c, o, U) = -\log P(O = o | C = c) = -u_0^T v_c + \log\left(\sum_{w \in Vocab} e^{u_w^T v_c}\right)$$

The derivative is :  $-u_0 + \sum u_w \cdot P(O = w | C = c) = U^T \cdot (\hat{y} - y) \quad w \in Vocab$

**ii.**

The derivative is zero when  $\hat{y}$  is close to  $y$

**c.**

- $u_w = u_o$ , the derivative with respect to  $u_w$  is :  $-v_c + P(O = o) \cdot v_c = (P(O = o) - 1) \cdot v_c = [(\hat{y} - y) \cdot y] \cdot v_c$
- $u_w = u_k \neq u_o$ , the derivative with respect to  $u_w$  is :  $P(O = w) \cdot v_c = \hat{y}_k \cdot v_c$

$\hat{y}_k$  is the probability distribution value at the  $k^{th}$  of  $\hat{y}$  for the possibility the context word is  $u_k$

**d.**

The derivative of  $J$  with respect to  $U$  is :

$$[\hat{y}_1.v_c, \hat{y}_2.v_c, (y - \hat{y}).y.v_c, y_{vocab}.v_c]$$

## g. Negative sampling loss

$$J_{neg-sample}(v_c, o, U) = -\log(\sigma(u_o^\top.v_c)) - \sum_{s=1}^K \log(\sigma(-u_{w_s}^\top.v_c))$$

The derivative with respect to  $v_c$  is :  $-u_o.(1 - \delta(u_o^\top.v_c)) + \sum u_{w_s}.(1 - \delta(-u_{w_s}^\top.v_c))$

$\delta$  is the sigmoid function.

The derivative with respect to  $u_o$  is :  $-v_c.(1 - \delta(u_o^\top.v_c))$

The derivative with respect to  $u_{w_s}$  is :  $v_c.(1 - \delta(-u_{w_s}^\top.v_c))$

## h.

$$i. \frac{dJ(v_c, w_{t-m}, \dots, w_{t+m}, U)}{dU} = \sum \frac{dJ(v_c, w_{t+j}, U)}{dU}$$

$$ii. \frac{dJ(v_c, w_{t-m}, \dots, w_{t+m}, U)}{dv_c} = \sum \frac{dJ(v_c, w_{t+j}, U)}{dv_c}$$

$$iii. \frac{dJ(v_c, w_{t-m}, \dots, w_{t+m}, U)}{dv_w} = \sum \frac{dJ(v_c, w_{t+j}, U)}{dv_w} = 0 \text{ with all } v_w \neq v_c$$

## Coding results

- Run with method (loss function) : NaiveSoftmax

iter 39970: 9.776979

iter 39980: 9.813174

iter 39990: 9.854022

iter 40000: 9.812206

→ sanity check: cost at convergence should be around or below 10

→ training took 94730 seconds (40000 iterations)

- Run with method (loss function) : NegSampling  
iter 39950: 9.730395  
iter 39960: 9.721694  
iter 39970: 9.668252  
iter 39980: 9.610189  
iter 39990: 9.573013  
iter 40000: 9.626349  
→ sanity check: cost at convergence should be around or below 10  
→ training took 7519 seconds (35000 → 40000 iterations)