Paxos summary

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This document provides a terse summary of the Basic Paxos (single-decree) consensus protocol as well as Multi-Paxos. It is intended as an accompaniment to a one-hour video lecture introducing Paxos, which was developed as part of a user study comparing Paxos with the Raft consensus algorithm. Multi-Paxos is not specified precisely in the literature; our goal here is to provide a fairly complete specification that stays close to Leslie Lamport's original description of Paxos in "The Part-Time Parliament." The version of Multi-Paxos described here has not been implemented or proven correct.

1 Basics

- proposal number (n) = (round number, server ID)
- \bullet T: a fixed timeout value used in the leader election algorithm
- α : concurrency limit in Multi-Paxos

1.1 Leader election algorithm

- \bullet Every T miliseconds, send an empty heartbeat message to every other server.
- A server acts as leader if it has not received a heartbeat message in the last 2T milliseconds from a server with higher ID.

2 Basic Paxos (Single-decree)

2.1 Persistent state per server

- minProposal: the number of the smallest proposal this server will accept, or 0 if it has never received a Prepare request
- acceptedProposal: the number of the last proposal the server has accepted, or 0 if it never accepted any
- accepted Value: the value from the most recent proposal the server has accepted, or null if it has never accepted a proposal
- maxRound: the largest round number the server has seen

2.2 Messages

2.2.1 Prepare (Phase 1)

Request fields:

• n: a new proposal number

Upon receiving a Prepare request, if $n \ge minProposal$, the acceptor sets minProposal to n. The response constitutes a promise to reject Accept messages with proposal numbers less than n in the future.

Response fields:

- [acceptedProposal: the acceptor's acceptedProposal]
- acceptedValue: the acceptor's acceptedValue

2.2.2 Accept (Phase 2)

Request fields:

- \bullet n: the same proposal number used in Prepare
- v: a value, either the highest numbered one from Prepare responses, or if none, then one from a client request

Upon receiving an Accept request, if $n \ge minProposal$, then:

- Set acceptedProposal = n
- Set acceptedValue = v
- Set minProposal = n

Response fields:

• n: the acceptor's minProposal

2.3 Proposer Algorithm: $write(inputValue) \rightarrow chosenValue$

- 1. Let n be a new proposal number (increment and persist maxRound).
- 2. Broadcast Prepare(n) requests to all acceptors.
- 3. Upon receiving Prepare responses (reply.acceptedProposal, reply.acceptedValue) from a majority of acceptors:
 - Let v be set as follows: if the maximum reply.acceptedProposal in the replies isn't 0, use its corresponding reply.acceptedValue. Otherwise, use inputValue.
- 4. Broadcast Accept(n, v) requests.
- 5. Upon receiving an Accept response with (reply.n):
 - If reply.n > n, set maxRound from n, and start over at step 1.
- 6. Wait until receiving Accept responses for n from a majority of acceptors.
- 7. Return v.

3 Multi-Paxos

3.1 Persistent state per acceptor

Each acceptor stores:

- lastLogIndex: the largest entry for which this server has accepted a proposal
- minProposal: the number of the smallest proposal this server will accept for any log entry, or 0 if it has never received a Prepare request. This applies globally to all entries.

Each acceptor also stores a log, where each log entry $i \in [1, lastLogIndex]$ has the following fields:

- acceptedProposal[i]: the number of the last proposal the server has accepted for this entry, or 0 if it never accepted any, or ∞ if acceptedValue[i] is known to be chosen
- accepted Value[i]: the value in the last proposal the server accepted for this entry, or null if it never accepted any

Define firstUnchosenIndex as the smallest log index i > 0 for which $acceptedProposal[i] < \infty$

3.2 Persistent state per proposer

• maxRound: the largest round number the proposer has seen

3.3 Soft (volatile) state per proposer

(I'm not doing a very strong separation here between the proposer and the acceptor. I allow proposers to both read and write into acceptor state sometimes.)

- nextIndex: the index of the next entry to use for a client request
- prepared: True means there is no need to issue Prepare requests (a majority of acceptors has responded to Prepare requests with noMoreAccepted true); initially false

3.4 Messages

3.4.1 Prepare (Phase 1)

Request fields:

- n: a new proposal number
- index: the log entry that the proposer is requesting information about

Upon receiving a Prepare request, if $request.n \ge minProposal$, the acceptor sets minProposal to request.n. The response constitutes a promise to reject Accept requests (for any log entry) with proposals numbered less than request.n.

Response fields:

- acceptedProposal: the acceptor's acceptedProposal[index]
- acceptedValue: the acceptor's acceptedValue[index]
- noMoreAccepted: set to true if this acceptor has never accepted a value for a log entry with index greater than index

3.4.2 Accept (Phase 2)

Request fields:

- \bullet n: the same proposal number used in the most recent Prepare
- index: identifies a log entry
- v: a value, either the highest numbered one from a Prepare response, or if none, then one from a client request
- firstUnchosenIndex: the sender's firstUnchosenIndex

Upon receiving an Accept request: if $n \ge minProposal$, then:

- Set acceptedProposal[index] = n
- Set acceptedValue[index] = v
- Set minProposal = n

For every index < request.firstUnchosenIndex, if acceptedProposal[index] = n, set acceptedProposal[index] to ∞ .

Response fields:

- \bullet n: the acceptor's minProposal
- ullet first Unchosen Index: the acceptor's first Unchosen Index.

3.4.3 Success (Phase 3)

Request fields:

- *index*: identifies a log entry
- ullet v: the chosen value for entry index

Upon receiving a Success request, set acceptedValue[index] to v and $acceptedProposal[index] = \infty$. Response fields:

 \bullet firstUnchosenIndex: the acceptor's firstUnchosenIndex.

When the sender receives the response, if reply.firstUnchosenIndex < firstUnchosenIndex then the sender sends Success(index = reply.firstUnchosenIndex, value = acceptedValue[reply.firstUnchosenIndex]).

3.5 Proposer Algorithm: $write(inputValue) \rightarrow bool$

- 1. If not leader or not done with leader initialization, return false.
- 2. (If *prepared* is true:)
 - (a) Let index = nextIndex, increment nextIndex.
 - (b) Go to step 6.
- 3. (Let index = firstUnchosenIndex and nextIndex = index + 1.)
- 4. Let n be a new proposal number (increment and persist maxRound)
- 5. Broadcast Prepare(n, index) requests to all acceptors.
- 6. Upon receiving *Prepare* responses (reply.acceptedProposal, reply.acceptedValue, reply.noMoreAccepted) from a majority of acceptors:

- Let v be set as follows: if the maximum reply.acceptedProposal in the replies isn't 0, use its corresponding reply.acceptedValue. Otherwise, use inputValue.
- If all acceptors in the majority responded with reply.noMoreAccepted, set prepared = true.
- 7. Broadcast Accept(index, n, v) requests to all acceptors.
- 8. Upon receiving an Accept response with (reply.n, reply.firstUnchosenIndex):
 - If reply.n > n, set maxRound from reply.n. Set prepared = false. Go to step 1.
 - If $reply.firstUnchosenIndex \leq lastLogIndex$ and $acceptedProposal[reply.firstUnchosenIndex] = \infty$,
 - $then send \ Success (index = reply.firstUnchosenIndex, value = acceptedValue[reply.firstUnchosenIndex]).$
- 9. Upon receiving Accept responses for n from a majority of acceptors:
 - Set $acceptedProposal[index] = \infty$ and acceptedValue[index] = v.
- 10. If v == inputValue, return true.
- 11. Go to step 2.

4 Reconfiguration

- Configuration is a list of ids and addresses of servers, stored as special log entries
- Configuration for choosing entry i determined by latest configuration in log at entry $i \alpha$ or below.
- α limits concurrency: can't choose entry $i + \alpha$ until entry i is chosen