

BBM 101

Introduction to Programming I

Lecture #06 – Arrays and Lists



Last time... Control Flow, Functions



Repeating yourself

```
for f in [30,40,50]:  
    print(f, (f-32)/9.0*5)
```

```
counter = 1  
while counter <= n:  
    s = s + counter  
    counter += 1
```

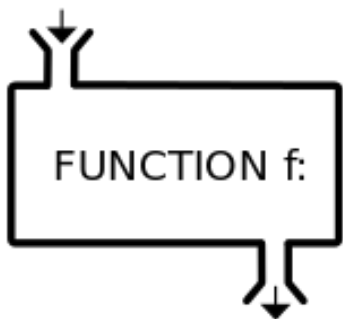


Making decisions

```
if val < 0:  
    result = - val  
else:  
    result = val
```

```
if height > 100:  
    print("space")  
elif height > 50:  
    print("mesosphere")  
elif height > 20:  
    print("stratosphere")  
else:  
    print("troposphere")
```

INPUT x



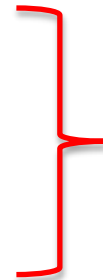
OUTPUT f(x)

Functions

```
def dbl_plus(x):  
    return 2*x + 1
```

Lecture Overview

- Arrays
- Collections
 - Lists
 - Tuples
 - Sets
 - Dictionaries



We will cover these later.

Disclaimer: Much of the material and slides for this lecture were borrowed from
—Ruth Anderson, Michael Ernst and Bill Howe's CSE 140 class

Data Structures

- *A data structure is way of organizing data*
 - Each data structure makes certain operations convenient or efficient
 - Each data structure makes certain operations inconvenient or inefficient
- **Example:** What operations are efficient with:
 - a file cabinet sorted by date?
 - a shoe box?



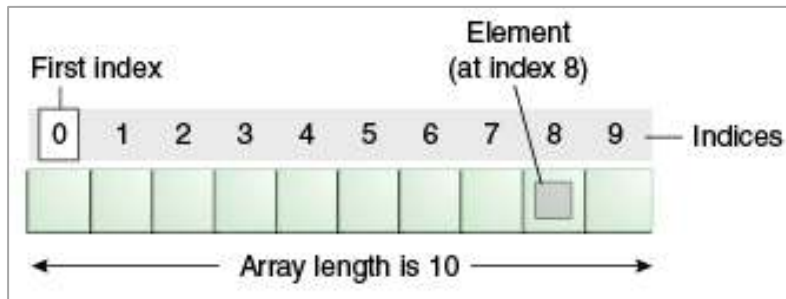
Lecture Overview

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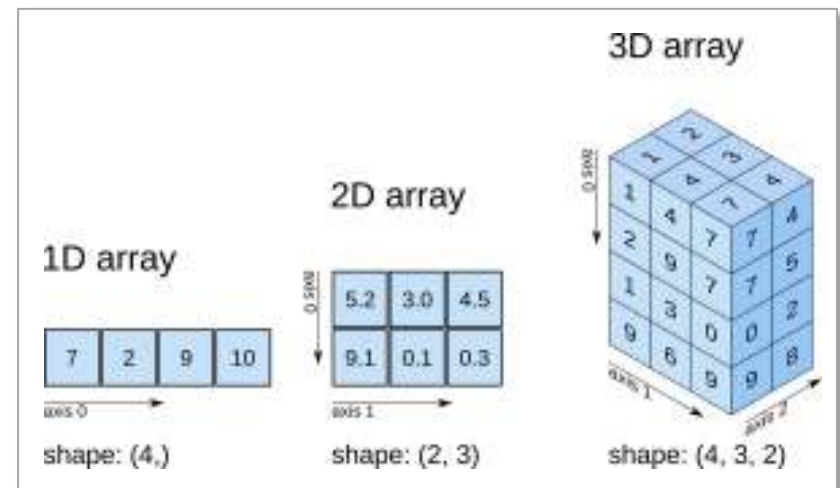
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An Array is ...

- a container which can hold a **fixed** number of items, and these items should be of the **same** type.
 - Each item stored in an array is called an **element**.
 - Each location of an element in an array has a numerical **index**, which is used to identify the element.



Wait for **Understanding Data** lecture
(Week 12) to learn more about arrays.




Lecture Overview

- Arrays
- Collections
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 - Dictionaries

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A Collection Groups Similar Things

- List: ordered
 - Set: unordered, no duplicates
 - Tuple: unmodifiable list
 - Dictionary: maps from values to values
Example: word \rightarrow definition
- 
- A yellow sticky note is attached to a surface with a red eraser. A yellow pencil is resting on the note. The note has some faint, illegible handwriting on it.



Lecture Overview

- Arrays
- Collections
 - Lists
 - Tuples
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 - Dictionaries

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What is a List?

- A list is an ordered sequence of values, where each value is identified by an index.
- What operations should a list support efficiently and conveniently?
 - Creation
 - Querying/Lookup
 - Mutation

List Creation

- Use square brackets to specify a list.
- Separate each element with a comma.

```
a = [3, 4, 5]
```

```
b = [ 5, 3, 'hi' ]
```

```
c = [ 4, 'a', a ]
```

```
d = [ 3, 1, 2*2, 1, 10/2, 10-1 ]
```

```
e = []          # empty list
```



List Creation: Example - 1

```
L = ['I did it all', 4, 'love']
```

```
for i in range(len(L)):  
    print(L[i])
```

```
>> I did it all
```

```
>> 4
```

```
>> love
```

List Creation: Example - 2

```
Techs = ['MIT', 'Caltech']  
Ivys = ['Harvard', 'Yale', 'Brown']  
Univs = [Techs, Ivys]  
Univs1 = [['MIT', 'Caltech'], ['Harvard', 'Yale', 'Brown']]
```

```
print('Univs =', Univs)  
print('Univs1 =', Univs1)  
print(Univs == Univs1)
```

```
>> Univs = [['MIT', 'Caltech'], ['Harvard', 'Yale', 'Brown']]  
>> Univs1 = [['MIT', 'Caltech'], ['Harvard', 'Yale', 'Brown']]  
>> True
```



List Creation: Example - 3

```
def findExtremeDivisors(n1, n2):  
    """Assumes that n1 and n2 are positive ints  
    Returns a list containing the smallest common  
    divisor > 1 and the largest common divisor  
    of n1 and n2"""  
    minVal = None  
    maxVal = None  
  
    for i in range(2, min(n1, n2) + 1):  
        if n1%i == 0 and n2%i == 0:  
            if minVal == None or i < minVal:  
                minVal = i  
            if maxVal == None or i > maxVal:  
                maxVal = i  
    return [[minVal], [maxVal]]
```

The **None** keyword is used to define a null value, or no value at all.

```
extreme_divisors= findExtremeDivisors(100, 200)  
print(extreme_divisors)
```

[[2], [100]]



How to Evaluate a List Expression

- `[a, b, c, d]` → list **creation**
 - To evaluate:
 - evaluate each element to a value, from left to right
 - make a list of the values
 - The elements can be arbitrary values, including lists
 - `["a", 3, 3.14*r*r, fahr_to_cent(-40), [3+4, 5*6]]`

Same tokens “[]”
with two *distinct*
meanings

- `a[b]` → list **indexing** or dereferencing

- To evaluate:
 - evaluate the list expression to a value
 - evaluate the index expression to a value
 - if the list value is not a list, execution terminates with an error
 - if the element is not in range (not a valid index), execution terminates with an error
 - the value is the given element of the list value (counting from **zero**)

List
expression

Index
expression

List Expression Examples

What does this mean (or is it an error)?

```
["four", "score", "and", "seven", "years"][2]
```

```
["four", "score", "and", "seven", "years"][0,2,3]
```

```
["four", "score", "and", "seven", "years"][[0,2,3]]
```

```
["four", "score", "and", "seven", "years"][[0,2,3][1]]
```

List Expression Examples

```
>>> ["four", "score", "and", "seven", "years"][2]  
'and'
```

```
>>> ["four", "score", "and", "seven", "years"][0,2,3]  
TypeError: list indices must be integers or slices, not tuple
```

```
>>> ["four", "score", "and", "seven", "years"][[0,2,3]]  
TypeError: list indices must be integers or slices, not list
```

```
>>> ["four", "score", "and", "seven", "years"][[0,2,3][1]]  
'and'
```

List Lookup

- Extracting part of the list:
 - Single element: `mylist[index]`
 - Sublist (“slicing”): `mylist[startidx : endidx]`
- Find/lookup in a list
 - `x in mylist`
 - Evaluates to a boolean value
 - `mylist.index(x)`
 - Return the int index in the list of the first item whose value is x. It is an error if there is no such item.
 - `list.count(x)`
 - Return the number of times x appears in the list.

List Lookup: Exercise

```
def index(somelist, value):  
    """Return the position of the first occurrence of  
       the element value in the list somelist.  
       Return None if value does not appear in  
       somelist."""  
  
    i = 0  
    for c in somelist:  
        if c == value:  
            return i  
        i = i + 1  
    return None
```

```
gettysburg = ["four", "score", "and",  
              "seven", "years", "ago"]  
index(gettysburg, "and")           # 2  
index(gettysburg, "years")         # 4  
gettysburg.count('seven')         # 1
```

List Mutation

- Insertion
- Removal
- Replacement
- Rearrangement

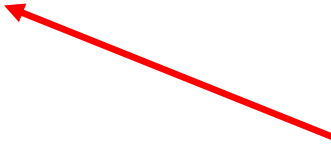
List Insertion

- **`mylist.append(x)`**
 - Extend the list by inserting `x` at the end
- **`mylist.extend(L)`**
 - Extend the list by appending all the items in the argument list
- **`mylist.insert(i, x)`**
 - Insert an item before a given position.
 - `a.insert(0, x)` inserts at the front of the list
 - `a.insert(len(a), x)` is equivalent to `a.append(x)`

List Concatenation using + operator

```
list1 = ["a", "b", "c"]  
list2 = [1, 2, 3]
```

```
list3 = list1 + list2  
print(list3)
```



Not the arithmetic
addition operator

```
["a", "b", "c", 1, 2, 3]
```


List Insertion: Examples

```
def findDivisors (n1, n2):  
    """Assumes that n1 and n2 are positive ints  
    Returns a list containing all common divisors  
    of n1 & n2"""  
    divisors = [] #the empty list  
    for i in range(1, min (n1, n2) + 1):  
        if n1%i == 0 and n2%i == 0:  
            divisors = divisors + [i]  
    return divisors
```

```
divisors = findDivisors(20, 100)  
print(divisors)
```

```
total = 0  
for d in divisors:  
    total += d  
print(total)
```

```
[1, 2, 4, 5, 10, 20]  
42
```



List Insertion: Examples

Python statement

```
>>> list1 = [1, 2, 3]

>>> list1.append(4)

>>> list1.insert(2, 5)

>>> list2 = [10, 20]
>>> list1.extend(list2)

>>> list1.append(list2)
```

Content of list1

```
[1, 2, 3]

[1, 2, 3, 4]

[1, 2, 5, 3, 4]

[1, 2, 5, 3, 4, 10, 20]

[1, 2, 5, 3, 4, 10, 20, [10, 20]]
```

```
>>> list1[7]
[10, 20]
>>> list1[7][0]
10
>>> list1[7][1]
20
```



List Removal

- `list.remove(x)`
 - Remove the first item from the list whose value is `x`
 - It is an error if there is no such item
- `list.pop([i])`
 - Remove the item at the given position in the list, and return it.
 - If no index is specified, `a.pop()` removes and returns the last item in the list.



Notation from the Python Library Reference:

The square brackets around the parameter, “[i]”, means the argument is *optional*. It does *not* mean you should type square brackets at that position.

List Removal - Examples

Python statement

Content of list1

```
>>> list1 = [1, 2, 3]
```

```
[1, 2, 3]
```

```
>>> list1.remove(2)
```

```
[1, 3]
```

```
>>> list2 = list1.copy()
```

```
>>> list1.extend(list2)
```

```
[1, 3, 1, 3]
```

```
>>> list1.remove(3)
```

```
[1, 1, 3]
```

```
>>> list1.pop()
```

```
[1, 1]
```

How can you remove
all occurrences of an
element?

List Replacement

- `mylist[index] = newvalue`
- `mylist[start : end] = newsublist`
 - Can change the length of the list
 - `start` is inclusive, `end` is not
 - `mylist[start : end] = []` *# removes multiple elements*
 - `a[len(a):] = L` *# is equivalent to a.extend(L)*

List Replacement - Examples

Python statement

Content of list1

```
>>> list1 = [1, 2, 3]
```

```
[1, 2, 3]
```

```
>>> list1[len(list1)-1] = 9
```

```
[1, 2, 9]
```

```
>>> list2 = list1
```

```
>>> list1[1:2] = list2
```

```
[1, 1, 2, 9, 9]
```

```
>>> list1[1:3] = list2
```

```
[1, 1, 1, 2, 9, 9, 9, 9]
```

```
>>> list2[3:8] = []
```

```
[1, 1, 1]
```

```
>>> list2 = [5, 6]
```

```
[5, 6]
```



List Slicing

`mylist[startindex : endindex]` evaluates to a **sublist** of the original list

- `mylist[index]` evaluates to an **element** of the original list
- Arguments are like those to the **range** function
 - `mylist[start : end : step]`
 - start index is inclusive, end index is exclusive
 - *All 3 indices are optional*
- Can assign to a slice: `mylist[s : e] = yourlist`

List Slicing: Examples

```
test_list = ['e0', 'e1', 'e2', 'e3', 'e4', 'e5', 'e6']
```

From e2 to the end of the list:

```
test_list[2:]
```

From beginning up to (but not including) e5:

```
test_list[:5]
```

Last element:

```
test_list[-1]
```

Last four elements:

```
test_list[-4:]
```

Everything except last three elements:

```
test_list[:-3]
```

Reverse the list:

```
test_list[::-1]
```

Get a copy of the whole list:

```
test_list[:]
```

List Rearrangement

- **`list.sort()`**
 - Sort the items of the list, **in place**.
 - “**in place**” means by modifying the original list, not by creating a new list.
- **`list.reverse()`**
 - Reverse the elements of the list, **in place**.

Sorting

```
hamlet = "to be or not to be that is the  
question".split()  
  
print("hamlet:", hamlet)  
  
print("sorted(hamlet):", sorted(hamlet))  
  
print("hamlet:", hamlet)  
  
print("hamlet.sort():", hamlet.sort())  
print("hamlet:", hamlet)  
  
print("hamlet.reverse():", hamlet.reverse())  
print("hamlet:", hamlet)
```

Sorting

```
hamlet: ['to', 'be', 'or', 'not', 'to', 'be', 'that', 'is',  
'the', 'question']
```

```
sorted(hamlet): ['be', 'be', 'is', 'not', 'or', 'question',  
'that', 'the', 'to', 'to']
```

```
hamlet: ['to', 'be', 'or', 'not', 'to', 'be', 'that', 'is',  
'the', 'question']
```

```
hamlet.sort(): None
```

```
hamlet: ['be', 'be', 'is', 'not', 'or', 'question', 'that',  
'the', 'to', 'to']
```

```
hamlet.reverse(): None
```

```
hamlet: ['to', 'to', 'the', 'that', 'question', 'or', 'not',  
'is', 'be', 'be']
```

Customizing the Sort Order

Goal: sort a list of names *by last name*

```
names = ["Isaac Newton", "Albert Einstein", "Niels Bohr", "Marie Curie", "Charles Darwin", "Louis Pasteur", "Galileo Galilei", "Margaret Mead"]
```

```
print("names:", names)
```

This does NOT work:

```
print("sorted(names):", sorted(names))
```

When sorting, how should we compare these names?

"Niels Bohr"

"Charles Darwin"

```
sorted(names): ['Albert Einstein', 'Charles Darwin', 'Galileo Galilei', 'Isaac Newton', 'Louis Pasteur', 'Margaret Mead', 'Marie Curie', 'Niels Bohr']
```

Sort Key

A **sort key** is a different value that you use to sort a list, instead of the actual values in the list

```
def last_name(str):  
    return str.split(" ")[1]  
  
print('last_name("Isaac Newton"):',  
last_name("Isaac Newton"))
```

Two ways to use a sort key:

1. Create a new list containing the sort key, and then sort it
2. Pass a key function to the sorted function

1. Use a sort key to create a new list

Create a **different list** that contains the sort key, sort it, then extract the relevant part:

```
names = ["Isaac Newton", "Fred Newton", "Niels Bohr"]
# keyed_names is a list of [lastname, fullname] lists
keyed_names = []
for name in names:
    keyed_names.append([last_name(name), name])
```

1) Create the new list.

Take a look at the list you created, it can now be sorted:

```
print("keyed_names:", keyed_names)
print("sorted(keyed_names):", sorted(keyed_names))
print("sorted(keyed_names, reverse = True):")
print(sorted(keyed_names, reverse = True))
```

sorted_names: ['Isaac Newton', 'Fred Newton', 'Niels Bohr']

(This works because Python compares two elements that are lists *elementwise*.)

```
sorted_keyed_names = sorted(keyed_names, reverse = True)
sorted_names = []
for keyed_name in sorted_keyed_names:
    sorted_names.append(keyed_name[1])
print("sorted_names:", sorted_names)
```

2) Sort the list new list.

3) Extract the relevant part.

1. Use a sort key to create a new list

Create a **different list** that contains the sort key, sort it, then extract the relevant part:

```
names = ["Isaac Newton", "Fred Newton", "Bohr", "Niels Bohr"]
# keyed_names is a list of [last_name, first_name]
keyed_names = []
for name in names:
    keyed_names.append([last_name, first_name])
```

Take a look at the list you created, it can not be sorted directly

```
print("keyed_names:", keyed_names)
print("sorted(keyed_names):", sorted(keyed_names))
print("sorted(keyed_names, reverse = True):")
print(sorted(keyed_names, reverse = True))
```

(This works because Python compares two elements that are lists *elementwise*.)

```
sorted_keyed_names = sorted(keyed_names, reverse = True)
sorted_names = []
for keyed_name in sorted_keyed_names:
    sorted_names.append(keyed_name[1])
print("sorted_names:", sorted_names)
```

keyed_names: [['Newton', 'Isaac Newton'], ['Newton', 'Fred Newton'], ['Bohr', 'Niels Bohr']]

sorted(keyed_names): [['Bohr', 'Niels Bohr'], ['Newton', 'Fred Newton'], ['Newton', 'Isaac Newton']]

sorted(keyed_names, reverse = True): [['Newton', 'Isaac Newton'], ['Newton', 'Fred Newton'], ['Bohr', 'Niels Bohr']]

sorted_names: ['Isaac Newton', 'Fred Newton', 'Niels Bohr']

2) Sort the list new list.

3) Extract the relevant part.

2. Use a sort key as the **key** argument

Supply the **key argument** to the **sorted** function or the **sort** function

```
def last_name(str):  
    return str.split(" ")[1]  
  
names = ["Isaac Newton", "Fred Newton", "Niels Bohr"]  
print("sorted(names, key = last_name):")  
print(sorted(names, key = last_name))  
  
print("sorted(names, key = last_name, reverse = True):")  
print(sorted(names, key = last_name, reverse = True))  
  
print(sorted(names, key = len))  
  
def last_name_len(name):  
    return len(last_name(name))  
  
print(sorted(names, key = last_name_len))
```

2. Use a sort key as the **key** argument

Supply the **key** argument to the **sorted** function or the **sort** function

```
def last_name(str):  
    return str.split(" ")[1]
```

```
names = ["Isaac Newton", "Fred Newton", "Niels Bohr"]  
print("sorted(names, key = last_name):")  
print(sorted(names, key = last_name))
```

```
print("sorted(names, key = last_name, reverse = True):")  
print(sorted(names, key = last_name, reverse = True))
```

```
print(sorted(names, key =
```

```
sorted(names, key = last_name): ['Niels Bohr',  
'Isaac Newton', 'Fred Newton']
```

```
def last_name_len(name):  
    return len(last_name(n
```

```
sorted(names, key = last_name, reverse = True):  
['Isaac Newton', 'Fred Newton', 'Niels Bohr']
```

```
print(sorted(names, key =
```

```
['Niels Bohr', 'Fred Newton', 'Isaac Newton']  
['Niels Bohr', 'Isaac Newton', 'Fred Newton']
```

Sorting: strings vs. numbers

- Sorting the powers of 5:

```
>>> sorted([125, 5, 3125, 625, 25])  
[5, 25, 125, 625, 3125]
```

```
>>> sorted(["125", "5", "3125", "625", "25"])  
['125', '25', '3125', '5', '625']
```

Sorting Algorithms Revisited

3.1 Simple sorts

3.1.1 Insertion sort

3.1.2 Selection sort

3.2 Efficient sorts

3.2.1 Merge sort

3.2.2 Heapsort

3.2.3 Quicksort

3.3 Bubble sort and variants

3.3.1 Bubble sort

3.3.2 Shell sort

3.3.3 Comb sort

3.4 Distribution sort

3.4.1 Counting sort

3.4.2 Bucket sort

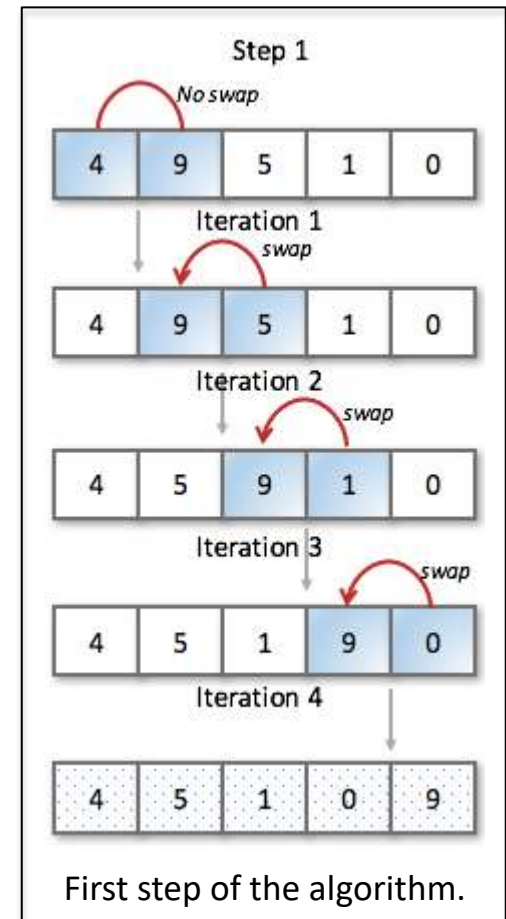
3.4.3 Radix sort



The screenshot shows a web browser window with the URL https://en.wikipedia.org/wiki/Sorting_algorithm. The page features the Wikipedia logo (a globe with symbols) and the text "WIKIPEDIA The Free Encyclopedia". On the left side, there is a sidebar with links: "Main page", "Contents", "Featured content", "Current events", "Random article", "Donate to Wikipedia", and "Wikipedia store". Below these links, there is a section for "Interaction" with a link to "Help". The main content area has tabs for "Article" and "Talk". The article title "Sorting algorithm" is prominently displayed. Below the title, it says "From Wikipedia, the free encyclopedia". The text of the article begins with "A **sorting algorithm** is an **algorithm** that puts elements of a **list** in a cert" and continues with "which require input data to be in sorted lists; it is also often useful for cal". A numbered list follows: "1. The output is in nondecreasing order (each element is no smaller than the previous one)." and "2. The output is a **permutation** (reordering) of the input." Below the list, the text continues: "Further, the data is often taken to be in an **array**, which allows random access." and "Since the dawn of computing, the sorting problem has attracted a great deal of attention. One of the most important comparison sorting algorithms is that they require **linearithmic** time – $O(n \log n)$." The word "linearithmic" is highlighted in blue.

Bubble Sort

- It repeatedly steps through the list to be sorted,
- compares each pair of adjacent items and swaps them if they are in the wrong order.
- The pass through the list is repeated until no swaps are needed, which indicates that the list is sorted.
- The algorithm, which is a comparison sort, is named for the way smaller elements "bubble" to the top of the list.

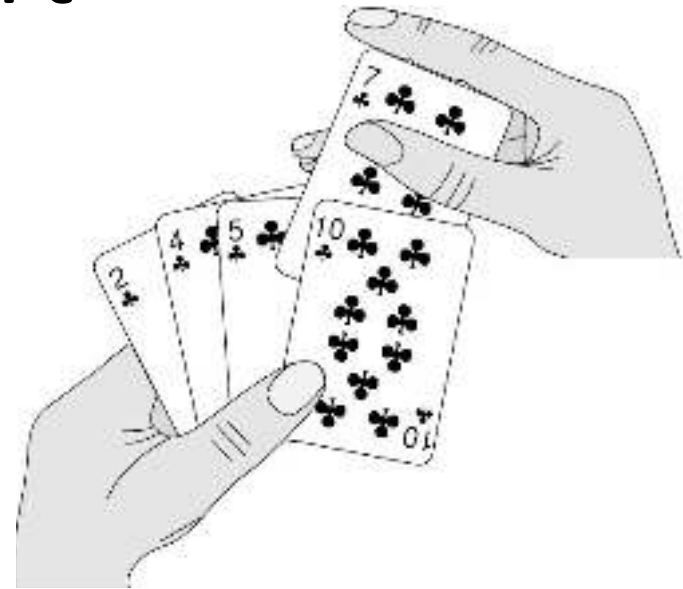
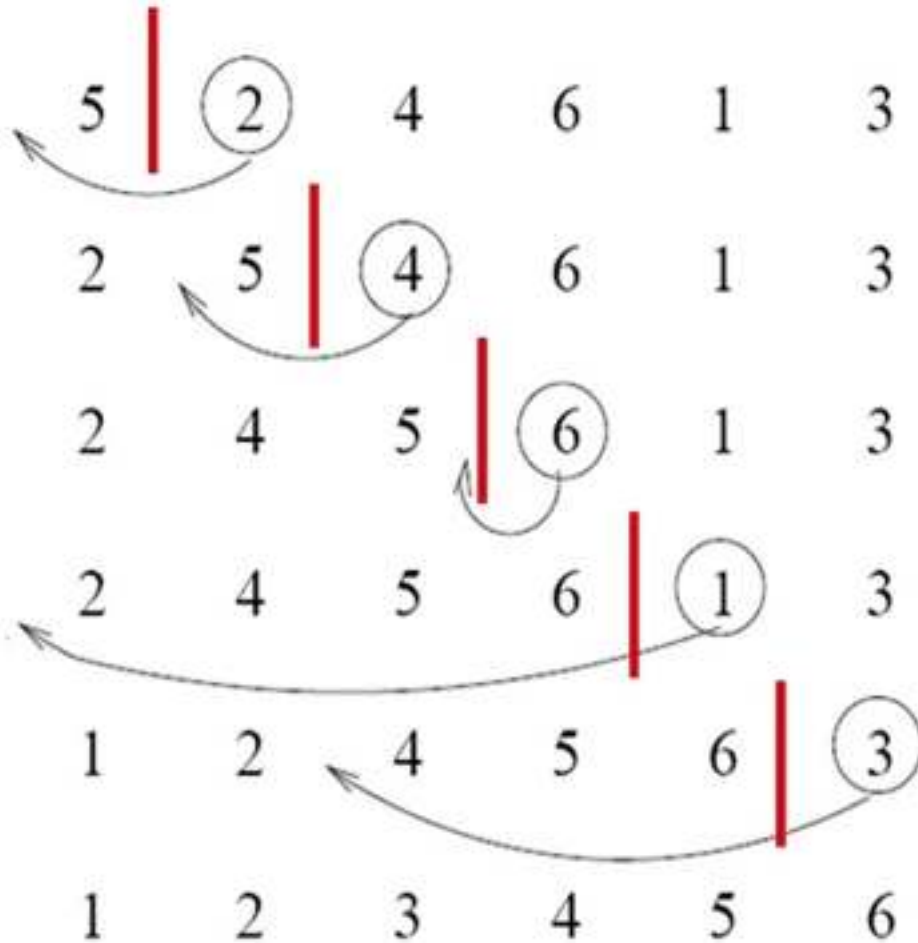


Bubble sort

```
def bubbleSort(alist):  
    for passnum in range(len(alist)-1,0,-1):  
        for i in range(passnum):  
            if alist[i]>alist[i+1]:  
                temp = alist[i]  
                alist[i] = alist[i+1]  
                alist[i+1] = temp  
  
alist = [54,26,93,17,77,31,44,55,20]  
bubbleSort(alist)  
print(alist)
```



Insertion sort



- maintain a sorted sublist in the lower positions of the list.
- Each new item is then “inserted” back into the previous sublist such that the sorted sublist is one item larger.

Done !

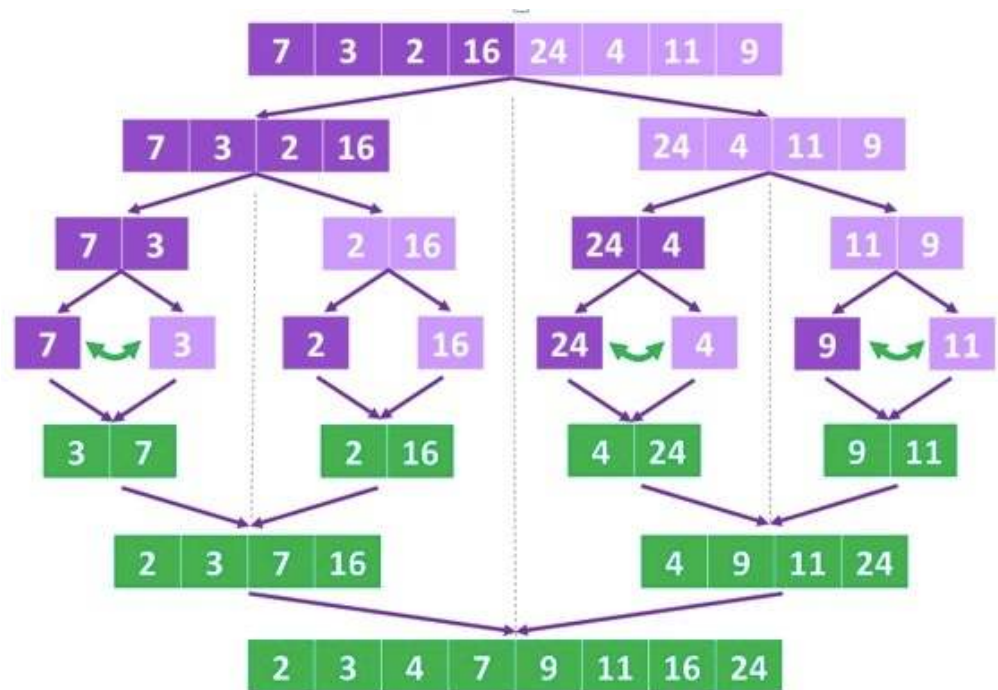
Insertion Sort

```
def insertionSort(alist):  
    for index in range(1,len(alist)):  
        currentvalue = alist[index]  
        position = index  
  
        while position>0 and alist[position-1]>currentvalue:  
            alist[position]=alist[position-1]  
            position = position-1  
  
        alist[position]=currentvalue  
  
alist = [54,26,93,17,77,31,44,55,20]  
insertionSort(alist)  
print(alist)
```



Merge Sort

- Merge sort is a prototypical divide-and-conquer algorithm.
 - Split list into sub-lists in two until you reach pair of value
 - Sort/swap pair of values if needed
 - Merge and sort sub-lists and repeat process until you merge to the full list.



Merge Sort

```
def merge(left, right):  
    result = []  
    (i,j) = (0, 0)  
  
    while i<len(left) and j<len(right):  
        if left[i]<right[j]:  
            result.append(left[i])  
            i = i + 1  
        else:  
            result.append(right[j])  
            j = j + 1  
  
    while i<len(left):  
        result.append(left[i])  
        i = i + 1  
  
    while j<len(right):  
        result.append(right[j])  
        j = j + 1  
  
    return result
```

Merge Sort

Visit this slide later when we learned about recursion.

```
def mergeSort(L) :  
    if len(L)<2:  
        return L[:]  
    else:  
        middle = len(L)//2  
        left = mergeSort(L[:middle])  
        right = mergeSort(L[middle:])  
        return merge(left, right)  
  
a = mergeSort([2,1,3,4,5,-1,8,6,7])
```



Three Ways to Define a List

- Explicitly write out the whole thing:

```
squares = [0, 1, 4, 9, 16, 25, 36, 49]
```

- Write a loop to create it:

```
squares = []  
for i in range(8):  
    squares.append(i*i)
```

- Write a list comprehension:

```
squares = [i*i for i in range(8)]
```

A list comprehension is a concise description of a list

A list comprehension is shorthand for a loop

Two ways to convert Centigrade to Fahrenheit

```
ctemps = [17.1, 22.3, 18.4, 19.1]
```

With a loop:

```
ftemps = []  
for c in ctemps:  
    f = celsius_to_fahrenheit(c)  
    ftemps.append(f)
```

With a list comprehension:

```
ftemps = [celsius_to_fahrenheit(c) for c in ctemps]
```

The comprehension is usually shorter, more readable, and more efficient.

Syntax of a Comprehension

```
[ (x,y) for x in seq1 for y in seq2 if sim(x,y) > threshold ]
```

expression

for clause (required)
assigns value to the
variable x

zero or more
additional
for clauses

zero or more **if** clauses

something
that can be
iterated

Semantics of a comprehension

```
[(x,y) for x in seq1 for y in seq2 if sim(x,y) > threshold]
```

```
result = []  
for x in seq1:  
    for y in seq2:  
        if sim(x,y) > threshold:  
            result.append( (x,y) )  
... use result ...
```


Types of comprehensions

List

```
[ i*2 for i in range(3) ]
```

Set

```
{ i*2 for i in range(3) }
```

Dictionary

```
{ key: value for item in sequence ... }  
{ i: i*2 for i in range(3) }
```

We will learn more
on sets and
dictionaries next
week.

Cubes of the first 10 natural numbers

Goal:

Produce: [0, 1, 8, 27, 64, 125, 216, 343, 512, 729]

With a loop:

```
cubes = []  
for x in range(10):  
    cubes.append(x**3)
```

With a list comprehension:

```
cubes = [x**3 for x in range(10)]
```

Powers of 2, 2^0 through 2^{10}

Goal: [1, 2, 4, 8, 16, 32, 64, 128, 256, 512, 1024]

[2^{i} for i in range(11)]**

Even elements of a list

Goal: Given an input list `nums`, produce a list of the even numbers in `nums`

```
nums = [3, 1, 4, 1, 5, 9, 2, 6, 5]
```

```
⇒ [4, 2, 6]
```

```
[num for num in nums if num % 2 == 0]
```

Dice Rolls

Goal: A list of all possible dice rolls.

With a loop:

```
rolls = []  
for r1 in range(1,7):  
    for r2 in range(1,7):  
        rolls.append((r1,r2))
```

With a list comprehension:

```
rolls = [ (r1,r2) for r1 in range(1,7)  
           for r2 in range(1,7)]
```

All above-average 2-die rolls

Goal: Result list should be a list of 2-tuples:

```
[(2, 6), (3, 5), (3, 6), (4, 4), (4, 5), (4, 6), (5, 3),  
(5, 4), (5, 5), (5, 6), (6, 2), (6, 3), (6, 4), (6, 5), (6, 6)]
```

```
[(r1, r2) for r1 in [1,2,3,4,5,6]  
            for r2 in [1,2,3,4,5,6]  
            if r1 + r2 > 7]
```

OR

```
[(r1, r2) for r1 in range(1, 7)  
            for r2 in range(8-r1, 7)]
```

Making a Matrix

Goal: A matrix where each element is the sum of its row and column numbers.

With a loop:

```
matrix = []
for i in range(5):
    row = []
    for j in range(5):
        row.append(i+j)
    matrix.append(row)
```



0	1	2	3	4
1	2	3	4	5
2	3	4	5	6
3	4	5	6	7
4	5	6	7	8

With a list comprehension:

```
matrix = [[i+j for j in range(5)] for i in range(5)]
```

Function $4x^2 - 4$

With a loop:

```
num_list = []  
for i in range(-10,11):  
    num_list.append(4*i**2 - 4)
```

With a list comprehension:

```
num_list = [4*i**2 - 4 for i in range(-10,11)]
```


Normalize a List

With a loop:

```
num_list = [6,4,2,8,9,10,3,2,1,3]
total = float(sum(num_list))
for i in range(len(num_list)):
    num_list[i] = num_list[i]/float(total)
```

With a list comprehension:

```
num_list = [i/total for i in num_list]
```

Dictionary Mapping Integers to Multiples Under 20

With a loop:

```
for n in range(1,11):
    multiples_list = []
    for i in range(1,21):
        if i%n == 0:
            multiples_list.append(i)
    multiples[n] = multiples_list
```

With a dictionary comprehension:

```
multiples = {n:[i for i in range(1,21) if i%n == 0]
for n in range(1,11) }
```

Revisit this slide
next week.

```
{1: [1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14,
15, 16, 17, 18, 19, 20], 2: [2, 4, 6, 8, 10, 12, 14,
16, 18, 20], 3: [3, 6, 9, 12, 15, 18], 4: [4, 8, 12,
16, 20], 5: [5, 10, 15, 20], 6: [6, 12, 18], 7: [7,
14], 8: [8, 16], 9: [9, 18], 10: [10, 20]}
```

A Word of Caution

List comprehensions are great, but they can get confusing.
Error on the side of readability.

```
nums = [n for n in range(100) if  
        sum([int(j) for j in str(n)]) % 7 == 0]
```

```
nums = []  
for n in range(100):  
    digit_sum = sum([int(j) for j in str(n)])  
    if digit_sum % 7 == 0:  
        nums.append(n)
```

Ternary Assignment

A common pattern in python

```
if x > threshold:  
    flag = True  
else:  
    flag = False
```

Or

```
flag = False  
if x > threshold:  
    flag = True
```

Ternary Assignment

A common pattern in python


```
if x > threshold:  
    flag = True  
else:  
    flag = False
```

```
flag = True if x > threshold else False
```

Ternary Expression
Three elements

Ternary Assignment

`flag = True if x > threshold else False`



Result if true Condition Result if false

- Only works for single expressions as results.
- Only works for if and else (no elif)

Ternary Assignment

Goal: A list of 'odd' or 'even' if that index is odd or even.

```
the_list = []
for i in range(16):
    if i%2 == 0:
        the_list.append('even')
    else:
        the_list.append('odd')
```

```
the_list = []
for i in range(16):
    the_list.append('even' if i%2 == 0 else 'odd')
```

```
the_list = ['even' if i%2 == 0 else 'odd' for i in range(16)]
```

Next time... Tuples, Sets, and Dictionaries

Tuples

```
t1 = ()  
t2 = (1, 'two', 3)  
print(t1)  
print(t2)
```

```
>> ()  
>> (1, 'two', 3)
```

Sets

```
odd = set([1, 3, 5])  
prime = set([2, 3, 5])  
empty = set([])
```

Dictionaries

