

1

$$(a) \quad t_{avg} = h * t_c + (1-h) * t_m$$

$$= (0.9 * 100) + (0.1) (1000) = 190 \text{ ns}$$

$$(b) \quad t_{avg} = h * t_c + (1-h) \left(\frac{8}{2} * t_m + \frac{8}{2} * t_m + t_c \right)$$

$$= 0.9 (100) + (0.1) \left(\frac{8}{1} * 1000 + 8 * 1000 + 100 \right)$$

$$= 1700 \text{ ns}$$

$$(c) \quad \text{Op \#1: } t_{avg} = 0.9 (100) + 0.1 (8 * 500 + 8 * 500 + 100)$$

$$= 900 \text{ ns}$$

$$\text{Speedup} = \frac{1100}{900} = 1.22$$

$$\frac{\text{Cost}}{\text{Speedup}} = \frac{x}{1.22}$$

$$\text{Op \#2: } t_{avg} = (0.9) (100) + 0.1 \left(\frac{8}{4} * 1000 + \frac{8}{4} * 1000 + 100 \right) = 500 \text{ ns}$$

$$\text{Speedup} = \frac{1100}{500} = 2.20$$

$$\frac{\text{Cost}}{\text{Speedup}} = \frac{x}{2.20}$$

→ option 2 is better because it yields more speedup for the same cost. $\frac{\text{Cost}}{\text{Speedup}}$ is lower

$$2) \text{ (a) Total Read Hit Time} = (1-w) \cdot t_c$$

$$\text{(b) Total Write Hit Time} = w \cdot t_m$$

$$\text{(c) Total Read Miss Penalty} = (1-w) \left(\frac{B}{c} \cdot t_m + t_c \right)$$

$$\text{(d) Total Write Miss Penalty} = w \cdot t_m$$

$$3) \text{ (a) } t_{avg} = .9(100) + .1(1000) = 190 \text{ ns}$$

$$\text{(b) } t_{avg} = .9(100) + .1 \left(\left(\frac{8}{2} \right) (1000) + \left(\frac{8}{2} \right) (1000) + 100 \right) = 900 \text{ ns}$$

$$\begin{aligned} \text{(c) } t_{avg} &= h(t_c) + (1-h) \left[w(t_m) + (1-w) \left(\left(\frac{B}{c} \right) (t_m) + \left(\frac{B}{c} \right) (t_m) + t_c \right) \right] \\ &= .9(100) + .1 \left[.3(1000) + .7 \left(\left(\frac{8}{2} \right) (1000) + \left(\frac{8}{2} \right) (1000) + 100 \right) \right] \\ &= 687 \end{aligned}$$

$$4) \text{ (a) } t_{avg} = .95(100) + .05(1000) = 145 \text{ ns}$$

$$\text{(b) } t_{avg} = .95(100) + .05 \left(\left(\left(\frac{8}{4} \right) (1000) \right) (2) + 100 \right) = 300 \text{ ns}$$

$$\begin{aligned} \text{(c) } t_{avg} &= h(t_c) + (1-h) \left(w(t_m) + (1-w) \left((2) \left(\frac{B}{c} \right) (t_m) + t_c \right) \right) \\ &= .95(100) + .05 \left[0.25(1000) + 0.75 \left((2) \left(\frac{8}{4} \right) (1000) + 100 \right) \right] \\ &= 261.25 \text{ ns} \end{aligned}$$

$$\begin{aligned} \text{(d) } t_{avg} &= h(w(t_m) + (1-w)(t_c)) + (1-h) \left(w(t_m) + (1-w) \left(\frac{B}{c} (t_m) + t_c \right) \right) \\ &= .95 \left(.25(1000) + .75(100) \right) + .05 \left(0.25(1000) + .75 \left(\frac{8}{4} (1000) + 100 \right) \right) \\ &= 400 \text{ ns} \end{aligned}$$