



Chapter 8: Relational Database Design

Database System Concepts, 6th Ed.

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Features of Good Relational Design

- In general, the goal of relational database design is to generate a set of relation schemas that allows us to store information without unnecessary redundancy, yet also allows us to retrieve information easily. This is accomplished by designing schemas that are in an appropriate normal form.
- It is possible to generate a set of relation schemas directly from the E-R design. Obviously, the goodness (or badness) of the resulting set of schemas depends on how good the E-R design was in the first place.



Schema For The University Database

- classroom(building, room number, capacity)
- department(dept_name, building, budget)
- course(course_id, title, dept_name, credits)
- instructor (ID, name, dept_name, salary)
- section(course_id, sec_id, semester, year, building, room_number, time_slot_id)
- teaches(ID, course_id, sec_id, semester, year)
- student(ID, name, dept_name, tot_cred)
- takes(ID, course_id, sec_id, semester, year, grade)
- advisor(s_ID, i_ID)
- time slot(time_slot_id, day, start_time, end_time)
- prereq(course_id, prereq_id)



Design Alternative: Larger Schemas

- Suppose we combine *instructor* and *department* into *inst_dept*
 - (No connection to relationship set *inst_dept*)
- Result is possible repetition of information

| <i>ID</i> | <i>name</i> | <i>salary</i> | <i>dept_name</i> | <i>building</i> | <i>budget</i> |
|-----------|-------------|---------------|------------------|-----------------|---------------|
| 22222 | Einstein | 95000 | Physics | Watson | 70000 |
| 12121 | Wu | 90000 | Finance | Painter | 120000 |
| 32343 | El Said | 60000 | History | Painter | 50000 |
| 45565 | Katz | 75000 | Comp. Sci. | Taylor | 100000 |
| 98345 | Kim | 80000 | Elec. Eng. | Taylor | 85000 |
| 76766 | Crick | 72000 | Biology | Watson | 90000 |
| 10101 | Srinivasan | 65000 | Comp. Sci. | Taylor | 100000 |
| 58583 | Califieri | 62000 | History | Painter | 50000 |
| 83821 | Brandt | 92000 | Comp. Sci. | Taylor | 100000 |
| 15151 | Mozart | 40000 | Music | Packard | 80000 |
| 33456 | Gold | 87000 | Physics | Watson | 70000 |
| 76543 | Singh | 80000 | Finance | Painter | 120000 |



A Combined Schema Without Repetition

- Consider combining relations
 - *sec_class(sec_id, building, room_number)* and
 - *section(course_id, sec_id, semester, year)*
- into one relation
 - *section(course_id, sec_id, semester, year, building, room_number)*
- No repetition in this case

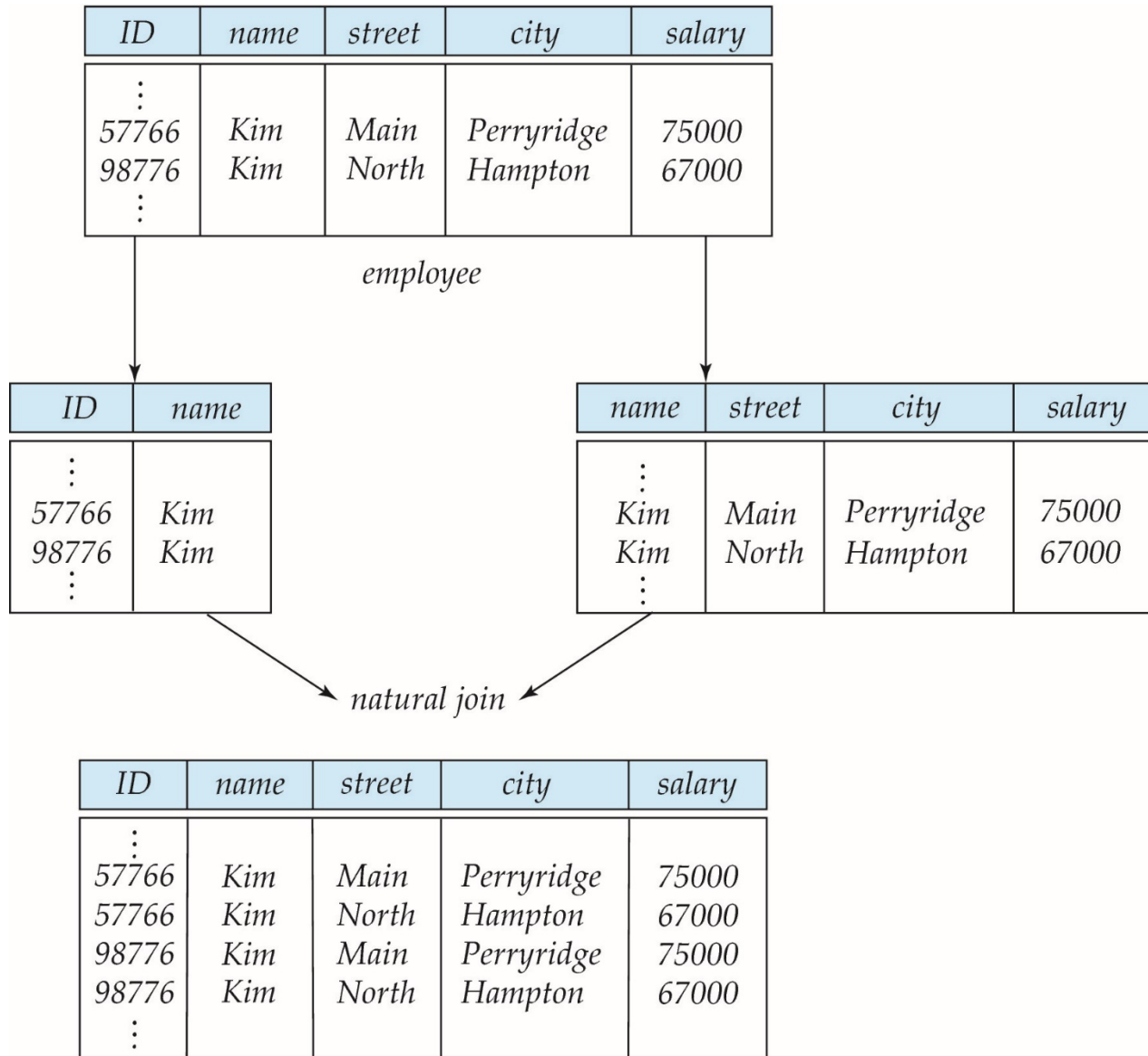


What About Smaller Schemas?

- Suppose we had started with *inst_dept*. How would we know to split up (**decompose**) it into *instructor* and *department*?
- Write a rule “if there were a schema (*dept_name*, *building*, *budget*), then *dept_name* would be a candidate key”
- Denote as a **functional dependency**:
$$dept_name \rightarrow building, budget$$
- In *inst_dept*, because *dept_name* is not a candidate key, the building and budget of a department may have to be repeated.
 - This indicates the need to decompose *inst_dept*
- Not all decompositions are good. Suppose we decompose *employee*(*ID*, *name*, *street*, *city*, *salary*) into
employee1 (*ID*, *name*)
employee2 (*name*, *street*, *city*, *salary*)
- The next slide shows how we lose information -- we cannot reconstruct the original *employee* relation -- and so, this is a **lossy decomposition**.



A Lossy Decomposition





Example of Lossless-Join Decomposition

- **Lossless join decomposition**
- Decomposition of $R = (A, B, C)$
 $R_1 = (A, B)$ $R_2 = (B, C)$

| A | B | C |
|----------|-----|-----|
| α | 1 | A |
| β | 2 | B |

r

| A | B |
|----------|-----|
| α | 1 |
| β | 2 |

$\Pi_{A,B}(r)$

| B | C |
|-----|-----|
| 1 | A |
| 2 | B |

$\Pi_{B,C}(r)$

$\Pi_A(r) \bowtie \Pi_B(r)$

| A | B | C |
|----------|-----|-----|
| α | 1 | A |
| β | 2 | B |



Data Normalization

- Primarily a tool to validate and improve a logical design so that it satisfies certain constraints that avoid unnecessary duplication of data
- The process of decomposing relations with anomalies to produce smaller, well-structured relations
- **Results of Normalization**
- Removes the following modification anomalies (integrity errors) with the database
 - Insertion
 - Deletion
 - Update



ANOMALIES

- Insertion

- inserting one fact in the database requires knowledge of other facts unrelated to the fact being inserted

- Deletion

- Deleting one fact from the database causes loss of other unrelated data from the database

- Update

- Updating the values of one fact requires multiple changes to the database



ANOMALIES EXAMPLES

TABLE: COURSE

| <u>COURSE#</u> | <u>SECTION#</u> | C_NAME |
|----------------|-----------------|-----------------|
| CIS564 | 072 | Database Design |
| CIS564 | 073 | Database Design |
| CIS570 | 072 | Oracle Forms |
| CIS564 | 074 | Database Design |
| | | |



ANOMALIES EXAMPLES

Insertion:

Suppose our university has approved a new course called CIS563:
SQL & PL/SQL.

| <u>COURSE#</u> | <u>SECTION#</u> | C_NAME |
|----------------|-----------------|-----------------|
| CIS564 | 072 | Database Design |
| CIS564 | 073 | Database Design |
| CIS570 | 072 | Oracle Forms |
| CIS564 | 074 | Database Design |
| | | |



ANOMALIES EXAMPLES

Deletion:

Suppose not enough students enrolled for the course CIS570 which had only one section 072. So, the school decided to drop this section and delete the section# 072 for CIS570 from the table COURSE. But then, what other relevant info also got deleted in the process?

| <u>COURSE#</u> | <u>SECTION#</u> | C_NAME |
|----------------|-----------------|-----------------|
| CIS564 | 072 | Database Design |
| CIS564 | 073 | Database Design |
| CIS570 | 072 | Oracle Forms |
| CIS564 | 074 | Database Design |
| | | |



ANOMALIES EXAMPLES

Update:

Suppose the course name (C_Name) for CIS 564 got changed to Database Management. How many times do you have to make this change in the COURSE table in its current form?

| <u>COURSE#</u> | <u>SECTION#</u> | C_NAME |
|----------------|-----------------|-----------------|
| CIS564 | 072 | Database Design |
| CIS564 | 073 | Database Design |
| CIS570 | 072 | Oracle Forms |
| CIS564 | 074 | Database Design |
| | | |

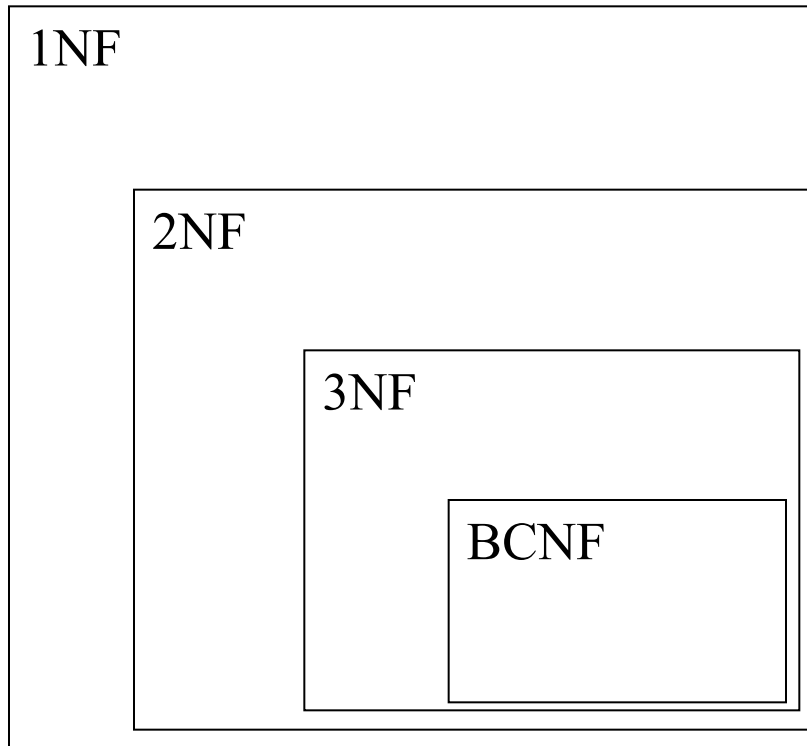


ANOMALIES

- So, a table (relation) is a stable (‘good’) table only if it is free from any of these anomalies at any point in time.
- You have to ensure that each and every table in a database is always free from these modification anomalies. And, how do you ensure that?
- ‘Normalization’ theory helps.



Normalization



a relation in BCNF, is also in 3NF

a relation in 3NF is also in 2NF

a relation in 2NF is also in 1NF



Normalization

We consider a relation in BCNF to be fully normalized.

The benefit of higher normal forms is that update semantics for the affected data are simplified. This means that applications required to maintain the database are simpler.

A design that has a lower normal form than another design has more redundancy. Uncontrolled redundancy can lead to data integrity problems.

First we introduce the concept of *functional dependency*



Functional Dependencies

Functional Dependencies

We say an attribute, B, has a *functional dependency* on another attribute, A, if for any two records, which have the same value for A, then the values for B in these two records must be the same. We illustrate this as:

$A \twoheadrightarrow B$

Example: Suppose we keep track of employee email addresses, and we only track one email address for each employee. Suppose each employee is identified by their unique employee number. We say there is a functional dependency of email address on employee number:

employee number \twoheadrightarrow email address



Functional Dependencies

| <u>EmpNum</u> | EmpEmail | EmpFname | EmpLname |
|---------------|----------------|----------|----------|
| <u>m</u> 123 | jdoe@abc.com | e Joh | e Do |
| 456 | psmith@abc.com | Peter | Smith |
| 555 | alee1@abc.com | Ala | Lee |
| 633 | pdoe@abc.com | Peter | Do |
| 787 | alee2@abc.com | Ala | Lee |

n

If EmpNum is the PK then the FDs:

EmpNum \twoheadrightarrow EmpEmail

EmpNum \twoheadrightarrow EmpFname

EmpNum \twoheadrightarrow EmpLname

must exist.



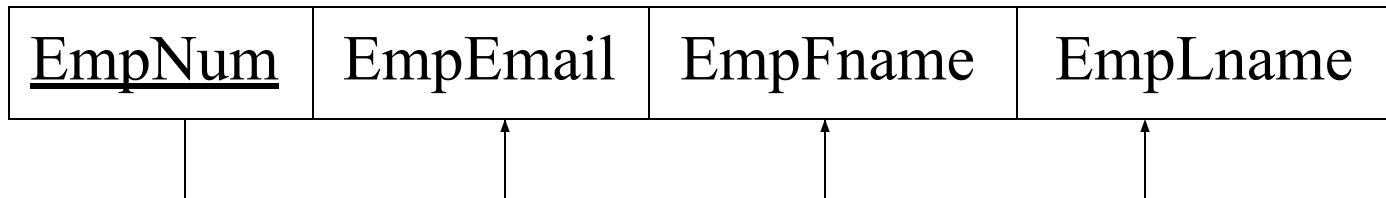
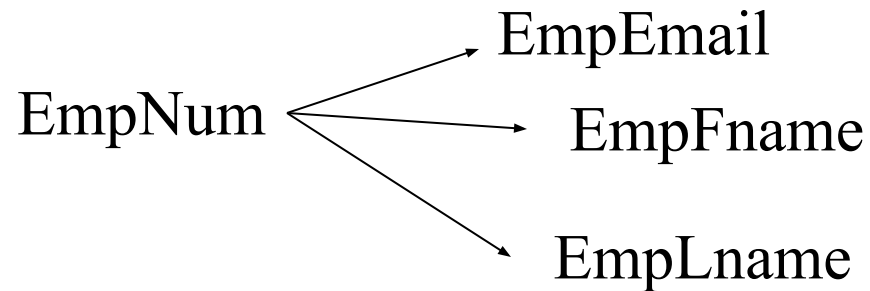
Functional Dependencies

EmpNum \square EmpEmail

EmpNum \square EmpFname

EmpNum \square EmpLname

*3 different ways
you might see FDs
depicted*





Determinant

Functional Dependency

EmpNum \square EmpEmail

Attribute on the LHS is known as the *determinant*

- EmpNum is a determinant of EmpEmail



Transitive dependency

Consider attributes A, B, and C, and where

$A \twoheadrightarrow B$ and $B \twoheadrightarrow C$.

Functional dependencies are transitive, which means that we also have the functional dependency

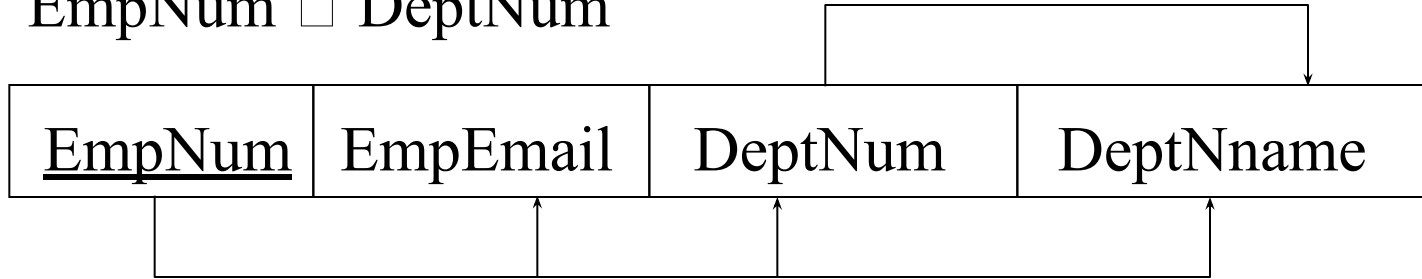
$A \twoheadrightarrow C$

We say that C is transitively dependent on A through B.

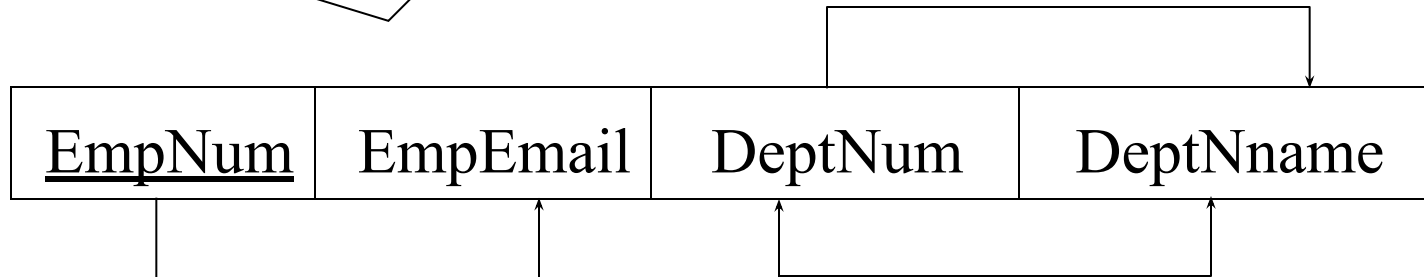
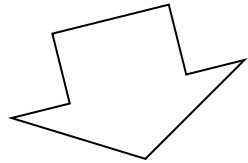


Transitive dependency

EmpNum \square DeptNum



DeptNum \square DeptName



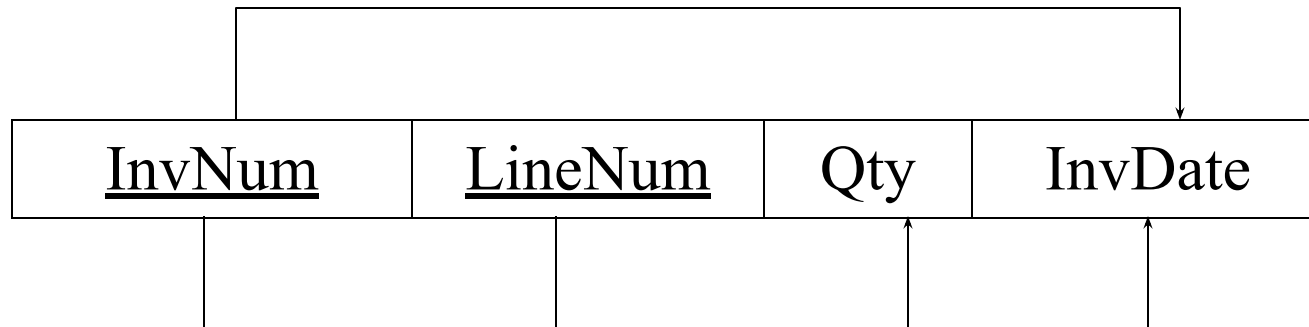
DeptName is *transitively dependent* on EmpNum via DeptNum

EmpNum \square DeptName



Partial dependency

A **partial dependency** exists when an attribute B is functionally dependent on an attribute A, and A is a component of a multipart candidate key.



Candidate keys: {InvNum, LineNum} InvDate is *partially dependent* on {InvNum, LineNum} as **InvNum is a determinant of InvDate and InvNum is part of a candidate key**



Closure of a Set of Functional Dependencies

- Given a set F of functional dependencies, there are certain other functional dependencies that are logically implied by F .
 - For example: If $A \rightarrow B$ and $B \rightarrow C$, then we can infer that $A \rightarrow C$
- The set of **all** functional dependencies logically implied by F is the **closure** of F . We denote the *closure* of F by F^+ . F^+ is a superset of F .
- Candidate Key Example:
 - $FD1: A \rightarrow B, B \rightarrow C, C \rightarrow D$
 - $FD2: A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A$
 - $FD3: A \rightarrow B, BC \rightarrow D, E \rightarrow C, D \rightarrow A$
- Prime Attribute VS Non-Prime Attribute



Closure of a Set of Functional Dependencies

- Given a set F set of functional dependencies, there are certain other functional dependencies that are logically implied by F .
 - For e.g.: If $A \rightarrow B$ and $B \rightarrow C$, then we can infer that $A \rightarrow C$
- The set of **all** functional dependencies logically implied by F is the **closure** of F .
- We denote the *closure* of F by F^+ .



Closure of a Set of Functional Dependencies

- We can find F^+ , the closure of F , by repeatedly applying Armstrong's Axioms:
 - if $\beta \subseteq \alpha$, then $\alpha \rightarrow \beta$ (**reflexivity**)
 - if $\alpha \rightarrow \beta$, then $\gamma \alpha \rightarrow \gamma \beta$ (**augmentation**)
 - if $\alpha \rightarrow \beta$, and $\beta \rightarrow \gamma$, then $\alpha \rightarrow \gamma$ (**transitivity**)
- These rules are
 - **sound** (generate only functional dependencies that actually hold), and
 - **complete** (generate all functional dependencies that hold).



Example

- $R = (A, B, C, G, H, I)$
 $F = \{ A \rightarrow B$
 $A \rightarrow C$
 $CG \rightarrow H$
 $CG \rightarrow I$
 $B \rightarrow H \}$
- some members of F^+
 - $A \rightarrow H$
 4 by transitivity from $A \rightarrow B$ and $B \rightarrow H$
 - $AG \rightarrow I$
 4 by augmenting $A \rightarrow C$ with G , to get $AG \rightarrow CG$
 and then transitivity with $CG \rightarrow I$
 - $CG \rightarrow HI$
 4 by augmenting $CG \rightarrow I$ to infer $CG \rightarrow CGI$,
 and augmenting of $CG \rightarrow H$ to infer $CGI \rightarrow HI$,
 and then transitivity



Closure of Functional Dependencies (Cont.)

- Additional rules:
 - If $\alpha \rightarrow \beta$ holds and $\alpha \rightarrow \gamma$ holds, then $\alpha \rightarrow \beta \gamma$ holds (union)
 - If $\alpha \rightarrow \beta \gamma$ holds, then $\alpha \rightarrow \beta$ holds and $\alpha \rightarrow \gamma$ holds (decomposition)
 - If $\alpha \rightarrow \beta$ holds and $\gamma \beta \rightarrow \delta$ holds, then $\alpha \gamma \rightarrow \delta$ holds (pseudotransitivity)

The above rules can be inferred from Armstrong's axioms.



Example of Attribute Set Closure

- $R = (A, B, C, G, H, I)$
- $F = \{A \rightarrow B$
 $A \rightarrow C$
 $CG \rightarrow H$
 $CG \rightarrow I$
 $B \rightarrow H\}$
- $(AG)^+$
 1. $result = AG$
 2. $result = ABCG$ ($A \rightarrow C$ and $A \rightarrow B$)
 3. $result = ABCGH$ ($CG \rightarrow H$ and $CG \subseteq AGBC$)
 4. $result = ABCGHI$ ($CG \rightarrow I$ and $CG \subseteq AGBCH$)
- Is AG a candidate key?
 1. Is AG a super key?
 1. Does $AG \rightarrow R?$ == Is $(AG)^+ \supseteq R$
 2. Is any subset of AG a superkey?
 1. Does $A \rightarrow R?$ == Is $(A)^+ \supseteq R$
 2. Does $G \rightarrow R?$ == Is $(G)^+ \supseteq R$



Closure of a Set of Functional Dependencies

$R(ABCDEF)$

$FD\{ C \rightarrow F, E \rightarrow A, EC \rightarrow D, A \rightarrow B\}$

$CK=\{EC\}$

$PA=\{E,C\}$

$NPA=\{A,B,D,F\}$



First Normal Form

First Normal Form

We say a relation is in **1NF** if all values stored in the relation are single-valued and atomic.

1NF places restrictions on the structure of relations.
Values must be simple.



First Normal Form

The following is **not** in 1NF

| <u>EmpNu</u> | EmpPhon | EmpDegrees |
|--------------|-----------|-------------------------|
| m 123 | e233-9876 | |
| 333 | 233-1231 | BA, BSc, |
| 679 | 233-1231 | BSc , MSc |

EmpDegrees is a multi-valued field:

employee 679 has two degrees: *BSc* and *MSc*

employee 333 has three degrees: *BA*, *BSc*, *PhD*



First Normal Form

- To obtain 1NF relations we must, replace the above with single value multiple row

| EmpNum | EmpPhone | EmpDegree |
|--------|----------|-----------|
| 123 | 233-9876 | |
| 333 | 233-1231 | BA |
| 333 | 233-1231 | BSc |
| 333 | 233-1231 | PhD |
| 679 | 233-1231 | BSc |
| 679 | 233-1231 | MSc |



First Normal Form

- To obtain 1NF relations we must, replace the above with single value multiple Column

| EmpNum | EmpPhone | EmpDegree 1 | EmpDegree 2 | EmpDegree 3 |
|--------|----------|----------------|----------------|----------------|
| 123 | 233-9876 | | | |
| 333 | 233-1231 | BA | BSc | PhD |
| 679 | 233-1231 | BSc | MSc | |



First Normal Form

To obtain 1NF relations we must, replace the above with two relations

Employee

| EmpNum | EmpPhone |
|---------------|-----------------|
| 123 | 233-9876 |
| 333 | 233-1231 |
| 679 | 233-1231 |

EmployeeDegree

| EmpNum | EmpDegree |
|---------------|------------------|
| 333 | BA |
| 333 | BSc |
| 333 | PhD |
| 679 | BSc |
| 679 | MSc |

An outer join between Employee and EmployeeDegree will produce the information we saw before



Second Normal Form

Second Normal Form

A relation is in **2NF** if it is in 1NF, and **every non-key attribute is fully dependent on each candidate key**. (That is, we don't have any partial functional dependency.)

- 2NF (and 3NF) both involve the concepts of key and non-key attributes.
- A *key attribute* is any attribute that is part of a key; any attribute that is not a key attribute, is a *non-key attribute*.

SECOND NORMAL FORM

Table purchase detail

| <u>Customer_id</u> | <u>Store_id</u> | Location |
|--------------------|-----------------|----------|
| 1 | 1 | Patna |
| 1 | 3 | Noida |
| 2 | 1 | Patna |
| 3 | 2 | Delhi |
| 4 | 3 | Noida |

- This table has a composite primary key i.e. customer id, store id. The non key attribute is location. In this case location depends on store id, which is part of the primary key.

After decomposing it into second normal form it looks like:

Table Purchase

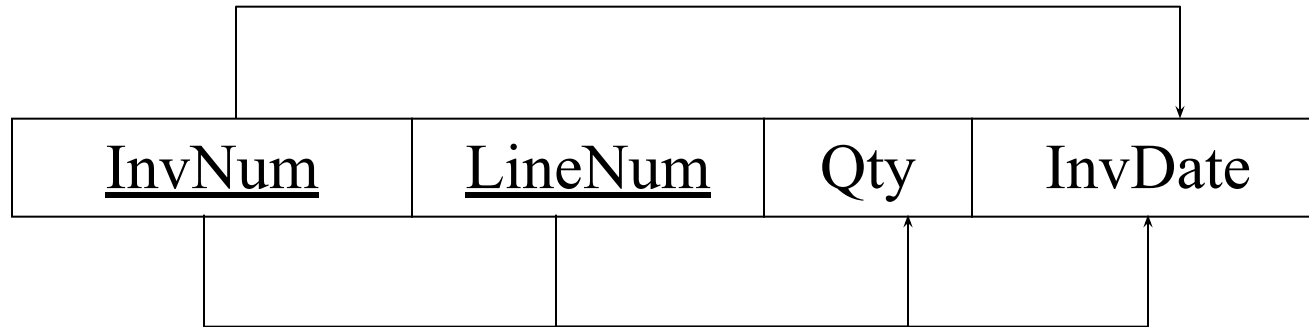
| <u>Customer_id</u> | <u>Store_id</u> |
|--------------------|-----------------|
| 1 | 1 |
| 1 | 3 |
| 2 | 1 |
| 3 | 2 |
| 4 | 3 |

Table Store

| <u>Store_id</u> | Location |
|-----------------|----------|
| 1 | Patna |
| 2 | Delhi |
| 3 | Noida |



Second Normal Form



We correct the situation by decomposing the original relation into two 2NF relations.

| | | |
|---------------|----------------|-----|
| <u>InvNum</u> | <u>LineNum</u> | Qty |
|---------------|----------------|-----|

| | |
|---------------|---------|
| <u>InvNum</u> | InvDate |
|---------------|---------|



Second Normal Form

R(ABCDEF)

FD{ $C \xrightarrow{\text{PD}} F$, $E \xrightarrow{\text{PD}} A$, $EC \rightarrow D$, $A \rightarrow B$ }

- A relation is in **2NF** if it is in 1NF, and every non-prime attribute is fully dependent on each candidate key (If L.H.S. is proper subset of candidate key and R.H.S. is non prime attribute then there is a partial dependency).

CK={EC}

PA={E,C}

NPA={A,B,D,F}

R(ABCDEF)

After Decomposition:

Step1: R1(ABCDE), R2(CF)

Step2: R11(BCDE), R12(AE), R2(CF)

Third Normal Form (3NF)

A table design is said to be in 3NF if both the following conditions hold:

- ▶ Table must be in 2NF
- ▶ Transitive functional dependency of non-prime attribute on any super key should be removed.

An attribute that is not part of any candidate key is known as non-prime attribute.

In other words 3NF can be explained like this: A table is in 3NF if it is in 2NF and for each functional dependency $X \rightarrow Y$ at least one of the following conditions hold:

- ▶ X is a super key of table
- ▶ Y is a prime attribute of table

An attribute that is a part of one of the candidate keys is known as prime attribute.

THIRD NORMAL FORM

Table Book Details

| Bood_id | Genre_id | Genre type | Price |
|---------|----------|------------|-------|
| 1 | 1 | Fiction | 100 |
| 2 | 2 | Sports | 110 |
| 3 | 1 | Fiction | 120 |
| 4 | 3 | Travel | 130 |
| 5 | 2 | sports | 140 |

- In the table, book_id determines genre_id and genre_id determines genre type. Therefore book_id determines genre type via genre_id and we have transitive functional dependency.

After decomposing it into third normal form it looks like:

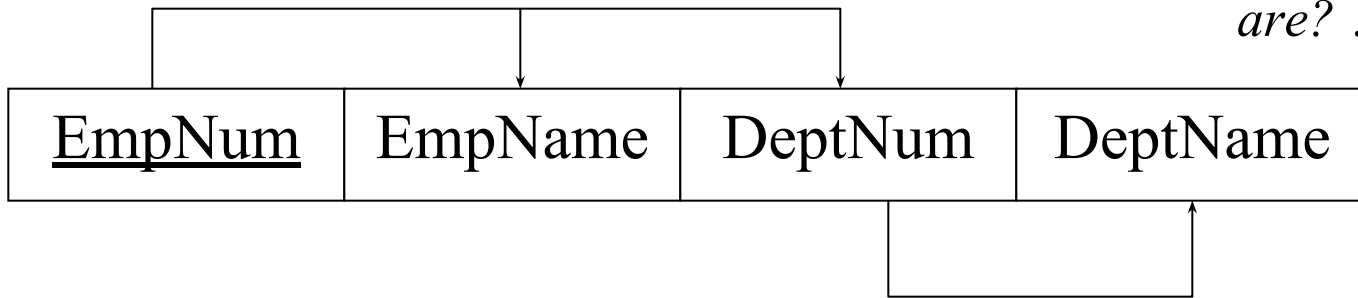
| TABLE BOOK | | |
|------------|----------|-------|
| Book_id | Genre_id | Price |
| 1 | 1 | 100 |
| 2 | 2 | 110 |
| 3 | 1 | 120 |
| 4 | 3 | 130 |
| 5 | 2 | 140 |

| TABLE GENRE | |
|-------------|------------|
| Genre_id | Genre type |
| 1 | Fiction |
| 2 | Sports |
| 3 | Travel |

Third Normal Form

Consider this **Employee** relation

*Candidate keys
are? ...*



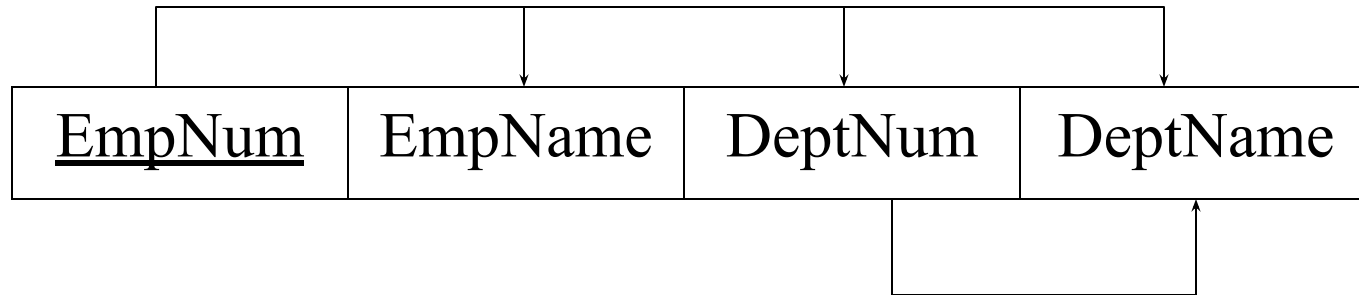
EmpName, DeptNum, and DeptName are non-key attributes.

DeptNum determines DeptName, a non-key attribute, and DeptNum is not a candidate key.

Is the relation in 3NF? ... no Is the relation in BCNF? ... no

Is the relation in 2NF? ... yes

Third Normal Form



We correct the situation by decomposing the original relation into two 3NF relations. Note the decomposition is *lossless*.



Verify these two relations are in 3NF.



Third Normal Form

$R(ABCD)$

$FD\{ AB \rightarrow C, C \xrightarrow{TD} D \}$

- A relation is in **3NF** if it is in 2NF, and no non-prime attribute is dependent on another non-prime attribute. (If L.H.S. is a candidate key or R.H.S. is prime attribute then it is already in 3NF otherwise not in 3NF).

$CK = \{AB\}$

$PA = \{A, B\}$

$NPA = \{C, D\}$

$R(ABCD)$

After Decomposition:

Step1: $R_1(ABC), R_2(CD)$

Boyce-Codd Normal Form (BCNF)

- It is an advance version of 3NF that's why it is also referred as 3.5NF. BCNF is stricter than 3NF. A table complies with BCNF if it is in 3NF and for every functional dependency $X \rightarrow Y$, X should be the super key of the table.

Boyce-Codd Normal Form

| Student | Course | Teacher |
|---------|--------|---------|
| Aman | DBMS | AYUSH |
| Aditya | DBMS | RAJ |
| Abhinav | E-COMM | RAHUL |
| Aman | E-COMM | RAHUL |
| abhinav | DBMS | RAJ |

- ▶ KEY: {Student, Course}
- ▶ Functional dependency
 {student, course} \rightarrow Teacher
 Teacher \rightarrow Course
- ▶ Problem: teacher is not superkey but determines course.

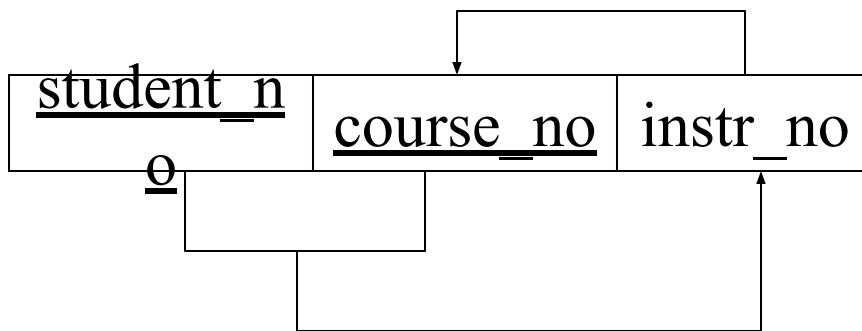
After decomposing it into Boyce-Codd normal form it looks like:

| Student | Course |
|---------|--------|
| Aman | DBMS |
| Aditya | DBMS |
| Abhinav | E-COMM |
| Aman | E-COMM |
| Abhinav | DBMS |

| Course | Teacher |
|--------|---------|
| DBMS | AYUSH |
| DBMS | RAJ |
| E-COMM | RAHUL |



In 3NF, but not in BCNF:



Instructor teaches one course only.

Student takes a course and has one instructor.

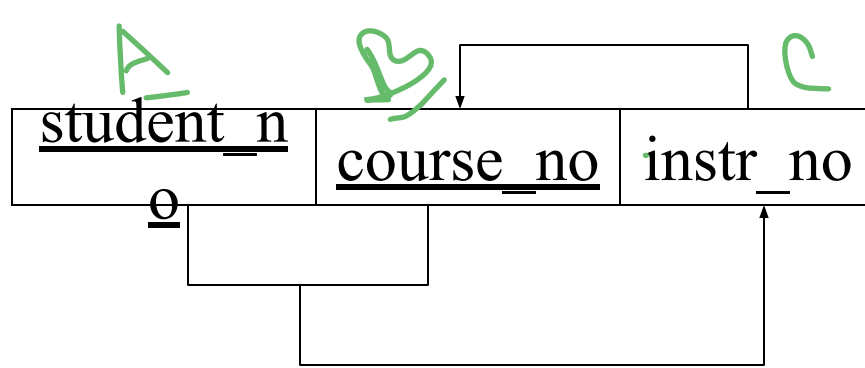
$\{\text{student_no}, \text{course_no}\} \rightarrow \text{instr_no}$

$\text{instr_no} \rightarrow \text{course_no}$

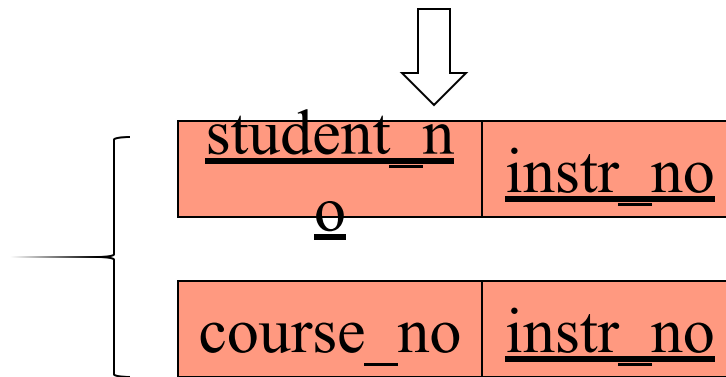
since we have $\text{instr_no} \rightarrow \text{course_no}$, but instr_no is not a Candidate key.



$R_1(B, C)$
 $R_2(A \rightarrow C)$
 $R_3(A, B)$



$A \rightarrow B$
 $B \rightarrow C$
 $C \rightarrow A$



BCNF

$\{student_no, instr_no\} \rightarrow student_no$
 $\{student_no, instr_no\} \rightarrow instr_no$
 $instr_no \rightarrow course_no$



Third Normal Form

$R(ABCEF)$

$FD\{ AB \rightarrow C, \underset{NC}{C \rightarrow E}, \underset{NC}{E \rightarrow F}, \underset{NC}{F \rightarrow A} \}$

- A relation is in BCNF if it is in 3NF, and non-prime attribute must be dependent on candidate key. (If L.H.S. is a candidate key then it is already in BCNF otherwise not in BCNF).

$CK = \{AB, FB, EB, CB\}$

$PA = \{A, B, C, E, F\}$

$NPA = \{\emptyset\}$

$R(ABCEF)$

After Decomposition:

$R_1(CE), R_2(EF), R_3(FA), R_4(ABC)$

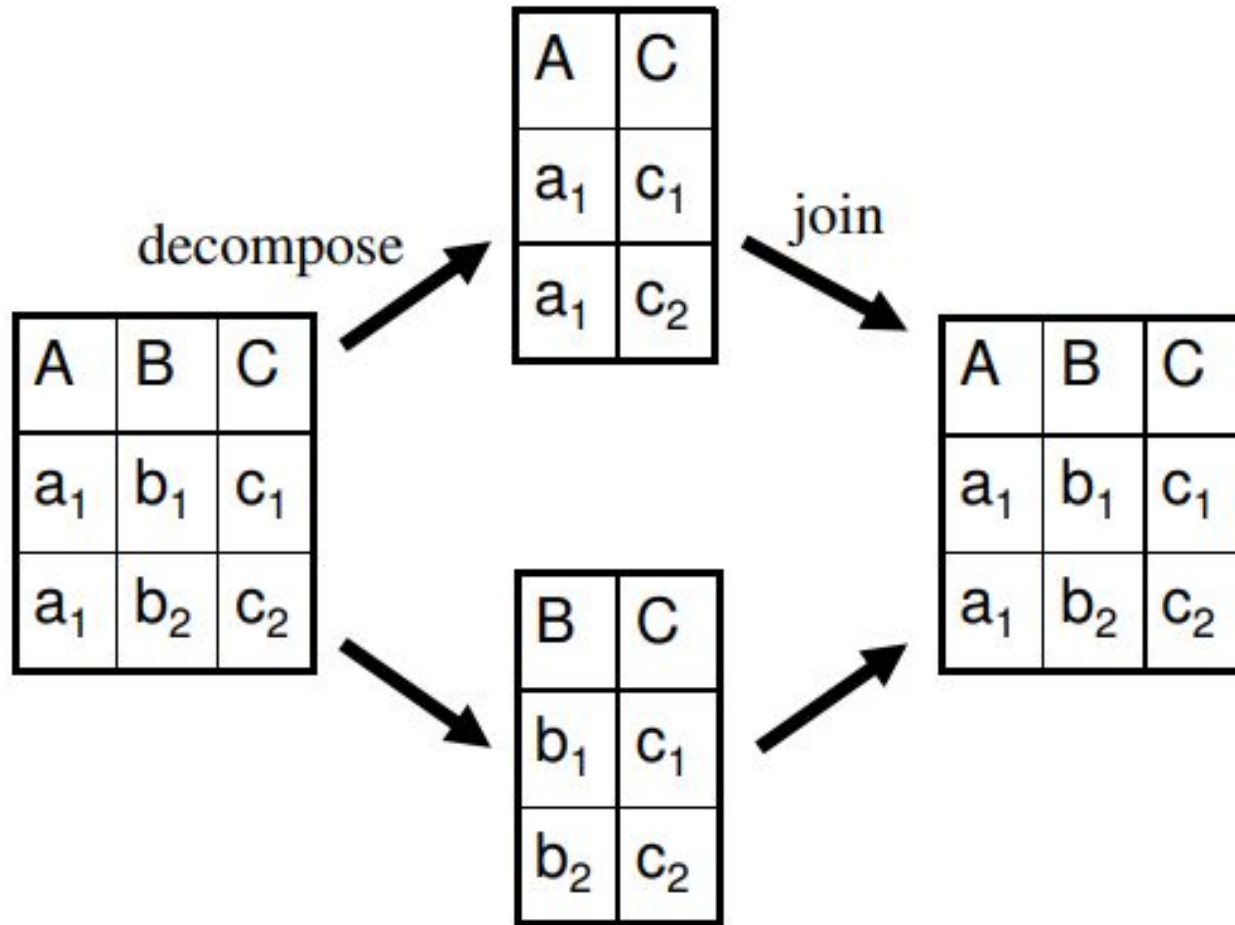


Goals of Normalization

- Let R be a relation scheme with a set F of functional dependencies.
- Decide whether a relation scheme R is in “good” form.
- In the case that a relation scheme R is not in “good” form, decompose it into a set of relation scheme $\{R_1, R_2, \dots, R_n\}$ such that
 - each relation scheme is in good form
 - the decomposition is a **lossless-join decomposition**
 - Preferably, the decomposition should be dependency preserving.



Example (Lossless-Join)





Testing for Lossless-Join Decomposition

- Rule: A decomposition of R into $(R1, R2)$ is *lossless*, iff:

$$R1 \cap R2 \rightarrow R1 \quad \text{or}$$

$$R1 \cap R2 \rightarrow R2$$

in F^+ .



Exercise: Lossless-join Decomposition

$R = \{A, B, C, D, E\}$.

$F = \{A \rightarrow BC, CD \rightarrow E, B \rightarrow D, E \rightarrow A\}$.



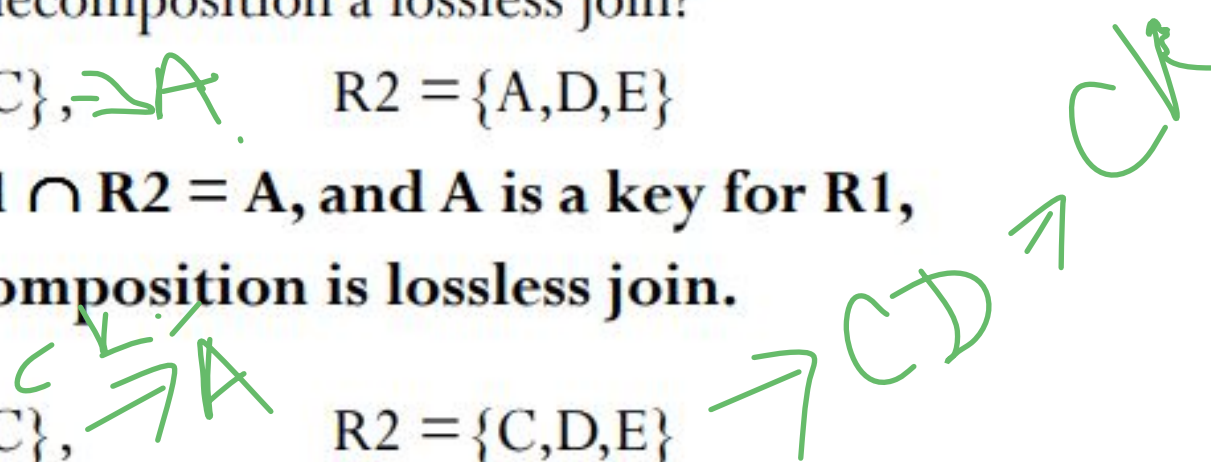
Is the following decomposition a lossless join?

1. $R_1 = \{A, B, C\}, \Rightarrow A$ $R_2 = \{A, D, E\}$

Since $R_1 \cap R_2 = A$, and A is a key for R_1 ,
the decomposition is lossless join.

2. $R_1 = \{A, B, C\}, \Rightarrow A$ $R_2 = \{C, D, E\}$

Since $R_1 \cap R_2 = C$, and C is not a key for R_1 or R_2 , the decomposition is not lossless join.





Exercise 3

$R = (A, B, C, D).$

$F = \{C \rightarrow D, C \rightarrow A, B \rightarrow C\}.$

Question 1: Identify all candidate keys for R.

Question 2: Identify the best normal form that R satisfies.

Question 3: Decompose R into a set of BCNF relations.

Question 4: Decompose R into a set of 3NF relations.



Exercise 3 Solution

$R = (A, B, C, D).$

$F = \{C \rightarrow D, C \rightarrow A, B \rightarrow C\}.$

Question 1: Identify all candidate keys for R.

$B^+ = B \quad (B \rightarrow B)$

$= BC \quad (B \rightarrow C)$

$= BCD \quad (C \rightarrow D)$

$= ABCD \quad (C \rightarrow A)$

so the candidate key is B.

B is the **ONLY** candidate key, because nothing determines B:

There is no rule that can produce B, except $B \rightarrow B$.



Exercise 3 Solution

$R = (A, B, C, D).$

$F = \{C \rightarrow D, C \rightarrow A, B \rightarrow C\}.$

Question 2: Identify the best normal form that R satisfies.

R is not 3NF, because:

$C \rightarrow D$ causes a violation,

$C \rightarrow D$ is non-trivial ($\{D\} \not\subseteq \{C\}$).

C is not a superkey.

D is not part of any candidate key.

$C \rightarrow A$ causes a violation

Similar to above

$B \rightarrow C$ causes no violation

Since R is not 3NF, it is not BCNF either.



Exercise 3 Solution

$R = (A, B, C, D).$

$F = \{C \rightarrow D, C \rightarrow A, B \rightarrow C\}.$

Question 3: Decompose R into a set of BCNF relations

(1) $C \rightarrow D$ and $C \rightarrow A$ both cause violations of BCNF.

Take $C \rightarrow D$: decompose R to $R_1 = \{A, B, C\}$, $R_2 = \{C, D\}.$

(2) Now check for violations in R_1 and R_2 . (Actually, using F^+)

R_1 still violates BCNF because of $C \rightarrow A$.

Decompose R_1 to $R_{11} = \{B, C\}$, $R_{12} = \{C, A\}.$

Final decomposition: $R_2 = \{C, D\}$, $R_{11} = \{B, C\}$, $R_{12} = \{C, A\}.$

No more violations: Done!



Exercise 3 Solution

$R = (A, B, C, D)$.

$F = \{C \rightarrow D, C \rightarrow A, B \rightarrow C\}$.

Question 4: Decompose R into a set of 3NF relations.

The canonical cover is $F_c = \{C \rightarrow DA, B \rightarrow C\}$.

For each functional dependency in F_c we create a table:

$R_1 = \{C, D, A\}$, $R_2 = \{B, C\}$.

The table R_2 contains the candidate key for R — we done.



Exercise 4

$R = (A, B, C, D)$

$F = \{AB \rightarrow C, AB \rightarrow D, C \rightarrow A, D \rightarrow B\}$

1. Is R in 3NF, why? If it is not, decompose it into 3NF
2. Is R in BCNF, why? If it is not, decompose it into BCNF



Exercise 4 Solution

$R = (A, B, C, D)$

$F = \{AB \rightarrow C, AB \rightarrow D, C \rightarrow A, D \rightarrow B\}$

1. Is R in 3NF, why? If it is not, decompose it into 3NF

Yes.

Find all the Candidate Keys:

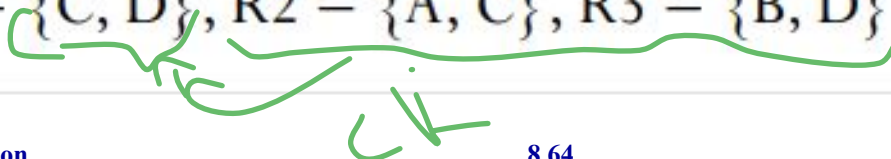
AB, BC, CD, AD

Check all FDs in F for 3NF condition

2. Is R in BCNF, why? If it is not, decompose it into BCNF

No. Because for $C \rightarrow A$, C is not a superkey. Similar for $D \rightarrow B$

$R1 = \{C, D\}, R2 = \{A, C\}, R3 = \{B, D\}$





End of Chapter

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