



# Chapter 2: Intro to Relational Model

**Database System Concepts, 6<sup>th</sup> Ed.**

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# Example of a Relation

<i>ID</i>	<i>name</i>	<i>dept_name</i>	<i>salary</i>
10101	Srinivasan	Comp. Sci.	65000
12121	Wu	Finance	90000
15151	Mozart	Music	40000
22222	Einstein	Physics	95000
32343	El Said	History	60000
33456	Gold	Physics	87000
45565	Katz	Comp. Sci.	75000
58583	Califieri	History	62000
76543	Singh	Finance	80000
76766	Crick	Biology	72000
83821	Brandt	Comp. Sci.	92000
98345	Kim	Elec. Eng.	80000

attributes  
(or columns)

tuples  
(or rows)



# Attribute Types

- The set of allowed values for each attribute is called the **domain** of the attribute
- Attribute values are (normally) required to be atomic; that is, indivisible
- The special value ***null*** is a member of every domain. Indicated that the value is “unknown”
- The null value causes complications in the definition of many operations



# Relation Schema and Instance

□  $A_1, A_2, \dots, A_n$  are attributes

□  $R = (A_1, A_2, \dots, A_n)$  is a relation schema

Example:

$instructor = (ID, name, dept\_name, salary)$

□ Formally, given sets  $D_1, D_2, \dots, D_n$  a **relation**  $r$  is a subset of

$D_1 \times D_2 \times \dots \times D_n$

Thus, a relation is a set of  $n$ -tuples  $(a_1, a_2, \dots, a_n)$  where each  $a_i \in D_i$

□ The current values (**relation instance**) of a relation are specified by a table

□ An element  $t$  of  $r$  is a tuple, represented by a row in a table



# Relations are Unordered

- Order of tuples is irrelevant (tuples may be stored in an arbitrary order)
- Example: *instructor* relation with unordered tuples

<i>ID</i>	<i>name</i>	<i>dept_name</i>	<i>salary</i>
22222	Einstein	Physics	95000
12121	Wu	Finance	90000
32343	El Said	History	60000
45565	Katz	Comp. Sci.	75000
98345	Kim	Elec. Eng.	80000
76766	Crick	Biology	72000
10101	Srinivasan	Comp. Sci.	65000
58583	Califieri	History	62000
83821	Brandt	Comp. Sci.	92000
15151	Mozart	Music	40000
33456	Gold	Physics	87000
76543	Singh	Finance	80000

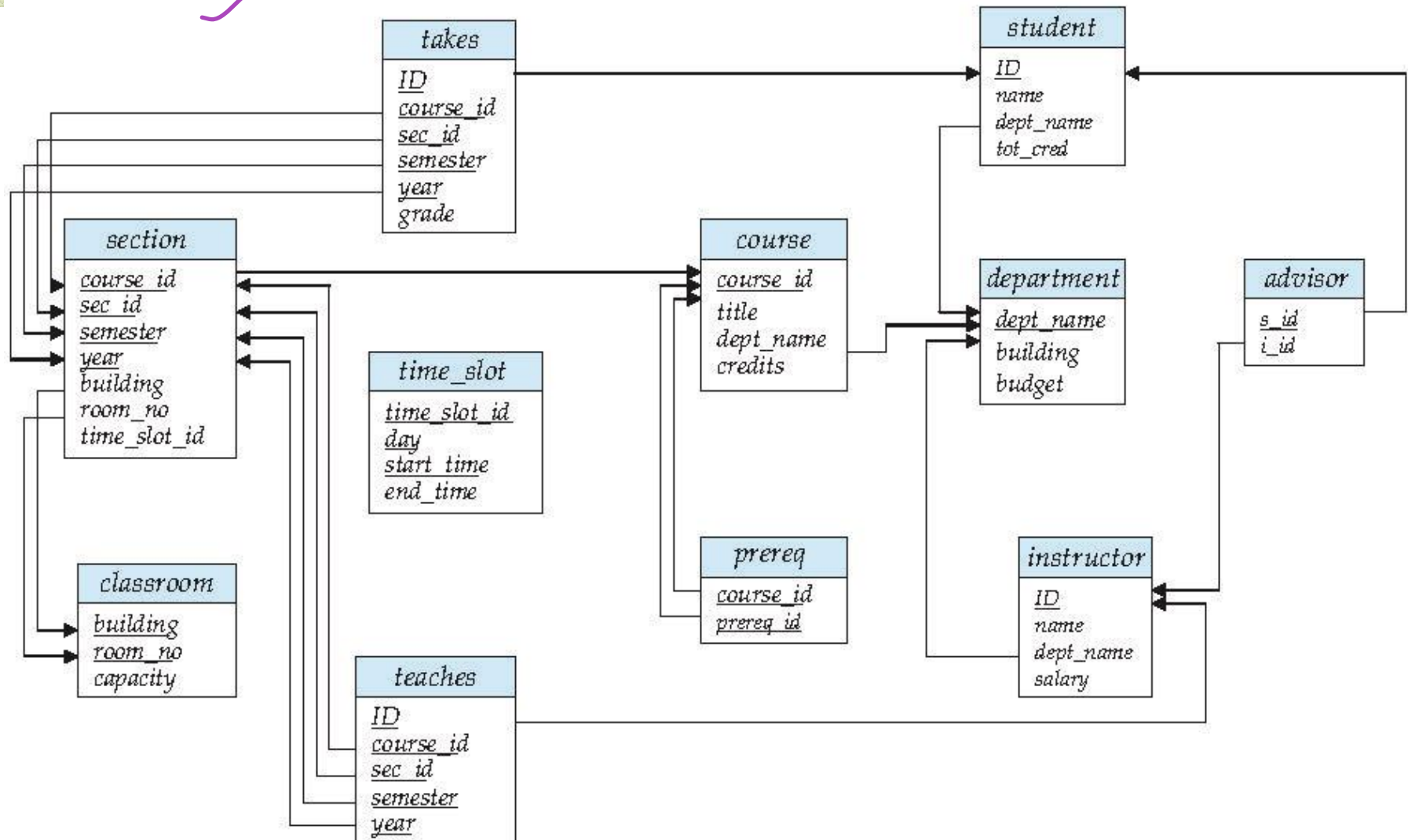


# Keys

- Let  $K \subseteq R$
- $K$  is a **superkey** of  $R$  if values for  $K$  are sufficient to identify a unique tuple of each possible relation  $r(R)$ 
  - Example:  $\{ID\}$  and  $\{ID, name\}$  are both superkeys of *instructor*.
- Superkey  $K$  is a **candidate key** if  $K$  is minimal  
Example:  $\{ID\}$  is a candidate key for *Instructor*
- One of the candidate keys is selected to be the primary key.
  - which one?
- **Foreign key** constraint: Value in one relation must appear in another
  - Referencing relation
  - Referenced relation
  - Example – *dept\_name* in *instructor* is a foreign key from *instructor* referencing *department*



# Schema Diagram for University Database





# Relational Query Languages

- ❑ Procedural vs .non-procedural, or declarative
- ❑ “Pure” languages:
  - ❑ Relational algebra
  - ❑ Tuple relational calculus
  - ❑ Domain relational calculus
- ❑ The above 3 pure languages are equivalent in computing power
- ❑ We will concentrate in this chapter on relational algebra
  - ❑ Not Turing-machine equivalent
  - ❑ consists of 6 basic operations





# Select Operation – selection of rows (tuples)

□ Relation r

A	B	C	D
$\alpha$	$\alpha$	1	7
$\alpha$	$\beta$	5	7
$\beta$	$\beta$	12	3
$\beta$	$\beta$	23	10

■  $\sigma_{A=B \wedge D > 5}(r)$

A	B	C	D
$\alpha$	$\alpha$	1	7
$\beta$	$\beta$	23	10



# Project Operation – selection of columns (Attributes)

□ Relation  $r$ :

$A$	$B$	$C$
$\alpha$	10	1
$\alpha$	20	1
$\beta$	30	1
$\beta$	40	2

□  $\Pi_{A,C}(r)$

$A$	$C$
$\alpha$	1
$\alpha$	1
$\beta$	1
$\beta$	2

 $=$ 

$A$	$C$
$\alpha$	1
$\beta$	1
$\beta$	2



# Union of two relations

□ Relations  $r, s$ :

$A$	$B$
$\alpha$	1
$\alpha$	2
$\beta$	1

$r$

$A$	$B$
$\alpha$	2
$\beta$	3

$s$

□  $r \cup s$ :

$A$	$B$
$\alpha$	1
$\alpha$	2
$\beta$	1
$\beta$	3



# Set difference of two relations

□ Relations  $r, s$ :

$A$	$B$
$\alpha$	1
$\alpha$	2
$\beta$	1

$r$

$A$	$B$
$\alpha$	2
$\beta$	3

$s$

□  $r - s$ :

$A$	$B$
$\alpha$	1
$\beta$	1



# Set intersection of two relations

□ Relation  $r, s$ :

$A$	$B$
$\alpha$	1
$\alpha$	2
$\beta$	1

$r$

$A$	$B$
$\alpha$	2
$\beta$	3

$s$

□  $r \cap s$

$A$	$B$
$\alpha$	2

Note:  $r \cap s = r - (r - s)$



# joining two relations -- Cartesian-product

□ Relations  $r, s$ :

$A$	$B$
$\alpha$	1
$\beta$	2

$r$

$C$	$D$	$E$
$\alpha$	10	a
$\beta$	10	a
$\beta$	20	b
$\gamma$	10	b

$s$

□  $r \times s$ :

$A$	$B$	$C$	$D$	$E$
$\alpha$	1	$\alpha$	10	a
$\alpha$	1	$\beta$	10	a
$\alpha$	1	$\beta$	20	b
$\alpha$	1	$\gamma$	10	b
$\beta$	2	$\alpha$	10	a
$\beta$	2	$\beta$	10	a
$\beta$	2	$\beta$	20	b
$\beta$	2	$\gamma$	10	b



# Cartesian-product – naming issue

□ Relations  $r, s$ :

$A$	$B$
$\alpha$	1
$\beta$	2

$r$

$B$	$D$	$E$
$\alpha$	10	a
$\beta$	10	a
$\beta$	20	b
$\gamma$	10	b

$s$

□  $r \times s$ :

$A$	$r.B$	$s.B$	$D$	$E$
$\alpha$	1	$\alpha$	10	a
$\alpha$	1	$\beta$	10	a
$\alpha$	1	$\beta$	20	b
$\alpha$	1	$\gamma$	10	b
$\beta$	2	$\alpha$	10	a
$\beta$	2	$\beta$	10	a
$\beta$	2	$\beta$	20	b
$\beta$	2	$\gamma$	10	b



# Renaming a Table

- Allows us to refer to a relation, (say  $E$ ) by more than one name.

$$\rho_x(E)$$

returns the expression  $E$  under the name  $X$

- Relations  $r$

$A$	$B$
$\alpha$	1
$\beta$	2

$r$

- 

$$r \times \rho_s(r)$$

$r.A$	$r.B$	$s.A$	$s.B$
$\alpha$	1	$\alpha$	1
$\alpha$	1	$\beta$	2
$\beta$	2	$\alpha$	1
$\beta$	2	$\beta$	2





# Composition of Operations

- Can build expressions using multiple operations
- Example:  $\sigma_{A=C}(r \times s)$

□  $r \times s$

A	B	C	D	E
$\alpha$	1	$\alpha$	10	a
$\alpha$	1	$\beta$	10	a
$\alpha$	1	$\beta$	20	b
$\alpha$	1	$\gamma$	10	b
$\beta$	2	$\alpha$	10	a
$\beta$	2	$\beta$	10	a
$\beta$	2	$\beta$	20	b
$\beta$	2	$\gamma$	10	b

□  $\sigma_{A=C}(r \times s)$

A	B	C	D	E
$\alpha$	1	$\alpha$	10	a
$\beta$	2	$\beta$	10	a
$\beta$	2	$\beta$	20	b



# Joining two relations – Natural Join

- Let  $r$  and  $s$  be relations on schemas  $R$  and  $S$  respectively. Then, the “natural join” of relations  $R$  and  $S$  is a relation on schema  $R \cup S$  obtained as follows:
  - Consider each pair of tuples  $t_r$  from  $r$  and  $t_s$  from  $s$ .
  - If  $t_r$  and  $t_s$  have the same value on each of the attributes in  $R \cap S$ , add a tuple  $t$  to the result, where
    - ▶  $t$  has the same value as  $t_r$  on  $r$
    - ▶  $t$  has the same value as  $t_s$  on  $s$



# Natural Join Example

Relations  $r, s$ :

$A$	$B$	$C$	$D$
$\alpha$	1	$\alpha$	a
$\beta$	2	$\gamma$	a
$\gamma$	4	$\beta$	b
$\alpha$	1	$\gamma$	a
$\delta$	2	$\beta$	b

$r$

$B$	$D$	$E$
1	a	$\alpha$
3	a	$\beta$
1	a	$\gamma$
2	b	$\delta$
3	b	$\epsilon$

$s$

Natural Join

$r \bowtie s$

$A$	$B$	$C$	$D$	$E$
$\alpha$	1	$\alpha$	a	$\alpha$
$\alpha$	1	$\alpha$	a	$\gamma$
$\alpha$	1	$\gamma$	a	$\alpha$
$\alpha$	1	$\gamma$	a	$\gamma$
$\delta$	2	$\beta$	b	$\delta$

$$\Pi_{A, r.B, C, r.D, E}(\sigma_{r.B=s.B \wedge r.D=s.D}(r \times s))$$



# Notes about Relational Languages

- Each Query input is a table (or set of tables)
- Each query output is a table.
- All data in the output table appears in one of the input tables
- Relational Algebra is not Turning complete
- Can we compute:
  - ✗ □ SUM
  - ✗ □ AVG
  - ✗ □ MAX
  - ✗ □ MIN



# Summary of Relational Algebra Operators

Symbol (Name)	Example of Use
$\sigma$ (Selection)	$\sigma \text{ salary} \geq 85000$ ( <i>instructor</i> )
	Return rows of the input relation that satisfy the predicate.
$\Pi$ (Projection)	$\Pi ID, salary$ ( <i>instructor</i> )
	Output specified attributes from all rows of the input relation. Remove duplicate tuples from the output.
$\times$ (Cartesian Product)	<i>instructor</i> $\times$ <i>department</i>
	Output pairs of rows from the two input relations that have the same value on all attributes that have the same name.
$\cup$ (Union)	$\Pi name$ ( <i>instructor</i> ) $\cup$ $\Pi name$ ( <i>student</i> )
	Output the union of tuples from the <i>two</i> input relations.
$-$ (Set Difference)	$\Pi name$ ( <i>instructor</i> ) $--$ $\Pi name$ ( <i>student</i> )
	Output the set difference of tuples from the two input relations.
$\bowtie$ (Natural Join)	<i>instructor</i> $\bowtie$ <i>department</i>
	Output pairs of rows from the two input relations that have the <u>same value on all attributes that have the same name.</u>



# End of Chapter 2

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