Section 5.3 Homework

Exercises 1 and 2, let f be a function that describes the number of steps required to carry out a certain algorithm. The number of items to be processed is represented by n. For each function, describe what happens to the number of steps if the number of items is doubled.

- 1. (a) f(n) = 1001Steps remain at 1001.
 - (b) f(n) = 3nNumber of steps double.
 - (c) $f(n) = 5n^2$ Number of steps quadruple.
 - (d) $f(n) = 2.5n^3$ Number of steps eight-fold.
- 2. (a) $f(n) = 1.4\log(n^2)$ Number of steps process by 1.4
 - (b) $f(n) = 2^n$ Number of steps is squared
 - (c) $f(n) = n\log(n)$ Number of steps doubles and adds 2n steps
 - (d) $f(n) = 100n^4$ Number of steps is multiplied by 16
- 4. Show that h(n) = 1 + 2 + 3 + ... + n is $O(n^2)$ $\frac{n(n-1)}{2} = \frac{n^2 n}{2} = O(n^2)$
- 11. Determine which of the following are in the same Θ -class. A function may be in a class by itself.

$$\Theta = \{f_6,\,f_{10},\,f_{11}\},\,\{f_1\},\,\{f_2\},\,\{f_3\},\,\{f_4\},\,\{f_5\},\,\{f_7\},\,\{f_8\},\,\{f_9\},\,\{f_{12}\}$$

- 12. Order the Θ classes in Exercise 11 from lowest to highest. $f_5,\ f_7,\ f_4,\ f_8,\ f_{10},\ f_{11},\ f_6,\ f_{12},\ f_1,\ f_2,\ f_3,\ f_9$
- 13. Consider the functions f_1 , f_2 , f_4 , f_5 , f_6 , f_{10} , f_{11} in Exercise 11. Match each of the functions with its Θ class from the following list: $\Theta(1)$, $\Theta(n)$, $\Theta(n\log(n))$, $\Theta(\log(n)$, $\Theta(n^2)$, $\Theta(\sqrt{n})$, $\Theta(2^n)$.

$$\Theta(1) = f_5
\Theta(n) = f_6, f_{10}, f_{11}
\Theta(n\log(n)) = f_1$$

$$\begin{array}{l} \Theta \, \log(n) = f_4 \\ \Theta \, (n^2) = f_2 \\ \Theta (\!\sqrt{n}), \, \Theta(2^n) = \text{null} \end{array}$$