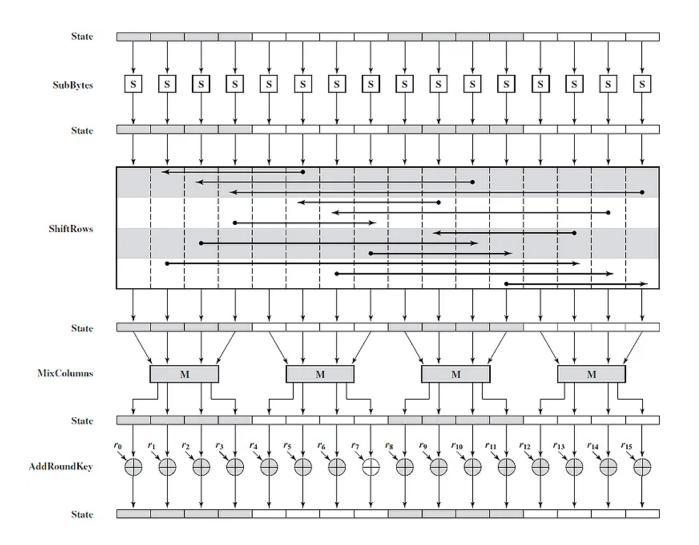
C | SecureAES

- High-Performance AES Encryption in C -

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Acknowledgements

Note (**XOR Operation and Modular Reduction in** $GF(2^n)$). In the context of Galois Field $GF(2^n)$, particularly in binary polynomial arithmetic, the XOR operation is equivalent to addition and also plays a crucial role in modular reduction. We explore this equivalence through the principles of field theory and polynomial arithmetic.

• Field Properties:

A Galois Field, $GF(p^n)$, is a finite field that contains a finite number of elements, where

- *p* is a prime number (base of the field) and
- n is a positive integer (degree of the field).

For the binary field $GF(2^n)$, p = 2, which implies that every element in this field is either 0 or 1.

• Addition in $GF(2^n)$:

In $GF(2^n)$, the addition of two elements is performed modulo 2. For any two elements $a, b \in GF(2^n)$, the addition is defined as:

$$a + b = a \oplus b$$

Since 2 is the base of the field, the addition wraps around upon reaching 2, which is effectively what the XOR operation does.

• Polynomial Representation:

Elements in $GF(2^n)$ can be represented as polynomials where each coefficient is in $GF(2) = \{0,1\}$. A general element can be written as:

$$a(x) = a_{n-1}x^{n-1} + a_{n-2}x^{n-2} + \dots + a_1x + a_0$$

where $a_i \in \{0, 1\}$ for all i.

• Modular Reduction:

Modular reduction in $GF(2^n)$ involves reducing a polynomial by a fixed irreducible polynomial of degree n, ensuring that the result remains within the field. Let m(x) be the irreducible polynomial. The reduction of a polynomial f(x) is given by: $f(x) \mod m(x)$

• XOR as Modular Reduction:

During modular reduction, the subtraction used in polynomial division becomes XOR, because subtraction and addition are the same in GF(2). Therefore, reducing a polynomial f(x) by m(x) is effectively performed using XOR on the coefficients of corresponding terms.

For example, if f(x) has a term x^k where $k \ge n$, and m(x) has a term x^k , then reducing f(x) by m(x) involves XORing the coefficients of x^k in f(x) and m(x), effectively eliminating the x^k term in f(x).

In summary, the XOR operation becomes equivalent to both addition and modular reduction in $GF(2^n)$ due to the binary nature of the field. This equivalence simplifies polynomial arithmetic in binary fields, making it a cornerstone of operations in cryptographic algorithms.

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Chapter 1

Block Cipher

Block ciphers are a fundamental component in cryptographic systems. They transform fixedsize blocks of plaintext into ciphertext using a symmetric key. The transformation is designed to be reversible only with knowledge of the key.

1.1 Definition and Structure

- Secure Pseudo-Random Permutation (PRP) and Substitution Groups:
 - Definition: A block cipher is considered a secure PRP if it is indistinguishable from a random permutation of the input bits, making it resistant to cryptanalysis.
 - Substitution Groups: Block ciphers often use substitution-permutation networks (SPNs) that include substitution groups. These groups perform non-linear transformations, crucial for creating cryptographic strength.
- Confidentiality for Fixed n-bit Data (Blocks):
 - Fixed Block Size: Block ciphers encrypt and decrypt data in fixed-size blocks (commonly 64 or 128 bits). This fixed size is crucial for the algorithm's structure and security.
 - **Padding Schemes:** When the data doesn't fit perfectly into a block, padding schemes are used to fill the remaining space, ensuring consistent block sizes.
- Block Cipher Operation Modes for Variable-Length Data:
 - Mode of Operation: To handle variable-length data, block ciphers use different modes of operation like CBC (Cipher Block Chaining), CFB (Cipher Feedback), and GCM (Galois/Counter Mode).
 - **Ensuring Security:** Each mode offers distinct features for security and efficiency, often enhancing the cipher's resistance to various attack vectors.
- Advantages Over Asymmetric Key Cryptography:
 - **High-Speed Computation:** Block ciphers are generally faster and require less computational power compared to asymmetric key cryptography.
 - **Suitability:** This makes them suitable for encrypting large volumes of data and in environments with limited resources.

• Deriving Other Cryptographic Functions:

- Versatility: Block ciphers can be used to design other cryptographic functions like hash functions, message authentication codes (MACs), and random number generators.
- Construction Techniques: Techniques like Cipher Block Chaining-MAC (CBC-MAC) and Counter mode (CTR) are examples of how block ciphers can be adapted for these purposes.

Block ciphers are a critical element in the cryptographic landscape, providing a versatile and efficient means for securing digital data. Their adaptability and robustness make them an indispensable tool in the design of secure communication protocols and cryptographic systems.

1.2 Modes of Operations

		Table 1.1.	Comparison	of Modes			
Mode	Integrity	Authentication	EncryptBlk	DecryptBlk	Padding	IV	$ P \stackrel{?}{=} C $
ECB	O	Χ	O	O	O	X	P < C
CBC	O	X	O	O	O	O	P < C
OFB	O	X	O	X	X	O	P = C
CFB	O	X	O	X	X	O	P = C
CTR	O	X	O	X	X	O	P = C
CBC – CS	O	X	O	O	X	O	P = C

Table 1.1: Comparison of Modes

1.2.1 Padding

Block ciphers require input lengths to be a multiple of the block size. Padding is used to extend the last block of plaintext to the required length. Without proper padding, the encryption process may be insecure or infeasible.

There are several padding schemes used in practice, such as:

Standard Name	Padding Method
PKCS#7	Pad with bytes all the same value as the number of padding bytesdd dd 04 04 04 04
ANSI X9.23	Pad with zeros, last byte is the number of padding bytesdd dd dd dd dd dd dd dd dd 00 00 00 05
ISO/IEC 7816-4	First byte is '80' (hex), followed by zerosdd dd dd dd dd dd dd dd dd 80 00 00 00 00
ISO 10126	Pad with random bytes, last byte is the number of padding bytesdd dd dd dd dd dd dd dd dd 2e 49 1b c1 aa 06

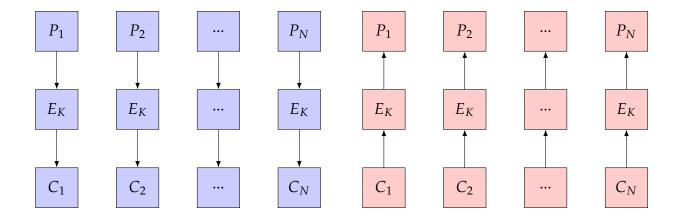
Table 1.2: Padding Standards in Block Ciphers

1.2.2 ECB (Electronic CodeBook)

Algorithm 1: Electronic CodeBook

```
Input: K \text{ and } P = P_1 \parallel \cdots \parallel P_N \ (P_i \in \{0,1\}^n)
Output: C = C_1 \parallel \cdots \parallel C_N \ (C_i \in \{0,1\}^n)
Output: P = P_1 \parallel \cdots \parallel P_N \ (P_i \in \{0,1\}^n)

1 for i \leftarrow 1 to N do
2 C_i \leftarrow \text{EncryptBlk}(K, P_i);
2 end
3 end
4 return C = C_1 \parallel \cdots \parallel C_N;
Input: C_i \leftarrow C_i \parallel \cdots \parallel C_i \leftarrow C_i \leftarrow C_i \leftarrow C_i \parallel \cdots \parallel C_i \leftarrow C
```



Remark 1.1.

(1) For a pair of plaintext/ciphertext (P, C) and (P', C'),

$$P = P' \implies C = C'$$
.

- (2) A single-bit error in the ciphertext affects only the corresponding block in the decryption.
- (3) Block order changes, as well as additions/deletions, are possible. Therefore, to ensure the integrity of the ciphertext (i.e., detection or prevention of tampering), it should be used in conjunction with a checksum or a Message Authentication Code (MAC).

CBC (Cipher Block Chaining)

Algorithm 2: Cipher Block Chaining

Input: K, IV and $P = P_1 \parallel \cdots \parallel P_N$ Output: $C = C_1 \parallel \cdots \parallel C_N$

1 C_0 ← IV;

2 for $i \leftarrow 1$ to N do

 $C_i \leftarrow \mathsf{EncryptBlk}(K, P_i \oplus C_{i-1});$

4 end

5 **return** $C = C_1 \| \cdots \| C_N$;

Input: K, IV and $C = C_1 \parallel \cdots \parallel C_N$ Output: $P = P_1 \parallel \cdots \parallel P_N$

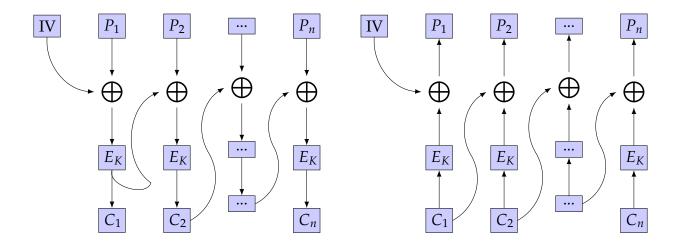
1 C_0 ← IV;

2 for $i \leftarrow 1$ to N do

 $P_i \leftarrow C_{i-1} \oplus \mathsf{DecryptBlk}(K, C_i);$

4 end

5 **return** $P = P_1 || \cdots || P_N;$



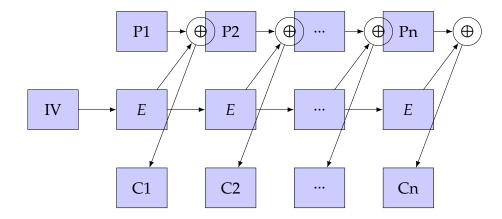
Remark 1.2.

(1) For a set of plaintext/ciphertext pairs (IV, P, C) and (IV', P', C'),

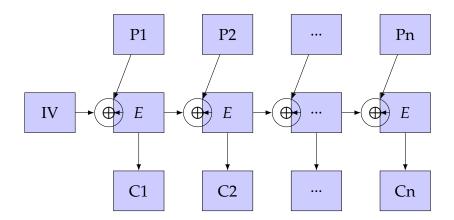
$$IV = IV' \wedge P = P' \implies C = C'.$$

- (2) A one-bit error in the ciphertext will affect the corresponding block and the subsequent block in the decryption process, thereby enabling the detection of such errors.
- (3) Altering the order of blocks, as well as adding or deleting them, is not possible.

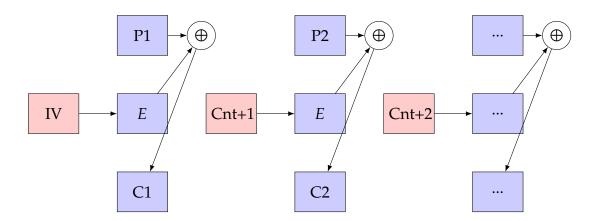
1.2.4 OFB (Output FeedBack)



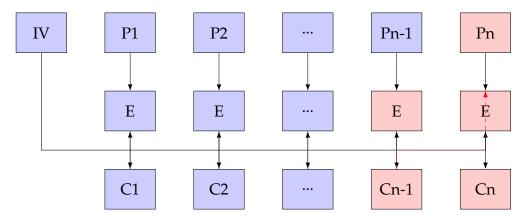
1.2.5 CFB (Ciphertext FeedBack)



1.2.6 CTR (CounTeR)



1.2.7 CBC - CS (Ciphertext Stealing)



Chapter 2

AES-128

2.1 Overview of AES-128

```
• KeyExpansion : \{0, 1\}^{128} \rightarrow \{0, 1\}^{1408 = 4 \cdot (10+1) \cdot 32}.
```

```
• AddRoundKey: \{0, 1\}^{128} \times \{0, 1\}^{128} \rightarrow \{0, 1\}^{128}.
```

• SubBytes/ShiftRows/MixColumns : $\{0, 1\}^{128} \rightarrow \{0, 1\}^{128}$.

Algorithm 3: Encryption of AES-128

```
Input: block \operatorname{src} \in \{0, 1\}^{128}, round-keys \{rk_i\}_{i=0}^{11} (rk_i \in \{0, 1\}^{128})

Output: block \operatorname{dst} \in \{0, 1\}^{128}

1 t \leftarrow \operatorname{AddRoundKey(src}, rk_0);

2 for i \leftarrow 1 to 9 do

3 | t \leftarrow (\operatorname{MixColumns} \circ \operatorname{ShiftRows} \circ \operatorname{SubBytes})(t);

4 | t \leftarrow \operatorname{AddRoundKey}(t, rk_i);

5 end

6 t \leftarrow (\operatorname{ShiftRows} \circ \operatorname{SubBytes})(t);

7 t \leftarrow \operatorname{AddRoundKey}(t, rk_{10});

8 \operatorname{dst} \leftarrow t;

9 return \operatorname{dst};
```

Algorithm 4: Decryption of AES-128

```
Input: block \operatorname{src} \in \{0,1\}^{128}, round-keys \{rk_i\}_{i=0}^{11} (rk_i \in \{0,1\}^{128})

Output: block \operatorname{dst} \in \{0,1\}^{128}

1 t \leftarrow \operatorname{AddRoundKey(src}, rk_{10});

2 for i \leftarrow 9 to 1 do

3 | t \leftarrow (\operatorname{InvSubBytes} \circ \operatorname{InvShiftRows})(t);

4 | t \leftarrow \operatorname{AddRoundKey}(t, rk_i);

5 | t \leftarrow \operatorname{InvMixColumns}(t);

6 end

7 t \leftarrow (\operatorname{InvShiftRows} \circ \operatorname{InvSubBytes})(t);

8 t \leftarrow \operatorname{AddRoundKey}(t, rk_0);

9 \operatorname{dst} \leftarrow t;

10 return \operatorname{dst};
```

2.2 Functions and Constants used in AES

2.2.1 Key Expansion

• RotWord: $\{0, 1\}^{32} \to \{0, 1\}^{32}$ is defined by

```
RotWord (X_0 \parallel X_1 \parallel X_2 \parallel X_3) := X_1 \parallel X_2 \parallel X_3 \parallel X_0 \text{ for } X_i \in \{0, 1\}^8.
```

Code 2.1: RotWord rotates the input word left by one byte

```
1 u32 RotWord(u32 word) {
2 return (word << 0x08) | (word >> 0x18);
3 }
```

• SubWord : $\{0, 1\}^{32} \rightarrow \{0, 1\}^{32}$ is defined by

```
SubWord(X_0 \parallel X_1 \parallel X_2 \parallel X_3) := s(X_0) \parallel s(X_1) \parallel s(X_2) \parallel s(X_3) for X_i \in \{0, 1\}^8.
```

Here, $s: \{0, 1\}^8 \to \{0, 1\}^8$ is the S-box.

Code 2.2: SubWord applies the S-box to each byte of the input word

```
1 u32 SubWord(u32 word) {
2 return (u32)s_box[word >> 0x18] << 0x18 |
3 (u32)s_box[(word >> 0x10) & 0xFF] << 0x10 |
4 (u32)s_box[(word >> 0x08) & 0xFF] << 0x08 |
5 (u32)s_box[word & 0xFF];
6 }
```

• Round Constant rCon:

The constant $rCon_i \in \mathbb{F}_{2^8}$ used in generating the *i*-th round key corresponds to the value of x^{i-1} in the binary finite field \mathbb{F}_{2^8} and is as follows:

Code 2.3: rCon Array Declaration

```
1 static const u32 rCon[10] = {
2      0x01000000, 0x02000000, 0x04000000, 0x08000000,
3      0x10000000, 0x20000000, 0x40000000, 0x80000000,
4      0x1b000000, 0x36000000
5 };
```

Algorithm 5: Key Schedule (AES-128)

```
Input: User key uk = (uk_0, ..., uk_{15}) (uk_i \in \{0, 1\}^8);   // uk \in \{0, 1\}^{128} is 16-byte
    Output: round-keys \{rk_i\}_{i=0}^{43} (rk_i \in \{0, 1\}^{32}); // \{rk_i\}_{i=0}^{43} \in \{0, 1\}^{1408} is 176-byte
 1 \ rk_0 \leftarrow uk_0 \parallel uk_1 \parallel uk_2 \parallel uk_3;
 2 rk_1 \leftarrow uk_4 \parallel uk_5 \parallel uk_6 \parallel uk_7;
 3 rk_2 \leftarrow uk_8 \parallel uk_9 \parallel uk_{10} \parallel uk_{11};
 4 \ rk_3 \leftarrow uk_{12} \parallel uk_{13} \parallel uk_{14} \parallel uk_{15};
 5 for i = 4 to 43 do
          t \leftarrow rk_{i-1};
          if i \mod 4 = 0 then
               /* SubWord \circ RotWord : \{0, 1\}^{32} \rightarrow \{0, 1\}^{32}
                                                                                                                                                   */
               t \leftarrow \text{RotWord}(t);
 8
               t \leftarrow \text{SubWord}(t);
               t \leftarrow t \oplus (rCon_{i/4} \parallel 0x00 \parallel 0x00 \parallel 0x00);
10
          end
11
          rk_i \leftarrow rk_{i-4} \oplus_{32} t;
13 end
```

Code 2.4: AES-128 Key Expansion

```
void KeyExpansion(const u8* uKey, u32* rKey) {
1
2
       u32 temp;
       int i = 0;
3
4
5
       // Copy the input key to the first round key
       while (i < 4) {
6
7
            rKey[i] = (u32)uKey[4*i] << 0x18
8
            (u32)uKey[4*i+1] << 0x10
9
            (u32)uKey[4*i+2] << 0x08
            (u32)uKey[4*i+3];
10
            i++;
11
       }
12
13
       i = 4;
14
15
       // Generate the remaining round keys
16
       while (i < 44) {</pre>
17
            temp = rKey[i-1];
18
            if (i % 4 == 0) {
19
                temp = SubWord(RotWord(temp)) ^ rCon[i/4-1];
20
21
            rKey[i] = rKey[i-4] \wedge temp;
22
23
            i++;
24
       }
25
   }
```

10 CHAPTER 2. AES-128

2.2.2 AddRoundKey

• AddRoundKey: $\{0, 1\}^{128} \times \{0, 1\}^{128} \to \{0, 1\}^{128}$ is defined by $\text{AddRoundKey}\left(\{X_i\}_{i=0}^{15}, \{rk_i\}_{i=0}^3\right) := \{X_i \oplus_8 uk_i\}_{i=0}^{15}.$

Code 2.5: AES AddRoundKey

```
void AddRoundKey(u8* state, const u32* rKey) {
1
      for (int i = 0; i < AES_BLOCK_SIZE; i++) {</pre>
2
3
          // i = 0, 1, 2, 3 => wordIndex = 0
          // i = 4, 5, 6, 7 \Rightarrow wordIndex = 1
4
          // i = 8, 9, 10, 11 => wordIndex = 2
          // i = 12, 13, 14, 15 => wordIndex = 3
6
7
          int wordIndex = i / 4;
          // i = 0, 1, 2, 3 => bytePosition = 0,
9
10
          // i = 4, 5, 6, 7 => bytePosition = 0, 1, 2,
          // i = 8, 9, 10, 11 => bytePosition = 0, 1, 2,
11
          // i = 12, 13, 14, 15 => bytePosition = 0, 1, 2,
12
          int bytePosition = i % 4;
13
14
15
     16
17
                      | 0
| 1
                                      | rKey[0] >> 0x18
18
                                      | rKey[0] >> 0x10
19
                        | 2
20
                                      | rKey[0] >> 0x08
                                  | rKey[0]
                       | 3
21
22
                                 | rKey[1] >> 24
                       | 0
     | 4-7 | 1
23
                                      | rKey[1] >> 16
| rKey[1] >> 8
24
                        | 1
                       | 2
25
                  | 3 | rKey[1]
26
27
28
29
30
31
32
          u32 shiftedWord =
33
              rKey[wordIndex] >> (8 * (3 - bytePosition));
34
35
          u8 keyByte = shiftedWord & 0xFF;
          state[i] ^= keyByte;
37
38
  /* Extract the corresponding byte from the round key word */
39
  // state[i] ^{=} (rKey[i / 4] >> (8 * (3 - (i % 4)))) & 0xFF;
40
41
      }
42
  }
```

2.2.3 SubBytes / InvSubBytes

• SubBytes : $\{0, 1\}^{128} \to \{0, 1\}^{128}$ is defined by

SubBytes(
$$\{X_i\}_{i=0}^{15}$$
) = $\{s(X_i)\}_{i=0}^{15}$.

• InvSubBytes: $\{0, 1\}^{128} \rightarrow \{0, 1\}^{128}$ is defined by

SubBytes(
$$\{X_i\}_{i=0}^{15}$$
) = $\{s^{-1}(X_i)\}_{i=0}^{15}$.

Table 2.1: Substitution Box

	00	01	02	03	04	05	06	07	08	09	0a	0b	0c	0d	0e	0f
00	63	7c	77	7b	f2	6b	6f	c5	30	01	67	2b	fe	d7	ab	76
10	ca	82			•••						•••					
30					•••											
40		•••	•••	•••	•••	•••	•••	•••			•••	•••	•••	•••	•••	
50		•••	•••	•••	•••		•••	•••	•••	•••	•••	•••	•••		•••	•••
60		•••	•••	•••	•••	•••	•••	•••	•••	•••	•••	•••	•••	•••	•••	•••
70		•••	•••	•••	•••	•••	•••	•••	•••	•••	•••	•••	•••	•••	•••	•••
80		•••	•••	•••	•••	•••	•••	•••	•••	•••	•••	•••	•••	•••	•••	•••
90		•••	•••	•••	•••	•••	•••	•••	•••	•••	•••	•••	•••	•••	•••	•••
a0		•••	•••	•••	•••		•••	•••	•••	•••	•••	•••	•••		•••	•••
b0		•••	•••	•••	•••	•••	•••	•••	•••	•••	•••	•••	•••	•••	•••	•••
c0		•••	•••	•••	•••	•••	•••	•••	•••	•••	•••	•••	•••	•••	•••	•••
d0		•••	•••	•••	•••		•••	•••			•••	•••	•••	c1	•••	
e0		•••	•••	•••	•••	•••	•••	•••			•••	•••	•••	•••	28	
f0		•••	•••		•••		•••	•••	•••	•••	•••	•••	•••	•••	•••	16

Code 2.6: Byte Substitution

```
void SubBytes(u8* state) {
    for (int i = 0; i < AES_BLOCK_SIZE; i++) {
        state[i] = s_box[state[i]];
}
}</pre>
```

Code 2.7: Inverse Byte Substitution

```
void SubBytes(u8* state) {
    for (int i = 0; i < AES_BLOCK_SIZE; i++) {
        state[i] = inv_s_box[state[i]];
    }
}</pre>
```

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2.2.4 ShiftRows / InvShiftRows

• ShiftRows: $\{0, 1\}^{128} \to \{0, 1\}^{128}$ is defined by

X_0	X_4	X_8	X_{12}		X_0	X_4	X_8	X_{12}
X_1	X_5	<i>X</i> ₉	X_{13}		X_5	<i>X</i> ₉	X_{13}	X_1
X_2	X_6	X_{10}	X_{14}	\Rightarrow	X_{10}	X_{14}	X_2	X_6
X_3	X_7	X_{11}	X_{15}		X_{15}	X_3	X_7	X_{11}

• InvShiftRows : $\{0, 1\}^{128} \rightarrow \{0, 1\}^{128}$ is defined by

X_0	X_4	X_8	X_{12}		X_0	X_4	X_8	X_{12}
X_1	X_5	<i>X</i> ₉	X_{13}		X_{13}	X_1	X_5	<i>X</i> ₉
X_2	X_6	X_{10}	X_{14}	\Rightarrow	X_{10}	X_{14}	X_2	X_6
X_3	X_7	X_{11}	X_{15}		X_7	X ₁₁	X_{15}	X_3

Code 2.8: ShiftRows

```
void ShiftRows(u8* state) {
1
2
       u8 temp;
3
       // Row 1: shift left by 1
4
5
       temp = state[1];
6
       state[1] = state[5];
7
       state[5] = state[9];
8
       state[9] = state[13];
9
       state[13] = temp;
10
       // Row 2: shift left by 2
11
12
       temp = state[2];
       state[2] = state[10];
13
14
       state[10] = temp;
       temp = state[6];
15
       state[6] = state[14];
16
       state[14] = temp;
17
18
       // Row 3: shift left by 3 (or right by 1)
19
       temp = state[15];
20
       state[15] = state[11];
21
22
       state[11] = state[7];
23
       state[7] = state[3];
24
       state[3] = temp;
25
  }
```

Code 2.9: Inverse ShiftRows

```
void InvShiftRows(u8* state) {
1
2
       u8 temp;
3
       // Row 1: shift left by 3 (or right by 1)
4
5
       temp = state[13];
6
       state[13] = state[9];
7
       state[9] = state[5];
8
       state[5] = state[1];
9
       state[1] = temp;
10
       // Row 2: shift left by 2
11
       temp = state[2];
12
13
       state[2] = state[10];
14
       state[10] = temp;
15
       temp = state[6];
16
       state[6] = state[14];
       state[14] = temp;
17
18
       // Row 3: shift left by 1
19
20
       temp = state[3];
       state[3] = state[7];
21
22
       state[7] = state[11];
23
       state[11] = state[15];
24
       state[15] = temp;
25
  }
```

2.2.5 MixColumns / InvMixColumns

• Multiplication in the finite filed GF(2⁸).

$$MUL_{GF256}: \{0, 1\}^8 \times \{0, 1\}^8 \rightarrow \{0, 1\}^8.$$

Here,

$$\{\mathbf{0},\mathbf{1}\}^8 \simeq GF(2^8) = \mathbb{F}_{2^8} := \mathbb{F}_2[z]/(z^8 + z^4 + z^3 + z + 1) = \{a_7z^7 + \dots + a_1z + a_0 : a_i \in \mathbb{F}_2\}.$$

Note that

$$a(z) \times b(z) := a(z) \times b(z) \mod (z^8 + z^4 + z^3 + z + 1)$$

Note. Given two polynomials a(x) and b(x) in $GF(2^8)$:

$$a(x) = a_7 x^7 + a_6 x^6 + a_5 x^5 + a_4 x^4 + a_3 x^3 + a_2 x^2 + a_1 x + a_0,$$

$$b(x) = b_7 x^7 + b_6 x^6 + b_5 x^5 + b_4 x^4 + b_3 x^3 + b_2 x^2 + b_1 x + b_0.$$

The algorithm performs polynomial multiplication in the finite field $GF(2^8)$. It uses a shift-and-add method, with an additional reduction step modulo an irreducible polynomial $m(x) = x^8 + x^4 + x^3 + x + 1$.

- 1. Initialization: Set p(x) = 0 to initialize the product polynomial.
- 2. Iterate over each bit of b(x), from LSB to MSB.
 - (i) If the current bit b_i of b(x) is 1, update p(x) as $p(x) \oplus a(x)$. In $GF(2^8)$, addition is equivalent to the XOR operation:

$$p(x) = p(x) \oplus a(x)$$
.

(ii) Shift a(x) left by 1 (multiply by x), increasing its degree by 1:

$$a(x) = a(x) \cdot x$$
.

(iii) If the coefficient of x^8 in a(x) is 1, reduce a(x) by m(x) to keep the degree under 8:

$$a(x) = a(x) \oplus m(x)$$
.

(iv) Shift b(x) right by 1 (divide by x) for the next iteration:

$$b(x) = b(x) / x$$
.

3. After all bits of b(x) are processed, p(x) be the product of a(x) and b(x) modulo m(x).

Note (**Modular Reduction in** $GF(2^8)$ **using XOR).** In the context of multiplication in the binary finite field $GF(2^8)$, modular reduction ensures that results of operations remain within the field. The use of XOR for modular reduction is due to the properties of polynomial arithmetic over GF(2) and the representation of elements in $GF(2^8)$.

- Polynomial Representation in $GF(2^8)$:
 - 1. **Elements as Polynomials**: Each element in $GF(2^8)$ can be represented as a polynomial of degree less than 8, where each coefficient is either 0 or 1, i.e.,

$$GF(2^8) = \mathbb{F}_2[x]/(x^8 + x^4 + x^3 + x + 1) = \left\{ a_7 x^7 + \dots + a_1 x + a_0 : a_i \in \mathbb{F}_2 \right\}.$$

This corresponds to an 8-bit binary number, with each bit representing a coefficient of the polynomial, i.e.,

$$a_7x^7 + \cdots + a_1x + a_0 \iff (a_7 \dots a_1a_0)_2.$$

2. **Binary Operations**: In GF(2), addition and subtraction are equivalent to the XOR operation, since 1 + 1 = 0 in this field, the same as $1 \oplus 1$.

- Modular Reduction with an Irreducible Polynomial

- 1. **Irreducible Polynomial**: In $GF(2^8)$, an irreducible polynomial of degree 8, typically $p(x) = x^8 + x^4 + x^3 + x + 1$ (represented as 0x11b in binary), is used for modular reduction.
- 2. **Modular Reduction Process**: After multiplying two polynomials, if the resulting polynomial's degree is 8 or higher, it must be reduced modulo the irreducible polynomial to ensure the result remains a polynomial of degree less than 8, thus staying within $GF(2^8)$.
- 3. **XOR for Reduction**: XOR is used for modular reduction in $GF(2^8)$ because polynomial subtraction in GF(2) is performed by XORing coefficients.
- Given two elements in $GF(2^8)$, a(x) and b(x), their product is $c(x) = a(x) \cdot b(x)$. If $deg(c(x)) \ge 8$, then c(x) must be reduced modulo the irreducible polynomial p(x). This is achieved by XORing the coefficients of c(x) and p(x):

$$c(x) = a(x) \cdot b(x) \mod p(x)$$

If c(x) has a term x^8 or higher, we subtract p(x) from c(x) to reduce its degree. In GF(2), subtraction is equivalent to addition, performed by XORing coefficients:

$$c'(x) = c(x) \oplus p(x)$$

This operation effectively eliminates the term x^8 (or higher) in c(x), ensuring that the result remains within $GF(2^8)$. Consider the product of two polynomials a(x) and b(x) in $GF(2^8)$:

$$a(x) = x^6 + x^4 + x^2 + x + 1$$
 and $b(x) = x^7 + x + 1$

The product $c(x) = a(x) \cdot b(x)$ might yield a polynomial of degree 8 or higher. To reduce c(x) modulo $p(x) = x^8 + x^4 + x^3 + x + 1$, we perform XOR between the coefficients of c(x) and p(x), ensuring the result stays within $GF(2^8)$.

Code 2.10: Multiplication in $GF(2^8)$

```
u8 MUL_GF256(u8 a, u8 b) {
2
       u8 res = 0;
3
       // Mask for detecting the MSB (0x80 = 0b10000000)
4
       u8 MSB_mask = 0x80;
5
       u8 MSB;
       /*
6
7
        * The reduction polynomial
8
        * (x^8 + x^4 + x^3 + x + 1) = 0b100011011
9
        * for AES, represented in hexadecimal
       */
10
       u8 \mod ulo = 0x1B;
11
12
       for (int i = 0; i < 8; i++) {
13
14
            // Add a to result if LSB(b)=1
15
            if (b & 1)
                res ^{\prime}= a;
16
17
            MSB = a & MSB_mask; // Store the MSB of a
18
19
            a <<= 1; // Multiplying it by x effectively
20
21
            // Reduce the result modulo the reduction polynomial
22
            if (MSB)
23
                a ^= modulo;
24
25
            b >>= 1; // Moving to the next bit
       }
26
27
28
       return res;
29
   }
30
31
   #define MUL_GF256(a, b) ({ \
       u8 res = 0; \
32
33
       u8 MSB_mask = 0x80; \
       u8 MSB; \
34
35
       u8 \mod ulo = 0x1B; \setminus
36
       u8 temp_a = (a); \
       u8 temp_b = (b); \
37
       for (int i = 0; i < 8; i++) { \</pre>
38
39
            if (temp_b & 1) \
            res ^= temp_a; \
40
41
            MSB = temp_a & MSB_mask; \
42
            temp_a <<= 1; \
            if (MSB) \
43
            temp_a ^= modulo; \
44
45
            temp_b >>= 1; \
46
       } \
47
       res; \
48
  })
```

• MixColumns : $\{0, 1\}^{128} \rightarrow \{0, 1\}^{128}$ is defined by

$$\text{MixColumns} \left(\begin{pmatrix} X_0 & X_4 & X_8 & X_{12} \\ X_1 & X_5 & X_9 & X_{13} \\ X_2 & X_6 & X_{10} & X_{14} \\ X_3 & X_7 & X_{11} & X_{15} \end{pmatrix} \right) := \begin{pmatrix} \mathbf{0} \times \mathbf{02} & \mathbf{0} \times \mathbf{03} & \mathbf{0} \times \mathbf{01} & \mathbf{0} \times \mathbf{01} \\ \mathbf{0} \times \mathbf{01} & \mathbf{0} \times \mathbf{02} & \mathbf{0} \times \mathbf{03} & \mathbf{0} \times \mathbf{01} \\ \mathbf{0} \times \mathbf{01} & \mathbf{0} \times \mathbf{01} & \mathbf{0} \times \mathbf{02} & \mathbf{0} \times \mathbf{03} \\ \mathbf{0} \times \mathbf{03} & \mathbf{0} \times \mathbf{01} & \mathbf{0} \times \mathbf{01} & \mathbf{0} \times \mathbf{02} \end{pmatrix} \begin{pmatrix} X_0 & X_4 & X_8 & X_{12} \\ X_1 & X_5 & X_9 & X_{13} \\ X_2 & X_6 & X_{10} & X_{14} \\ X_3 & X_7 & X_{11} & X_{15} \end{pmatrix}.$$

• InvMixColums: $\{0, 1\}^{128} \rightarrow \{0, 1\}^{128}$ is defined by

$$\text{MixColums} \begin{pmatrix} \begin{pmatrix} X_0 & X_4 & X_8 & X_{12} \\ X_1 & X_5 & X_9 & X_{13} \\ X_2 & X_6 & X_{10} & X_{14} \\ X_3 & X_7 & X_{11} & X_{15} \end{pmatrix} := \begin{pmatrix} \mathbf{0} \mathbf{x} \mathbf{0} \mathbf{e} & \mathbf{0} \mathbf{x} \mathbf{0} \mathbf{b} & \mathbf{0} \mathbf{x} \mathbf{0} \mathbf{d} & \mathbf{0} \mathbf{x} \mathbf{0} \mathbf{9} \\ \mathbf{0} \mathbf{x} \mathbf{0} \mathbf{9} & \mathbf{0} \mathbf{x} \mathbf{0} \mathbf{e} & \mathbf{0} \mathbf{x} \mathbf{0} \mathbf{b} & \mathbf{0} \mathbf{x} \mathbf{0} \mathbf{d} \\ \mathbf{0} \mathbf{x} \mathbf{0} \mathbf{b} & \mathbf{0} \mathbf{x} \mathbf{0} \mathbf{e} & \mathbf{0} \mathbf{x} \mathbf{0} \mathbf{e} \end{pmatrix} \begin{pmatrix} X_0 & X_4 & X_8 & X_{12} \\ X_1 & X_5 & X_9 & X_{13} \\ X_2 & X_6 & X_{10} & X_{14} \\ X_3 & X_7 & X_{11} & X_{15} \end{pmatrix}.$$

Code 2.11: MixColumns

```
1
   void MixColumns(u8* state) {
2
       u8 temp[4];
       // Multiply and add the elements in the column
3
       // by the fixed polynomial
4
       for (int i = 0; i < 4; i++) {
5
            temp[0] =
6
                MUL_GF256(0x02, state[i * 4]) ^
7
8
                MUL_GF256(0x03, state[i * 4 + 1]) ^
                state[i * 4 + 2] ^
9
                state[i * 4 + 3];
10
11
           temp[1] =
12
                state[i * 4] ^
13
                MUL_GF256(0x02, state[i * 4 + 1]) ^
14
                MUL_GF256(0x03, state[i * 4 + 2]) ^
15
                state[i * 4 + 3];
16
17
           temp[2] =
18
                state[i * 4] ^
19
                state[i * 4 + 1] ^
20
                MUL_GF256(0x02, state[i * 4 + 2]) ^
21
22
                MUL_GF256(0x03, state[i * 4 + 3]);
23
            temp[3] =
24
                MUL_GF256(0x03, state[i * 4]) ^
25
                state[i * 4 + 1] ^
26
                state[i * 4 + 2] ^
27
                MUL_GF256(0x02, state[i * 4 + 3]);
28
29
30
           // Copy the mixed column back to the state
            for (int j = 0; j < 4; j++)
31
                state[i * 4 + j] = temp[j];
32
       }
33
34
  }
```

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Code 2.12: Inverse MixColumns

```
void InvMixColumns(u8* state) {
1
2
       u8 temp[4];
3
4
       for (int i = 0; i < 4; i++) {
5
           temp[0] =
               MUL_GF256(0x0e, state[i * 4]) ^
6
7
               MUL_GF256(0x0b, state[i * 4 + 1]) ^
8
               MUL_GF256(0x0d, state[i * 4 + 2]) ^
9
               MUL_GF256(0x09, state[i * 4 + 3]);
10
11
           temp[1] =
               MUL_GF256(0x09, state[i * 4]) ^
12
               MUL_GF256(0x0e, state[i * 4 + 1]) ^
13
14
               MUL_GF256(0x0b, state[i * 4 + 2]) ^
15
               MUL_GF256(0x0d, state[i * 4 + 3]);
16
17
           temp[2] =
               MUL_GF256(0x0d, state[i * 4]) ^
18
19
               MUL_GF256(0x09, state[i * 4 + 1]) ^
20
               MUL_GF256(0x0e, state[i * 4 + 2]) ^
               MUL_GF256(0x0b, state[i * 4 + 3]);
21
22
23
           temp[3] =
                MUL_GF256(0x0b, state[i * 4]) ^
24
               MUL_GF256(0x0d, state[i * 4 + 1]) ^
25
               MUL_GF256(0x09, state[i * 4 + 2]) ^
26
               MUL_GF256(0x0e, state[i * 4 + 3]);
27
28
           for (int j = 0; j < 4; j++)
29
                state[i * 4 + j] = temp[j];
30
31
       }
32
  }
```

Chapter 3

AES - 128 / 192 / 256 (Byte Version)

3.1 Specification

Table 3.1: Parameters of the Block Cipher AES (1-word = 32-bit)

	Block	Key	Number of	Round-Key	Number of	Total Size of
Algorithms	Size	Length	Rounds	Length	Round-Keys	Round-Keys
	$(N_b$ -word)	$(N_k$ -word)	(N_r)	(word)	$(N_r + 1)$	$(N_b(N_r+1))$
AES-128	4	4 (4·32-bit)	10	4	11	44 (176-byte)
AES-192	4	6 (6·32-bit)	12	4	13	52 (208-byte)
AES-256	4	8 (8·32-bit)	14	4	15	60 (240-byte)

Code 3.1: Configuration in C

```
// Define macros for AES key length
  #define AES_VERSION 128 // Can be 128, 192, or 256
  // Define macro for AES block size
  #define AES_BLOCK_SIZE 16
  // Define Nk and Nr based on AES key length
  #if AES_VERSION == 128
       #define Nk 4
8
  #elif AES_VERSION == 192
       #define Nk 6
10
  #elif AES_VERSION == 256
11
12
       #define Nk 8
13
  #else
       #error "Invalid AES ky length"
15 #endif
16
17
  #define Nr (Nk + 6) // 10 / 12 / 14
18 | #define ROUND_KEYS_SIZE (16 * (Nr + 1)) // 176 / 208 / 240
```

Code 3.2: Configuration in Rust

```
// Define a constant for the AES key length.
1
2
  pub const AES_VERSION: u32 = 128; // Can be 128, 192, or 256
3
   // Define constant for AES block size
4
  pub const AES_BLOCK_SIZE: usize = 16;
6
7
   // Define constants Nk and Nr based on AES key length
8
  pub const NK: usize = match AES_VERSION {
9
       128 = > 4,
       192 = 6
10
       256 => 8,
11
       _ => panic!("Invalid AES key length"),
12
13
   };
14
15
  pub const NR: usize = NK + 6;
  pub const ROUND_KEYS_SIZE: usize = 16 * (NR + 1);
```

3.2 Key Expansion (General Version)

Algorithm 6: Key Schedule (General Version) **Input:** User-key $uk = (uk_0, ..., uk_{N_k-1}) (uk_i \in \{0, 1\}^8);$ // uk is 16/24/32-byte **Output:** Round-key $\{rk_i\}_{i=0}^{4(N_r+1)-1} (rk_i \in \{0, 1\}^{32})$ /* $\{rk_i\}_{i=0}^{4(N_r+1)-1}$ is 176/208/240-byte */ $1 l \leftarrow N_k/4$; // l = 4, 6, 82 **for** i = 0 **to** l - 1 **do** $rk_i \leftarrow uk_{4i} \parallel uk_{4i+1} \parallel uk_{4i+2} \parallel uk_{4i+3};$ 4 end 5 for i = l to $4(N_r + 1) - 1$ do $t \leftarrow rk_{i-1}$; if $i \mod l = 0$ then 7 $t \leftarrow (SubWord \circ RotWord)(t);$ 8 $t \leftarrow t \oplus_{32} (\text{rCon}_{i/l} \parallel 0 \times 000 \parallel 0 \times 000 \parallel 0 \times 000);$ 9 **else if** $l > 6 \&\& i \mod l = 4$ **then** 10 $t \leftarrow \text{SubWord}(t);$ 11 end 12 $rk_i \leftarrow rk_{i-1} \oplus_{32} t$; 13 14 end

Code 3.3: Key Expansion in C (General ver.)

```
void KeyExpansion(const u8* uKey, u32* rKey) {
1
2
       u32 temp;
3
       for (int i = 0; i < Nk; i++) {
4
5
           rKey[i] = (u32)uKey[4*i] << 0x18
                      (u32)uKey[4*i+1] << 0x10
6
7
                      (u32)uKey[4*i+2] << 0x08
                      (u32)uKey[4*i+3];
8
       }
9
10
       for (int i = Nk; i < (Nr + 1) * 4; i++) {
11
           temp = rKey[i - 1];
12
           if (i % Nk == 0) {
13
                temp = SubWord(RotWord(temp)) ^ rCon[i / Nk - 1];
14
           } else if (Nk > 6 \&\& i \% Nk == 4) {
15
                // Additional S-box transformation for AES-256
16
17
                temp = SubWord(temp);
18
19
           rKey[i] = rKey[i - Nk] ^ temp;
20
       }
21
   }
```

Code 3.4: Key Expansion Test

```
void RANDOM_KEY_GENERATION(u8* key) {
1
2
       srand((u32) time(NULL));
3
4
       // Initialize pointer to the start of the key array
5
       u8* p = key;
6
7
       // Set the counter to 16 bytes
8
       int cnt = 0;
9
10
       // Loop until all 16 bytes are filled
       while (cnt < AES_BLOCK_SIZE) {</pre>
11
            *p = rand() & 0xff; // Assign a random byte (0 to 255)
12
                                 // Move to the next byte
13
           p++;
                                 // Decrement the byte count
14
           cnt++;
15
       }
16
   }
17
   void KeyExpansionTest() {
18
19
       u8 uKey[AES_BLOCK_SIZE] = { 0x00, };
20
       RANDOM_KEY_GENERATION(uKey);
       // u8 uKey[AES_BLOCK_SIZE] = {
21
             0x2b, 0x7e, 0x15, 0x16, 0x28, 0xae, 0xd2, 0xa6,
22
23
       //
             0xab, 0xf7, 0x15, 0x88, 0x09, 0xcf, 0x4f, 0x3c
       // };
24
       for (int i = 0; i < AES_BLOCK_SIZE; i++) {</pre>
25
           printf("%02x", uKey[i]);
26
       } printf("\n");
27
28
       u32 rKeys[ROUND_KEYS_SIZE / sizeof(u32)];
29
       KeyExpansion(uKey, rKeys);
30
       for (int i = 0; i < ROUND_KEYS_SIZE / sizeof(u32); i++) {</pre>
31
           printf("%08x\n", rKeys[i]);
32
33
       }
34
  }
35
36
  int main() {
       KeyExpansionTest();
37
38
       return 0;
39
   }
```

8-bit AES - 128 / 192 / 256 3.3

Algorithm 7: Encryption of 8-bit AES

```
Input: block \operatorname{src} \in \{0, 1\}^{128}, round-keys \{rk_i\}_{i=0}^{N_r+1} (rk_i \in \{0, 1\}^{32*4})
    Output: block dst \in \{0, 1\}^{128}
                                                // AddRoundKey: \{0, 1\}^{8*16} \times \{0, 1\}^{32*4} \rightarrow \{0, 1\}^{8*16}
 1 t ← AddRoundKey(src, rk_0);
 2 for i \leftarrow 1 to N_r - 1 do
                                                                               // SubBytes: \{0, 1\}^{8*16} \rightarrow \{0, 1\}^{8*16}
        t \leftarrow \text{SubBytes}(t);
                                                                             // ShiftRows: \{0,1\}^{8*16} \rightarrow \{0,1\}^{8*16}
        t \leftarrow \text{ShiftRows}(t);
                                                                            // MixColumns: \{0, 1\}^{8*16} \rightarrow \{0, 1\}^{8*16}
        t \leftarrow \text{MixColumns}(t);
        t \leftarrow AddRoundKey(t, rk_i);
7 end
s t \leftarrow \text{SubBytes}(t);
9 t \leftarrow \text{ShiftRows}(t);
10 t \leftarrow AddRoundKey(t, rk_{N_r});
11 dst ← t;
12 return dst;
```

Code 3.5: 8-bit AES Encryption

```
void AES_Encrypt(const u8* plaintext, const u8* key,
1
       u8* ciphertext) {
2
       // AES-128/192/256: roundKey[44]/roundKey[52]/roundKey[60]
3
4
       u32 roundKey[ROUND_KEYS_SIZE / sizeof(u32)];
       u8 state[AES_BLOCK_SIZE]; // state[16]
5
6
7
       // Copy plaintext to state
       for (int i = 0; i < AES_BLOCK_SIZE; i++)</pre>
8
9
           state[i] = plaintext[i];
10
11
       KeyExpansion(key, roundKey);
12
13
   // 0: roundKey[ 0] | roundKey[1] | roundKey[ 2] | roundKey[
                                                                        31
14
       AddRoundKey(state, roundKey); // Initial round
15
       for (int round = 1; round <= Nr; round++) { // Main rounds</pre>
16
           SubBytes(state); ShiftRows(state);
17
           if (round != Nr) MixColumns(state);
18
   // 1: roundKey[ 4] | roundKey[5] | roundKey[ 6] | roundKey[
19
                                                                        7]
   // 2: roundKey[ 8] | roundKey[9] | roundKey[10] | roundKey[
                                                                       11]
20
21
   // i: roundKey[4*i] |
                                                        | roundKey[4*i+3]
           AddRoundKey(state, roundKey + 4 * round);
22
23
       }
24
25
       // Copy state to ciphertext
       for (int i = 0; i < AES_BLOCK_SIZE; i++)</pre>
26
27
           ciphertext[i] = state[i];
28
  }
```

Algorithm 8: Decryption of 8-bit AES

```
Input: block \operatorname{src} \in \{0,1\}^{128}, round-keys \{rk_i\}_{i=0}^{N_r+1} (rk_i \in \{0,1\}^{32*4})

Output: block \operatorname{dst} \in \{0,1\}^{128}

1 t \leftarrow \operatorname{AddRoundKey}(\operatorname{src}, rk_{N_r});
2 \operatorname{for} i \leftarrow N_r - 1 \operatorname{to} 1 \operatorname{do}

3 | t \leftarrow \operatorname{InvShiftRows}(t);
4 | t \leftarrow \operatorname{InvSubBytes}(t);
5 | t \leftarrow \operatorname{AddRoundKey}(t, rk_i);
6 | t \leftarrow \operatorname{InvMixColumns}(t);
7 \operatorname{end}
8 t \leftarrow \operatorname{InvShiftRows}(t);
9 t \leftarrow \operatorname{InvSubBytes}(t);
10 t \leftarrow \operatorname{AddRoundKey}(t, rk_0);
11 \operatorname{dst} \leftarrow t;
12 \operatorname{return} \operatorname{dst};
```

Code 3.6: 8-bit AES Decryption

```
void AES_Decrypt(const u8* ciphertext, const u8* key,
1
2
       u8* plaintext) {
3
       u32 roundKey[ROUND_KEYS_SIZE / sizeof(u32)];
       u8 state[AES_BLOCK_SIZE];
4
5
       KeyExpansion(key, roundKey);
6
7
8
       for (int i = 0; i < AES_BLOCK_SIZE; i++)</pre>
            state[i] = ciphertext[i];
9
10
       // Initial round with the last round key
11
       AddRoundKey(state, roundKey + 4 * Nr);
12
13
       // Main rounds in reverse order
14
       for (int round = Nr - 1; round >= 0; round--) {
15
16
           InvShiftRows(state);
           InvSubBytes(state);
17
                                                        | roundKey[4*i+3]
   // i: roundKey[4*i] |
18
                              . . .
   // 1: roundKey[ 4] | roundKey[5] | roundKey[ 6] | roundKey[
                                                                         7]
19
   // 0: roundKey[ 0] | roundKey[1] | roundKey[ 2] | roundKey[
20
                                                                         31
           AddRoundKey(state, roundKey + 4 * round);
21
22
           if (round != 0)
23
                InvMixColumns(state);
       }
24
25
       for (int i = 0; i < AES_BLOCK_SIZE; i++)</pre>
26
27
           plaintext[i] = state[i];
28
```

Chapter 4

Pre-Computation using SubMix

4.1 SubMix and InvSubInvMix

```
• SubMix : \{0,1\}^{128} \rightarrow \{0,1\}^{128} and InvSubInvMix : \{0,1\}^{128} \rightarrow \{0,1\}^{128} are defined by SubMix := MixColumns \circ SubBytes InvSubInvMix := InvMixColumns \circ InvSubBytes.
```

Algorithm 9: Encryption and Decryption of AES using SubMix and InvSubInvMix

```
Input: block \operatorname{src} \in \{0, 1\}^{128}, round-keys \{rk_i\}_{i=0}^{N_r+1} (rk_i \in \{0, 1\}^{128})
   Output: block dst \in \{0, 1\}^{128}
 1 Function AES_ENC:
                                                                        1 Function AES_DEC:
        t \leftarrow \text{src};
                                                                                t \leftarrow \text{src};
         t \leftarrow AddRoundKey(t, rk_0);
                                                                                t \leftarrow AddRoundKey(t, rk_{N_r});
        for i \leftarrow 1 to N_r - 1 do
                                                                                for i \leftarrow N_r - 1 downto 1 do
              t \leftarrow \text{ShiftRows}(t);
                                                                                     t \leftarrow \text{InvShiftRows}(t);
 5
                                                                        5
                                                                                     t \leftarrow InvSubInvMix(t);
              t \leftarrow \mathbf{SubMix}(t);
 6
              t \leftarrow AddRoundKey(t, rk_i);
                                                                                     t' \leftarrow \text{InvMixColumns}(rk_i);
                                                                        7
                                                                                     t \leftarrow AddRoundKey(t, t');
                                                                        8
         t \leftarrow \text{SubBytes}(t);
                                                                                end
                                                                        9
        t \leftarrow \text{ShiftRows}(t);
                                                                                t \leftarrow \text{InvShiftRows}(t);
10
                                                                       10
         t \leftarrow AddRoundKey(t, rk_{N_r});
                                                                                t \leftarrow \text{InvSubBytes}(t);
                                                                       11
11
                                                                                t \leftarrow AddRoundKey(t, rk_0);
        dst \leftarrow t;
                                                                       12
12
        return dst;
                                                                                dst \leftarrow t;
                                                                       13
                                                                                return dst;
14 end
                                                                       15 end
```

4.2 8×32 Table Look Up

Convert the 8-bit string $\{X_i\}_{i=0}^{15} (X_i \in \{0, 1\}^8)$ into a 32-bit string $\{W_i\}_{i=0}^3 (W_i \in \{0, 1\}^{32})$ as follows:

$$W_i := (X_{4i} \ll 24) \parallel (X_{4i+1} \ll 16) \parallel (X_{4i+2} \ll 8) \parallel (X_{4i+3}) \in \{0, 1\}^{32}$$

for i = 0, 1, 2, 3. In other words,

X_0	$(W_0 \gg 0x18) \& 0xff$	X_4	$(W_1 \gg 0 \text{x} 18) \& 0 \text{x} ff$
X_1	$(W_0 \gg 0 \text{x} 10) \& 0 \text{x} ff$	X_5	$(W_1 \gg 0 \text{x} 10) \& 0 \text{x} \text{ff}$
X_2	$(W_0 \gg 0x08) \& 0xff$	X_6	$(W_1 \gg 0 \times 0 \times 0 \times 0 \times 1)$ & 0xff
X_3	(W_0) & $0xff$	X_7	(W_1) & $0xff$
X_8	$(W_2 \gg 0 \text{x} 18) \& 0 \text{x} ff$	X_{12}	$(W_3 \gg 0 \text{x} 18) \& 0 \text{x} ff$
<i>X</i> ₉	$(W_2 \gg 0 \text{x} 10) \& 0 \text{x} \text{ff}$	X_{13}	$(W_3 \gg 0 \text{x} 10) \& 0 \text{x} \text{ff}$
X_{10}	$(W_2 \gg 0 \times 0$	X_{14}	$(W_3 \gg 0 \times 0 \times 0 \times 0 \times 0 \times 1 \times 0 \times 1 \times 0 \times 1 \times 0 \times 1 \times 0 \times 0$
X_{11}	(W_2) & $0xff$	X_{15}	(W_3) & $0xff$

Note that

X_0	X_1	X_2	X_3	X_4	X_5	X_6	X_7	X_8	X_9	X_{10}	X_{11}	X_{12}	X_{13}	X_{14}	X_{15}
	V	V_0			V	V_1				W_2			V	V_3	

```
Algorithm 10: SubMix and InvSubInvMix
  Input: (W_0, W_1, \overline{W_2, W_3}) \in \{0, 1\}^{128 = 32 \times 4}
                                                                     Input: (W_0, W_1, W_2, W_3) \in \{0, 1\}^{128 = 32 \times 4}
                                                                     Output: (U_0, U_1, U_2, U_3) \in \{0, 1\}^{128 = 32 \times 4}
  Output: (V_0, V_1, V_2, V_3) \in \{0, 1\}^{128 = 32 \times 4}
1 Function SubMix:
                                                                  1 Function InvSubInvMix:
                                                                          for i \leftarrow 0 to 3 do
       for i \leftarrow 0 to 3 do
            V_i \leftarrow Te_0 ((W_i \gg 0x18) \& 0xff)
                                                                               U_i \leftarrow Td_0 ((W_i \gg 0x18) \& 0xff)
3
                                                                   3
                                                                                     \bigoplus_{32} Td_1 ((W_i \gg 0x10) \& 0xff)
                  \bigoplus_{32} Te_1 ((W_i \gg 0x10) \& 0xff)
4
                                                                   4
                  \bigoplus_{32} Te_2 ((W_i \gg 0x08) \& 0xff)
                                                                                     \bigoplus_{32} Td_2 ((W_i \gg 0x08) \& 0xff)
                                                                   5
5
                  \bigoplus_{32} Te_3(W_i \& 0xff);
                                                                                     \bigoplus_{32} Td_3(W_i \& 0xff);
                                                                   6
6
       end
                                                                          end
                                                                   7
7
       return (V_0, V_1, V_2, V_3);
                                                                          return (U_0, U_1, U_2, U_3);
                                                                   8
9 end
                                                                  9 end
```

4.3 Generation of 8×32 Tables

Note that

$$\begin{pmatrix} V_0 & V_4 & V_8 & V_{12} \\ V_1 & V_5 & V_9 & V_{13} \\ V_2 & V_6 & V_{10} & V_{14} \\ V_3 & V_7 & V_{11} & V_{15} \end{pmatrix} = \operatorname{SubMix} \begin{pmatrix} \begin{pmatrix} X_0 & X_4 & X_8 & X_{12} \\ X_1 & X_5 & X_9 & X_{13} \\ X_2 & X_6 & X_{10} & X_{14} \\ X_3 & X_7 & X_{11} & X_{15} \end{pmatrix} := \\ \begin{pmatrix} 0 \times 02 & 0 \times 03 & 0 \times 01 & 0 \times 01 \\ 0 \times 01 & 0 \times 02 & 0 \times 03 & 0 \times 01 \\ 0 \times 01 & 0 \times 02 & 0 \times 03 & 0 \times 01 \end{pmatrix} \begin{pmatrix} s(X_0) & s(X_4) & s(X_8) & s(X_{12}) \\ s(X_1) & s(X_5) & s(X_9) & s(X_{13}) \\ s(X_2) & s(X_6) & s(X_{10}) & s(X_{14}) \\ s(X_3) & s(X_7) & s(X_{11}) & s(X_{15}) \end{pmatrix}'$$

$$\begin{pmatrix} U_0 & V_4 & U_8 & U_{12} \\ U_1 & V_5 & U_9 & U_{13} \\ U_2 & V_6 & U_{10} & U_{14} \\ U_3 & V_7 & U_{11} & U_{15} \end{pmatrix} = \operatorname{InvSubInvMix} \begin{pmatrix} \begin{pmatrix} X_0 & X_4 & X_8 & X_{12} \\ X_1 & X_5 & X_9 & X_{13} \\ X_2 & X_6 & X_{10} & X_{14} \\ X_3 & X_7 & X_{11} & X_{15} \end{pmatrix} := \\ \begin{pmatrix} 0 \times 0e & 0 \times 0b & 0 \times 0d & 0 \times 09 \\ 0 \times 09 & 0 \times 0e & 0 \times 0b & 0 \times 0d \\ 0 \times 0d & 0 \times 09 & 0 \times 0e & 0 \times 0b \end{pmatrix} \begin{pmatrix} s^{-1}(X_0) & s^{-1}(X_4) & s^{-1}(X_8) & s^{-1}(X_{12}) \\ s^{-1}(X_1) & s^{-1}(X_5) & s^{-1}(X_{10}) & s^{-1}(X_{14}) \\ s^{-1}(X_3) & s^{-1}(X_7) & s^{-1}(X_{11}) & s^{-1}(X_{14}) \end{pmatrix}.$$

Then

$$\begin{pmatrix} V_{4i} \\ V_{4i+1} \\ V_{4i+2} \\ V_{4i+3} \end{pmatrix} = \begin{pmatrix} 0 \times 02 & 0 \times 03 & 0 \times 01 & 0 \times 01 \\ 0 \times 01 & 0 \times 02 & 0 \times 03 & 0 \times 01 \\ 0 \times 01 & 0 \times 01 & 0 \times 02 & 0 \times 03 \\ 0 \times 03 & 0 \times 01 & 0 \times 01 & 0 \times 02 \end{pmatrix} \begin{pmatrix} s(X_{4i}) \\ s(X_{4i+1}) \\ s(X_{4i+2}) \\ s(X_{4i+3}) \end{pmatrix}$$

$$= s(X_{4i}) \begin{pmatrix} 0 \times 02 \\ 0 \times 01 \\ 0 \times 01 \\ 0 \times 03 \end{pmatrix} \oplus_{32} s(X_{4i+1}) \begin{pmatrix} 0 \times 03 \\ 0 \times 02 \\ 0 \times 01 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+2}) \begin{pmatrix} 0 \times 01 \\ 0 \times 03 \\ 0 \times 02 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+3}) \begin{pmatrix} 0 \times 01 \\ 0 \times 03 \\ 0 \times 02 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+3}) \begin{pmatrix} 0 \times 01 \\ 0 \times 03 \\ 0 \times 02 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+3}) \begin{pmatrix} 0 \times 01 \\ 0 \times 03 \\ 0 \times 02 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+3}) \begin{pmatrix} 0 \times 01 \\ 0 \times 03 \\ 0 \times 02 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+3}) \begin{pmatrix} 0 \times 01 \\ 0 \times 03 \\ 0 \times 02 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+3}) \begin{pmatrix} 0 \times 01 \\ 0 \times 03 \\ 0 \times 02 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+3}) \begin{pmatrix} 0 \times 01 \\ 0 \times 03 \\ 0 \times 02 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+3}) \begin{pmatrix} 0 \times 01 \\ 0 \times 03 \\ 0 \times 02 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+3}) \begin{pmatrix} 0 \times 01 \\ 0 \times 03 \\ 0 \times 02 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+3}) \begin{pmatrix} 0 \times 01 \\ 0 \times 04 \\ 0 \times 04 \\ 0 \times 04 \\ 0 \times 04 \end{pmatrix} \oplus_{32} s(X_{4i+3}) \begin{pmatrix} 0 \times 01 \\ 0 \times 04 \\ 0$$

We define $Te_i/Td_i: \{0,1\}^8 \to \{0,1\}^{32} (i \in \{0,1,2,3\})$ as follows:

$$Te_{0}(X) := \begin{pmatrix} \mathbf{0} \times \mathbf{0} & 2 \otimes_{8} s(X) & s(X) & s(X) & s(X) & \mathbf{0} \times \mathbf{0} & 3 \otimes_{8} s(X) \end{pmatrix},$$

$$Te_{1}(X) := \begin{pmatrix} \mathbf{0} \times \mathbf{0} & 3 \otimes_{8} s(X) & \mathbf{0} \times \mathbf{0} & 2 \otimes_{8} s(X) & s(X)$$

and

$$\begin{split} Td_0(X) &:= \left(\ \mathbf{0x0e} \otimes_8 s^{-1}(X) \ , \ \mathbf{0x09} \otimes_8 s^{-1}(X) \ , \ \mathbf{0x0d} \otimes_8 s^{-1}(X) \ , \ \mathbf{0x0b} \otimes_8 s^{-1}(X) \ , \ \mathbf{0x0b} \otimes_8 s^{-1}(X) \ , \ \mathbf{0x0e} \otimes_8 s^{-1}(X) \ , \ \mathbf{0x09} \otimes_8 s^{-1}(X) \ , \ \mathbf{0x0d} \otimes_8 s^{-1}(X) \ , \ \mathbf{0x0d} \otimes_8 s^{-1}(X) \ , \ \mathbf{0x0e} \otimes$$

SubMix/InvSubInvMix : $\{0, 1\}^{128} \rightarrow \{0, 1\}^{128}$ are computed as follows:

SubMix
$$(W_0, W_1, W_2, W_3) := (V_0, V_1, V_2, V_3),$$

InvSubInvMix $(W_0, W_1, W_2, W_3) := (U_0, U_1, U_2, U_3)$

where
$$\begin{cases} W_0 \coloneqq X_0 \parallel X_1 \parallel X_2 \parallel X_3 \\ W_1 \coloneqq X_4 \parallel X_5 \parallel X_6 \parallel X_7 \\ W_2 \coloneqq X_8 \parallel X_9 \parallel X_{10} \parallel X_{11} \\ W_3 \coloneqq X_{12} \parallel X_{13} \parallel X_{14} \parallel X_{15} \end{cases} \qquad (W_i \in \{\textbf{0}, \textbf{1}\}^{32}) \text{ and}$$

$$V_0 \coloneqq Te_0(X_0) \quad \oplus_{32} \quad Te_1(X_1) \quad \oplus_{32} \quad Te_2(X_2) \quad \oplus_{32} \quad Te_3(X_3),$$

$$V_1 \coloneqq Te_0(X_4) \quad \oplus_{32} \quad Te_1(X_5) \quad \oplus_{32} \quad Te_2(X_6) \quad \oplus_{32} \quad Te_3(X_7),$$

$$V_2 \coloneqq Te_0(X_8) \quad \oplus_{32} \quad Te_1(X_9) \quad \oplus_{32} \quad Te_2(X_{10}) \quad \oplus_{32} \quad Te_3(X_{11}),$$

$$V_3 \coloneqq Te_0(X_{12}) \quad \oplus_{32} \quad Te_1(X_{13}) \quad \oplus_{32} \quad Te_2(X_{14}) \quad \oplus_{32} \quad Te_3(X_{15}),$$

$$U_0 \coloneqq Td_0(X_0) \quad \oplus_{32} \quad Td_1(X_1) \quad \oplus_{32} \quad Td_2(X_2) \quad \oplus_{32} \quad Td_3(X_3),$$

$$U_1 \coloneqq Td_0(X_4) \quad \oplus_{32} \quad Td_1(X_5) \quad \oplus_{32} \quad Td_2(X_6) \quad \oplus_{32} \quad Td_3(X_7),$$

$$U_2 \coloneqq Td_0(X_8) \quad \oplus_{32} \quad Td_1(X_9) \quad \oplus_{32} \quad Td_2(X_{10}) \quad \oplus_{32} \quad Td_3(X_{11}),$$

$$U_3 \coloneqq Td_0(X_{12}) \quad \oplus_{32} \quad Td_1(X_{13}) \quad \oplus_{32} \quad Td_2(X_{14}) \quad \oplus_{32} \quad Td_3(X_{15}).$$

4.4 Implementation of SubMix and InvSubInvMix

Code 4.1: SubMix

```
void SubMix(u8* state) {
1
       u32 temp[4];
2
3
       // temp[0] = Te0[state[ 0]] ^ Te1[state[ 1]] ^
4
5
                     Te2[state[ 2]] ^ Te3[state[ 3]];
       // temp[1] = Te0[state[ 4]] ^ Te1[state[ 5]] ^
6
7
                     Te2[state[ 6]] ^ Te3[state[ 7]];
       //
8
       // temp[2] = Te0[state[ 8]] ^ Te1[state[ 9]] ^
9
                     Te2[state[10]] ^ Te3[state[11]];
       // temp[3] = Te0[state[11]] ^ Te1[state[12]] ^
10
                     Te2[state[13]] ^ Te3[state[14]];
11
       //
12
       for (int i = 0; i < 4; i++) {
13
14
           temp[i] = Te0[state[4*i + 0]] ^
                      Te1[state[4*i + 1]] ^
15
16
                      Te2[state[4*i + 2]] ^
                      Te3[state[4*i + 3]];
17
18
       }
19
       for (int i = 0; i < 4; i++) {</pre>
20
21
           state[4*i + 0] = (temp[i] >> 0x18) & 0xff;
           state[4*i + 1] = (temp[i] >> 0x10) & 0xff;
22
23
           state[4*i + 2] = (temp[i] >> 0x08) & 0xff;
           state[4*i + 3] = temp[i] & 0xff;
24
25
       }
26
  }
```

Code 4.2: InvSubInvMix

```
void InvSubInvMix(u8* state) {
1
2
       u32 temp[4];
3
       for (int i = 0; i < 4; i++) {
4
5
            temp[i] = Td0[state[4*i + 0]] ^
                      Td1[state[4*i + 1]] ^
6
7
                      Td2[state[4*i + 2]] ^
                      Td3[state[4*i + 3]];
8
9
       }
10
       for (int i = 0; i < 4; i++) {
11
12
           state[4*i + 0] = (temp[i] >> 0x18) & 0xff;
13
           state[4*i + 1] = (temp[i] >> 0x10) & 0xff;
           state[4*i + 2] = (temp[i] >> 0x08) & 0xff;
14
15
           state[4*i + 3] = temp[i] & 0xff;
       }
16
17
   }
```

Chapter 5

32-bit AES

Code 5.1: SubWord applies the S-box to each byte of the input word

```
/* Table Annotation:
1
2
   | i | Shift | Mask
                            | Description
  |---|-----|------|------
3
  | 0 | 0x18 | 0xFF << 0x18 | Process most significant byte (1st) |
4
5
   | 1 | 0x10 | 0xFF \ll 0x10 | Process 2nd byte
  \mid 2 \mid 0x08 \mid 0xFF << 0x08\mid Process 3rd byte
7
   | 3 | 0x00 | 0xFF << 0x00 | Process least significant byte (4th)|
8
9
10
  u32 SubWord(u32* word) {
11
      u8 temp;
       for (int i = 0; i < 4; i++) {
12
           temp = Te3[(*word >> (0x18 - 0x08 * i)) & 0x000000ff];
13
           *word &= \sim (0xFF << (0x18 - 0x08 * i)); // Clear the byte
14
           *word |= (temp & 0x0000000ff) << (0x18 - 0x08 * i); // Set
15
              the new value
       }
16
  }
17
```

Code 5.2: SubWord applies the S-box to each byte of the input word

```
u32 SubWord(u32 word) {
1
2
       u8 temp0, temp1, temp2, temp3;
3
       // Process the most significant byte (1st byte)
4
       temp0 = Te3[(word >> 24) & 0x000000ff];
5
       word &= 0x00fffffff; // Clear the most significant byte
6
7
       word \mid = (temp0 & 0x000000ff) << 24; // Set the new value
8
9
       // Process the 2nd byte
10
       temp1 = Te3[(word >> 16) & 0x000000ff];
       word &= 0xff00ffff; // Clear the 2nd byte
11
       word \mid = (temp1 & 0x000000ff) << 16; // Set the new value
12
13
14
       // Process the 3rd byte
15
       temp2 = Te3[(word >> 8) & 0x000000ff];
       word &= 0xffff00ff; // Clear the 3rd byte
16
17
       word \mid = (temp2 & 0x000000ff) << 8; // Set the new value
18
       // Process the least significant byte (4th byte)
19
20
       temp3 = Te3[word & 0x000000ff];
       word &= 0xffffff00; // Clear the least significant byte
21
22
       word \mid = (temp3 & 0x000000ff); // Set the new value
23
24
       return word;
25
  }
```

Code 5.3: SubWord applies the S-box to each byte of the input word

Chapter 6

Base64 Encoding and Decoding

6.1 Introduction

Base64 encoding is a method of converting binary data into a set of 64 printable characters from the ASCII standard. This encoding is commonly used to encode data when there is a requirement to transmit binary data over media that are designed to deal with textual data. The Base64 index table consists of the characters A-Z, a-z, 0-9, plus two additional characters, commonly + and /, for a total of 64 characters.

6.2 Principles of Base64 Encoding

Base64 encoding processes data in blocks of 3 bytes (24 bits) at a time. Each block of 24 bits is then divided into four 6-bit groups. Each 6-bit group is used as an index into the Base64 character table, resulting in a 4-character encoding of the original 24-bit block.

Let the input stream be a sequence of bits represented by **b**. This stream is divided into blocks of 24 bits:

$$\mathbf{b} = b_1 b_2 b_3 \dots b_{24} b_{25} b_{26} \dots$$

Each block of 24 bits $(b_1b_2 \dots b_{24})$ is then split into four 6-bit groups:

$$\mathbf{g}_1 = b_1 b_2 \dots b_6$$
, $\mathbf{g}_2 = b_7 b_8 \dots b_{12}$, $\mathbf{g}_3 = b_{13} b_{14} \dots b_{18}$, $\mathbf{g}_4 = b_{19} b_{20} \dots b_{24}$

Each group \mathbf{g}_i is then converted into a decimal index n_i :

$$n_i = \sum_{k=0}^{5} g_{i,k} \cdot 2^{5-k}$$

where $g_{i,k}$ is the k-th bit of group \mathbf{g}_i .

Each index n_i is used to select a character from the Base64 table, forming the encoded string.

6.3 Principles of Base64 Decoding

Base64 decoding is the reverse process. Each character in the encoded string is mapped back to its corresponding 6-bit group. These groups are then concatenated to form the original byte sequence.

Given a Base64 encoded string, each character is converted back into a 6-bit group according to the Base64 index table. Let these groups be \mathbf{d}_1 , \mathbf{d}_2 , \mathbf{d}_3 , \mathbf{d}_4 . The original 24-bit block is reconstructed by concatenating these groups:

$$\mathbf{b'} = \mathbf{d}_1 \mathbf{d}_2 \mathbf{d}_3 \mathbf{d}_4$$

The binary sequence \mathbf{b}' is then divided back into the original bytes to retrieve the original data.

6.4 Padding in Base64 Encoding

In cases where the input byte sequence is not a multiple of 3, padding is used. The input is padded with zeros to form a complete 24-bit block. The corresponding Base64 encoded output is then padded with the '=' character to indicate that padding was used. The number of '=' characters used indicates the number of bytes that were added as padding (one byte of padding results in two '=' characters, and two bytes of padding results in one '=' character).

Appendix A

Additional Data A

A.1 Substitution-BOX

```
static const u8 s_box[256] = {
2
       0x63, 0x7c, 0x77, 0x7b, 0xf2, 0x6b, 0x6f, 0xc5,
       0x30, 0x01, 0x67, 0x2b, 0xfe, 0xd7, 0xab, 0x76,
3
4
       0xca, 0x82, 0xc9, 0x7d, 0xfa, 0x59, 0x47, 0xf0,
5
       0xad, 0xd4, 0xa2, 0xaf, 0x9c, 0xa4, 0x72, 0xc0,
       0xb7, 0xfd, 0x93, 0x26, 0x36, 0x3f, 0xf7, 0xcc,
7
       0x34, 0xa5, 0xe5, 0xf1, 0x71, 0xd8, 0x31, 0x15,
       0x04, 0xc7, 0x23, 0xc3, 0x18, 0x96, 0x05, 0x9a,
8
       0x07, 0x12, 0x80, 0xe2, 0xeb, 0x27, 0xb2, 0x75,
9
       0x09, 0x83, 0x2c, 0x1a, 0x1b, 0x6e, 0x5a, 0xa0,
10
       0x52, 0x3b, 0xd6, 0xb3, 0x29, 0xe3, 0x2f, 0x84,
11
                   0x00, 0xed, 0x20, 0xfc, 0xb1, 0x5b,
12
       0x53, 0xd1,
       0x6a, 0xcb,
                   0xbe, 0x39, 0x4a, 0x4c, 0x58, 0xcf,
13
       0xd0, 0xef, 0xaa, 0xfb, 0x43, 0x4d, 0x33, 0x85,
14
15
       0x45, 0xf9, 0x02, 0x7f, 0x50, 0x3c, 0x9f, 0xa8,
16
       0x51, 0xa3, 0x40, 0x8f, 0x92, 0x9d, 0x38, 0xf5,
       0xbc, 0xb6, 0xda, 0x21, 0x10, 0xff, 0xf3, 0xd2,
17
       0xcd, 0x0c, 0x13, 0xec, 0x5f, 0x97, 0x44, 0x17,
18
       0xc4, 0xa7, 0x7e, 0x3d, 0x64, 0x5d, 0x19, 0x73,
19
       0x60, 0x81, 0x4f, 0xdc, 0x22, 0x2a, 0x90, 0x88,
20
       0x46, 0xee, 0xb8, 0x14, 0xde, 0x5e, 0x0b, 0xdb,
21
22
       0xe0, 0x32, 0x3a, 0x0a, 0x49, 0x06, 0x24, 0x5c,
       0xc2, 0xd3, 0xac, 0x62, 0x91, 0x95, 0xe4, 0x79,
23
       0xe7, 0xc8, 0x37, 0x6d, 0x8d, 0xd5, 0x4e, 0xa9,
24
25
       0x6c, 0x56, 0xf4, 0xea, 0x65, 0x7a, 0xae, 0x08,
       0xba, 0x78, 0x25, 0x2e, 0x1c, 0xa6, 0xb4, 0xc6,
26
       0xe8, 0xdd, 0x74, 0x1f, 0x4b, 0xbd, 0x8b, 0x8a,
27
       0x70, 0x3e, 0xb5, 0x66, 0x48, 0x03, 0xf6, 0x0e,
28
29
       0x61, 0x35, 0x57, 0xb9, 0x86, 0xc1, 0x1d, 0x9e,
       0xe1, 0xf8, 0x98, 0x11, 0x69, 0xd9, 0x8e, 0x94,
30
                   0x87, 0xe9, 0xce, 0x55, 0x28, 0xdf,
       0x9b, 0x1e,
31
       0x8c, 0xa1, 0x89, 0x0d, 0xbf, 0xe6, 0x42, 0x68,
32
       0x41, 0x99, 0x2d, 0x0f, 0xb0, 0x54, 0xbb, 0x16
33
   };
```

```
static const u8 inv_s_box[256] = {
2
       0x52, 0x09, 0x6a, 0xd5, 0x30, 0x36, 0xa5, 0x38,
3
       0xbf, 0x40, 0xa3, 0x9e, 0x81, 0xf3, 0xd7, 0xfb,
                   0x39, 0x82, 0x9b, 0x2f, 0xff, 0x87,
4
       0x7c, 0xe3,
5
       0x34, 0x8e, 0x43, 0x44, 0xc4, 0xde, 0xe9, 0xcb,
       0x54, 0x7b, 0x94, 0x32, 0xa6, 0xc2, 0x23, 0x3d,
6
7
       Oxee, 0x4c, 0x95, 0x0b, 0x42, 0xfa, 0xc3, 0x4e,
       0x08, 0x2e, 0xa1, 0x66, 0x28, 0xd9, 0x24, 0xb2,
8
9
       0x76, 0x5b, 0xa2, 0x49, 0x6d, 0x8b, 0xd1, 0x25,
       0x72, 0xf8, 0xf6, 0x64, 0x86, 0x68, 0x98, 0x16,
10
                   0x5c, 0xcc, 0x5d, 0x65, 0xb6, 0x92,
11
       0xd4, 0xa4,
       0x6c, 0x70, 0x48, 0x50, 0xfd, 0xed, 0xb9, 0xda,
12
       0x5e, 0x15, 0x46, 0x57, 0xa7, 0x8d, 0x9d, 0x84,
13
                   0xab, 0x00, 0x8c, 0xbc, 0xd3, 0x0a,
14
       0x90, 0xd8,
       0xf7, 0xe4, 0x58, 0x05, 0xb8, 0xb3, 0x45, 0x06,
15
       0xd0, 0x2c, 0x1e, 0x8f, 0xca, 0x3f, 0x0f, 0x02,
16
17
       0xc1, 0xaf, 0xbd, 0x03, 0x01, 0x13, 0x8a, 0x6b,
       0x3a, 0x91, 0x11, 0x41, 0x4f, 0x67, 0xdc, 0xea,
18
19
       0x97, 0xf2, 0xcf, 0xce, 0xf0, 0xb4, 0xe6, 0x73,
       0x96, 0xac,
                   0x74, 0x22, 0xe7, 0xad, 0x35, 0x85,
20
       0xe2, 0xf9, 0x37, 0xe8, 0x1c, 0x75, 0xdf, 0x6e,
21
       0x47, 0xf1, 0x1a, 0x71, 0x1d, 0x29, 0xc5, 0x89,
22
23
       0x6f, 0xb7, 0x62, 0x0e, 0xaa, 0x18, 0xbe, 0x1b,
24
       0xfc, 0x56, 0x3e, 0x4b, 0xc6, 0xd2, 0x79, 0x20,
       0x9a, 0xdb, 0xc0, 0xfe, 0x78, 0xcd, 0x5a, 0xf4,
25
       0x1f, 0xdd, 0xa8, 0x33, 0x88, 0x07, 0xc7, 0x31,
26
       0xb1, 0x12, 0x10, 0x59, 0x27, 0x80, 0xec, 0x5f,
27
       0x60, 0x51, 0x7f, 0xa9, 0x19, 0xb5, 0x4a, 0x0d,
28
       0x2d, 0xe5, 0x7a, 0x9f, 0x93, 0xc9, 0x9c, 0xef,
29
       0xa0, 0xe0, 0x3b, 0x4d, 0xae, 0x2a, 0xf5, 0xb0,
30
31
       0xc8, 0xeb, 0xbb, 0x3c, 0x83, 0x53, 0x99, 0x61,
       0x17, 0x2b, 0x04, 0x7e, 0xba, 0x77, 0xd6, 0x26,
32
       0xe1, 0x69, 0x14, 0x63, 0x55, 0x21, 0x0c, 0x7d
33
34
   };
```