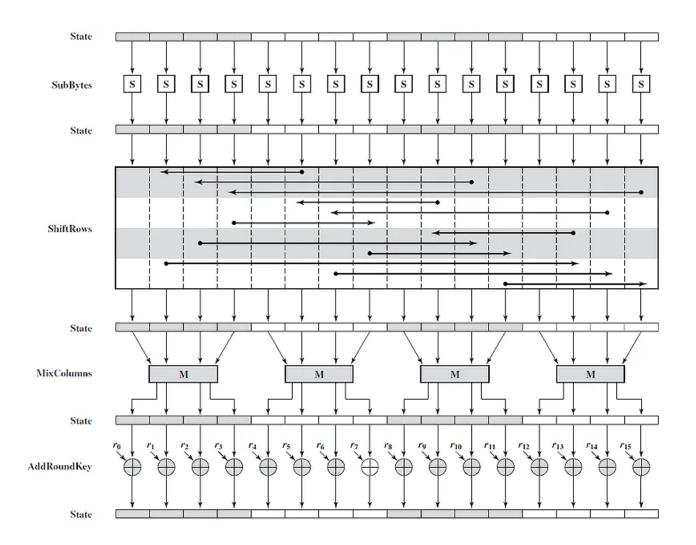
C | SecureAES

- High-Performance AES Encryption in C -

Ji Yong-Hyeon



Department of Information Security, Cryptology, and Mathematics

College of Science and Technology Kookmin University

September 18, 2024

Acknowledgements

Note (**XOR Operation and Modular Reduction in** $GF(2^n)$). In the context of Galois Field $GF(2^n)$, particularly in binary polynomial arithmetic, the XOR operation is equivalent to addition and also plays a crucial role in modular reduction. We explore this equivalence through the principles of field theory and polynomial arithmetic.

• Field Properties:

A Galois Field, $GF(p^n)$, is a finite field that contains a finite number of elements, where

- p is a prime number (base of the field) and
- n is a positive integer (degree of the field).

For the binary field $GF(2^n)$, p = 2, which implies that every element in this field is either 0 or 1.

• Addition in $GF(2^n)$:

In $GF(2^n)$, the addition of two elements is performed modulo 2. For any two elements $a, b \in GF(2^n)$, the addition is defined as:

$$a + b = a \oplus b$$

Since 2 is the base of the field, the addition wraps around upon reaching 2, which is effectively what the XOR operation does.

• Polynomial Representation:

Elements in $GF(2^n)$ can be represented as polynomials where each coefficient is in $GF(2) = \{0,1\}$. A general element can be written as:

$$a(x) = a_{n-1}x^{n-1} + a_{n-2}x^{n-2} + \dots + a_1x + a_0$$

where $a_i \in \{0, 1\}$ for all i.

• Modular Reduction:

Modular reduction in $GF(2^n)$ involves reducing a polynomial by a fixed irreducible polynomial of degree n, ensuring that the result remains within the field. Let m(x) be the irreducible polynomial. The reduction of a polynomial f(x) is given by: $f(x) \mod m(x)$

• XOR as Modular Reduction:

During modular reduction, the subtraction used in polynomial division becomes XOR, because subtraction and addition are the same in GF(2). Therefore, reducing a polynomial f(x) by m(x) is effectively performed using XOR on the coefficients of corresponding terms.

For example, if f(x) has a term x^k where $k \ge n$, and m(x) has a term x^k , then reducing f(x) by m(x) involves XORing the coefficients of x^k in f(x) and m(x), effectively eliminating the x^k term in f(x).

In summary, the XOR operation becomes equivalent to both addition and modular reduction in $GF(2^n)$ due to the binary nature of the field. This equivalence simplifies polynomial arithmetic in binary fields, making it a cornerstone of operations in cryptographic algorithms.

Contents

| 1 | Bloc | k Cipher | |
|---|------|---|------------|
| | 1.1 | Definition and Structure | |
| | 1.2 | Modes of Operations | |
| | | 1.2.1 Padding | 2 |
| | | 1.2.2 ECB (Electronic CodeBook) | 3 |
| | | 1.2.3 CBC (Cipher Block Chaining) | 4 |
| | | 1.2.4 OFB (Output FeedBack) | 5 |
| | | 1.2.5 CFB (Ciphertext FeedBack) | 5 |
| | | 1.2.6 CTR (CounTeR) | |
| | | 1.2.7 CBC - CS (Ciphertext Stealing) | |
| 2 | AES | Algorithm | 7 |
| | | | |
| 3 | AES | | |
| | 3.1 | Overview of AES-128 | |
| | 3.2 | Functions and Constants used in AES | |
| | | 3.2.1 Key Expansion | |
| | | 3.2.2 AddRoundKey | |
| | | 3.2.3 SubBytes / InvSubBytes | |
| | | 3.2.4 ShiftRows / InvShiftRows | |
| | | 3.2.5 MixColumns / InvMixColumns | 18 |
| 4 | AES | - 128 / 192 / 256 (Byte Version) | 2 3 |
| | 4.1 | Specification | 23 |
| | 4.2 | Key Expansion (General Version) | |
| | 4.3 | 8-bit AES - 128 / 192 / 256 | 27 |
| 5 | Pre- | Computation using SubMix | 29 |
| | 5.1 | SubMix and InvSubInvMix | |
| | 5.2 | 8×32 Table Look Up | |
| | 5.3 | Generation of 8 × 32 Tables | |
| | 5.4 | Implementation of SubMix and InvSubInvMix | |
| 6 | 32-b | t AES | 34 |
| Δ | Δdd | tional Data A | 26 |
| | | Substitution-ROX | 36 |
| | | | |

Chapter 1

Block Cipher

Block ciphers are a fundamental component in cryptographic systems. They transform fixedsize blocks of plaintext into ciphertext using a symmetric key. The transformation is designed to be reversible only with knowledge of the key.

1.1 Definition and Structure

- Secure Pseudo-Random Permutation (PRP) and Substitution Groups:
 - Definition: A block cipher is considered a secure PRP if it is indistinguishable from a random permutation of the input bits, making it resistant to cryptanalysis.
 - Substitution Groups: Block ciphers often use substitution-permutation networks (SPNs) that include substitution groups. These groups perform non-linear transformations, crucial for creating cryptographic strength.
- Confidentiality for Fixed n-bit Data (Blocks):
 - Fixed Block Size: Block ciphers encrypt and decrypt data in fixed-size blocks (commonly 64 or 128 bits). This fixed size is crucial for the algorithm's structure and security.
 - **Padding Schemes:** When the data doesn't fit perfectly into a block, padding schemes are used to fill the remaining space, ensuring consistent block sizes.
- Block Cipher Operation Modes for Variable-Length Data:
 - Mode of Operation: To handle variable-length data, block ciphers use different modes of operation like CBC (Cipher Block Chaining), CFB (Cipher Feedback), and GCM (Galois/Counter Mode).
 - **Ensuring Security:** Each mode offers distinct features for security and efficiency, often enhancing the cipher's resistance to various attack vectors.
- Advantages Over Asymmetric Key Cryptography:
 - **High-Speed Computation:** Block ciphers are generally faster and require less computational power compared to asymmetric key cryptography.
 - **Suitability:** This makes them suitable for encrypting large volumes of data and in environments with limited resources.

• Deriving Other Cryptographic Functions:

- Versatility: Block ciphers can be used to design other cryptographic functions like hash functions, message authentication codes (MACs), and random number generators.
- Construction Techniques: Techniques like Cipher Block Chaining-MAC (CBC-MAC) and Counter mode (CTR) are examples of how block ciphers can be adapted for these purposes.

Block ciphers are a critical element in the cryptographic landscape, providing a versatile and efficient means for securing digital data. Their adaptability and robustness make them an indispensable tool in the design of secure communication protocols and cryptographic systems.

1.2 Modes of Operations

| | | Table 1.1. | Comparison | of Modes | | | |
|----------|-----------|----------------|------------|------------|---------|----|---------------------------|
| Mode | Integrity | Authentication | EncryptBlk | DecryptBlk | Padding | IV | $ P \stackrel{?}{=} C $ |
| ECB | O | Χ | O | O | O | X | P < C |
| CBC | O | X | O | O | O | O | P < C |
| OFB | O | X | O | X | X | O | P = C |
| CFB | O | X | O | X | X | O | P = C |
| CTR | O | X | O | X | X | O | P = C |
| CBC – CS | O | X | O | O | X | O | P = C |

Table 1.1: Comparison of Modes

1.2.1 Padding

Block ciphers require input lengths to be a multiple of the block size. Padding is used to extend the last block of plaintext to the required length. Without proper padding, the encryption process may be insecure or infeasible.

There are several padding schemes used in practice, such as:

| Standard Name | Padding Method |
|----------------|--|
| PKCS#7 | Pad with bytes all the same value as the number of padding bytesdd dd 04 04 04 04 |
| ANSI X9.23 | Pad with zeros, last byte is the number of padding bytesdd dd dd dd dd dd dd dd dd 00 00 00 05 |
| ISO/IEC 7816-4 | First byte is '80' (hex), followed by zerosdd dd dd dd dd dd dd dd dd 80 00 00 00 00 |
| ISO 10126 | Pad with random bytes, last byte is the number of padding bytesdd dd dd dd dd dd dd dd dd 2e 49 1b c1 aa 06 |

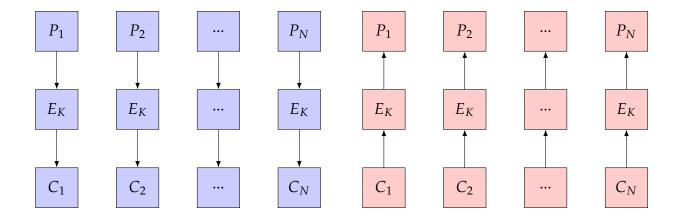
Table 1.2: Padding Standards in Block Ciphers

1.2.2 ECB (Electronic CodeBook)

Algorithm 1: Electronic CodeBook

```
Input: K \text{ and } P = P_1 \parallel \cdots \parallel P_N \ (P_i \in \{0,1\}^n)
Output: C = C_1 \parallel \cdots \parallel C_N \ (C_i \in \{0,1\}^n)
Output: P = P_1 \parallel \cdots \parallel P_N \ (P_i \in \{0,1\}^n)

1 for i \leftarrow 1 to N do
2 C_i \leftarrow \text{EncryptBlk}(K, P_i);
2 end
3 end
4 return C = C_1 \parallel \cdots \parallel C_N;
Input: C_i \leftarrow C_i \parallel \cdots \parallel C_i \leftarrow C_i \leftarrow C_i \leftarrow C_i \parallel \cdots \parallel C_i \leftarrow C
```



Remark 1.1.

(1) For a pair of plaintext/ciphertext (P, C) and (P', C'),

$$P = P' \implies C = C'$$
.

- (2) A single-bit error in the ciphertext affects only the corresponding block in the decryption.
- (3) Block order changes, as well as additions/deletions, are possible. Therefore, to ensure the integrity of the ciphertext (i.e., detection or prevention of tampering), it should be used in conjunction with a checksum or a Message Authentication Code (MAC).

CBC (Cipher Block Chaining)

Algorithm 2: Cipher Block Chaining

Input: K, IV and $P = P_1 \parallel \cdots \parallel P_N$ Output: $C = C_1 \parallel \cdots \parallel C_N$

1 C_0 ← IV;

2 for $i \leftarrow 1$ to N do

 $C_i \leftarrow \mathsf{EncryptBlk}(K, P_i \oplus C_{i-1});$

4 end

5 **return** $C = C_1 \| \cdots \| C_N$;

Input: K, IV and $C = C_1 \parallel \cdots \parallel C_N$ Output: $P = P_1 \parallel \cdots \parallel P_N$

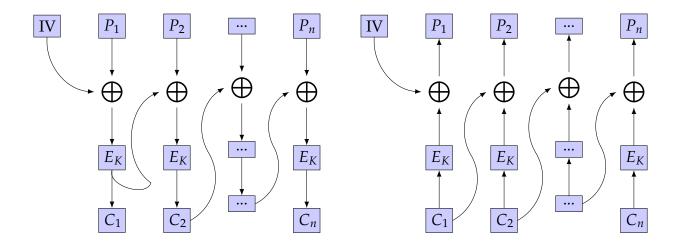
1 C_0 ← IV;

2 for $i \leftarrow 1$ to N do

 $P_i \leftarrow C_{i-1} \oplus \mathsf{DecryptBlk}(K, C_i);$

4 end

5 **return** $P = P_1 || \cdots || P_N;$



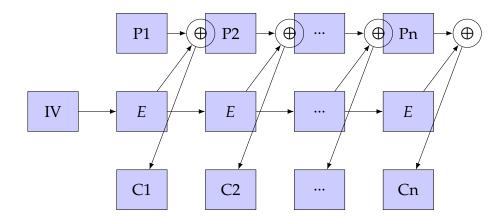
Remark 1.2.

(1) For a set of plaintext/ciphertext pairs (IV, P, C) and (IV', P', C'),

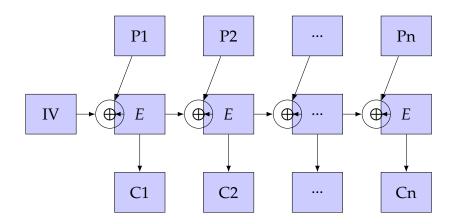
$$IV = IV' \wedge P = P' \implies C = C'.$$

- (2) A one-bit error in the ciphertext will affect the corresponding block and the subsequent block in the decryption process, thereby enabling the detection of such errors.
- (3) Altering the order of blocks, as well as adding or deleting them, is not possible.

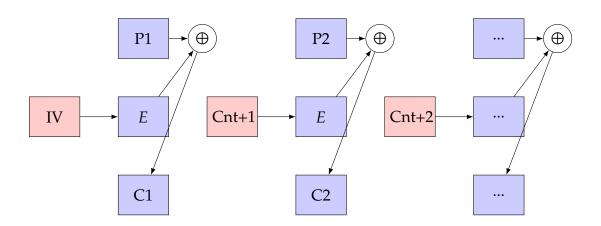
1.2.4 OFB (Output FeedBack)

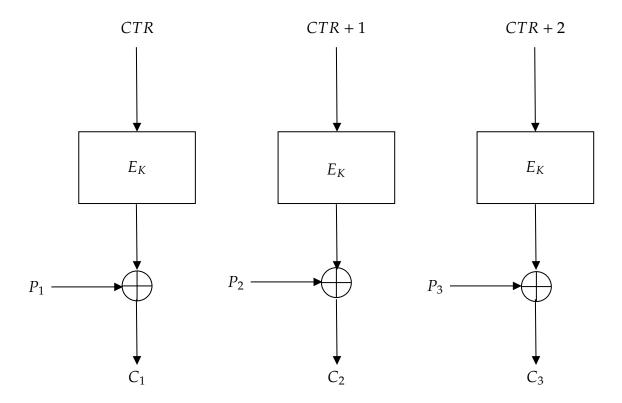


1.2.5 CFB (Ciphertext FeedBack)

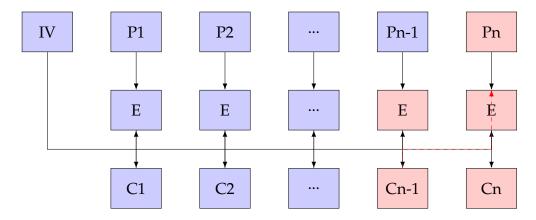


1.2.6 CTR (CounTeR)





1.2.7 CBC - CS (Ciphertext Stealing)



Chapter 2

AES Algorithm

Let
$$m(x) := x^8 + x^4 + x^3 + x + 1$$
.

$$GF(2^{8}) = GF(2)[x]/\langle x^{8} + x^{4} + x^{3} + x + 1 \rangle$$

$$= GF(2)[x]/\langle m(x) \rangle$$

$$= \left\{ b_{0} + b_{1}x + \dots + b_{6}x^{6} + b_{7}x^{7} + \langle m(x) \rangle : b_{0}, b_{1}, \dots, b_{6}, b_{7} \in GF(2) \right\}$$

$$= \left\{ \sum_{i=0}^{7} b_{i}x^{i} + \langle m(x) \rangle : b_{i} \in \{0, 1\} \right\}.$$

Let f(x), $g(x) \in GF(2^8)$, say,

$$f(x) = \sum_{i=0}^{7} a_i x^i + \langle m(x) \rangle, \quad g(x) = \sum_{i=0}^{7} b_j x^j + \langle m(x) \rangle.$$

Then

$$f(x) + g(x) = \sum_{i=0}^{7} (a_i + b_i)x^i + \langle m(x) \rangle = \sum_{i=0}^{7} (a_i \oplus b_i)x^i + \langle m(x) \rangle.$$

Here, \oplus : $GF(2) \times GF(2) \rightarrow GF(2)$. And

$$f(x) \cdot g(x) = m(x) \cdot q(x) + r(x).$$

Here $\deg r \leq 7$.

We define

Then

1.
$$f(x) = a_0 + a_1x + \cdots + a_6x^6 + a_7x^7$$

2.

$$x \cdot f(x) = a_0 x + a_1 x^2 + \dots + a_6 x^7 + a_7 x^8$$

$$= a_0 x + a_1 x^2 + \dots + a_6 x^7 + a_7 (x^4 + x^3 + x + 1) \quad \because x^8 \equiv x^4 + x^3 + x + 1 \pmod{m(x)}$$

$$= \begin{cases} \sum_{i=0}^6 a_i x^{i+1} + 0 & : a_7 = 0 \\ \sum_{i=0}^6 a_i x^{i+1} + (x^4 + x^3 + x + 1) & : a_7 = 1 \end{cases}$$

$$= \begin{cases} (f(x) \ll 1) & : a_7 = 0 \\ (f(x) \ll 1) \oplus \mathbf{0} \mathbf{x} \mathbf{1} \mathbf{b} & : a_7 = 1 \end{cases}$$

```
1 u8 GF256_xtime(u8 f) {
2    return (f & 0x80) ? (f << 1) ^ 0x1b : f << 1;
3 }
```

$$g(x) \cdot f(x) = \sum_{i=0}^{7} g(x)a_{i}x^{i}$$

$$= g(x)a_{0} + \sum_{i=1}^{7} g(x)a_{i}x^{i}$$

$$= g(x)a_{0} + x \sum_{i=1}^{7} g(x)a_{i}x^{i-1}$$

$$= g(x)a_{0} + x \left(g(x)a_{1} + \sum_{i=2}^{7} g(x)a_{i}x^{i-2}\right)$$

$$= g(x)a_{0} + x \left(g(x)a_{1} + x \left(g(x)a_{2} + \sum_{i=3}^{7} g(x)a_{i}x^{i-3}\right)\right)$$

$$= \cdots$$

$$= g(x)a_{0} + x(g(x)a_{1} + x(g(x)a_{2} + x(g(x)a_{3} + x(g(x)a_{4} + x(g(x)a_{5} + x(g(x)a_{6} + x(g(x)a_{7}))))))$$

That is,

$$\begin{array}{ccc}
x & \cdot 0 & +(g(x) \cdot a_7) \\
x & \cdot (g(x) \cdot a_7) & +(g(x) \cdot a_6) \\
x & \cdot (x \cdot (g(x) \cdot a_7) + (g(x) \cdot a_6)) & +(g(x) \cdot a_5)
\end{array}$$

Step 1. $x \cdot 0 + g(x) \cdot a_7$

```
Step 2. x \cdot (g(x) \cdot a_7) + (g(x) \cdot a_6)

Step 3. x \cdot (x \cdot (g(x) \cdot a_7) + (g(x) \cdot a_6)) + (g(x) \cdot a_5)

...

Final. g \cdot a_0 + x(g \cdot a_1 + \dots + x(g \cdot a_5 + x(g \cdot a_6 + x(g \cdot a_7))))
```

```
u8 GF256_mul(u8 f, u8 g) {
1
2
     u8 h = 0x00; // h = f * g
3
     u8 coef;
4
5
     for (i8 i = 7; i >= 0; i--) {
        coef = (f >> i) & 0x01; // Get the coefficient f_i
6
        7
8
9
     }
10
11
     return h;
12 }
```

```
1
   u8 GF256_MUL(u8 f, u8 g) {
       u8 h = 0;
2
       for (i8 = 0; i < 8; i++) {</pre>
3
            h = (g \& 1) * f;
4
5
            g >>= 1; // g = g / 2.
6
7
            u8 \text{ msb} = f \& 0x80;
                        // f = f * 2.
8
            f <<= 1;
9
            // Conditional XOR without branching.
            f = (0 - ((f \& 0x80) >> 7)) \& 0x1b; // (f \& 0x80) is the
10
               msb
       }
11
12
13
       return h;
14 }
```

Chapter 3

AES-128

3.1 Overview of AES-128

```
• KeyExpansion : \{0, 1\}^{128} \rightarrow \{0, 1\}^{1408=4 \cdot (10+1) \cdot 32}.
```

- AddRoundKey: $\{0, 1\}^{128} \times \{0, 1\}^{128} \rightarrow \{0, 1\}^{128}$.
- SubBytes/ShiftRows/MixColumns : $\{0, 1\}^{128} \rightarrow \{0, 1\}^{128}$.

Algorithm 3: Encryption of AES-128

```
Input: block \operatorname{src} \in \{0,1\}^{128}, round-keys \{rk_i\}_{i=0}^{11} (rk_i \in \{0,1\}^{128})

Output: block \operatorname{dst} \in \{0,1\}^{128}

1 t \leftarrow \operatorname{AddRoundKey(src}, rk_0);

2 \operatorname{for} i \leftarrow 1 \operatorname{to} 9 \operatorname{do}

3 | t \leftarrow (\operatorname{MixColumns} \circ \operatorname{ShiftRows} \circ \operatorname{SubBytes})(t);

4 | t \leftarrow \operatorname{AddRoundKey}(t, rk_i);

5 \operatorname{end}

6 t \leftarrow (\operatorname{ShiftRows} \circ \operatorname{SubBytes})(t);

7 t \leftarrow \operatorname{AddRoundKey}(t, rk_{10});

8 \operatorname{dst} \leftarrow t;

9 \operatorname{return} \operatorname{dst};
```

Algorithm 4: Decryption of AES-128

```
Input: block \operatorname{src} \in \{0, 1\}^{128}, round-keys \{rk_i\}_{i=0}^{11} (rk_i \in \{0, 1\}^{128})

Output: block \operatorname{dst} \in \{0, 1\}^{128}

1 t \leftarrow \operatorname{AddRoundKey(src}, rk_{10});

2 \operatorname{for} i \leftarrow 9 \operatorname{to} 1 \operatorname{do}

3 | t \leftarrow (\operatorname{InvSubBytes} \circ \operatorname{InvShiftRows})(t);

4 | t \leftarrow \operatorname{AddRoundKey}(t, rk_i);

5 | t \leftarrow \operatorname{InvMixColumns}(t);

6 \operatorname{end}

7 t \leftarrow (\operatorname{InvShiftRows} \circ \operatorname{InvSubBytes})(t);

8 t \leftarrow \operatorname{AddRoundKey}(t, rk_0);

9 \operatorname{dst} \leftarrow t;

10 \operatorname{return} \operatorname{dst};
```

3.2 Functions and Constants used in AES

3.2.1 Key Expansion

• RotWord : $\{0, 1\}^{32} \to \{0, 1\}^{32}$ is defined by

```
RotWord (X_0 \parallel X_1 \parallel X_2 \parallel X_3) := X_1 \parallel X_2 \parallel X_3 \parallel X_0 \text{ for } X_i \in \{0, 1\}^8.
```

Code 3.1: RotWord rotates the input word left by one byte

```
1 u32 RotWord(u32 word) {
2 return (word << 0x08) | (word >> 0x18);
3 }
```

• SubWord : $\{0,1\}^{32} \to \{0,1\}^{32}$ is defined by

```
SubWord(X_0 \parallel X_1 \parallel X_2 \parallel X_3) := s(X_0) \parallel s(X_1) \parallel s(X_2) \parallel s(X_3) for X_i \in \{0, 1\}^8.
```

Here, $s: \{0, 1\}^8 \to \{0, 1\}^8$ is the S-box.

Code 3.2: SubWord applies the S-box to each byte of the input word

• Round Constant rCon:

The constant $rCon_i \in \mathbb{F}_{2^8}$ used in generating the *i*-th round key corresponds to the value of x^{i-1} in the binary finite field \mathbb{F}_{2^8} and is as follows:

Code 3.3: rCon Array Declaration

```
1 static const u32 rCon[10] = {
2      0x01000000, 0x02000000, 0x04000000, 0x08000000,
3      0x10000000, 0x20000000, 0x40000000, 0x80000000,
4      0x1b000000, 0x36000000
5 };
```

Algorithm 5: Key Schedule (AES-128)

```
Input: User key uk = (uk_0, ..., uk_{15}) (uk_i \in \{0, 1\}^8);   // uk \in \{0, 1\}^{128} is 16-byte
    Output: round-keys \{rk_i\}_{i=0}^{43} (rk_i \in \{0, 1\}^{32}); // \{rk_i\}_{i=0}^{43} \in \{0, 1\}^{1408} is 176-byte
 1 \ rk_0 \leftarrow uk_0 \parallel uk_1 \parallel uk_2 \parallel uk_3;
 2 rk_1 \leftarrow uk_4 \parallel uk_5 \parallel uk_6 \parallel uk_7;
 3 rk_2 \leftarrow uk_8 \parallel uk_9 \parallel uk_{10} \parallel uk_{11};
 4 \ rk_3 \leftarrow uk_{12} \parallel uk_{13} \parallel uk_{14} \parallel uk_{15};
 5 for i = 4 to 43 do
          t \leftarrow rk_{i-1};
          if i \mod 4 = 0 then
               /* SubWord \circ RotWord : \{0, 1\}^{32} \rightarrow \{0, 1\}^{32}
                                                                                                                                                   */
               t \leftarrow \text{RotWord}(t);
 8
               t \leftarrow \text{SubWord}(t);
               t \leftarrow t \oplus (rCon_{i/4} \parallel 0x00 \parallel 0x00 \parallel 0x00);
10
          end
11
          rk_i \leftarrow rk_{i-4} \oplus_{32} t;
13 end
```

Code 3.4: AES-128 Key Expansion

```
void KeyExpansion(const u8* uKey, u32* rKey) {
1
2
       u32 temp;
       int i = 0;
3
4
5
       // Copy the input key to the first round key
       while (i < 4) {
6
7
            rKey[i] = (u32)uKey[4*i] << 0x18
8
            (u32)uKey[4*i+1] << 0x10
9
            (u32)uKey[4*i+2] << 0x08
            (u32)uKey[4*i+3];
10
            i++;
11
       }
12
13
       i = 4;
14
15
       // Generate the remaining round keys
16
       while (i < 44) {</pre>
17
            temp = rKey[i-1];
18
            if (i % 4 == 0) {
19
                temp = SubWord(RotWord(temp)) ^ rCon[i/4-1];
20
21
            rKey[i] = rKey[i-4] \wedge temp;
22
23
            i++;
24
       }
25
   }
```

CHAPTER 3. AES-128

3.2.2 AddRoundKey

14

• AddRoundKey: $\{0, 1\}^{128} \times \{0, 1\}^{128} \to \{0, 1\}^{128}$ is defined by $\text{AddRoundKey}\left(\{X_i\}_{i=0}^{15}, \{rk_i\}_{i=0}^3\right) := \{X_i \oplus_8 uk_i\}_{i=0}^{15}.$

Code 3.5: AES AddRoundKey

```
void AddRoundKey(u8* state, const u32* rKey) {
1
      for (int i = 0; i < AES_BLOCK_SIZE; i++) {</pre>
2
3
          // i = 0, 1, 2, 3 => wordIndex = 0
          // i = 4, 5, 6, 7 \Rightarrow wordIndex = 1
4
          // i = 8, 9, 10, 11 => wordIndex = 2
          // i = 12, 13, 14, 15 => wordIndex = 3
6
7
          int wordIndex = i / 4;
          // i = 0, 1, 2, 3 => bytePosition = 0,
9
10
          // i = 4, 5, 6, 7 => bytePosition = 0, 1, 2,
          // i = 8, 9, 10, 11 => bytePosition = 0, 1, 2,
11
          // i = 12, 13, 14, 15 => bytePosition = 0, 1, 2,
12
          int bytePosition = i % 4;
13
14
15
     16
17
                      | 0
| 1
                                      | rKey[0] >> 0x18
18
                                      | rKey[0] >> 0x10
19
                        | 2
20
                                      | rKey[0] >> 0x08
                                  | rKey[0]
                       | 3
21
22
                                 | rKey[1] >> 24
                       | 0
     | 4-7 | 1
23
                                      | rKey[1] >> 16
| rKey[1] >> 8
24
                        | 1
                       | 2
25
                  | 3 | rKey[1]
26
27
28
29
30
31
32
          u32 shiftedWord =
33
              rKey[wordIndex] >> (8 * (3 - bytePosition));
34
35
          u8 keyByte = shiftedWord & 0xFF;
          state[i] ^= keyByte;
37
38
  /* Extract the corresponding byte from the round key word */
39
  // state[i] ^{=} (rKey[i / 4] >> (8 * (3 - (i % 4)))) & 0xFF;
40
41
      }
42
  }
```

3.2.3 SubBytes / InvSubBytes

• SubBytes : $\{0, 1\}^{128} \to \{0, 1\}^{128}$ is defined by

SubBytes(
$$\{X_i\}_{i=0}^{15}$$
) = $\{s(X_i)\}_{i=0}^{15}$.

• InvSubBytes: $\{0, 1\}^{128} \rightarrow \{0, 1\}^{128}$ is defined by

SubBytes(
$$\{X_i\}_{i=0}^{15}$$
) = $\{s^{-1}(X_i)\}_{i=0}^{15}$.

Table 3.1: Substitution Box

| | 00 | 01 | 02 | 03 | 04 | 05 | 06 | 07 | 08 | 09 | 0a | 0b | 0c | 0d | 0e | 0f |
|----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 00 | 63 | 7c | 77 | 7b | f2 | 6b | 6f | c5 | 30 | 01 | 67 | 2b | fe | d7 | ab | 76 |
| 10 | ca | 82 | | | | | | | | | | | ••• | | ••• | |
| 30 | | | | | | | | | | | | | | | | |
| 40 | | | | | ••• | | | | | | | | ••• | | ••• | |
| 50 | | | ••• | ••• | ••• | | ••• | ••• | ••• | ••• | ••• | ••• | ••• | | ••• | |
| 60 | | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• |
| 70 | | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• |
| 80 | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• |
| 90 | | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• |
| a0 | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• |
| b0 | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• |
| c0 | | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• |
| d0 | ••• | ••• | ••• | ••• | ••• | | ••• | ••• | | ••• | ••• | ••• | ••• | c1 | ••• | ••• |
| e0 | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | ••• | 28 | ••• |
| f0 | | ••• | ••• | | ••• | | ••• | ••• | | ••• | ••• | ••• | ••• | ••• | ••• | 16 |

Code 3.6: Byte Substitution

```
void SubBytes(u8* state) {
    for (int i = 0; i < AES_BLOCK_SIZE; i++) {
        state[i] = s_box[state[i]];
    }
}</pre>
```

Code 3.7: Inverse Byte Substitution

```
void InvSubBytes(u8* state) {
    for (int i = 0; i < AES_BLOCK_SIZE; i++) {
        state[i] = inv_s_box[state[i]];
    }
}</pre>
```

3.2.4 ShiftRows / InvShiftRows

• ShiftRows: $\{0, 1\}^{128} \to \{0, 1\}^{128}$ is defined by

| X_0 | X_4 | X_8 | X_{12} | | X_0 | X_4 | X_8 | X_{12} |
|-------|-------|-----------------------|----------|-------------------|----------|----------|----------|----------|
| X_1 | X_5 | <i>X</i> ₉ | X_{13} | \Longrightarrow | X_5 | X_9 | X_{13} | X_1 |
| X_2 | X_6 | X_{10} | X_{14} | <i>→</i> | X_{10} | X_{14} | X_2 | X_6 |
| X_3 | X_7 | X_{11} | X_{15} | | X_{15} | X_3 | X_7 | X_{11} |

• InvShiftRows: $\{0, 1\}^{128} \rightarrow \{0, 1\}^{128}$ is defined by

| X_0 | X_4 | X_8 | X_{12} | | X_0 | X_4 | X_8 | X_{12} |
|-------|-------|----------|----------|---------------|----------|-----------------|----------|----------|
| X_1 | X_5 | X_9 | X_{13} | | X_{13} | X_1 | X_5 | X_9 |
| X_2 | X_6 | X_{10} | X_{14} | \Rightarrow | X_{10} | X_{14} | X_2 | X_6 |
| X_3 | X_7 | X_{11} | X_{15} | | X_7 | X ₁₁ | X_{15} | X_3 |

Code 3.8: ShiftRows

```
void ShiftRows(u8* state) {
1
2
       u8 temp;
3
       // Row 1: shift left by 1
4
5
       temp = state[1];
6
       state[1] = state[5];
7
       state[5] = state[9];
8
       state[9] = state[13];
9
       state[13] = temp;
10
       // Row 2: shift left by 2
11
12
       temp = state[2];
       state[2] = state[10];
13
       state[10] = temp;
14
       temp = state[6];
15
       state[6] = state[14];
16
       state[14] = temp;
17
18
       // Row 3: shift left by 3 (or right by 1)
19
       temp = state[15];
20
       state[15] = state[11];
21
       state[11] = state[7];
22
23
       state[7] = state[3];
24
       state[3] = temp;
25
  }
```

Code 3.9: Inverse ShiftRows

```
void InvShiftRows(u8* state) {
1
2
       u8 temp;
3
       // Row 1: shift left by 3 (or right by 1)
4
5
       temp = state[13];
6
       state[13] = state[9];
7
       state[9] = state[5];
8
       state[5] = state[1];
9
       state[1] = temp;
10
       // Row 2: shift left by 2
11
       temp = state[2];
12
13
       state[2] = state[10];
14
       state[10] = temp;
15
       temp = state[6];
16
       state[6] = state[14];
       state[14] = temp;
17
18
       // Row 3: shift left by 1
19
20
       temp = state[3];
       state[3] = state[7];
21
22
       state[7] = state[11];
23
       state[11] = state[15];
24
       state[15] = temp;
25
  }
```

3.2.5 MixColumns / InvMixColumns

• Multiplication in the finite filed GF(2⁸).

$$MUL_{GF256}: \{0, 1\}^8 \times \{0, 1\}^8 \rightarrow \{0, 1\}^8.$$

Here,

$$\{\mathbf{0},\mathbf{1}\}^8 \simeq GF(2^8) = \mathbb{F}_{2^8} := \mathbb{F}_2[z]/(z^8 + z^4 + z^3 + z + 1) = \{a_7z^7 + \dots + a_1z + a_0 : a_i \in \mathbb{F}_2\}.$$

Note that

$$a(z) \times b(z) := a(z) \times b(z) \mod (z^8 + z^4 + z^3 + z + 1)$$

Note. Given two polynomials a(x) and b(x) in $GF(2^8)$:

$$a(x) = a_7 x^7 + a_6 x^6 + a_5 x^5 + a_4 x^4 + a_3 x^3 + a_2 x^2 + a_1 x + a_0,$$

$$b(x) = b_7 x^7 + b_6 x^6 + b_5 x^5 + b_4 x^4 + b_3 x^3 + b_2 x^2 + b_1 x + b_0.$$

The algorithm performs polynomial multiplication in the finite field $GF(2^8)$. It uses a shift-and-add method, with an additional reduction step modulo an irreducible polynomial $m(x) = x^8 + x^4 + x^3 + x + 1$.

- 1. Initialization: Set p(x) = 0 to initialize the product polynomial.
- 2. Iterate over each bit of b(x), from LSB to MSB.
 - (i) If the current bit b_i of b(x) is 1, update p(x) as $p(x) \oplus a(x)$. In $GF(2^8)$, addition is equivalent to the XOR operation:

$$p(x) = p(x) \oplus a(x)$$
.

(ii) Shift a(x) left by 1 (multiply by x), increasing its degree by 1:

$$a(x) = a(x) \cdot x$$
.

(iii) If the coefficient of x^8 in a(x) is 1, reduce a(x) by m(x) to keep the degree under 8:

$$a(x) = a(x) \oplus m(x)$$
.

(iv) Shift b(x) right by 1 (divide by x) for the next iteration:

$$b(x) = b(x) / x$$
.

3. After all bits of b(x) are processed, p(x) be the product of a(x) and b(x) modulo m(x).

Note (**Modular Reduction in** $GF(2^8)$ **using XOR).** In the context of multiplication in the binary finite field $GF(2^8)$, modular reduction ensures that results of operations remain within the field. The use of XOR for modular reduction is due to the properties of polynomial arithmetic over GF(2) and the representation of elements in $GF(2^8)$.

- Polynomial Representation in $GF(2^8)$:
 - 1. **Elements as Polynomials**: Each element in $GF(2^8)$ can be represented as a polynomial of degree less than 8, where each coefficient is either 0 or 1, i.e.,

$$GF(2^8) = \mathbb{F}_2[x]/(x^8 + x^4 + x^3 + x + 1) = \left\{ a_7 x^7 + \dots + a_1 x + a_0 : a_i \in \mathbb{F}_2 \right\}.$$

This corresponds to an 8-bit binary number, with each bit representing a coefficient of the polynomial, i.e.,

$$a_7x^7 + \cdots + a_1x + a_0 \iff (a_7 \dots a_1a_0)_2.$$

2. **Binary Operations**: In GF(2), addition and subtraction are equivalent to the XOR operation, since 1 + 1 = 0 in this field, the same as $1 \oplus 1$.

- Modular Reduction with an Irreducible Polynomial

- 1. **Irreducible Polynomial**: In $GF(2^8)$, an irreducible polynomial of degree 8, typically $p(x) = x^8 + x^4 + x^3 + x + 1$ (represented as 0x11b in binary), is used for modular reduction.
- 2. **Modular Reduction Process**: After multiplying two polynomials, if the resulting polynomial's degree is 8 or higher, it must be reduced modulo the irreducible polynomial to ensure the result remains a polynomial of degree less than 8, thus staying within $GF(2^8)$.
- 3. **XOR for Reduction**: XOR is used for modular reduction in $GF(2^8)$ because polynomial subtraction in GF(2) is performed by XORing coefficients.
- Given two elements in $GF(2^8)$, a(x) and b(x), their product is $c(x) = a(x) \cdot b(x)$. If $deg(c(x)) \ge 8$, then c(x) must be reduced modulo the irreducible polynomial p(x). This is achieved by XORing the coefficients of c(x) and p(x):

$$c(x) = a(x) \cdot b(x) \mod p(x)$$

If c(x) has a term x^8 or higher, we subtract p(x) from c(x) to reduce its degree. In GF(2), subtraction is equivalent to addition, performed by XORing coefficients:

$$c'(x) = c(x) \oplus p(x)$$

This operation effectively eliminates the term x^8 (or higher) in c(x), ensuring that the result remains within $GF(2^8)$. Consider the product of two polynomials a(x) and b(x) in $GF(2^8)$:

$$a(x) = x^6 + x^4 + x^2 + x + 1$$
 and $b(x) = x^7 + x + 1$

The product $c(x) = a(x) \cdot b(x)$ might yield a polynomial of degree 8 or higher. To reduce c(x) modulo $p(x) = x^8 + x^4 + x^3 + x + 1$, we perform XOR between the coefficients of c(x) and p(x), ensuring the result stays within $GF(2^8)$.

CHAPTER 3. AES-128

Code 3.10: Multiplication in $GF(2^8)$

```
u8 MUL_GF256(u8 a, u8 b) {
2
       u8 res = 0;
3
       // Mask for detecting the MSB (0x80 = 0b10000000)
4
       u8 MSB_mask = 0x80;
5
       u8 MSB;
       /*
6
7
        * The reduction polynomial
8
        * (x^8 + x^4 + x^3 + x + 1) = 0b100011011
9
        * for AES, represented in hexadecimal
       */
10
       u8 \mod ulo = 0x1B;
11
12
       for (int i = 0; i < 8; i++) {
13
14
            // Add a to result if LSB(b)=1
15
            if (b & 1)
                res ^{\prime}= a;
16
17
            MSB = a & MSB_mask; // Store the MSB of a
18
19
            a <<= 1; // Multiplying it by x effectively
20
21
            // Reduce the result modulo the reduction polynomial
22
            if (MSB)
23
                a ^= modulo;
24
25
            b >>= 1; // Moving to the next bit
26
       }
27
28
       return res;
29
   }
30
31
   #define MUL_GF256(a, b) ({ \
       u8 res = 0; \
32
33
       u8 MSB_mask = 0x80; \
34
       u8 MSB; \
35
       u8 \mod ulo = 0x1B; \setminus
36
       u8 temp_a = (a); \
       u8 temp_b = (b); \
37
       for (int i = 0; i < 8; i++) { \</pre>
38
39
            if (temp_b & 1) \
            res ^= temp_a; \
40
41
            MSB = temp_a & MSB_mask; \
42
            temp_a <<= 1; \
            if (MSB) \
43
            temp_a ^= modulo; \
44
45
            temp_b >>= 1; \
46
       } \
47
       res; \
48
  })
```

• MixColumns : $\{0, 1\}^{128} \rightarrow \{0, 1\}^{128}$ is defined by

$$\text{MixColumns} \begin{pmatrix} \begin{pmatrix} X_0 & X_4 & X_8 & X_{12} \\ X_1 & X_5 & X_9 & X_{13} \\ X_2 & X_6 & X_{10} & X_{14} \\ X_3 & X_7 & X_{11} & X_{15} \end{pmatrix} \end{pmatrix} := \begin{pmatrix} \mathbf{0} \times \mathbf{02} & \mathbf{0} \times \mathbf{03} & \mathbf{0} \times \mathbf{01} & \mathbf{0} \times \mathbf{01} \\ \mathbf{0} \times \mathbf{01} & \mathbf{0} \times \mathbf{02} & \mathbf{0} \times \mathbf{03} & \mathbf{0} \times \mathbf{01} \\ \mathbf{0} \times \mathbf{01} & \mathbf{0} \times \mathbf{01} & \mathbf{0} \times \mathbf{02} & \mathbf{0} \times \mathbf{03} \\ \mathbf{0} \times \mathbf{03} & \mathbf{0} \times \mathbf{01} & \mathbf{0} \times \mathbf{01} & \mathbf{0} \times \mathbf{02} \end{pmatrix} \begin{pmatrix} X_0 & X_4 & X_8 & X_{12} \\ X_1 & X_5 & X_9 & X_{13} \\ X_2 & X_6 & X_{10} & X_{14} \\ X_3 & X_7 & X_{11} & X_{15} \end{pmatrix}.$$

• InvMixColums : $\{0, 1\}^{128} \rightarrow \{0, 1\}^{128}$ is defined by

$$\text{MixColums} \begin{pmatrix} \begin{pmatrix} X_0 & X_4 & X_8 & X_{12} \\ X_1 & X_5 & X_9 & X_{13} \\ X_2 & X_6 & X_{10} & X_{14} \\ X_3 & X_7 & X_{11} & X_{15} \end{pmatrix} := \begin{pmatrix} \mathbf{0} \mathbf{x} \mathbf{0} \mathbf{e} & \mathbf{0} \mathbf{x} \mathbf{0} \mathbf{b} & \mathbf{0} \mathbf{x} \mathbf{0} \mathbf{d} & \mathbf{0} \mathbf{x} \mathbf{0} \mathbf{9} \\ \mathbf{0} \mathbf{x} \mathbf{0} \mathbf{9} & \mathbf{0} \mathbf{x} \mathbf{0} \mathbf{e} & \mathbf{0} \mathbf{x} \mathbf{0} \mathbf{b} & \mathbf{0} \mathbf{x} \mathbf{0} \mathbf{d} \\ \mathbf{0} \mathbf{x} \mathbf{0} \mathbf{d} & \mathbf{0} \mathbf{x} \mathbf{0} \mathbf{9} & \mathbf{0} \mathbf{x} \mathbf{0} \mathbf{e} & \mathbf{0} \mathbf{x} \mathbf{0} \mathbf{b} \\ \mathbf{0} \mathbf{x} \mathbf{0} \mathbf{b} & \mathbf{0} \mathbf{x} \mathbf{0} \mathbf{d} & \mathbf{0} \mathbf{x} \mathbf{0} \mathbf{9} & \mathbf{0} \mathbf{x} \mathbf{0} \mathbf{e} \end{pmatrix} \begin{pmatrix} X_0 & X_4 & X_8 & X_{12} \\ X_1 & X_5 & X_9 & X_{13} \\ X_2 & X_6 & X_{10} & X_{14} \\ X_3 & X_7 & X_{11} & X_{15} \end{pmatrix}.$$

Code 3.11: MixColumns

```
1
   void MixColumns(u8* state) {
2
       u8 temp[4];
       // Multiply and add the elements in the column
3
       // by the fixed polynomial
4
       for (int i = 0; i < 4; i++) {
5
            temp[0] =
6
                MUL_GF256(0x02, state[i * 4]) ^
7
8
                MUL_GF256(0x03, state[i * 4 + 1]) ^
                state[i * 4 + 2] ^
9
                state[i * 4 + 3];
10
11
           temp[1] =
12
                state[i * 4] ^
13
                MUL_GF256(0x02, state[i * 4 + 1]) ^
14
                MUL_GF256(0x03, state[i * 4 + 2]) ^
15
                state[i * 4 + 3];
16
17
           temp[2] =
18
                state[i * 4] ^
19
                state[i * 4 + 1] ^
20
                MUL_GF256(0x02, state[i * 4 + 2]) ^
21
22
                MUL_GF256(0x03, state[i * 4 + 3]);
23
            temp[3] =
24
                MUL_GF256(0x03, state[i * 4]) ^
25
                state[i * 4 + 1] ^
26
                state[i * 4 + 2] ^
27
                MUL_GF256(0x02, state[i * 4 + 3]);
28
29
30
           // Copy the mixed column back to the state
            for (int j = 0; j < 4; j++)
31
                state[i * 4 + j] = temp[j];
32
       }
33
  }
```

22 *CHAPTER 3. AES-*128

Code 3.12: Inverse MixColumns

```
void InvMixColumns(u8* state) {
1
2
       u8 temp[4];
3
4
       for (int i = 0; i < 4; i++) {
5
           temp[0] =
               MUL_GF256(0x0e, state[i * 4]) ^
6
7
               MUL_GF256(0x0b, state[i * 4 + 1]) ^
8
               MUL_GF256(0x0d, state[i * 4 + 2]) ^
9
               MUL_GF256(0x09, state[i * 4 + 3]);
10
11
           temp[1] =
               MUL_GF256(0x09, state[i * 4]) ^
12
               MUL_GF256(0x0e, state[i * 4 + 1]) ^
13
14
               MUL_GF256(0x0b, state[i * 4 + 2]) ^
15
               MUL_GF256(0x0d, state[i * 4 + 3]);
16
17
           temp[2] =
               MUL_GF256(0x0d, state[i * 4]) ^
18
19
               MUL_GF256(0x09, state[i * 4 + 1]) ^
20
               MUL_GF256(0x0e, state[i * 4 + 2]) ^
               MUL_GF256(0x0b, state[i * 4 + 3]);
21
22
23
           temp[3] =
                MUL_GF256(0x0b, state[i * 4]) ^
24
               MUL_GF256(0x0d, state[i * 4 + 1]) ^
25
               MUL_GF256(0x09, state[i * 4 + 2]) ^
26
               MUL_GF256(0x0e, state[i * 4 + 3]);
27
28
           for (int j = 0; j < 4; j++)
29
                state[i * 4 + j] = temp[j];
30
31
       }
32
  }
```

Chapter 4

AES - 128 / 192 / 256 (Byte Version)

4.1 Specification

Table 4.1: Parameters of the Block Cipher AES (1-word = 32-bit)

| | Block | Key | Number of | Round-Key | Number of | Total Size of |
|------------|---------------|---------------|-----------|-----------|-------------|----------------|
| Algorithms | Size | Length | Rounds | Length | Round-Keys | Round-Keys |
| | $(N_b$ -word) | $(N_k$ -word) | (N_r) | (word) | $(N_r + 1)$ | $(N_b(N_r+1))$ |
| AES-128 | 4 | 4 (4·32-bit) | 10 | 4 | 11 | 44 (176-byte) |
| AES-192 | 4 | 6 (6·32-bit) | 12 | 4 | 13 | 52 (208-byte) |
| AES-256 | 4 | 8 (8·32-bit) | 14 | 4 | 15 | 60 (240-byte) |

Code 4.1: Configuration in C

```
// Define macros for AES key length
  #define AES_VERSION 128 // Can be 128, 192, or 256
  // Define macro for AES block size
  #define AES_BLOCK_SIZE 16
  // Define Nk and Nr based on AES key length
  #if AES_VERSION == 128
       #define Nk 4
8
  #elif AES_VERSION == 192
       #define Nk 6
10
  #elif AES_VERSION == 256
11
12
       #define Nk 8
13
  #else
       #error "Invalid AES ky length"
15 #endif
16
17
  #define Nr (Nk + 6) // 10 / 12 / 14
18 | #define ROUND_KEYS_SIZE (16 * (Nr + 1)) // 176 / 208 / 240
```

Code 4.2: Configuration in Rust

```
// Define a constant for the AES key length.
1
2
  pub const AES_VERSION: u32 = 128; // Can be 128, 192, or 256
3
   // Define constant for AES block size
4
  pub const AES_BLOCK_SIZE: usize = 16;
6
   // Define constants Nk and Nr based on AES key length
7
8
  pub const NK: usize = match AES_VERSION {
9
       128 = > 4,
       192 = 6
10
       256 => 8,
11
       _ => panic!("Invalid AES key length"),
12
13
   };
14
15
  pub const NR: usize = NK + 6;
  pub const ROUND_KEYS_SIZE: usize = 16 * (NR + 1);
```

4.2 Key Expansion (General Version)

Algorithm 6: Key Schedule (General Version) **Input:** User-key $uk = (uk_0, ..., uk_{N_k-1}) (uk_i \in \{0, 1\}^8);$ // uk is 16/24/32-byte **Output:** Round-key $\{rk_i\}_{i=0}^{4(N_r+1)-1} (rk_i \in \{0, 1\}^{32})$ /* $\{rk_i\}_{i=0}^{4(N_r+1)-1}$ is 176/208/240-byte */ $1 l \leftarrow N_k/4$; // l = 4, 6, 82 **for** i = 0 **to** l - 1 **do** $rk_i \leftarrow uk_{4i} \parallel uk_{4i+1} \parallel uk_{4i+2} \parallel uk_{4i+3};$ 4 end 5 for i = l to $4(N_r + 1) - 1$ do $t \leftarrow rk_{i-1}$; if $i \mod l = 0$ then 7 $t \leftarrow (SubWord \circ RotWord)(t);$ 8 $t \leftarrow t \oplus_{32} (\text{rCon}_{i/l} \parallel 0 \times 000 \parallel 0 \times 000 \parallel 0 \times 000);$ 9 **else if** $l > 6 \&\& i \mod l = 4$ **then** 10 $t \leftarrow \text{SubWord}(t);$ 11 end 12 $rk_i \leftarrow rk_{i-1} \oplus_{32} t$; 13 14 end

Code 4.3: Key Expansion in C (General ver.)

```
void KeyExpansion(const u8* uKey, u32* rKey) {
1
2
       u32 temp;
3
       for (int i = 0; i < Nk; i++) {
4
5
           rKey[i] = (u32)uKey[4*i] << 0x18
                      (u32)uKey[4*i+1] << 0x10
6
7
                      (u32)uKey[4*i+2] << 0x08
                      (u32)uKey[4*i+3];
8
       }
9
10
       for (int i = Nk; i < (Nr + 1) * 4; i++) {
11
           temp = rKey[i - 1];
12
           if (i % Nk == 0) {
13
                temp = SubWord(RotWord(temp)) ^ rCon[i / Nk - 1];
14
           } else if (Nk > 6 \&\& i \% Nk == 4) {
15
                // Additional S-box transformation for AES-256
16
17
                temp = SubWord(temp);
18
19
           rKey[i] = rKey[i - Nk] ^ temp;
20
       }
21
   }
```

Code 4.4: Key Expansion Test

```
void RANDOM_KEY_GENERATION(u8* key) {
1
2
       srand((u32) time(NULL));
3
4
       // Initialize pointer to the start of the key array
5
       u8* p = key;
6
7
       // Set the counter to 16 bytes
8
       int cnt = 0;
9
10
       // Loop until all 16 bytes are filled
       while (cnt < AES_BLOCK_SIZE) {</pre>
11
12
            *p = rand() & 0xff; // Assign a random byte (0 to 255)
                                 // Move to the next byte
13
           p++;
                                 // Decrement the byte count
14
           cnt++;
15
       }
16
   }
17
   void KeyExpansionTest() {
18
19
       u8 uKey[AES_BLOCK_SIZE] = { 0x00, };
20
       RANDOM_KEY_GENERATION(uKey);
       // u8 uKey[AES_BLOCK_SIZE] = {
21
             0x2b, 0x7e, 0x15, 0x16, 0x28, 0xae, 0xd2, 0xa6,
22
23
       //
             0xab, 0xf7, 0x15, 0x88, 0x09, 0xcf, 0x4f, 0x3c
       // };
24
       for (int i = 0; i < AES_BLOCK_SIZE; i++) {</pre>
25
           printf("%02x", uKey[i]);
26
       } printf("\n");
27
28
       u32 rKeys[ROUND_KEYS_SIZE / sizeof(u32)];
29
       KeyExpansion(uKey, rKeys);
30
       for (int i = 0; i < ROUND_KEYS_SIZE / sizeof(u32); i++) {</pre>
31
           printf("%08x\n", rKeys[i]);
32
33
       }
34
   }
35
36
  int main() {
37
       KeyExpansionTest();
38
       return 0;
39
   }
```

11 dst ← t; 12 **return** dst;

4.3 8-bit AES - 128 / 192 / 256

Algorithm 7: Encryption of 8-bit AES **Input:** block $\operatorname{src} \in \{0, 1\}^{128}$, round-keys $\{rk_i\}_{i=0}^{N_r+1}$ $(rk_i \in \{0, 1\}^{32*4})$ Output: block dst $\in \{0, 1\}^{128}$ // AddRoundKey: $\{0, 1\}^{8*16} \times \{0, 1\}^{32*4} \rightarrow \{0, 1\}^{8*16}$ 1 t ← AddRoundKey(src, rk_0); 2 for $i \leftarrow 1$ to $N_r - 1$ do // SubBytes: $\{0, 1\}^{8*16} \rightarrow \{0, 1\}^{8*16}$ $t \leftarrow \text{SubBytes}(t);$ // ShiftRows: $\{0,1\}^{8*16} \rightarrow \{0,1\}^{8*16}$ $t \leftarrow \text{ShiftRows}(t);$ // MixColumns: $\{0, 1\}^{8*16} \rightarrow \{0, 1\}^{8*16}$ $t \leftarrow \text{MixColumns}(t);$ $t \leftarrow AddRoundKey(t, rk_i);$ 7 end s $t \leftarrow \text{SubBytes}(t)$; 9 $t \leftarrow \text{ShiftRows}(t)$; 10 $t \leftarrow AddRoundKey(t, rk_{N_r});$

Code 4.5: 8-bit AES Encryption

```
void AES_Encrypt(const u8* plaintext, const u8* key,
1
       u8* ciphertext) {
2
       // AES-128/192/256: roundKey[44]/roundKey[52]/roundKey[60]
3
4
       u32 roundKey[ROUND_KEYS_SIZE / sizeof(u32)];
       u8 state[AES_BLOCK_SIZE]; // state[16]
5
6
7
       // Copy plaintext to state
       for (int i = 0; i < AES_BLOCK_SIZE; i++)</pre>
8
9
           state[i] = plaintext[i];
10
11
       KeyExpansion(key, roundKey);
12
   // 0: roundKey[ 0] | roundKey[1] | roundKey[ 2] | roundKey[
13
                                                                        31
       AddRoundKey(state, roundKey); // Initial round
14
15
       for (int round = 1; round <= Nr; round++) { // Main rounds</pre>
16
           SubBytes(state); ShiftRows(state);
17
           if (round != Nr) MixColumns(state);
18
   // 1: roundKey[ 4] | roundKey[5] | roundKey[ 6] | roundKey[
19
                                                                        7]
   // 2: roundKey[ 8] | roundKey[9] | roundKey[10] | roundKey[
                                                                       11]
20
21
   // i: roundKey[4*i] |
                                                        | roundKey[4*i+3]
           AddRoundKey(state, roundKey + 4 * round);
22
23
       }
24
25
       // Copy state to ciphertext
       for (int i = 0; i < AES_BLOCK_SIZE; i++)</pre>
26
           ciphertext[i] = state[i];
27
28
  }
```

Algorithm 8: Decryption of 8-bit AES

```
Input: block \operatorname{src} \in \{0,1\}^{128}, round-keys \{rk_i\}_{i=0}^{N_r+1} (rk_i \in \{0,1\}^{32*4})

Output: block \operatorname{dst} \in \{0,1\}^{128}

1 t \leftarrow \operatorname{AddRoundKey}(\operatorname{src}, rk_{N_r});

2 \operatorname{for} i \leftarrow N_r - 1 \operatorname{to} 1 \operatorname{do}

3 | t \leftarrow \operatorname{InvShiftRows}(t);

4 | t \leftarrow \operatorname{InvSubBytes}(t);

5 | t \leftarrow \operatorname{AddRoundKey}(t, rk_i);

6 | t \leftarrow \operatorname{InvMixColumns}(t);

7 \operatorname{end}

8 t \leftarrow \operatorname{InvShiftRows}(t);

9 t \leftarrow \operatorname{InvSubBytes}(t);

10 t \leftarrow \operatorname{AddRoundKey}(t, rk_0);

11 \operatorname{dst} \leftarrow t;

12 \operatorname{return} \operatorname{dst};
```

Code 4.6: 8-bit AES Decryption

```
void AES_Decrypt(const u8* ciphertext, const u8* key,
1
2
       u8* plaintext) {
3
       u32 roundKey[ROUND_KEYS_SIZE / sizeof(u32)];
       u8 state[AES_BLOCK_SIZE];
4
5
       KeyExpansion(key, roundKey);
6
7
8
       for (int i = 0; i < AES_BLOCK_SIZE; i++)</pre>
            state[i] = ciphertext[i];
9
10
       // Initial round with the last round key
11
       AddRoundKey(state, roundKey + 4 * Nr);
12
13
       // Main rounds in reverse order
14
       for (int round = Nr - 1; round >= 0; round--) {
15
16
           InvShiftRows(state);
           InvSubBytes(state);
17
                                                        | roundKey[4*i+3]
   // i: roundKey[4*i] |
18
                              . . .
   // 1: roundKey[ 4] | roundKey[5] | roundKey[ 6] | roundKey[
                                                                         7]
19
   // 0: roundKey[ 0] | roundKey[1] | roundKey[ 2] | roundKey[
20
                                                                         31
           AddRoundKey(state, roundKey + 4 * round);
21
22
           if (round != 0)
                InvMixColumns(state);
23
       }
24
25
       for (int i = 0; i < AES_BLOCK_SIZE; i++)</pre>
26
27
           plaintext[i] = state[i];
28
```

Chapter 5

Pre-Computation using SubMix

5.1 SubMix and InvSubInvMix

```
• SubMix : \{0,1\}^{128} \rightarrow \{0,1\}^{128} and InvSubInvMix : \{0,1\}^{128} \rightarrow \{0,1\}^{128} are defined by SubMix := MixColumns \circ SubBytes InvSubInvMix := InvMixColumns \circ InvSubBytes.
```

Algorithm 9: Encryption and Decryption of AES using SubMix and InvSubInvMix

```
Input: block \operatorname{src} \in \{0, 1\}^{128}, round-keys \{rk_i\}_{i=0}^{N_r+1} (rk_i \in \{0, 1\}^{128})
   Output: block dst \in \{0, 1\}^{128}
 1 Function AES_ENC:
                                                                        1 Function AES_DEC:
        t \leftarrow \text{src};
                                                                                t \leftarrow \text{src};
         t \leftarrow AddRoundKey(t, rk_0);
                                                                                t \leftarrow AddRoundKey(t, rk_{N_r});
        for i \leftarrow 1 to N_r - 1 do
                                                                                for i \leftarrow N_r - 1 downto 1 do
              t \leftarrow \text{ShiftRows}(t);
                                                                                     t \leftarrow \text{InvShiftRows}(t);
 5
                                                                        5
              t \leftarrow \mathbf{SubMix}(t);
                                                                                     t \leftarrow InvSubInvMix(t);
 6
              t \leftarrow AddRoundKey(t, rk_i);
                                                                                     t' \leftarrow \text{InvMixColumns}(rk_i);
                                                                        7
                                                                                     t \leftarrow AddRoundKey(t, t');
                                                                        8
         t \leftarrow \text{SubBytes}(t);
                                                                                end
                                                                        9
        t \leftarrow \text{ShiftRows}(t);
                                                                                t \leftarrow \text{InvShiftRows}(t);
                                                                       10
10
         t \leftarrow AddRoundKey(t, rk_{N_r});
                                                                                t \leftarrow \text{InvSubBytes}(t);
                                                                       11
11
                                                                                t \leftarrow AddRoundKey(t, rk_0);
        dst \leftarrow t;
                                                                       12
12
        return dst;
                                                                                dst \leftarrow t;
                                                                       13
                                                                                return dst;
14 end
                                                                       15 end
```

5.2 8×32 Table Look Up

Convert the 8-bit string $\{X_i\}_{i=0}^{15} (X_i \in \{0, 1\}^8)$ into a 32-bit string $\{W_i\}_{i=0}^3 (W_i \in \{0, 1\}^{32})$ as follows:

$$W_i := (X_{4i} \ll 24) \parallel (X_{4i+1} \ll 16) \parallel (X_{4i+2} \ll 8) \parallel (X_{4i+3}) \in \{0, 1\}^{32}$$

for i = 0, 1, 2, 3. In other words,

| X_0 | $(W_0 \gg 0x18) \& 0xff$ | X_4 | $(W_1 \gg 0 \text{x} 18) \& 0 \text{x} ff$ |
|-----------------------|---|----------|--|
| X_1 | $(W_0 \gg 0 \text{x} 10) \& 0 \text{x} ff$ | X_5 | $(W_1 \gg 0 \text{x} 10) \& 0 \text{xff}$ |
| X_2 | $(W_0 \gg 0x08) \& 0xff$ | X_6 | $(W_1 \gg 0 \times 0 \times 0) \& 0 \times ff$ |
| X_3 | (W_0) & $0xff$ | X_7 | (W_1) & $0xff$ |
| X_8 | $(W_2 \gg 0 \text{x} 18) \& 0 \text{x} ff$ | X_{12} | $(W_3 \gg 0 \text{x} 18) \& 0 \text{x} ff$ |
| <i>X</i> ₉ | $(W_2 \gg 0 \text{x} 10) \& 0 \text{x} ff$ | X_{13} | $(W_3 \gg 0 \times 10) \& 0 \times ff$ |
| X_{10} | $(W_2 \gg 0 \times 0$ | X_{14} | $(W_3 \gg 0 \times 0 \times 0) \& 0 \times ff$ |
| X ₁₁ | (W_2) & 0xff | X_{15} | (W_3) & $0xff$ |

Note that

| X_0 | X_1 | X_2 | X_3 | X_4 | X_5 | X_6 | X_7 | X_8 | X_9 | X_{10} | X_{11} | X_{12} | X_{13} | X_{14} | X_{15} |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|----------|----------|----------|----------|----------|
| | V | V_0 | | | V | V_1 | | | | W_2 | | | V | V_3 | |

```
Algorithm 10: SubMix and InvSubInvMix
  Input: (W_0, W_1, \overline{W_2, W_3}) \in \{0, 1\}^{128 = 32 \times 4}
                                                                     Input: (W_0, W_1, W_2, W_3) \in \{0, 1\}^{128 = 32 \times 4}
                                                                     Output: (U_0, U_1, U_2, U_3) \in \{0, 1\}^{128 = 32 \times 4}
  Output: (V_0, V_1, V_2, V_3) \in \{0, 1\}^{128 = 32 \times 4}
1 Function SubMix:
                                                                  1 Function InvSubInvMix:
                                                                          for i \leftarrow 0 to 3 do
       for i \leftarrow 0 to 3 do
                                                                               U_i \leftarrow Td_0 ((W_i \gg 0x18) \& 0xff)
            V_i \leftarrow Te_0 ((W_i \gg 0x18) \& 0xff)
3
                                                                   3
                  \bigoplus_{32} Te_1 ((W_i \gg 0x10) \& 0xff)
                                                                                     \bigoplus_{32} Td_1 ((W_i \gg 0x10) \& 0xff)
4
                                                                   4
                  \bigoplus_{32} Te_2 ((W_i \gg 0x08) \& 0xff)
                                                                                     \bigoplus_{32} Td_2 ((W_i \gg 0x08) \& 0xff)
                                                                   5
5
                  \bigoplus_{32} Te_3(W_i \& 0xff);
                                                                                     \bigoplus_{32} Td_3(W_i \& 0xff);
                                                                   6
6
       end
                                                                          end
                                                                   7
7
       return (V_0, V_1, V_2, V_3);
                                                                          return (U_0, U_1, U_2, U_3);
                                                                   8
9 end
                                                                  9 end
```

5.3 Generation of 8×32 Tables

Note that

$$\begin{pmatrix} V_0 & V_4 & V_8 & V_{12} \\ V_1 & V_5 & V_9 & V_{13} \\ V_2 & V_6 & V_{10} & V_{14} \\ V_3 & V_7 & V_{11} & V_{15} \end{pmatrix} = \operatorname{SubMix} \begin{pmatrix} \begin{pmatrix} X_0 & X_4 & X_8 & X_{12} \\ X_1 & X_5 & X_9 & X_{13} \\ X_2 & X_6 & X_{10} & X_{14} \\ X_3 & X_7 & X_{11} & X_{15} \end{pmatrix} := \\ \begin{pmatrix} 0 \times 02 & 0 \times 03 & 0 \times 01 & 0 \times 01 \\ 0 \times 01 & 0 \times 02 & 0 \times 03 & 0 \times 01 \\ 0 \times 01 & 0 \times 01 & 0 \times 02 & 0 \times 03 \\ 0 \times 03 & 0 \times 01 & 0 \times 01 & 0 \times 02 \end{pmatrix} \begin{pmatrix} s(X_0) & s(X_4) & s(X_8) & s(X_{12}) \\ s(X_1) & s(X_5) & s(X_9) & s(X_{13}) \\ s(X_2) & s(X_6) & s(X_{10}) & s(X_{14}) \\ s(X_3) & s(X_7) & s(X_{11}) & s(X_{15}) \end{pmatrix}' \\ \begin{pmatrix} U_0 & V_4 & U_8 & U_{12} \\ U_1 & V_5 & U_9 & U_{13} \\ U_2 & V_6 & U_{10} & U_{14} \\ U_3 & V_7 & U_{11} & U_{15} \end{pmatrix} = \operatorname{InvSubInvMix} \begin{pmatrix} \begin{pmatrix} X_0 & X_4 & X_8 & X_{12} \\ X_1 & X_5 & X_9 & X_{13} \\ X_2 & X_6 & X_{10} & X_{14} \\ X_3 & X_7 & X_{11} & X_{15} \end{pmatrix} := \\ \begin{pmatrix} 0 \times 0e & 0 \times 0b & 0 \times 0d & 0 \times 09 \\ 0 \times 09 & 0 \times 0e & 0 \times 0b & 0 \times 0d \\ 0 \times 0d & 0 \times 09 & 0 \times 0e & 0 \times 0b \end{pmatrix} \begin{pmatrix} s^{-1}(X_0) & s^{-1}(X_4) & s^{-1}(X_8) & s^{-1}(X_{12}) \\ s^{-1}(X_1) & s^{-1}(X_5) & s^{-1}(X_{10}) & s^{-1}(X_{14}) \\ s^{-1}(X_3) & s^{-1}(X_7) & s^{-1}(X_{11}) & s^{-1}(X_{15}) \end{pmatrix}$$

Then

$$\begin{pmatrix} V_{4i} \\ V_{4i+1} \\ V_{4i+2} \\ V_{4i+3} \end{pmatrix} = \begin{pmatrix} 0 \times 02 & 0 \times 03 & 0 \times 01 & 0 \times 01 \\ 0 \times 01 & 0 \times 02 & 0 \times 03 & 0 \times 01 \\ 0 \times 01 & 0 \times 01 & 0 \times 02 & 0 \times 03 \\ 0 \times 03 & 0 \times 01 & 0 \times 01 & 0 \times 02 \end{pmatrix} \begin{pmatrix} s(X_{4i}) \\ s(X_{4i+1}) \\ s(X_{4i+2}) \\ s(X_{4i+3}) \end{pmatrix}$$

$$= s(X_{4i}) \begin{pmatrix} 0 \times 02 \\ 0 \times 01 \\ 0 \times 01 \\ 0 \times 03 \end{pmatrix} \oplus_{32} s(X_{4i+1}) \begin{pmatrix} 0 \times 03 \\ 0 \times 02 \\ 0 \times 01 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+2}) \begin{pmatrix} 0 \times 01 \\ 0 \times 03 \\ 0 \times 02 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+3}) \begin{pmatrix} 0 \times 01 \\ 0 \times 03 \\ 0 \times 02 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+3}) \begin{pmatrix} 0 \times 01 \\ 0 \times 03 \\ 0 \times 02 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+3}) \begin{pmatrix} 0 \times 01 \\ 0 \times 03 \\ 0 \times 02 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+3}) \begin{pmatrix} 0 \times 01 \\ 0 \times 03 \\ 0 \times 02 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+3}) \begin{pmatrix} 0 \times 01 \\ 0 \times 03 \\ 0 \times 02 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+3}) \begin{pmatrix} 0 \times 01 \\ 0 \times 03 \\ 0 \times 02 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+3}) \begin{pmatrix} 0 \times 01 \\ 0 \times 03 \\ 0 \times 02 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+3}) \begin{pmatrix} 0 \times 01 \\ 0 \times 03 \\ 0 \times 02 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+3}) \begin{pmatrix} 0 \times 01 \\ 0 \times 03 \\ 0 \times 02 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+3}) \begin{pmatrix} 0 \times 01 \\ 0 \times 03 \\ 0 \times 02 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+3}) \begin{pmatrix} 0 \times 01 \\ 0 \times 03 \\ 0 \times 02 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+3}) \begin{pmatrix} 0 \times 01 \\ 0 \times 03 \\ 0 \times 02 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+3}) \begin{pmatrix} 0 \times 01 \\ 0 \times 03 \\ 0 \times 02 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+3}) \begin{pmatrix} 0 \times 01 \\ 0 \times 03 \\ 0 \times 02 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+3}) \begin{pmatrix} 0 \times 01 \\ 0 \times 03 \\ 0 \times 02 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+3}) \begin{pmatrix} 0 \times 01 \\ 0 \times 03 \\ 0 \times 02 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+3}) \begin{pmatrix} 0 \times 01 \\ 0 \times 03 \\ 0 \times 02 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+1}) \begin{pmatrix} 0 \times 01 \\ 0 \times 01 \\ 0 \times 01 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+1}) \begin{pmatrix} 0 \times 01 \\ 0 \times 01 \\ 0 \times 01 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+1}) \begin{pmatrix} 0 \times 01 \\ 0 \times 01 \\ 0 \times 01 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+1}) \begin{pmatrix} 0 \times 01 \\ 0 \times 01 \\ 0 \times 01 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+1}) \begin{pmatrix} 0 \times 01 \\ 0 \times 01 \\ 0 \times 01 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+1}) \begin{pmatrix} 0 \times 01 \\ 0 \times 01 \\ 0 \times 01 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+1}) \begin{pmatrix} 0 \times 01 \\ 0 \times 01 \\ 0 \times 01 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+1}) \begin{pmatrix} 0 \times 01 \\ 0 \times 01 \\ 0 \times 01 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+1}) \begin{pmatrix} 0 \times 01 \\ 0 \times 01 \\ 0 \times 01 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+1}) \begin{pmatrix} 0 \times 01 \\ 0 \times 01 \\ 0 \times 01 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+1}) \begin{pmatrix} 0 \times 01 \\ 0 \times 01 \\ 0 \times 01 \end{pmatrix} \oplus_{32} s(X_{4i+1}) \begin{pmatrix} 0 \times 01 \\ 0 \times 01 \\ 0$$

We define $Te_i/Td_i: \{0,1\}^8 \to \{0,1\}^{32} (i \in \{0,1,2,3\})$ as follows:

$$Te_{0}(X) := \begin{pmatrix} \mathbf{0} \times \mathbf{0} & 2 \otimes_{8} s(X) & s(X) & s(X) & s(X) & \mathbf{0} \times \mathbf{0} & 3 \otimes_{8} s(X) \end{pmatrix},$$

$$Te_{1}(X) := \begin{pmatrix} \mathbf{0} \times \mathbf{0} & 3 \otimes_{8} s(X) & \mathbf{0} \times \mathbf{0} & 2 \otimes_{8} s(X) & s(X)$$

and

$$\begin{split} Td_0(X) &:= \left(\ \mathbf{0x0e} \otimes_8 s^{-1}(X) \ , \ \mathbf{0x09} \otimes_8 s^{-1}(X) \ , \ \mathbf{0x0d} \otimes_8 s^{-1}(X) \ , \ \mathbf{0x0b} \otimes_8 s^{-1}(X) \ , \ \mathbf{0x0b} \otimes_8 s^{-1}(X) \ , \ \mathbf{0x0d} \otimes$$

SubMix/InvSubInvMix : $\{0,1\}^{128} \rightarrow \{0,1\}^{128}$ are computed as follows:

SubMix
$$(W_0, W_1, W_2, W_3) := (V_0, V_1, V_2, V_3),$$

InvSubInvMix $(W_0, W_1, W_2, W_3) := (U_0, U_1, U_2, U_3)$

where
$$\begin{cases} W_0 \coloneqq X_0 \parallel X_1 \parallel X_2 \parallel X_3 \\ W_1 \coloneqq X_4 \parallel X_5 \parallel X_6 \parallel X_7 \\ W_2 \coloneqq X_8 \parallel X_9 \parallel X_{10} \parallel X_{11} \\ W_3 \coloneqq X_{12} \parallel X_{13} \parallel X_{14} \parallel X_{15} \end{cases} \qquad (W_i \in \{\textbf{0}, \textbf{1}\}^{32}) \text{ and}$$

$$V_0 \coloneqq Te_0(X_0) \quad \oplus_{32} \quad Te_1(X_1) \quad \oplus_{32} \quad Te_2(X_2) \quad \oplus_{32} \quad Te_3(X_3),$$

$$V_1 \coloneqq Te_0(X_4) \quad \oplus_{32} \quad Te_1(X_5) \quad \oplus_{32} \quad Te_2(X_6) \quad \oplus_{32} \quad Te_3(X_7),$$

$$V_2 \coloneqq Te_0(X_8) \quad \oplus_{32} \quad Te_1(X_9) \quad \oplus_{32} \quad Te_2(X_{10}) \quad \oplus_{32} \quad Te_3(X_{11}),$$

$$V_3 \coloneqq Te_0(X_{12}) \quad \oplus_{32} \quad Te_1(X_{13}) \quad \oplus_{32} \quad Te_2(X_{14}) \quad \oplus_{32} \quad Te_3(X_{15}),$$

$$U_0 \coloneqq Td_0(X_0) \quad \oplus_{32} \quad Td_1(X_1) \quad \oplus_{32} \quad Td_2(X_2) \quad \oplus_{32} \quad Td_3(X_3),$$

$$U_1 \coloneqq Td_0(X_4) \quad \oplus_{32} \quad Td_1(X_5) \quad \oplus_{32} \quad Td_2(X_6) \quad \oplus_{32} \quad Td_3(X_7),$$

$$U_2 \coloneqq Td_0(X_8) \quad \oplus_{32} \quad Td_1(X_9) \quad \oplus_{32} \quad Td_2(X_{10}) \quad \oplus_{32} \quad Td_3(X_{11}),$$

$$U_3 \coloneqq Td_0(X_{12}) \quad \oplus_{32} \quad Td_1(X_{13}) \quad \oplus_{32} \quad Td_2(X_{14}) \quad \oplus_{32} \quad Td_3(X_{15}).$$

5.4 Implementation of SubMix and InvSubInvMix

Code 5.1: SubMix

```
void SubMix(u8* state) {
1
       u32 temp[4];
2
3
       // temp[0] = Te0[state[ 0]] ^ Te1[state[ 1]] ^
4
5
                     Te2[state[ 2]] ^ Te3[state[ 3]];
       // temp[1] = Te0[state[ 4]] ^ Te1[state[ 5]] ^
6
7
                     Te2[state[ 6]] ^ Te3[state[ 7]];
       //
8
       // temp[2] = Te0[state[ 8]] ^ Te1[state[ 9]] ^
9
                     Te2[state[10]] ^ Te3[state[11]];
       // temp[3] = Te0[state[11]] ^ Te1[state[12]] ^
10
                     Te2[state[13]] ^ Te3[state[14]];
11
       //
12
       for (int i = 0; i < 4; i++) {
13
14
           temp[i] = Te0[state[4*i + 0]] ^
                      Te1[state[4*i + 1]] ^
15
16
                      Te2[state[4*i + 2]] ^
                      Te3[state[4*i + 3]];
17
18
       }
19
       for (int i = 0; i < 4; i++) {</pre>
20
21
           state[4*i + 0] = (temp[i] >> 0x18) & 0xff;
           state[4*i + 1] = (temp[i] >> 0x10) & 0xff;
22
23
           state[4*i + 2] = (temp[i] >> 0x08) & 0xff;
           state[4*i + 3] = temp[i] & 0xff;
24
25
       }
26
  }
```

Code 5.2: InvSubInvMix

```
void InvSubInvMix(u8* state) {
1
2
       u32 temp[4];
3
       for (int i = 0; i < 4; i++) {
4
5
            temp[i] = Td0[state[4*i + 0]] ^
                      Td1[state[4*i + 1]] ^
6
7
                      Td2[state[4*i + 2]] ^
                      Td3[state[4*i + 3]];
8
9
       }
10
       for (int i = 0; i < 4; i++) {
11
12
           state[4*i + 0] = (temp[i] >> 0x18) & 0xff;
           state[4*i + 1] = (temp[i] >> 0x10) & 0xff;
13
           state[4*i + 2] = (temp[i] >> 0x08) & 0xff;
14
15
           state[4*i + 3] = temp[i] & 0xff;
       }
16
17
   }
```

Chapter 6

32-bit AES

Code 6.1: SubWord applies the S-box to each byte of the input word

```
/* Table Annotation:
1
  | i | Shift | Mask
                            | Description
  |---|-----|------|------
3
  | 0 | 0x18 | 0xFF << 0x18 | Process most significant byte (1st) |
4
5
   | 1 | 0x10 | 0xFF \ll 0x10 | Process 2nd byte
  \mid 2 \mid 0x08 \mid 0xFF << 0x08\mid Process 3rd byte
7
   | 3 | 0x00 | 0xFF << 0x00 | Process least significant byte (4th)|
8
9
10
  u32 SubWord(u32* word) {
11
      u8 temp;
       for (int i = 0; i < 4; i++) {
12
           temp = Te3[(*word >> (0x18 - 0x08 * i)) & 0x000000ff];
13
           *word &= \sim (0xFF << (0x18 - 0x08 * i)); // Clear the byte
14
           *word |= (temp & 0x0000000ff) << (0x18 - 0x08 * i); // Set
15
              the new value
       }
16
  }
17
```

Code 6.2: SubWord applies the S-box to each byte of the input word

```
u32 SubWord(u32 word) {
1
2
       u8 temp0, temp1, temp2, temp3;
3
       // Process the most significant byte (1st byte)
4
       temp0 = Te3[(word >> 24) & 0x000000ff];
5
       word &= 0x00fffffff; // Clear the most significant byte
6
7
       word \mid = (temp0 & 0x000000ff) << 24; // Set the new value
8
9
       // Process the 2nd byte
10
       temp1 = Te3[(word >> 16) & 0x000000ff];
       word &= 0xff00ffff; // Clear the 2nd byte
11
       word \mid = (temp1 & 0x000000ff) << 16; // Set the new value
12
13
14
       // Process the 3rd byte
15
       temp2 = Te3[(word >> 8) & 0x000000ff];
       word &= 0xffff00ff; // Clear the 3rd byte
16
17
       word \mid = (temp2 & 0x000000ff) << 8; // Set the new value
18
       // Process the least significant byte (4th byte)
19
20
       temp3 = Te3[word & 0x000000ff];
       word &= 0xffffff00; // Clear the least significant byte
21
22
       word \mid = (temp3 & 0x000000ff); // Set the new value
23
24
       return word;
25
  }
```

Code 6.3: SubWord applies the S-box to each byte of the input word

Appendix A

Additional Data A

A.1 Substitution-BOX

```
static const u8 s_box[256] = {
2
       0x63, 0x7c, 0x77, 0x7b, 0xf2, 0x6b, 0x6f, 0xc5,
       0x30, 0x01, 0x67, 0x2b, 0xfe, 0xd7, 0xab, 0x76,
3
4
       0xca, 0x82, 0xc9, 0x7d, 0xfa, 0x59, 0x47, 0xf0,
5
       0xad, 0xd4, 0xa2, 0xaf, 0x9c, 0xa4, 0x72, 0xc0,
       0xb7, 0xfd, 0x93, 0x26, 0x36, 0x3f, 0xf7, 0xcc,
7
       0x34, 0xa5, 0xe5, 0xf1, 0x71, 0xd8, 0x31, 0x15,
       0x04, 0xc7, 0x23, 0xc3, 0x18, 0x96, 0x05, 0x9a,
8
       0x07, 0x12, 0x80, 0xe2, 0xeb, 0x27, 0xb2, 0x75,
9
       0x09, 0x83, 0x2c, 0x1a, 0x1b, 0x6e, 0x5a, 0xa0,
10
       0x52, 0x3b, 0xd6, 0xb3, 0x29, 0xe3, 0x2f, 0x84,
11
                   0x00, 0xed, 0x20, 0xfc, 0xb1, 0x5b,
12
       0x53, 0xd1,
       0x6a, 0xcb,
                   0xbe, 0x39, 0x4a, 0x4c, 0x58, 0xcf,
13
       0xd0, 0xef, 0xaa, 0xfb, 0x43, 0x4d, 0x33, 0x85,
14
15
       0x45, 0xf9, 0x02, 0x7f, 0x50, 0x3c, 0x9f, 0xa8,
16
       0x51, 0xa3, 0x40, 0x8f, 0x92, 0x9d, 0x38, 0xf5,
       0xbc, 0xb6, 0xda, 0x21, 0x10, 0xff, 0xf3, 0xd2,
17
       0xcd, 0x0c, 0x13, 0xec, 0x5f, 0x97, 0x44, 0x17,
18
       0xc4, 0xa7, 0x7e, 0x3d, 0x64, 0x5d, 0x19, 0x73,
19
       0x60, 0x81, 0x4f, 0xdc, 0x22, 0x2a, 0x90, 0x88,
20
       0x46, 0xee, 0xb8, 0x14, 0xde, 0x5e, 0x0b, 0xdb,
21
22
       0xe0, 0x32, 0x3a, 0x0a, 0x49, 0x06, 0x24, 0x5c,
       0xc2, 0xd3, 0xac, 0x62, 0x91, 0x95, 0xe4, 0x79,
23
       0xe7, 0xc8, 0x37, 0x6d, 0x8d, 0xd5, 0x4e, 0xa9,
24
25
       0x6c, 0x56, 0xf4, 0xea, 0x65, 0x7a, 0xae, 0x08,
       0xba, 0x78, 0x25, 0x2e, 0x1c, 0xa6, 0xb4, 0xc6,
26
       0xe8, 0xdd, 0x74, 0x1f, 0x4b, 0xbd, 0x8b, 0x8a,
27
       0x70, 0x3e, 0xb5, 0x66, 0x48, 0x03, 0xf6, 0x0e,
28
29
       0x61, 0x35, 0x57, 0xb9, 0x86, 0xc1, 0x1d, 0x9e,
       0xe1, 0xf8, 0x98, 0x11, 0x69, 0xd9, 0x8e, 0x94,
30
                   0x87, 0xe9, 0xce, 0x55, 0x28, 0xdf,
       0x9b, 0x1e,
31
       0x8c, 0xa1, 0x89, 0x0d, 0xbf, 0xe6, 0x42, 0x68,
32
       0x41, 0x99, 0x2d, 0x0f, 0xb0, 0x54, 0xbb, 0x16
33
   };
```

```
static const u8 inv_s_box[256] = {
2
       0x52, 0x09, 0x6a, 0xd5, 0x30, 0x36, 0xa5, 0x38,
3
       0xbf, 0x40, 0xa3, 0x9e, 0x81, 0xf3, 0xd7, 0xfb,
                   0x39, 0x82, 0x9b, 0x2f, 0xff, 0x87,
4
       0x7c, 0xe3,
5
       0x34, 0x8e, 0x43, 0x44, 0xc4, 0xde, 0xe9, 0xcb,
       0x54, 0x7b, 0x94, 0x32, 0xa6, 0xc2, 0x23, 0x3d,
6
7
       Oxee, 0x4c, 0x95, 0x0b, 0x42, 0xfa, 0xc3, 0x4e,
       0x08, 0x2e, 0xa1, 0x66, 0x28, 0xd9, 0x24, 0xb2,
8
9
       0x76, 0x5b, 0xa2, 0x49, 0x6d, 0x8b, 0xd1, 0x25,
       0x72, 0xf8, 0xf6, 0x64, 0x86, 0x68, 0x98, 0x16,
10
                   0x5c, 0xcc, 0x5d, 0x65, 0xb6, 0x92,
11
       0xd4, 0xa4,
       0x6c, 0x70, 0x48, 0x50, 0xfd, 0xed, 0xb9, 0xda,
12
       0x5e, 0x15, 0x46, 0x57, 0xa7, 0x8d, 0x9d, 0x84,
13
                   0xab, 0x00, 0x8c, 0xbc, 0xd3, 0x0a,
14
       0x90, 0xd8,
       0xf7, 0xe4, 0x58, 0x05, 0xb8, 0xb3, 0x45, 0x06,
15
       0xd0, 0x2c, 0x1e, 0x8f, 0xca, 0x3f, 0x0f, 0x02,
16
17
       0xc1, 0xaf, 0xbd, 0x03, 0x01, 0x13, 0x8a, 0x6b,
       0x3a, 0x91, 0x11, 0x41, 0x4f, 0x67, 0xdc, 0xea,
18
19
       0x97, 0xf2, 0xcf, 0xce, 0xf0, 0xb4, 0xe6, 0x73,
       0x96, 0xac,
                   0x74, 0x22, 0xe7, 0xad, 0x35, 0x85,
20
       0xe2, 0xf9, 0x37, 0xe8, 0x1c, 0x75, 0xdf, 0x6e,
21
       0x47, 0xf1, 0x1a, 0x71, 0x1d, 0x29, 0xc5, 0x89,
22
23
       0x6f, 0xb7, 0x62, 0x0e, 0xaa, 0x18, 0xbe, 0x1b,
24
       0xfc, 0x56, 0x3e, 0x4b, 0xc6, 0xd2, 0x79, 0x20,
       0x9a, 0xdb, 0xc0, 0xfe, 0x78, 0xcd, 0x5a, 0xf4,
25
       0x1f, 0xdd, 0xa8, 0x33, 0x88, 0x07, 0xc7, 0x31,
26
       0xb1, 0x12, 0x10, 0x59, 0x27, 0x80, 0xec, 0x5f,
27
       0x60, 0x51, 0x7f, 0xa9, 0x19, 0xb5, 0x4a, 0x0d,
28
       0x2d, 0xe5, 0x7a, 0x9f, 0x93, 0xc9, 0x9c, 0xef,
29
       0xa0, 0xe0, 0x3b, 0x4d, 0xae, 0x2a, 0xf5, 0xb0,
30
31
       0xc8, 0xeb, 0xbb, 0x3c, 0x83, 0x53, 0x99, 0x61,
       0x17, 0x2b, 0x04, 0x7e, 0xba, 0x77, 0xd6, 0x26,
32
       0xe1, 0x69, 0x14, 0x63, 0x55, 0x21, 0x0c, 0x7d
33
   };
34
```