# **Cryptol: A Comprehensive Guide**

- Mastering the Art of Cryptol Programming -

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### Cryptol vs EasyCrypt

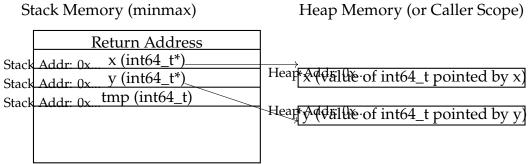
- **Cryptol**: Cryptol is a domain-specific language designed specifically for specifying cryptographic algorithms. A creation by Galois, Inc., it's a tool used primarily for creating high-assurance cryptographic software. Cryptol allows developers to write cryptographic algorithms in a way that directly reflects the mathematical specifications, which makes it easier to analyze and verify for correctness and security.
- EasyCrypt: On the other hand, EasyCrypt is a toolset designed for the formal verification of cryptographic proofs. It provides a framework for developing and verifying mathematical proofs of the security of cryptographic constructions, such as encryption schemes, signature schemes, and hash functions. EasyCrypt operates at a higher level of abstraction compared to Cryptol and is used for proving the security properties of cryptographic protocols mathematically.

If you're comparing them from a user perspective, Cryptol is more about the implementation and specification of cryptographic algorithms, making sure they are implemented correctly according to their mathematical definitions. EasyCrypt is more about proving the theoretical security properties of cryptographic protocols and systems.

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# Research (HIGHT)



Note: Actual stack and heap addresses will vary based on system memory layout and usage.

## CH<sub>1</sub>

# 2.1 Basic Syntax

#### **Identifiers**

#### Examples of Identifier

name	name1	name'	longer_name
Name	Name2	Name"	longerName

### **Keywords and Built-in Operators**

### Keywords

as	extern	include	interface	parameter	property	where
by	hiding	infix	let	pragma	submodule	else
constraint	if	infixl	module	primitive	then	
down	import	infixr	newtype	private	type	

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### **Built-in Type-level Operators**

#### Keywords

Operator	Meaning
+	Addition
_	Subtraction
*	Multiplication
/	Division
/^	Ceiling Division (/ rounded up)
%	Modulus
%^	Ceiling Modulus (Computing Padding)
^^	Exponentiation
1g2	Ceiling logarithm (base 2)
width	Bit Width (equal to 1g2(n+1))
max	Maximum
min	Minimum

#### **Numeric Literals**

#### Examples of Literals

```
254  // Decimal literal
0254  // Decimal literal
0b11111110  // Binary literal
0xFE  // Hexadecimal literal
0xfe  // Hexadecimal literal
```

#### Polynomial Literals

```
<| x^6 + x^4 + x^2 + x^1 + 1 |> // : [7], equal to 0b1010111 
 <math><| x^4 + x^3 + x |> // : [5], equal to 0b11010
```

#### Fractional Literals

```
10.2
10.2e3 // 10.2 * 10^3
0x30.1 // 3 * 64 + 1/16
0x30.1p4 // (3 * 64 + 1/16) * 2^4
```

Using \_

```
0b_0000_0010
0x_FFFF_FFEA
```

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# 2.2 Expressions

### **Calling Functions**

```
f 2  // call 'f' with parameter '2'
g x y  // call 'g' with two parameters: 'x' and 'y'
h (x,y) // call 'h' with one parameter, the pair '(x,y)'
```

# **AES on Cryptol**

### 3.1 Add Round Key

```
type AES128 = 4
type AES192 = 6
type AES256 = 8
type Nk = AES128
// For Cryptol 2.x | x > 0
// NkValid: 'Nk -> Bit
// property NkValid k = (k == 'AES128) || (k == 'AES192) || (k == 'AES256)
// Number of blocks and Number of rounds
type Nb = 4
type Nr = 6 + Nk
type AESKeySize = (Nk*32)
// Helper type definitions
type GF28
               = [8]
               = [4][Nb]GF28
type State
type RoundKey = State
type KeySchedule = (RoundKey, [Nr-1]RoundKey, RoundKey)
```

## **HIGHT on Cryptol**

### **SAWScript Helper Functions**

#### 1. alloc\_init

Given a type ty and a value v of type ty, the function alloc\_init allocates memory to store v and returns a pointer p to this memory.

$$alloc\_init(ty, v) = \begin{cases} p \leftarrow crucible\_alloc(ty); \\ crucible\_points\_to(p, v); \\ return \ p; \end{cases}$$

#### 2. alloc\_init\_readonly

Given a type ty and a value v of type ty, the function alloc\_init\_readonly allocates read-only memory to store v and returns a pointer p to this memory.

$$\text{alloc\_init\_readonly}(ty, v) = \begin{cases} p \leftarrow \text{crucible\_alloc\_readonly}(ty); \\ \text{crucible\_points\_to}(p, v); \\ \text{return } p; \end{cases}$$

### 3. ptr\_to\_fresh

Given a name n and a type ty, the function  $ptr_to_fresh$  allocates a fresh variable x of type ty and returns a tuple (x, p) where p is a pointer to x.

$$ptr\_to\_fresh(n, ty) = \begin{cases} x \leftarrow crucible\_fresh\_var(n, ty); \\ p \leftarrow alloc\_init(ty, crucible\_term(x)); \\ return(x, p); \end{cases}$$

#### 4. ptr\_to\_fresh\_readonly

Given a name n and a type ty, the function  $ptr_to_fresh_readonly$  allocates a fresh variable x of type ty and returns a tuple (x, p) where p is a read-only pointer to x.

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```
\mathsf{ptr\_to\_fresh\_readonly}(n,ty) = \begin{cases} x \leftarrow \mathsf{crucible\_fresh\_var}(n,ty); \\ p \leftarrow \mathsf{alloc\_init\_readonly}(ty,\mathsf{crucible\_term}(x)); \\ \mathsf{return}\;(x,p); \end{cases}
```

#### 5. global\_points\_to

Given a name n and a value v, the function global\_points\_to asserts that the global variable n has a value of v.

```
global\_points\_to(n,v) = \{crucible\_points\_to(crucible\_global(n), crucible\_term(v)); \}
```

#### 6. global\_alloc\_init

Given a name n and a value v, the function global\_alloc\_init declares that n is initialized and asserts that it has the value v.

$$\label{eq:global_alloc_init} \begin{split} \text{global\_alloc\_init}(n,v) = \begin{cases} \text{crucible\_alloc\_global}(n); \\ \text{global\_points\_to}(n,v); \end{cases} \end{split}$$

### **LLVM Integer Type Aliases**

```
i8 = llvm_int(8);
i16 = llvm_int(16);
i32 = llvm_int(32);
i64 = llvm_int(64);
i128 = llvm_int(128);
i384 = llvm_int(384);
i512 = llvm_int(512);
```

### 4.1 Key Schedule

- 4.1.1 Whitening-Key
- 4.1.2 LFSR(Left Feedback Shift Register)
- 4.1.3 Sub-Key
- 4.1.4 Encryption and Decryption Key

# 4.2 Encryption

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# 4.3 Decryption

$$\begin{array}{ccc} \text{Plaintext State} & \xrightarrow{\mathbf{Enc}_{AES}} & \text{Ciphertext State} \\ & & & & \downarrow \mathbf{Dec}_{AES} \\ \text{Plaintext State} & \xrightarrow{id} & \text{Plaintext State} \end{array}$$

### Research

In Cryptol 'foldl' is a higher-order function that reduces a sequence (or list) to a single value by iteratively applying a binary function, starting from the left side of the sequence. It is similar to the fold operation found in many functional programming languages.

To understand 'foldl', lets break it down mathematically. Given:

- A binary operation 'f' of type '(b, a) -> b'
- An initial value 'z' of type 'b'
- A sequence 'xs' of type '[n]a' (a sequence of 'n' elements, each of type 'a')

The 'foldl' function can be defined as:

$$foldl f z [x_0, x_1, \ldots, x_{n-1}]$$

This can be described recursively as:

- 1. If the sequence is empty, the result is the initial value 'z'.
- 2. Otherwise, apply the function 'f' to the initial value 'z' and the first element of the sequence ' $x_0$ ', then recursively apply 'foldl' to the result of this function application and the rest of the sequence.

Mathematically, this is:

$$foldl f z [] = z$$
  
 $foldl f z (x : xs) = foldl f (f z x) xs$ 

**Example** Let's take a concrete example to illustrate foldl. Suppose we want to compute the sum of a list of numbers using foldl.

Let.

- f(a, b) = a + b (binary addition function)
- z = 0 (initial value)
- xs = [1, 2, 3, 4] (sequence of numbers)

Using foldl to compute the sum:

$$foldl(+)0[1,2,3,4]$$

Step-by-step:

- 1. Start with initial value z = 0.
- 2. Apply the function to the initial value and the first element: f(0,1) = 0 + 1 = 1
- 3. Apply foldl to the result and the rest of the sequence: foldl(+) 1 [2,3,4]
- 4. Repeat: f(1,2) = 1 + 2 = 3, foldl(+) 3[3,4]
- 5. Continue: f(3,3) = 3 + 3 = 6, foldl(+) 6[4]
- 6. Finally: f(6,4) = 6 + 4 = 10, foldl(+) 10

Since the sequence is now empty, the result is 10.

#### **Summary**

- 'foldl' starts with an initial value and iterates through the sequence from left to right.
- It applies a binary function to the current accumulated value and the current element of the sequence.
- The result of this function application becomes the new accumulated value.
- The process repeats until the sequence is exhausted, at which point the accumulated value is returned as the result.

Understanding foldl helps in performing various reduction operations over sequences in a concise and functional manner in Cryptol.

#### **Algorithm 1:** General GCM

```
Input: N, PT, key, AAD
    Output: R
 1 Zero \leftarrow 0;
 2 Step1:
        CT, H, Y \leftarrow AES - CTR(PT, Zero, key);
        R \leftarrow AAD|0|CT|0|Len;
 6 end
 7 Step2:
        for i \leftarrow 1 to \log_2(N) do
             t \leftarrow t^2;
             *(H+4i) \leftarrow t;
10
        end
11
12 end
13 Step3:
        R \leftarrow 0;
14
        if N \gg 9 == 1 then
15
            R \leftarrow \text{parallel\_ghash\_512}(R, H);
16
        end
17
        for i \leftarrow 8 to 4 do
18
             if N \gg i == 1 then
19
                  temp \leftarrow parallel\_ghash\_2^i(src, H);
20
                  R \leftarrow R \cdot H^{2^{i+1}} \oplus temp;
21
             end
22
        end
23
24 end
25 R \leftarrow R \oplus Y;
26 return R;
```

# **Bibliography**

[1] Galois, Inc. *Cryptol Reference Manual*. Available at https://galoisinc.github.io/cryptol/master/RefMan.html. Accessed April 2024.