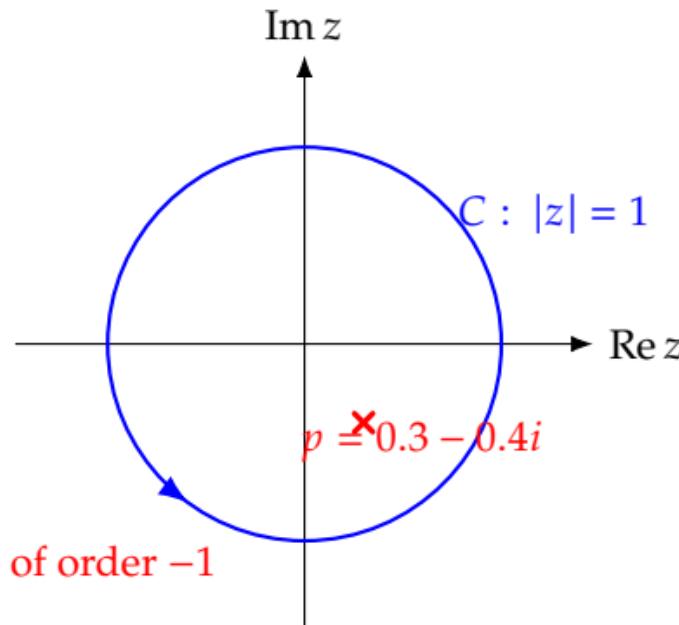
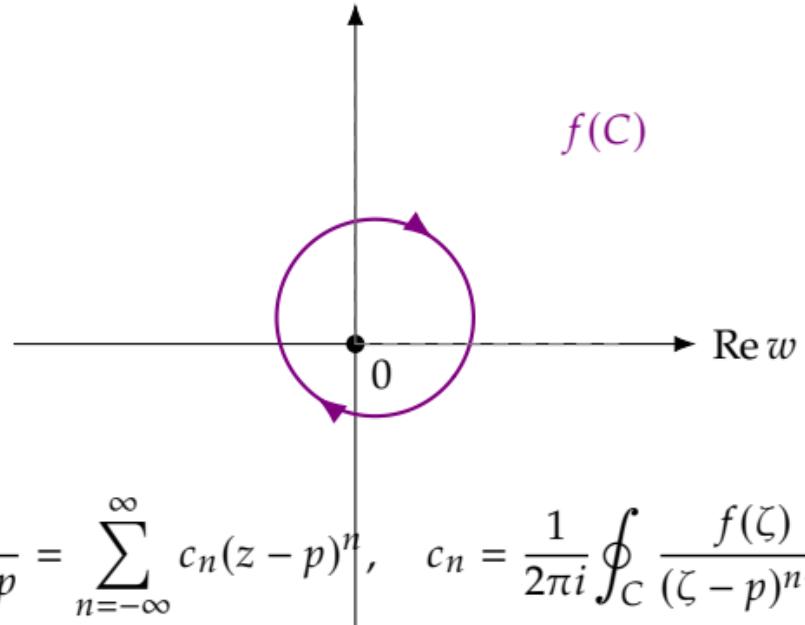


z -plane



$$f(z) = \frac{1}{z-p}, \quad \text{ord}_p f = \text{Res}\left(\frac{df}{f}, p\right) = \frac{1}{2\pi i} \oint_C \frac{-\cancel{f(z)}}{z-p} = 1/(z-p): c_{-1} = \frac{1}{2\pi i} \oint_C f(\zeta) d\zeta = 1, \quad c_n = 0 \ (n \neq -1).$$

$w = f(z)$ -plane
 $\text{Im } w$



$$f(z) = \frac{1}{z-p} = \sum_{n=-\infty}^{\infty} c_n (z-p)^n, \quad c_n = \frac{1}{2\pi i} \oint_C \frac{f(\zeta)}{(\zeta-p)^{n+1}} d\zeta.$$

$$\text{wind}(f(C), 0) = -1 \Rightarrow \oint_C \frac{f'(z)}{f(z)} dz = -2\pi i.$$