

# Software Verification

## Lecture 01. Introduction to Software Analysis

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# Motivation

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# 1. Motivation

1. Software systems are mostly unsafe.

2. Software errors cost the U.S. economy \$60B ( $\approx$  82조) every year.

(1996) Explosion of the Arian-5 rocket. \$8 billion ( $\approx$  11조)

(1998) NASA's Mars climate orbiter lost in space. \$125 million ( $\approx$  1700억)

(2000) Accidents in radiation therapy system. 8 patients died

(2007) Air control system shutdown in LA airport. 6,000 passengers stranded

(2012) Glitch in trading software of Knight Capital. \$440 million ( $\approx$  6000억)

(2014) Airbag malfunction of Nissan vehicles. \$1 million vehicles recalled

# 1. Motivation

## 3. Current Technologies for Safe Software

(a) Code Review

(b) Testing

(c) Debugging

(d) Simulation

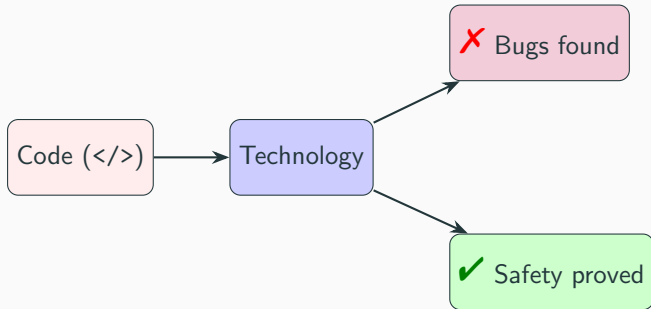
(e) ...

# Software Analysis

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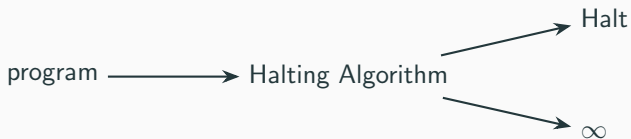
## 2.1 Software Analysis

- Technology for catching bugs or proving correctness of software.



## 2.2 A Hard Limit

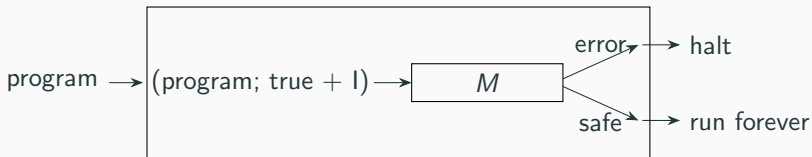
- The Halting problem is not computable. (Alan Turing, 1936)





## 2.2 A Hard Limit

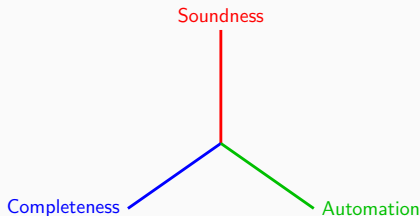
- If exact analysis is possible, we can solve the Halting problem.



- Rice's Theorem (1951): any non-trivial semantic property of a program is undecidable.

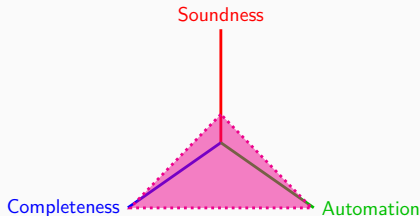
## 2.3 Trade-off

- Three desirable properties
  - **Soundness**: all program behaviors are captured
  - **Completeness**: only program behaviors are captured
  - **Automation**: without human intervention
- Achieving all of them is generally infeasible

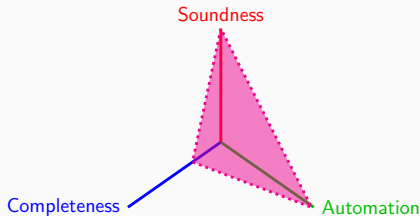


## 2.3 Trade-off

- Completeness + Automation (Testing)

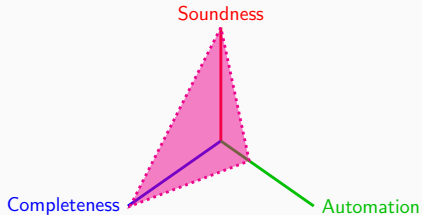


- Sound + Automation (Static Analysis, Compiler)

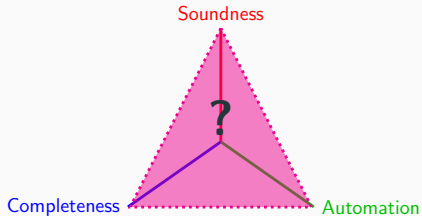


## 2.3 Trade-off

- Soundness + Completeness (Program Verification)



- And ...



# Basic Principle

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### 3. Basic Principle

- Observe the program behavior by “executing” the program
  - Report errors found during the execution
  - When no error is found, report “verified”
- Three types of program execution:
  - **Concrete execution**
  - **Symbolic execution**
  - **Abstract execution**
  - and their combinations, e.g., concolic execution

### 3. Basic Principle

- Concrete

$$2 * 3 - 6 = 0$$

- Symbolic

$$a * b + (-c) = 0$$

- Abstract

$$(\mathbb{R}, +, *)$$

## 3.1 SW Analysis based on Concrete Execution

### Software Analysis based on Concrete Execution (Testing)

- Execute the program with concrete inputs, analyzing individual program states separately.



## 3.1 SW Analysis based on Concrete Execution

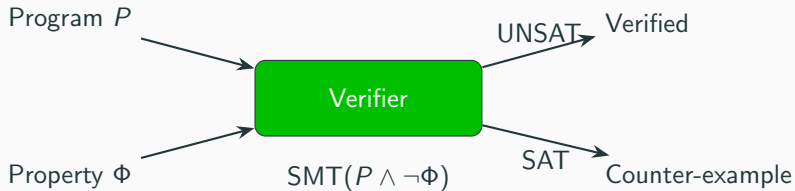
- Error-triggering test? (Test Vector)
- Probability of the error? (assume  $0 \leq x, y \leq 10,000$ )
- **Types of Fuzzing**
  - Blackbox Fuzzing
  - Greybox Fuzzing
  - Whitebox Fuzzing

## 3.2 SW Analysis based on Symbolic Execution

### Software Analysis based on Symbolic Execution

- Execute the program with symbolic inputs, analyzing each program path only once.

### 3.2.1 Example: Symbolic Verification



- Represent program behavior and property as a formula in logic.
- Determine the satisfiability of the formula.

## 3.3 SW Analysis based on Abstract Execution (★)

### Software Analysis based on Abstract Execution (Static Analysis)

- Execute the program with abstract inputs, analyzing all program behaviors simultaneously.

# Abstract Interpretation

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## 4.1 Principles of Abstract Interpretation

$$30 \times 12 + 11 \times 9 = ?$$

- Dynamic Analysis (Testing): 459
- Static Analysis: a Variety of Answers
  - “integer”, “odd integer”, positive integer”, “ $400 \leq n \leq 500$ ”, etc.

## 4.1 Principles of Abstract Interpretation

- Static Analysis Process:

1. Choose abstract value (domain), e.g.,  $\hat{V} = \{\top, e, o, \perp\}$
2. Define the program execution in terms of abstract values:
3. “Execute” the program:

$$e \hat{\times} e \hat{+} o \hat{\times} o = o$$

# Summary

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# Summary: Software Analysis

- Basically classified based on how programs are interpreted:
  - Techniques based on concrete execution
  - Techniques based on symbolic execution
  - Techniques based on abstract execution
- Each approach has its own strengths and weaknesses: e.g.,

	Sound	Complete	Automatic	When
Testing/Fuzzing	✗	✓	✓	Dynamic (Runtime)
Symbolic Execution	✗	✓	✓	Static/Dynamic
Static Analysis	✓	✗	✓	Static
Program Verification	✓	✓	✗	Static
?	⋮	⋮	⋮	⋮

**Questions?**