



Heterogeneity in hour-by-hour demand responses to the electricity spot price *

Thor Donsby Noe [†]

Cathrine Falbe Pedersen [‡]

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Abstract

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Keywords: • • • •

*We are thankful to Frederik Roose Øvlisen for his useful supervision. All errors remain our own.

[†]*E-mail:* thornoe@gmail.com (T. D. Noe).

[‡]*E-mail:* cathrinefp@gmail.com (Cathrine F. Pedersen).

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1. INTRODUCTION

The focus of this paper is to estimate how the hour-by-hour electricity consumption responds to hourly electricity prices for hourly settled consumers (i.e. bigger firms) respectively flex and residual settled consumers (ie. small firms and households). Estimating how price elasticities of demand of electricity has been an economic area of interest for a long time and increasingly so.

The electricity market has changed vastly over the past few decades in the direction of more competition and a larger share of intermittent, renewable energy production capacity. The climate crisis and the related ongoing political debate suggests that this will be equally if not more important in the near future. To policy makers and voters alike decarbonization is strongly linked to greater electrification, but this will only be true if this renewable energy production is large enough to answer to demand. Efficient and environmentally sustainable electricity provision implies that electricity production and thus electricity supply fluctuates according to weather conditions, namely wind speed and sunshine. Heterogeneity and changes over time in demand responses can help predicting potential demand flexibility in the future as this is the main limit for further increasing the reliance on wind and solar power along with the infeasibility of electricity storage. From a policy point of view this can also reveal the potential for time-of-use tariffs (and other demand responses) which are being regarded as the most cost-efficient tool for promoting a more sustainable electricity consumption cf. Albadi and El-Saadany (2008).

"We contribute to the existing literature by ..."
tilføjes

We use hourly observations since January 2016 on aggregated consumption for 52 of the local grid companies in Denmark. To account for heterogeneity across the grid companies we estimate the price-elasticity both grid-by-grid and on aggregate while controlling for grid-level specific effects. The problems of endogeneity resulting from the simultaneity of demand and supply mechanics is handled by instrumenting the hourly price by both lagged prices and the prognosis for wind power production. *** » OUR RESULTS «***

The paper proceeds by giving a brief account of related studies in section 2. Section 3 covers the price formation in the electricity market by going into detail with the market itself in 3.1, the production side in 3.2 and perspectives of the demand side in 3.4. The data used for our empirical analysis is described in section 4 while we go into details with the econometric estimation method in section 5. Results from the analysis are presented and discussed in 6. Section 7 concludes.

2. LITERATURE REVIEW

Estimating price elasticities of electricity and has been an area of interest for economists for a long time and increasingly so. Deregulation of the electricity market made it important to measure how a broad spectre of consumers (residential, industrial and commercial) react to changing electricity prices.

The supply side is becoming even more volatile following the increased share of renewable energy

driven by political goals and competitive establishment costs. In the case of a very inelastic electricity demand Wolak and Patrick (2001) outlines how an oligopolistic supply side can capitalize on intraday peaks in demand, however, firms that are able to have a more flexible energy use can face clear advantages in the market while on aggregate making it possible to further increase the share of renewables in the electricity supply.

Thus, it is of importance to conduct better empirical estimations of how consumers respond at a micro level - in particular because taxes often are used as a policy tool to incentivize a decreased consumption of power. In the following we highlight the key contributions in this area.

2.1. Modest price elasticity of demand

Patrick and Wolak (2001) were among the first to estimate the demand-side responses to electricity prices for intraday-markets. For firms in England and Wales they find the overall magnitude of the real-time price elasticity of electricity demand to be quite low, though significant. Similar results on an hour-to-hour basis are found for the Netherlands according to Lijesen (2007).

Regarding residential electricity demand most estimates of the demand response to price changes of electricity are in the range -2.01 to -0.004 in the short run and -2.25 to -0.04 in the long run as reported in Espey and Espey (2004), who does a meta analysis of 248 estimates in 36 non-time-of-day studies. With the median being -0.28 in the short run and -0.81 in the long run, elasticities tend to be bigger in the long run which is in accordance with economic reasoning since consumers better can better modify their capital stock in the long term. These estimates rely on a wide range of different empirical approaches.

2.2. Heterogeneous effects

Fan and Hyndman (2011) estimate yearly own-price elasticities for Southern Australia at the aggregated level using consumption on a half-hourly basis using a log-linear model. The authors find heterogeneous effects across quantiles, depending on how extreme the weather is.

Though only being able to use the average firm-level responses within each code of British Industrial Classification (BIC) Patrick and Wolak (2001) find a substantial heterogeneity across industries not only in terms of the magnitude of the own-price elasticity of electricity demand but also in the within-day patterns of cross-price elasticities.

2.3. Endogeneity problems

Estimating demands-side responses to shifting electricity prices is associated with potential problems of endogeneity as price and consumptions/production are simultaneous. That is, a higher expected demand can push up the overall prices and vice versa. An example of such a mechanism

Also an unobserved factor can influence both prices and demand.

is that increasing demand-side competition can lead to imports of electricity from more expensive energy sources (Burke and Abayasekara, 2017) resulting in price increases. Therefore lagged prices are often included to avoid an omitted variable bias and to combat endogeneity (Lijesen, 2007), however, this inclusion creates a dynamic bias instead. This is, however, not likely to be as big of an issue in our estimation, because we only consider demand responses in the short run and the bias is likely to be bigger when estimating long term elasticities (Okajima and Okajima, 2013).

Bönte et al. (2015) were able to use wind speed as an instrument for the spot market price, however, the effectiveness of this strategy might be isolated to Germany due to their feed-in-tariff for Renewable Energy Sources that is designed to directly affect the price. Likewise, Graf and Woza-bal (2013) tried using emissions right and prices for primary energy as instruments but to limited success. For the US Burke and Abayasekara (2017) use the state level share of coal and hydro as an instrument for yearly prices as they have generally been the two cheaper source of electricity.

2.4. Estimation methods

When data is limited to total electricity demand it is common to apply a two stage least square (2SLS) regression and either include a time trend (Lijesen, 2007) or estimate the elasticity year-by-year (Bönte et al., 2015).

For more dis-aggregated data different methods can be utilized. Unobserved heterogeneity must be accounted for, usually by including unit-specific fixed-effects. On household level data one option is to use Seemingly Unrelated Regression Equations (SUR/SURE) (Vesterberg et al., 2014).

3. ECONOMIC THEORY/EN ANDEN TITEL

3.1. The electricity market

In order to understand how the price of electricity is formed it is necessary understand how the nature of the supply side, demand side and the workings of the electricity market. The electricity market differs from the majority of other markets because demand and supply must synchronize completely at all times. Storing electricity is possible, but at best highly inefficient and thus too costly to implement practically. Instead supply must be at least as great as demand at all times if blackouts are to be avoided. Historically this has been ensured through the production of a surplus of electricity. This is, however, costly both in terms of inefficiency and because of the associated negative externalities due to carbon dioxide emissions from fossil fueled power plants.

The electricity market consists of both the physical infrastructure required for electricity generation and transport while it on the other hand is also a well-organized market.

There are several ways to organize the market. Within the European Union most of the decisions related to the organization of the energy market happen at the supranational level. It In recent

years the electricity market has undergone great changes following the Third Energy Package. The package aims at improving the functioning of the energy market by ensuring more competition and transparency through unbundling of suppliers from operators, greater independence of regulators, more cross-border cooperation and better transparency in retail markets.¹ This has increased the number of actors on the electricity market that now comprises consumers, producers, distributors, Independent TSO (Transmission System Operators - the owner of the transmission infrastructure), DSO (Distribution System Operators) and balance responsible actors.

In recent years the electricity market has undergone many changes to induce competition and reduce surplus production and thus "unnecessary" carbon dioxide emissions. The move towards more market liberalization still recognizes that the distribution net constitutes a natural monopoly. In many countries including Denmark the firm in charge maintaining and building the grid is still state-controlled while the remaining market operators are private. Competition is then ensured by letting third parties get access to the electric grids in a transparent way. This is only one of several ways to organize a market which has been adopted by the EU, that furthermore wants to promote a single energy market. This is elaborated in section 3.3.

Firms and residential households enter the energy market differently. They face different prices that are formed in different ways. This is described further below.

3.1.1. The retail market

The retail market is comprised by the suppliers and the consumers. The group of consumers consists of both small firms and residential consumers. In the retail-market the suppliers act as intermediaries between the power generators and the consumers. The suppliers then enter the wholesale market (described below) on behalf of the retail consumers and buy electricity from the generators. The consumers are then offered a contract that typically implies that the retail consumers face a single fixed price.

The residential electricity consumers have historically not been treated as 'genuine demanders' (Kirschen, 2003). Instead of facing the actual cost of electricity they instead sign contracts where a distributor acts as a middleman that trades electricity in the market on behalf of its customers, but they receive a premium for undertaking the market risk. The distributors and the consumers then undergo contracts where the price of electricity is typically fixed for up to a year. This insulates the retail consumers from the spot price that better reflects the cost of electricity production at a given point in time. This "distance" to the actual price of electricity is exacerbated even more by the tariffs on electricity that the residential consumers face. These are particularly high in Denmark as they on average make up 62 percent of electricity bills excluding VAT (20 percent).² In addition to the cost of electricity itself each consumer pays a distribution grid tariff, a transmission grid tariff, an electricity tax, PSO (Public service obligation) and sales tax (VAT).

¹<https://ec.europa.eu/energy/en/topics/markets-and-consumers/market-legislation>

²elpris.dk

3. Economic theory/En anden titel

Explain
what
smart
meters
are

It is, however, worth noting that the way residential customers are settled is likely to change in the future as smart meters are adopted more widely. .

For instance Denmark has decided to enrol smart meters to all consumers by 2020 in the Energy Agreement from 2013. In Denmark several grid companies have already rolled out the smart meters which allows for more flexible settlement such that demand can respond to different prices.

3.1.2. The wholesale market

Large scale electricity consumers ³ enter into the wholesale market for electricity. Here electricity is bought and sold in different markets depending on how well in advance before the actual time of delivery the electricity is traded. Electricity is thus traded via

Long term contracts Electricity bought and sold further ahead of time than the day before consumption can be agreed upon by undergoing long term contracts or from trades in the forward market. In the forward market futures, forwards, Electricity Price Area Differentials (EPADs) and put and call options are traded. The products are traded either bilaterally or as stocks at NASDAQ OMX Commodities and serves as a way to reduce risks by ensuring a fixed price or insurance against realized price differentials. The value of the futures (and forwards) shifts based on the reference price that is the official nordic day-ahead price.

The day-ahead market The day-ahead market (The spot-market) is where the majority of electricity is traded either for specific hours or blocks thereof. The price is determined in an auction where all bids and asks are aggregated to form the hourly supply and demand - while the market clearing price is determined by where they intersect subject to the capacity constraints in the market. All the actors in the market (generators, distributors and wholesale clients) pay or receive the same price within a price region. Distributional bottlenecks between regions entails price differences within the market. This price, also referred to as the spot price, thus reflects how much power producers believe they can supply which in turn depends on weather prognoses, expected plant shutdowns etc. but also how much consumers (retail and wholesale) are expected to consume given the physical constraints of the electric grid. It should be noted that Nord Pool Spot have both lower and upper price caps outside of which bids are reduced by a fixed percentage rate.

The intra-day market The day-ahead market closes at 12 pm the preceding day but from 2 pm and up until an hour before time of delivery trade can occur on the intra-day market where. Here electricity is sold in blocks, hours and 15 minute intervals. Similar to the spot-market this is operated by Nord Pool. The quantities traded in the intra-day market is much smaller than the day-ahead market but this is likely to change as a larger share of the production capacity

³In Denmark this entail firms that consume more than 100.000 kWh a year, to whom hourly settlement is obligatory.

is constituted by renewables. From 2016 to 2017 the traded volume in the intraday-market increased by 35 per cent for the Nordic/Baltic/German markets. ^{t4}

The balancing market If gaps between supply and demand remain after the closing of the intraday market they must be balanced by the responsible system operator. Each of the actors in the market rarely live completely up to their obligations for instance more or less wind power can be produced or firms may consume unforeseeable large amounts of electricity. This necessitates that the responsible Transmission System Operator (TSO), Energinet⁵ in Denmark, balances during the delivery period.

3.2. Production and supply of electricity

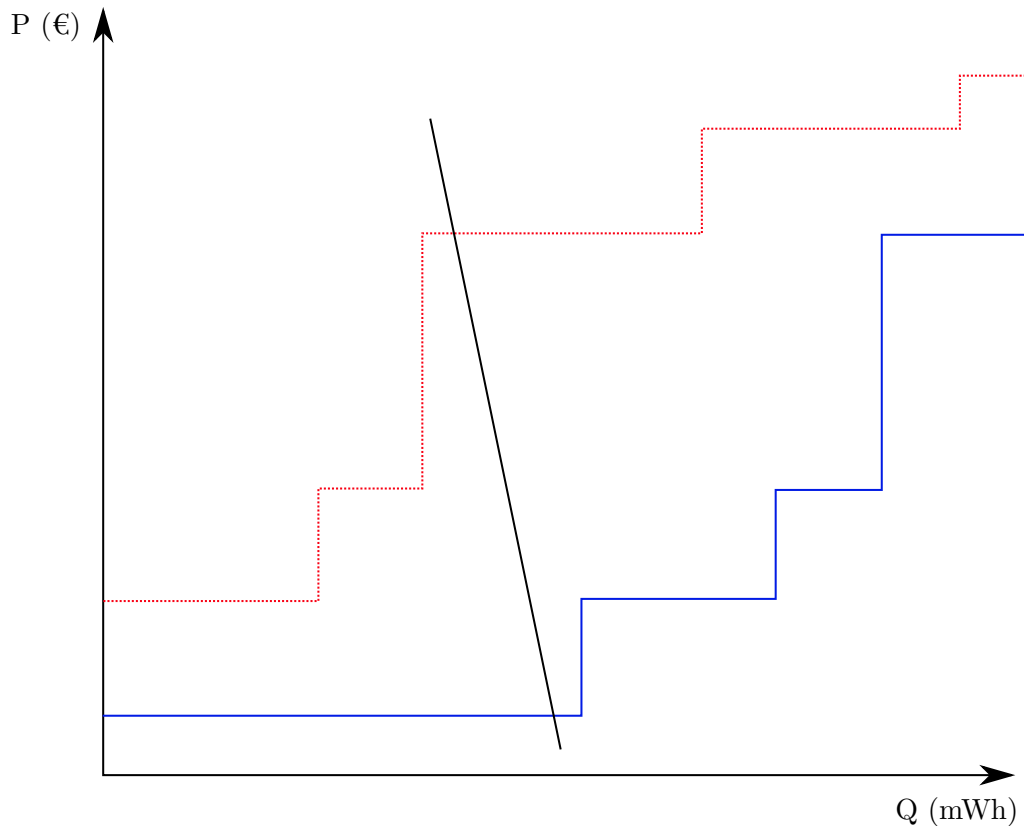
Electricity is supplied by different kinds of power plants that each has their own advantages in terms of when they can produce and how fast they reach an efficient production level. In most of Europe the most common types of power include lignite, coal, gas, nuclear, solar, wind and hydro, ranged from the more emission intense to the least. The marginal cost of electricity from renewable sources are far because almost no (costly) inputs are needed, but these typically require certain weather conditions outside the control of the supplier. Coal and lignite power plants have higher costs running and have to be running for a while to reach efficient production, but do not rely on external parameters. These are typically used as a part of the base-load and are typically used as part of the base-load. The available production capacities and weather conditions thus shape the supply curve.

For each supplier it is optimal (at least in the short term) to ask for the marginal cost of producing electricity at a given point in time. This implies that the supply curve and thus the order in which generators are dispatched reflects the merit order. If the weather conditions are right electricity from renewable sources are dispatched first and then hard coal and lignite plants. If the share of renewables in the productional capacity is large the supply curve is shifted to the right. The marginal costs of electricity production from carbonizing plants are even higher in the EU where the supplier has to buy emission quotas such that renewable and low-emission power production is prioritized.

⁴https://www.nordpoolgroup.com/globalassets/download-center/annual-report/annual-report-nord-pool_2017.pdf

⁵<https://en.energinet.dk>

Figure 1: Merit Order Effect



All receive the same price such that low cost production rewarded. Convergence of prices would be obtained if the interconnection capacity is sufficient.

In the case where the demand for electricity is particularly high i.e. at a peak costs (financial and external) very high are also very high and mainly high-emission. Demand peak \Rightarrow higher prices that are sufficiently high to cover costs of higher cost production units when answering to spikes in demand.

3.3. (European) Market Integration

As mentioned in previous sections the European Energy Market has and is undergoing great changes in order to achieve what is considered a more efficient and thus well-functioning market. This is believed to be insured by inducing more competition in the energy sector - not just from ownership unbundling but also through freer movement of energy. Freer movement of energy would thus imply that electricity is allowed to flow to where it is needed the most. The end goal is thus a single, free (European) energy market. This is currently constrained by limited cross-grid transmission capacities. Depending on demand and supply on each side then a connecting capacity make up potential bottlenecks that can result in different prices. This is evident even for

the relatively small market of Denmark where two price regions exists because the Great Belt Link "only" has a capacity of 600 MW.

Even though capacity constraints are still binding improved integration the Danish market is linked to the Northern European market. Trade happens at the electricity exchange 'Nord Pool'. Nord pool has already combined 13 markets; The Nordic countries, the Baltic countries, Germany, Austria, France, Belgium, the Netherlands and the UK. This and future integration implies that electricity prices in Denmark are under great influence from production conditions abroad. A low hydro reserve in Norway may thus increase Danish electricity prices and sunshine in Germany may vice versa lower prices.

Increased market integration means more harmonised prices and thus lower price volatility. Market integration can pose a solution to achieve an increased share of energy produced by intermittent renewable sources without increasing price volatility and uncertainty. Market integration allows for changes in the composition of the production capacities within the electrical grid to something more optimal where they complement each other => . **Citér nogle der fortæller om hvordan vind/sol og hydro er gode kombinationer - måske bogkapitel will do the trick.** This may become increasingly important as the EU is moving towards achieving its target of 50 percent renewable energy production in 2030 following the Paris Agreement.

3.4. Demand of electricity

It is often deemed more cost-efficient to reduce demand in periods of peak demand as opposed to dispatching high-merit generation plants. This can be prompted through demand responses. Demand responses can be defined as the resulting deviations from normal electricity consumption patterns in response to changes in the electricity price over time. These are often designed to induce lower consumption when demand is particularly high (Albadi and El-Saadany, 2008). Examples include time-of-use tariffs, real time pricing and demand bidding. If implemented effectively they can benefit individuals through lower bills, but also the entire market by deferring or avoided distribution and transmission upgrades, increasing reliability, reducing price volatility and improving the efficiency of the electricity market. For demand responses to provide these benefits consumption should be price sensitive. There are, however, many reasons why demand for electricity can be quite inelastic. If demand, as expected, turns out to be highly inelastic this either points to policies that try to change the demand curve itself or more centralized solutions where for instance the supply side of the market is targeted instead.

Better than "Theory of demand-side response to electricity prices"?

The market of electricity itself differs from most other markets as described above. This complexity of the market and its price formation the price is even higher because the nature of the demand for electricity is of indirect character. Electricity demand, for retail and wholesale consumers alike, is shaped by the demand for the use of other appliances that require electricity to function. This indirectness implies that less information on costs is available to the consumer

at the time of consumption which makes responding difficult. In order to calculate the price of using an appliance knowledge of both electricity prices and how much each device uses is required. Elasticities thus answer the limits of decentralized solutions to ...

In terms of demand of electricity there is an important distinction to make between residential and wholesale electricity consumers. But it is a common feature for both types of consumers that electricity is hard to replace. Much of firms' physical capital run on electricity while the same applies for most household appliances needed for at-home production of food etc. Similarly society's reliance on electricity is increasing as more infrastructure is becoming digitalized and moving away from fossil fuels. Electricity thus a necessity for economic growth and functioning of developed and industrialized economies. Still wholesale and retail consumers differ not only in how they enter into the market but also in the nature of their demand. The differences described further below affect how flexible consumers are and different elasticities are thus to be expected.

Demand for wholesale consumers

Wholesale consumers enter into the wholesale market themselves, as indicated, by their name. This implies that wholesale consumers face the real time prices. Wholesale consumers thus have incentives to lower their consumption when it is costly to produce electricity and prices thus are high. With the exception of when price caps are binding they can thus respond to the state of the market. Firms are also mostly exempt from paying tariffs on their electricity.

For wholesale consumers electricity typically constitute a greater share of all costs as compared to residential consumers. The possible cost reductions that monitoring of prices makes possible are non-negligible. This suggests that most wholesale consumers should be relatively more price sensitive than retail consumers.

On the other hand firms are also subject to more restrictions in regards to when they operate as this is typically in business hours depending, of course, on the nature of the firm i.e. what industry it is in. Similarly firms are often required to deliver a product or a service subject to a contract which does not allow firms to postpone production for too long. This is, however, not likely to affect the hour-by-hour elasticity greatly.

Demand theory for retail consumers

Small scale consumers are more insulated from price fluctuations because they enter the energy market only through a middleman and contracts typically involve a fixed price per kWh albeit this may change in the future. New EU directives dictate that more billing options should be made available to retail consumers in the future. One reason why retail consumers are not flexibly settled yet is that the physical infrastructure required (remotely read meters/smart meters) is not widely installed. In fact many demand responses rely on the consumer being able to inform themselves on the real time prices.

Even if residential consumers and small firms faced real-time prices they ... One obvious limitation to the flexibility of demand is that demand responses require knowledge of prices at a given

point in time. Furthermore it can be costly to take actions in order to reduce demand. Combined these factors may make it optimal for small consumers to not adhere to market signals except when prices are extremely high (Wolak, 2011), which could be due to the introduction of a price based demand response). This implies that many consumers have to rely on behavioral rules when deciding how much energy to consume cf. (Kirschen, 2003).

Another aspect has to do with how electricity is regarded as a good. Kirschen (2003) points to the fact that electricity is regarded as a good that is indispensable and essential to quality of life. It has always been marketed as easily accessible in terms of usage and availability although this may not genuinely be the case.

Residential consumers is more flexible than industrial in at least one aspect: They are better able to forego some consumption. While some consumption is postponed usage of other appliances constitutes foregone consumption instead. Examples include lighting, entertainment related.

Tariffs constitute a considerable share of the electricity bill for residential consumers as described in section 3.1. When tariffs are very large they may overshadow any price fluctuations and thus make it more difficult for residential consumers to adjust their consumption. Tariffs and taxes, unless Pigouvian, are distortionary because prices serve as the suppliers' only signal of the true cost of production at a given point in time.

This all adds up to an expected weak elasticity.

4. DATA AND VARIABLES

We have scraped most of our data from various web sources in respect of the terms of use. The descriptive statistics for the main variables are shown in Table 1 and described in further detail for the remainder of this section.

For the regressions we log-transform electricity consumption, the number of electricity meters, and the electricity spot price. Before taking the natural logarithm the variables are censored with 1 as the lower bound whereby we loose some information as the spot price is negative for a few instances due to exceed wind power production.

4. Data and variables

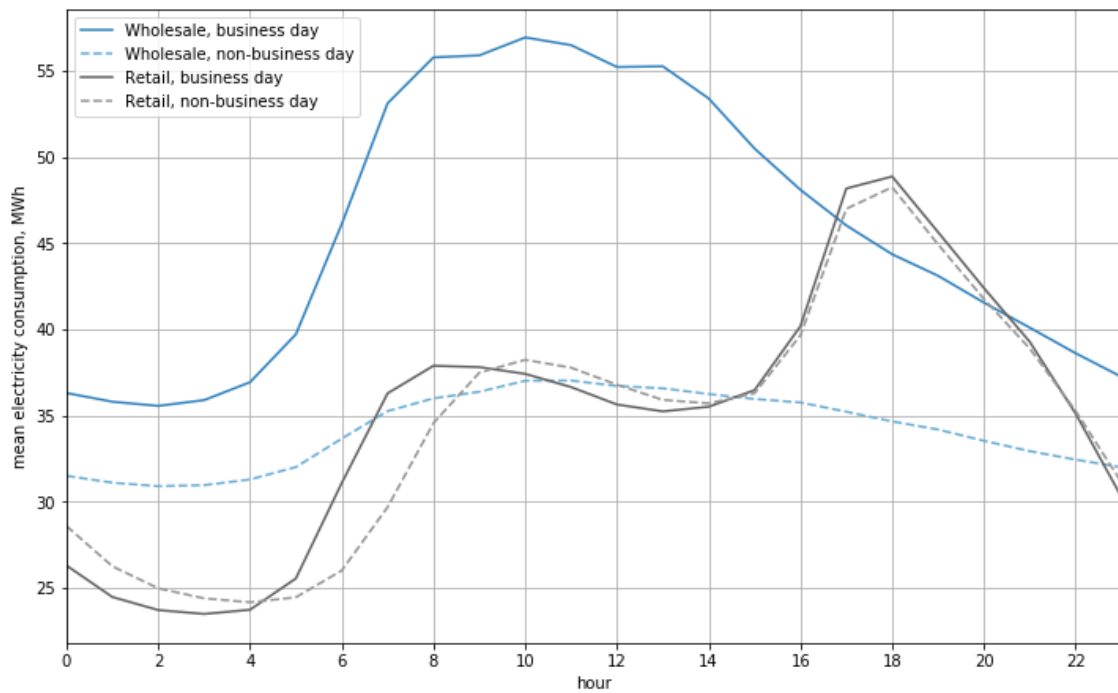
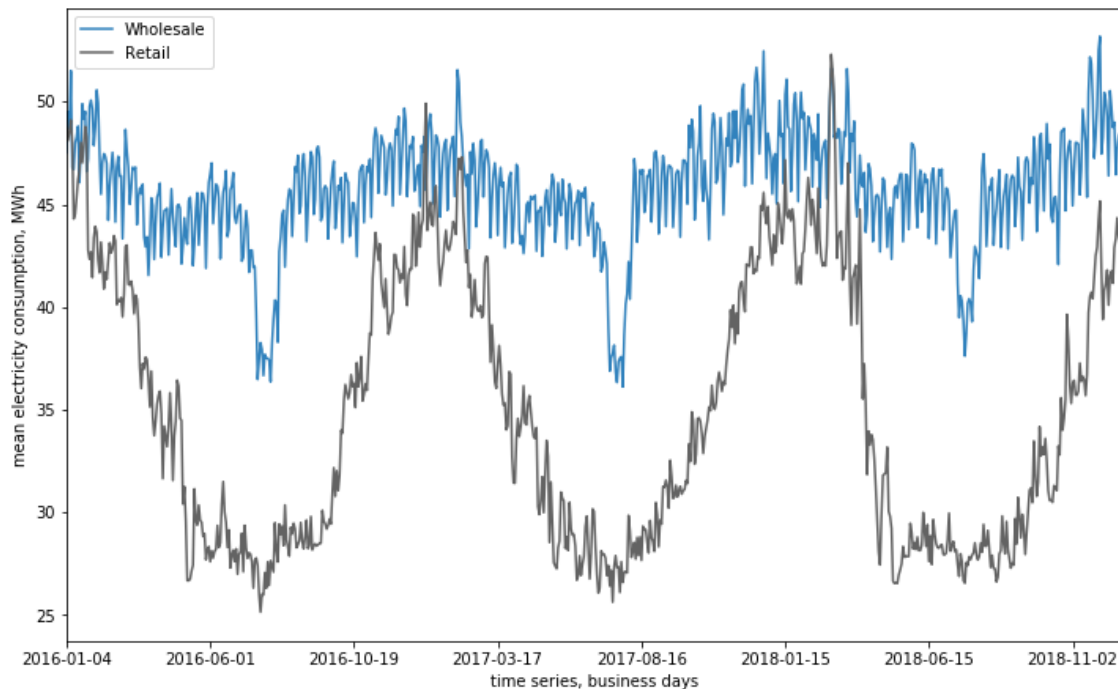
Table 1: Descriptive statistics

	mean	sd	min	p50	max
Wholesale electricity consumption, MWh	41.92935	92.16819	.082169	7.644501	757.5571
Retail electricity consumption, MWh	34.7628	80.92455	0	7.593214	906.3964
Number of wholesale meters	1113.68	2659.874	15	210.5	17674
Number of retail meters	68474.39	160277.3	1080	16564.5	1006061
- of which flex-settled	4836.807	39416.33	0	0	596267
- of which residual	63637.58	146395.8	974	16106	998864
Electricity spot price, DKK	253.3359	108.2735	-398.61	235.17	1898.9
Wind power prognosis for DK1, GWh	1.225359	.9221094	0	1.002	3.973
Wind power prognosis for DK2, GWh	.3266759	.2702798	0	.249	1.084
Wind power prognosis for Sweden, GWh	1.862874	1.118507	.062	1.668	5.84
Price region DK1 (Western Denmark)	.8125	.3903125	0	1	1
Share time-of-use tariff (Radius only)	.000155	.0084536	0	0	.5926748
Temperature	9.116639	6.923547	-11.9	8.8	31.4
Daytime	.5135255	.4857338	0	.6666667	1
Time trend	547.4559	316.4119	0	547	1095
Holiday (not in a weekend)	.0437643	.2045702	0	0	1
Observations	1,262,400				

4.1. Grid-level consumption

The Danish Transmission System Operator (TSO), Energinet provides public access to hourly aggregated consumption data⁶ since January 2016 for each grid company grouped by hourly-settled consumption, flex settled consumption, and residual consumption. This allows us to distinguish between wholesale and retail consumption. Hourly-settled consumption consists of all firms with an annual electricity consumption of at least 100,000 kWh. Flex-settled consumption was introduced in January 2018 such that households and small firms can also have their electricity consumption settled flexibly according to hour-by-hour prices. Though installation of smart meters to enable flex-settling is only being introduced gradually, this allows a portion of residential consumers and small firms to respond to price changes at an hourly rather than a yearly or quarterly basis. The residual consumption is the remaining retail electricity consumption for which flex-settling is not used, thus, including all households and small firms till December 1 2017 and a majority throughout 2018 as well.

⁶Scraped from energidataservice.dk/en/dataset/consumptionpergridarea using their transparent API via SQL statements.

Figure 2: Mean electricity consumption by hour and type**Figure 3:** Time series for mean electricity consumption (business days)

As shown in figure 2 and 3 both wholesale and retail consumption follow clear patterns not only within the day but also between days and across the year. That is, wholesale consumption is at its lowest on weekends and bank holidays as well as during the summer holiday while retail

4. Data and variables

consumption peaks for the hours 5-7 PM (from here written as hours 17-19) and during the winter half of the year.

For each grid we include the number of metering points⁷ by each of the three consumer categories. This data is monthly by the 1st of the month. For studies on state-level data it is likewise common to control for size (Burke and Abayasekara, 2017).

The landscape of grid companies have changed drastically. From consisting of 74 grid companies by early 2016, only 56 grid companies remained by the end of 2018 (see figure A.1 in appendix A). Removing the two grids with less than 10 metering points and the six grids with no wholesale consumption leaves us with 48 grids of which no less than 39 are located in Western Denmark. For a merged grid company we apply the sum of grids included in a future merge to each prior month as described in appendix A.

4.2. Spot market prices and wind power prognosis

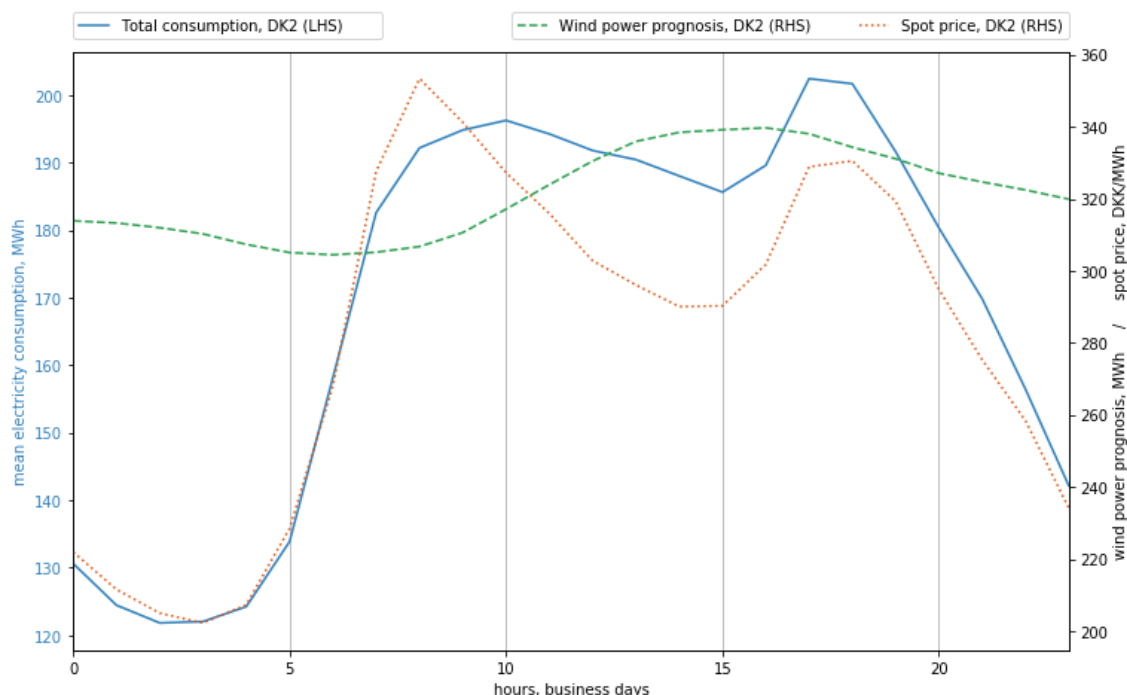
We include the hour-by-hour spot market price on the day-ahead-market for the price region DK1 (Western Denmark) or DK2 (Eastern Denmark) depending on where the grid company is located (see section 3). An important factor for the spot price on the day-ahead-market is the hour-by-hour wind power prognosis for the following day.⁸ While being less volatile than wind power production, price is nonetheless highly volatile from day to day while having increased in 2018 as illustrated by the time series in figure B.2 and B.3 (appendix B).

The wind power prognosis first and foremost takes into account weather forecasts in relation to the positions and capacity of windmills but also takes into account the expected demand as some wind mills can possibly be turned off if the expected price is too low. However, except for a slight peak in the afternoon and evening that is more likely due to sea and land breezes, wind power does not seem to care much for consumption patterns during the day (figure 4 for DK2 and B.4 for DK1) and especially not across weekdays (figure B.5).

On the contrary, the daily pattern of the spot price on average follows the pattern of demand by and large. The biggest gap between price and total consumption seen in figure 4 occurs during the afternoon where the low price relative to demand could possibly be explained by the higher wind power production.

⁷Received from Energinet after request.

⁸'Elspot prices' and 'Wind power prognosis' by price region and year is updated daily after 2PM by Nord Pool and downloadable at nordpoolgroup.com/historical-market-data

Figure 4: Total consumption, wind power and spot price by hour (business days)

4.3. Time-of-use tariff

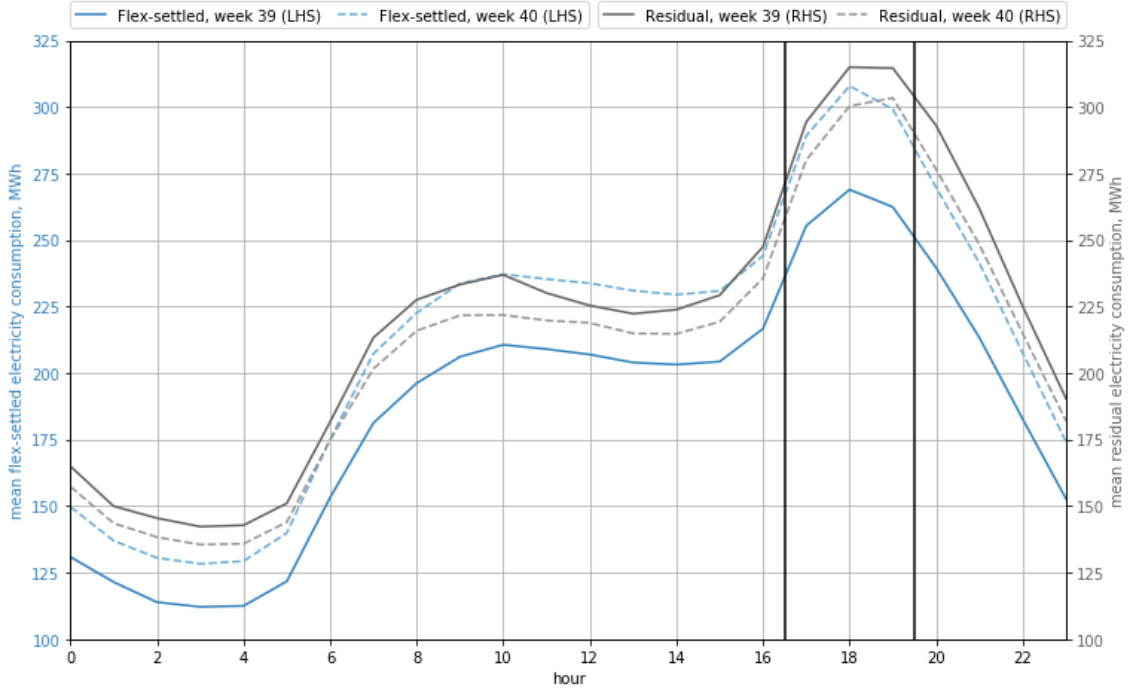
From December 2017 grid companies have been allowed to introduce time-of-use (TOU) tariffs for retail consumption in order to send signals that can direct the more flexible tasks away from the peak hours around dinnertime. Thus, two of the bigger grid companies have already introduced TOU tariffs for the peak-hours 17-19 for the months October-March in which electricity consumption is also higher due to the lack of daylight. While Konstant initially only runs an experiment for a smaller group of flex-settled consumers, Radius is introducing a full-scale TOU tariff scheme while exchanging the old prepayment meters with smart meters for the 600,000 retail customers in the Copenhagen metropolitan area.⁹

The variable for the TOU tariff represents the share of retail customers in Radius exposed to the tariff. As seen in Figure 5 and Table 1 below the increasing share ends near 60 pct. in December 2018. The concept of aggregate data makes it difficult to demarcate changes in behavior from changes in composition. In figure 5 we try to investigate the discontinuity around October 1 2018 as week 39 is in September and week 40 is in October. From a graphical inspection no clear response to the TOU tariff stands out, except that flex-settled consumers have higher consumption during the day and residual consumers during the night which might be due to sociodemographic differences between the areas with smart meters and those where it has yet to be implemented.

⁹See ing.dk/artikel/nu-loebes-fleksible-elforbrug-omsider-gang-209251 (Danish).

4. Data and variables

Figure 5: Flex-settled and residual consumption by week (Radius, 2018)



4.4. Weather data

The outside temperature is relevant to the extent that electrical heaters or air conditioning is used (Lijesen, 2007; Vesterberg et al., 2014). As the electricity consumption *ceteris paribus* is expected to be higher for both low-end and high-end temperatures, we let the effect of temperature enter as a 2nd order polynomial in the estimation of electricity consumption.¹⁰

Lighting is used more in the absence of daylight. Therefore, an indicator for daytime is included such that $daytime = 1$ for hours between sunrise and sunset and e.g. $daytime = 0.25$ for $hour = 7$ if sunrise was a quarter past 7.¹¹

Taking advantage of the dense size of Denmark, temperature and daytime are not scraped by the location of each of the 52 grid companies which often cross municipality-borders but for the two most populace municipalities and applied to all grids within that price region.¹²

4.5. Time variables

Year dummies as well as a time trend indicating the number of days since January 1 2016 are included to account for economic growth (increase in electricity consumption), technological progress

¹⁰Scraped via iterative lookups in the records of the Danish Meteorological Institute at dmi.dk/vejarkiv/

¹¹Sunrise and sunset are scraped for each date in the sample via iterative lookups at soltider.dk

¹²Temperature is for the municipalities of Aarhus and Copenhagen respectively while sunrise and sunset are for the City Hall Square in each of the two cities.

(decrease in electricity consumption) (Lijesen, 2007), or compositional changes that can affect electricity consumption other than the number of meters.

Danish bank holidays as well as a few other common holidays with lower wholesale electricity consumption¹³ are taken into account in order to do sample split regressions for business days and non-business days, the latter including holidays and weekends.

5. EMPIRICAL STRATEGY

5.1. Baseline model

Our baseline model is a Random Effects (RE) model to be estimated using feasible Generalized Least Squares (fGLS). Electricity consumption e for grid company i at time t (date by hour) is given by:

$$\begin{aligned} \ln e_{it} = & \varepsilon \ln \hat{p}_{rt} + \delta \ln n_{im} + \mathbf{w}'_{rt} \lambda + \gamma \text{ days} \\ & + \eta_{year} + \eta_{week} + \eta_{month} \cdot \eta_{hour} + \eta_{day} \cdot \eta_{hour} + \psi_i + u_{it} \end{aligned} \quad (5.1)$$

Where p is the electricity spot price in price region r at time t , n is the number of meters at the beginning of the month m , \mathbf{w} is a vector of weather variables for the given price region r at time t . Time variables include the time trend $days$. The η 's represent dummies for each year and each ISO week number, as well as dummies for hour of the day interacted with each month and each day of the week respectively. ψ_i is the grid-specific time-invariant constant term that is treated as random and u_{it} is the idiosyncratic error term.

We use a log-log specification for electricity consumption, the spot price, and the number of meters as it allows us to model demand responses across grid areas of different size. Furthermore, log-log is the more standard specification which allows for a more direct comparison to the results in other studies (Burke and Abayasekara, 2017). Other attractive properties include that the estimation provides the elasticity directly and does not predict non-positive electricity consumption, furthermore, the specification reduces the impact of outliers and are found to reduce systematic patterns in the estimated residuals (Burke and Abayasekara, 2017).

The specification is first estimated for each hour of the days to identify peak-hours, off-peak, and the shoulder-period.

5.2. Instrumenting for prices

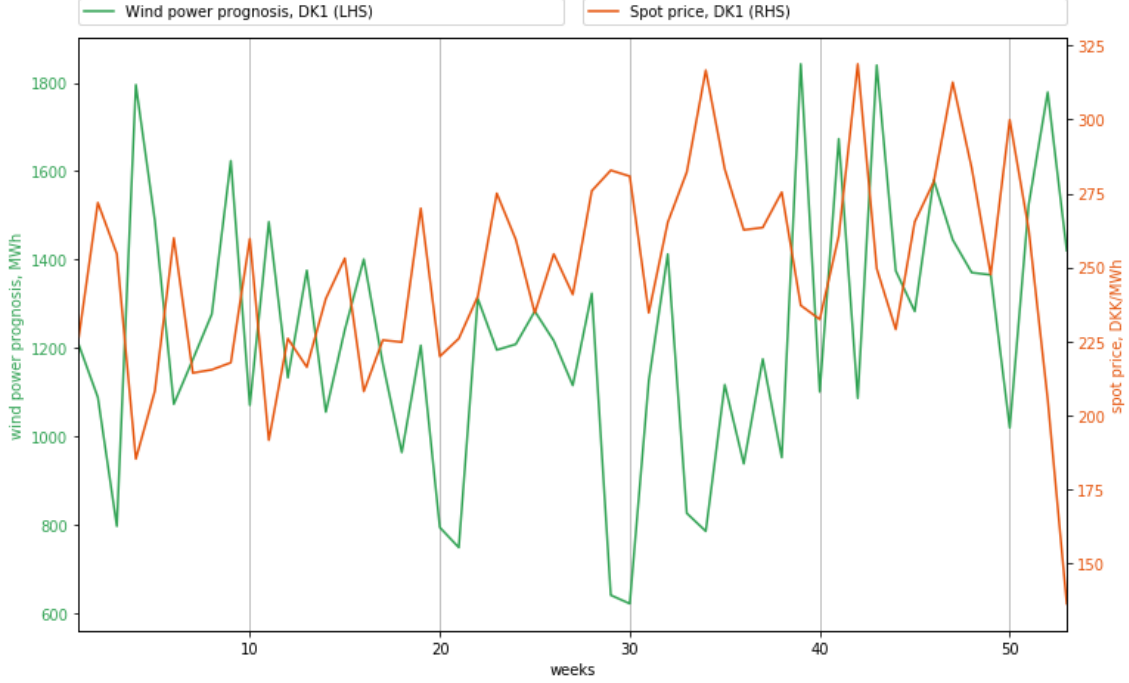
To circumvent the simultaneity problem described in section 2.3 we consider using lagged prices or wind-power production as price instruments. This makes sense as the marginal cost of production

¹³ January 2 (the day after New Year's Day), May 1 (International Workers' Day), Friday after Ascension Day, June 5 (Constitution Day), last Friday before Christmas, and the days between Christmas and New Year's. All holidays according to kalendersiden.dk

5. Empirical strategy

is close to zero, such that a high expected wind-power production will increase the overall supply capacity and drive down the prices as seen in figure 6 (and figure 6 in appendix B for DK2).

Figure 6: Wind power prognosis and spot price by week (DK1)



5.3. Effect of Time-of-use tariff

Since 2018 flex-settled consumers in the Copenhagen metropolitan area are charged a time-of-use (TOU) tariff for the hours 17-19. To estimate this effect the baseline specification (5.1) is estimated for the hours 17-19 solely for the grid company Radius using 2SLS, thus, without the grid-area random effect ψ_i but including a term for the effect of the TOU tariff:

$$\beta \frac{n_{f_{month}}}{nr_{month}} \tau_{year, month} \quad (5.2)$$

Where n_f is the number of flex-settled meters by month, nr is the total number of meters for retail customers, and τ is a dummy for being in January-March or October-December in 2018. To isolate the effect of the TOU tariff we need to assume that residual consumers do not react on the tariff, on the contrary their consumption is assumed to follow the same hour-by-day, hour-by-month, and week patterns as the previous years and the effect of year dummies and the time trend to be evenly distributed across the year.

As Figure ?? shows, a weakness is that the monthly records for the number of flex-settled meters provides a lack which can result in an upward bias of $\hat{\beta}$.

5.4. Random Effects estimation

Different candidates for panel data estimation

- Least Squares Dummy Variables estimation (LSDV)
 - Unobserved heterogeneity, $\psi_i > 0$, leads to serial correlation
- Fixed Difference estimation (FD)
 - Strict exogeneity assumption, $cov(u_{it}, \mathbf{x}_{it}) = 0$, is violated by hourly-patterns
- Fixed Effects estimation (FE)
 - Time-demeaned, too extreme
- Dynamic Panel Estimation using Generalized Methods of Moments (GMM)
 - Only necessary if including lagged prices as instruments

We choose the **Random Effects estimator (RE)** for wholesale consumption

- Critical assumption for RE: No endogeneity, i.e. $cov(\psi_i, \mathbf{x}_{it}) = 0$.
- Hausman test: $\hat{\beta}_{RE} = \hat{\beta}_{FE}$ no endogeneity, thus both RE and FE are consistent, but RE is more efficient.

Estimate RE estimation using **feasible Generalized Least Squares (fGLS)**

1st stage: Estimate eq. (5.1) using LSDV estimation \rightarrow store $\hat{\lambda} = 1 - \left(\frac{\sigma_u^2}{\sigma_u^2 + T\sigma_\alpha^2} \right)^{\frac{1}{2}}$

2nd stage: LSDV using $\hat{\lambda}$ to estimate the quasi-time demeaned system of the form: $y_{it} - \hat{\lambda}\bar{y}_i = \beta_0(1 - \hat{\lambda}) + \beta_1(\mathbf{x}_{it} - \hat{\lambda}\bar{\mathbf{x}}_i) + \psi_i(1 - \hat{\lambda}) + u_{it} - \hat{\lambda}u_{it}$.

5.5. Robustness checks

The robustness of the elasticity for wholesale electricity demand in the peak-hours 12-15 is tested by splitting the sample by region, year, and month respectively to look for heterogeneous effects. Furthermore, we run do the estimation for each grid area and for the mean of each price region using 2SLS. As the FE estimates are identical, however less efficient, we also try to weight the estimates by the number of wholesale meters in each grid.

Tests of the robustness of the effect of the TOU tariff is less straight forward. We try including the dummy constructed for Radius in estimation of retail electricity demand in different grids.

6. RESULTS AND DISCUSSION

6.1. Results for wholesale

For the peak-hours 11-15 on business days wholesale of electricity is estimated to decrease with 5.5 pct. when the spot price doubles, other things equal (Table 2).

6. Results and discussion

Table 2: log wholesale electricity consumption (REIV)

	(1) Peak: 11-15 b/se	(2) Off-peak: 00-04 b/se	(3) Shoulder b/se	(4) Non-business day b/se
log spot price	-0.0484*** (0.0163)	-0.0266*** (0.0094)	-0.0333** (0.0149)	-0.0189* (0.0099)
log wholesale meters	0.1578*** (0.0375)	0.1422*** (0.0399)	0.1255*** (0.0332)	0.1424*** (0.0375)
Temperature	-0.0036*** (0.0008)	-0.0014** (0.0006)	-0.0022*** (0.0004)	-0.0038*** (0.0006)
Temperature squared	0.0002*** (0.0000)	0.0001*** (0.0000)	0.0001*** (0.0000)	0.0002*** (0.0000)
Daytime			0.0198*** (0.0052)	0.0966*** (0.0085)
Time variables	Yes	Yes	Yes	Yes
R^2 within	0.3614	0.1576	0.5797	0.1414
R^2 between	0.9492	0.9140	0.9375	0.9250
Number of groups	48	48	48	48
Obs. per group	3,675	3,675	13,178	8,660

Cluster robust standard errors are in parentheses. * $p < 0.10$, ** $p < 0.05$, *** $p < 0.01$.

Log spot price is instrumented for by wind power prognosis for the same and the other region.

6.2. Results for households and small companies

For the grid company Radius operating in the Copenhagen metropolitan area flex-settled customers (households and small companies) are charged a Time-of-Use (TOU) tariff of 0.835 DKK (0.112 EUR) for the hours 17-19 from October-March as opposed to 0.3236 DKK otherwise (0.043 EUR). The estimated effect of this tariff is found to be a decrease in electricity demand of 1.9 pct. However, on business days the smaller effect of 1.4 pct. is only statistically significant at the 10% level while the decrease is 4.4 pct. on non-business days. Table 3 shows pooled 2SLS estimates of electricity consumption for households and small companies in Radius for the hours 17, 18, and 19. The estimation results also show a small elasticity for the hourly spot price which is instrumented for by wind power prognosis for DK2 and DK1. This is despite that for two of the three years none of the consumers pay the spot market price rather than a quarterly average.

Table 3: log retail electricity consumption in Radius, hours 17-19 (P2SLS)

	(1) All days	(2) Business days	(3) Non-business days
	b/se	b/se	b/se
log spot price	-0.0184** (0.0076)	-0.0251*** (0.0081)	0.0061 (0.0179)
Share time-of-use tariff	-0.0219*** (0.0081)	-0.0137* (0.0080)	-0.0408** (0.0174)
log retail meters	-1.6012* (0.8606)	-1.2889 (0.9208)	0.3618 (1.6832)
Temperature	-0.0029*** (0.0006)	-0.0040*** (0.0007)	-0.0026** (0.0013)
Temperature squared	0.0000 (0.0000)	0.0000 (0.0000)	-0.0000 (0.0000)
Daytime	-0.0450*** (0.0104)	-0.0450*** (0.0108)	-0.0250 (0.0198)
Time variables	Yes	Yes	Yes
Adj. R^2	0.9462	0.9587	0.9297
Observations	3,288	2,205	1,083

Robust standard errors are in parentheses. * $p < 0.10$, ** $p < 0.05$, *** $p < 0.01$.

Log spot price is instrumented for by wind power prognosis.

6.3. The validity of instruments

Table 4: Reduced form of log spot price for DK1 (POLS)

	(1) Price DK1	(2) Price DK1	(3) Price DK1	(4) Price DK1
	b/se	b/se	b/se	b/se
Wind power prognosis same region	-0.0920*** (0.0137)	-0.0951*** (0.0130)	-0.1617*** (0.0079)	
Wind power prognosis other region	-0.2727*** (0.0478)	-0.2724*** (0.0479)		
Wind power prognosis for Sweden	-0.0048 (0.0057)			
log wholesale meters	-0.6420 (0.9546)	-0.6021 (0.9505)	-1.0020 (0.9144)	-2.1420** (0.9763)
Temperature	-0.0236*** (0.0033)	-0.0238*** (0.0033)	-0.0235*** (0.0034)	-0.0357*** (0.0039)
Temperature squared	0.0008*** (0.0001)	0.0008*** (0.0001)	0.0008*** (0.0001)	0.0014*** (0.0002)
Time variables	Yes	Yes	Yes	Yes
Adj. R^2	0.4604	0.4605	0.4550	0.3666
Observations	3,675	3,675	3,675	3,675

Robust standard errors are in parentheses. * $p < 0.10$, ** $p < 0.05$, *** $p < 0.01$.
Business days, hours 11-15. Baseline: year 2016 and each hour for December.

Test for endogeneity (Appendix C) and overidentifying restrictions (Appendix D). (StataCorp, 2017).

6.4. Heterogeneity and robustness

Heterogeneous effects

Figure 7: Wholesale elasticity by hour

Figure 8: Wholesale peak-elasticity by log grid size

6.5. Discussion

The estimated elasticities that we obtain are in size and statistical significance close to what others have obtained (insert references). they all point to the same thing - namely that even for the

most elastic part of the market electricity demand is inelastic. This suggests that the prospects of using demand response programs are limited.

Decentralized solutions should focus on moves of the demand curve rather than along. The small magnitude of the effect and how weak evidence from the Time-of-use introduced in Radius' grid points in the same direction.

The time-of-use tariff did seem to have an effect outside of the area that was actually affected by the tariff. This could be a response from knowing that electricity demand and thus emissions from production are high in the peak period. This extra piece of information could be the driver of the result rather than an effect from changed prices. So even though people do not appear to respond much to prices of electricity this could just be due to little available information.

There could still be decentralized solutions to the problem. One obvious solution would be to limit the number of contracts where consumers pay a fixed price and increase contracts with flexible settlement and then do this in combination with programs that provide more information to what the price of electricity is, but also the cost of using a given appliance during peak compared to off-peak or shoulder periods. Legislation such that price examples are provided - even though this could burden the producers and ultimately result in higher prices for the appliance itself. Another concern here is that this could also have the opposite effect if the price provided then is perceived as too small to matter rather than exacerbate prices. This would likely be the case if people rely on heuristics.

Furthermore there is much experimental research devoted to look into getting people to conserve energy because consumers standard economic tools does not appear to have much of an effect. This paper highlights the importance of these results. Examples include (Allcott, 2011) where US consumers are informed about how their own consumption of energy compares to that of their neighbours which especially causes those with a relatively high consumption to adjust it to a level closer to that of their neighbours thereby conforming to social norms. This points to a similar solution of trying to change what is perceived as "normal consumption" and how electricity is perceived as a necessary good. From descriptive analysis we note that consumption is much lower in summer so potential to reduce in wintertime too despite higher requirements for electrical heating and lighting. Another example is (Saele and Grande, 2011) where they use information in combination with a DR-mechanism. Authors find that costumers respond more than in other studies and conclude that it especially has potential for consumers with electrical heating which is not of much relevance to Denmark.

Demand side management may not be the most easiliy implemented and effects may not be enough to really make a difference. These intiatives may be cost-effective but there is also limited evidence of how persistent the effects are over time.

Given how costly it can be for the consumer to alter their consumption behaviours there may be a bigger need for more centralized solutions to the issue.

7. Conclusion

One option could be to directly affect and alter the supplying capacities.

Increased market integration may actually satisfy many of these requirements. As discussed More integrated electrical grids in terms of greater connecting capacities across the current price regions. This could lead to less price volatility in spite of more reliance on intermittent renewables. This corresponds to diversification of generation portfolio. Eventhough some of the generated electricity is lost from transportation over large distances improvements to the connecting capacities could still smooth out price differences across grids. This could make an electricity production that relies on intermittent renewable sources more stable. This would almost correspond to invest across a market index which would make individual price risk from each producer smaller. It would for allow for complementary production capacities among the energy producers. This is already happening but could be part of getting rid of fossil reliant energy production. Hydro and wind energy for example complement each other well. Hydro makes a great reserve which can be deployed in all kinds of weather so useful when the wind does not blow and then cheap wind power can be used to pump water reserves full again. Initiatives in this direction are already being taken at the European level with the 'Clean Energy for all Europeans' package consisting of 8 legislative acts and the renewable energy directive.

This alone may not be enough. This may not be as feasible because it relies on

6.6. Possible extensions

One possible extension could be to include grid-specific effects other than the random constant term. This is feasible yet cumbersome. The motivation being that one can expect a exists great variation between companies in terms of size, distribution of customers (residential and commercial), industry-intensity. Both at a certain point in time and regarding the time patterns. In our estimation results the time trend does not carry much explanatory power given the other controls, however, this can be due to effects of different direction for different grids covering different areas of the country.

A very tractable extension would be to use micro data which would allow to control for compositional changes in the presence of heterogeneous consumers. Similarly more detailed data would allow for an exploration of further heterogeneities in terms of who is more or less responsive to electricity prices. This would be useful for both the wholesale market where it could be interesting to look at businesses in different industries while for the retail consumers it would be interesting to explore how educational level affects price responsiveness.

7. CONCLUSION

We estimate statistically significant own-price elasticities of demand for wholesale consumers and a statistically significant effect of the time-of-use (TOU) tariff in the grid company Radius. However,

the economic magnitude of the quite modest is debatable.

Literature in this field is quite large but there is still substantial room for improvement, especially within the field of estimating hour-by-hour responses at the micro-level to capture heterogeneity in this aspect.

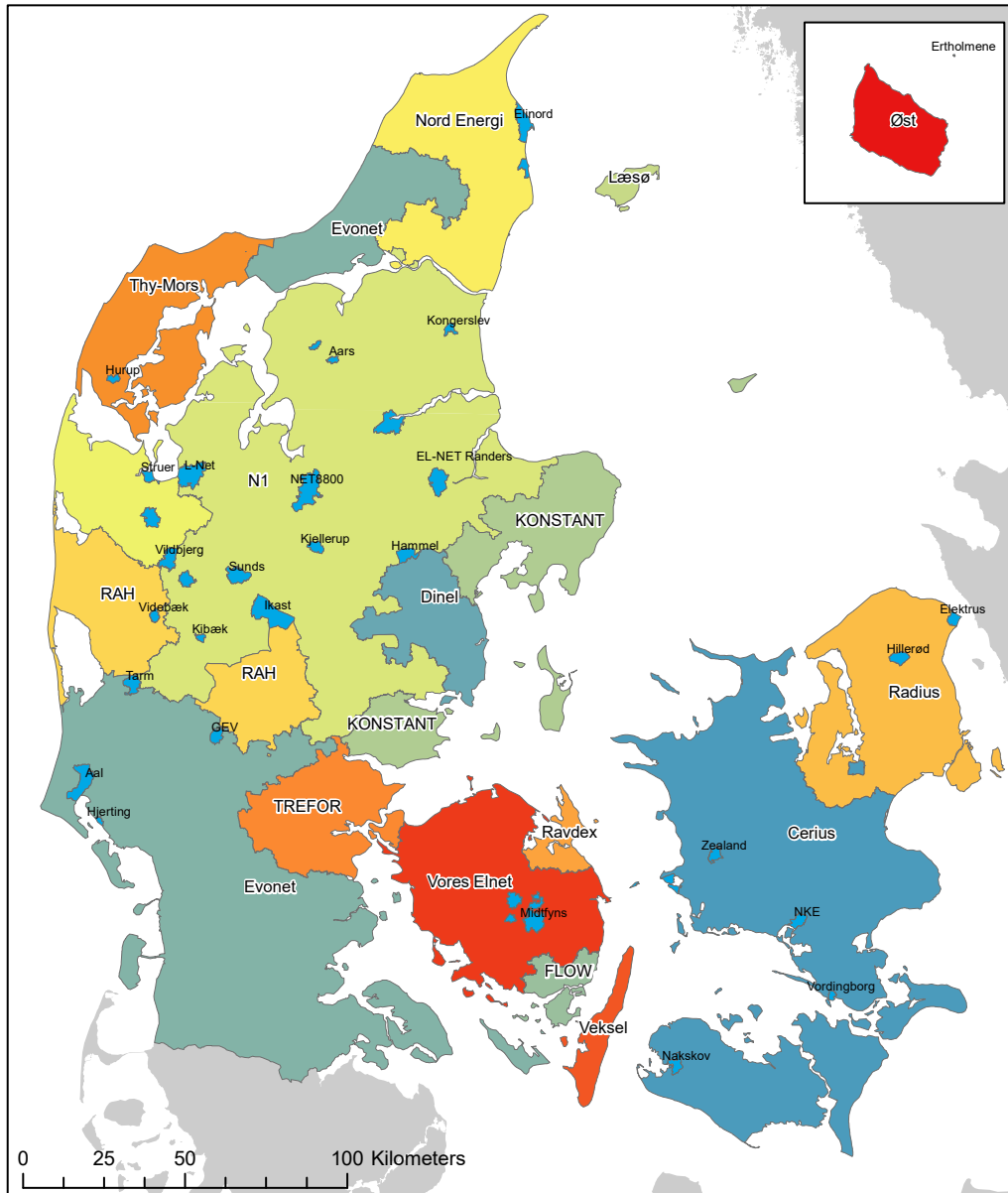
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A. GRID COMPANIES

Figure A.1: Grid companies by may 2019



Source: Danish Energy Agency (Energistyrelsen).

Mergers during 2016-2018:

- Nord Energi took over Taars by December 2017 and Hirtshals by January 2018.
- Læsø took over Hornum by October 2017.
- EnergiMidt merged with HEF, AKE, Bjerringbro, ELRO, EnergiMidt Vest, Borris, and Sdr. Felding by January 2018 and Nibe by April 2018, taking the name Eniig and later N1.
- Dinel was founded as a merge of Brabrand, Viby, GE, and Østjysk by April 17.
- SE took over VOS and Ærø by January 2018, later renaming to Evonet.
- RAH Net took over RAH Net 2 by December 2017 and MES Net by March 2018.

B. DATA FOR WIND POWER PROGNOSIS AND SPOT PRICE

Figure B.2: Time series for wind power prognosis and spot price (Western Denmark)

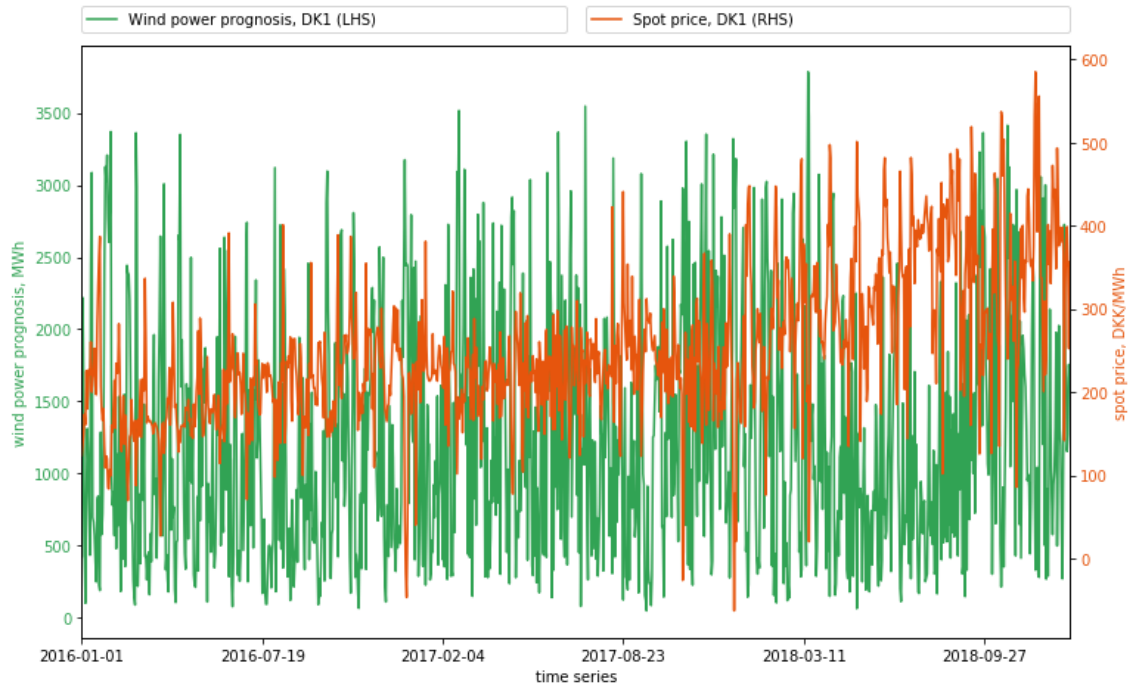


Figure B.3: Time series for wind power prognosis and spot price (Eastern Denmark)

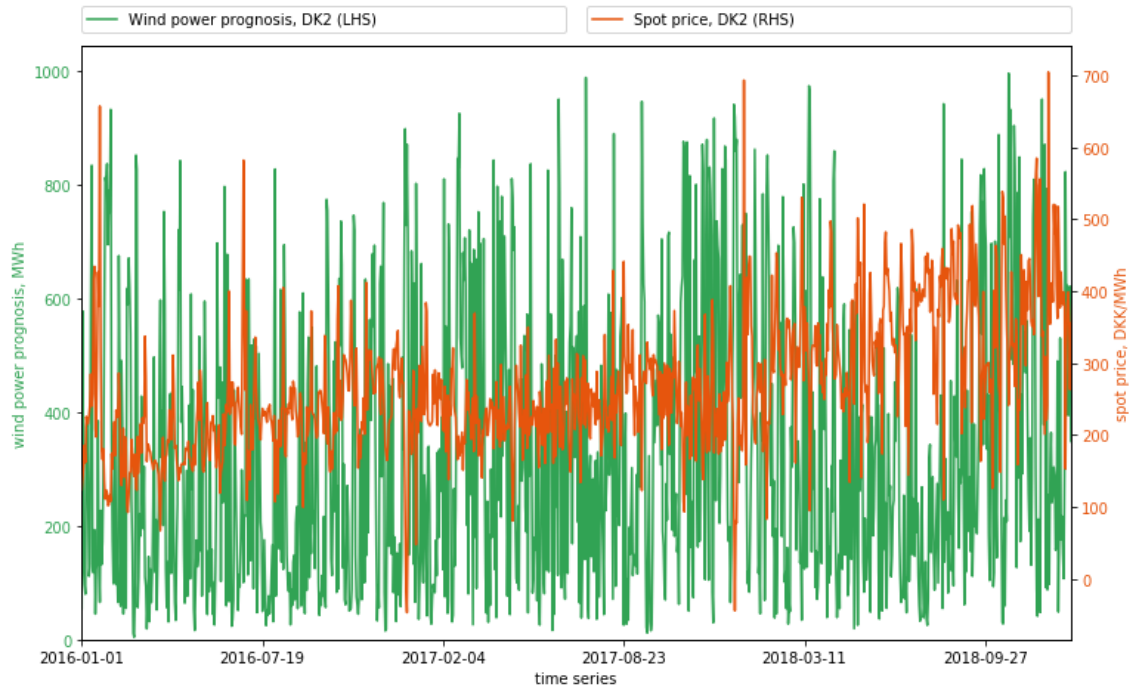


Figure B.4: Total consumption, wind power and spot price by hour (business days)

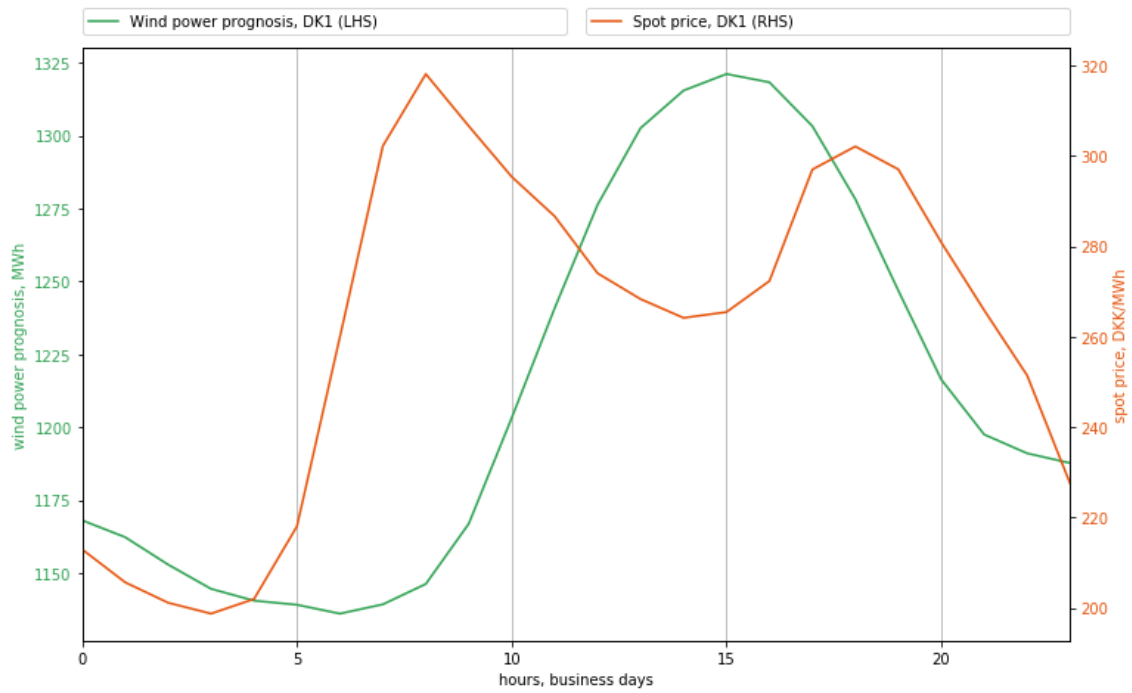
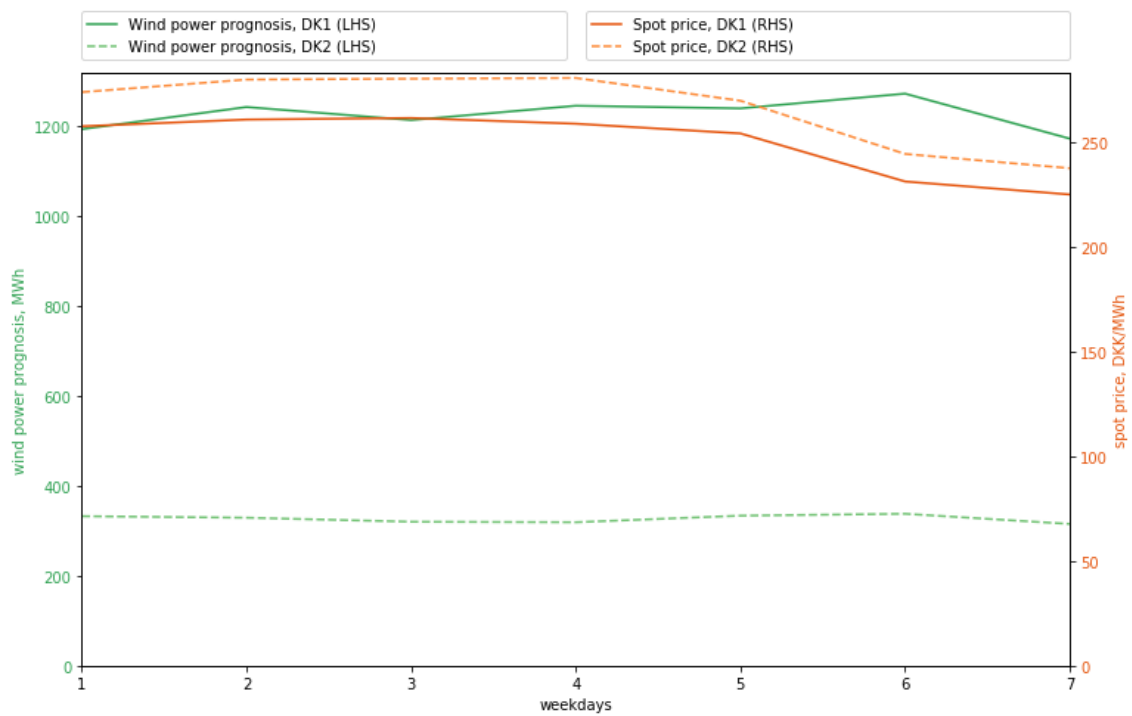
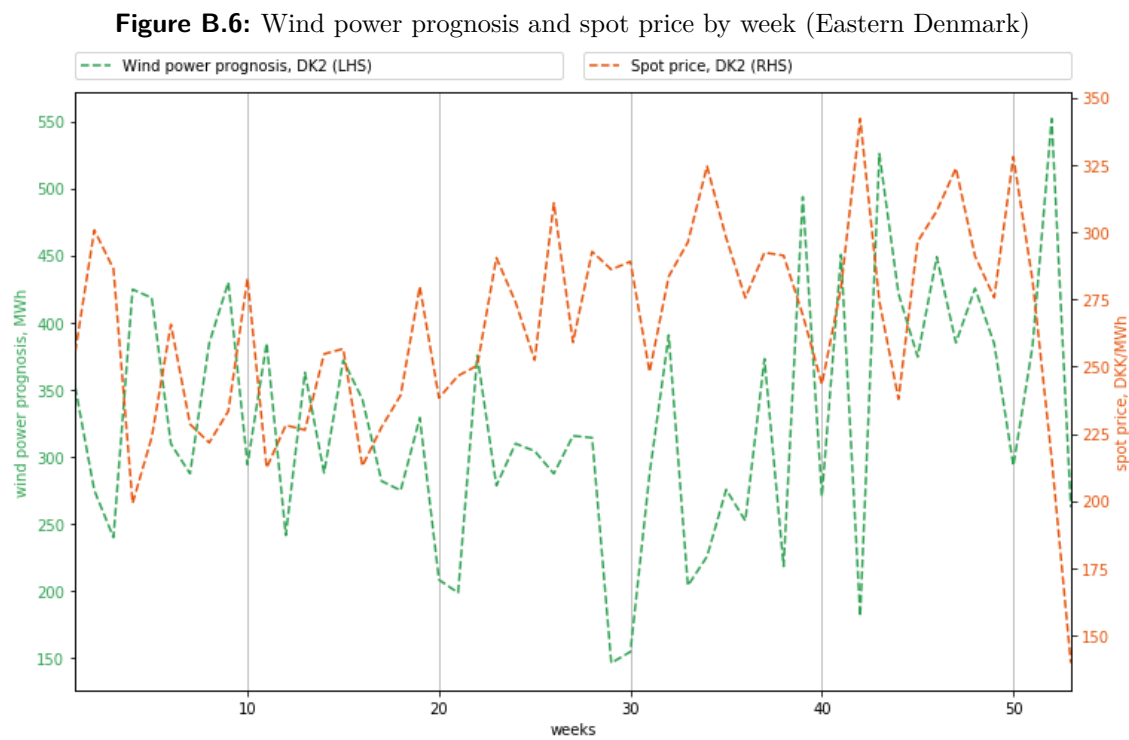


Figure B.5: Wind power prognosis and spot price by weekday



B. Data for wind power prognosis and spot price



C. TESTING FOR ENDOGENEITY

D. TESTING FOR OVERIDENTIFYING RESTRICTIONS