Introduction to Machine Learning (67577)

Exercise III – Classification

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**Theoretical Questions**

**Bayes Optimal and LDA**

1. Show that :

We know from bayes theorem that , therefore it is sufficient to show that .

Suppose in the first case that . If so, thus the corresponding would be (as ). For the other case, , which in turn means , so would be . We can write those in compart form as followed

1. Show that where :

From Q.1 we have , and we know that for calculating , taking will provide the same result. If so, let us concentrate on the following:

Substituting we have

Since the first is not a function of , it will not affect the result of . Let us simplify the second component

Since is the same for both , :

Yet again, is not a function of , therefore is not relevant for the calculation of . In conclusion we have

And consequently

1. Write your formula for estimating , and based on :

We can calculate the mean by summing the ratio of occurrences:

The probability would be the sum of occurrences divided by the total size

Similar to what we have seen in lecture 1, we can write

And

**Type I errors**

1. Let us write the possible cases, given that indicates spam and is non-spam:
2. If the current mail is non-spam (:
3. (true negative): I have correctly identified the mail as non spam
4. (false positive): I have declared the mail is spam (which is wrong)
5. If the current mail is spam (:
6. (true positive): I have correctly identified the mail as spam
7. (false negative): I have declared the mail is non-spam (which is wrong)

1.b is denoted a Type-I error – we would wish to avoid declaring regular mail as spam

2.b is not as bad, though still an error.

**SVM – Formulation**

1. Write the Hard-SVM problem as a QP problem:

We can set , so the QP takes the form of

Since , , so for we have the QP set. (as )

Simplifying the conditions:

Or in matrix form

Therefore, in matrix form for every :

This finishes the transition to QP

()

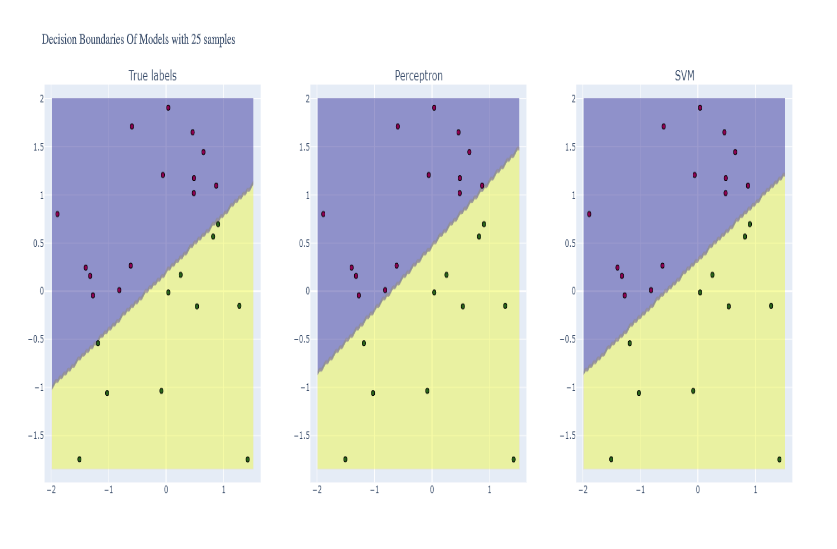
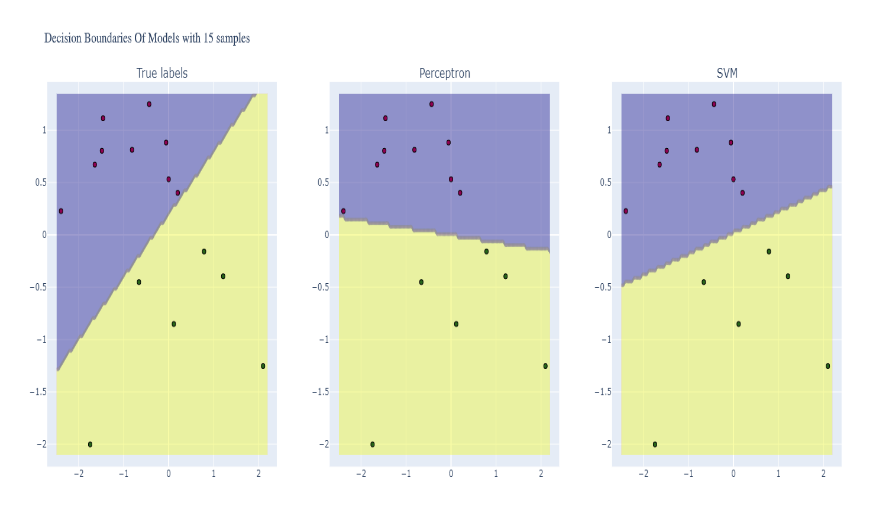
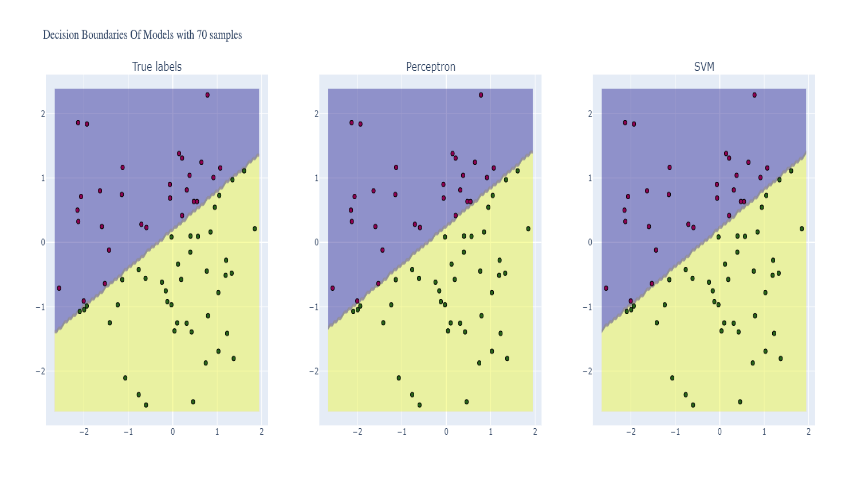
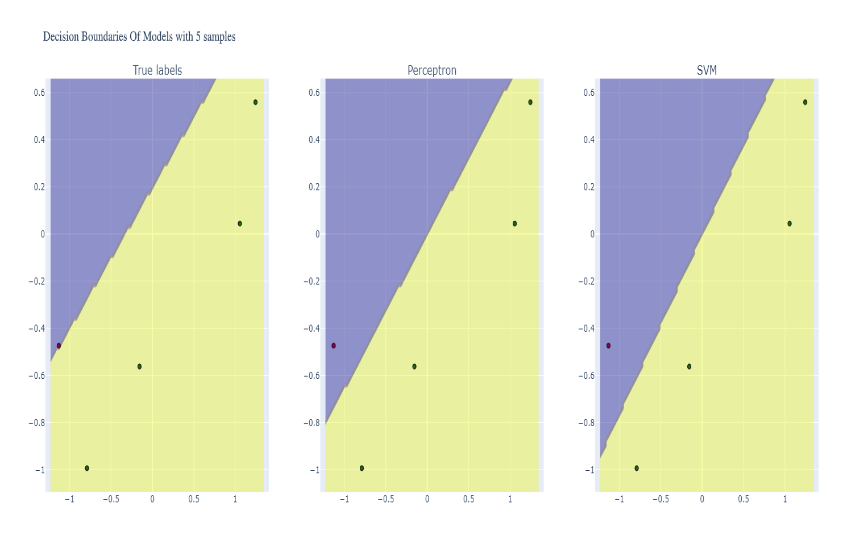
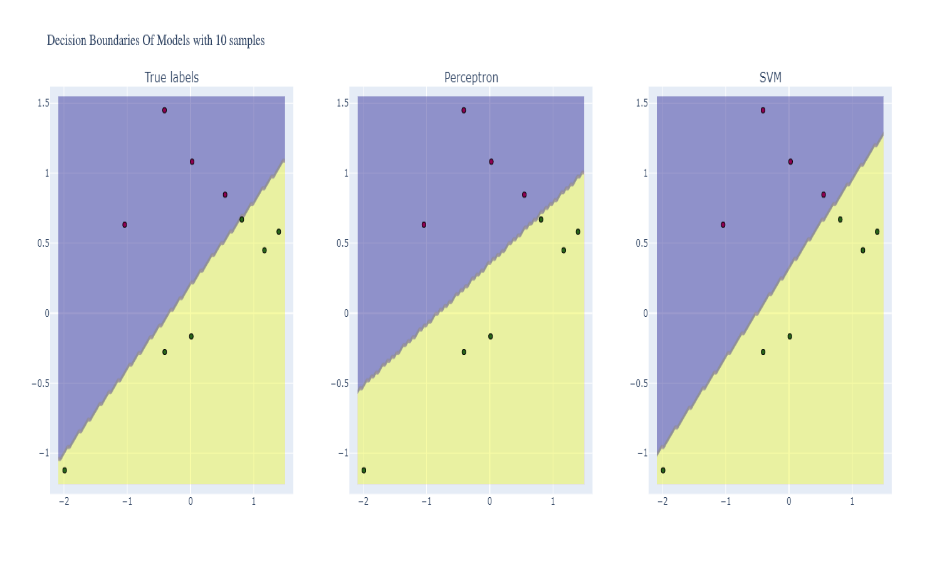
1. Showing problem equivalence

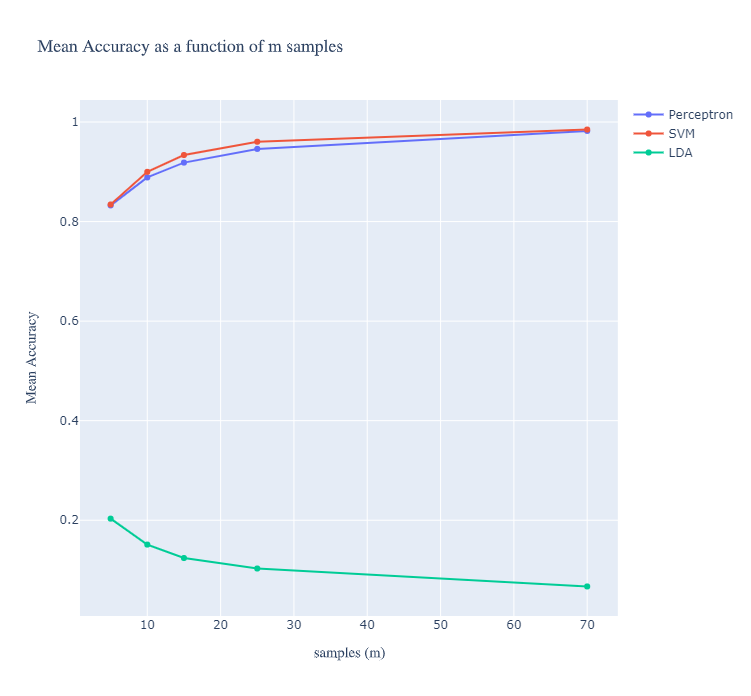
Minimizing separately

Explicitly writing the condition for

**Practical Questions**

**Implemention and simulation-comparison of different classifiers**

1. Code
2. Code
3.  decision boundaries of models with samples of True Labels, Perceptron and SVM
4. Mean accuracy as a function of for SVM, Perceptron and LDA



1. It appears that classification using LDA returns lower accuracy rates. This might be due to the fact that LDA classification does not necessarily represent a plane, and this may cause overfitting. On the other hand, both Perceptron and SVM classification returned similar accuracies, and classified the data with high rates.

**Classification of two digits from the MNIST Dataset**