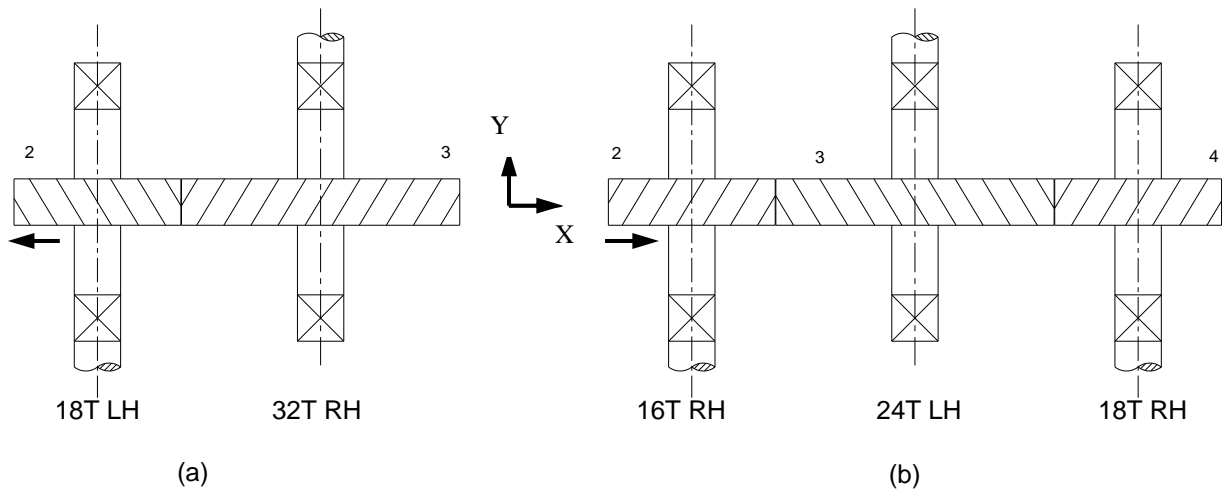


1- The gears in the two trains shown below have a normal module of 6 mm, a normal pressure angle of 20° and a 30° helix angle. For both gear trains the transmitted load is 3500 N.

a) Find the forces acting on each gear in part a if the pinion is rotating in the clockwise direction about the y-axis.

b) For part b find the forces acting on gear 3. The pinion rotates ccw and gear 3 is an idler gear.



a) Forces acting on the pinion:

$$W_{32}^t = 3500 \text{ N (-ve Z)}$$

$$\tan \Phi_t = \tan \Phi_n / \cos \psi = 0.42$$

$$W_{32}^r = W_{32}^t \tan \Phi_t = 3500 * 0.42 = 1470.9 \text{ N (-ve X)}$$

$$W_{32}^a = W_{32}^t \tan \psi = 3500 * \tan 30 = 2020.7 \text{ N (+ve Y)}$$

Forces acting on the gear:

$$W_{23}^t = W_{32}^t = 3500 \text{ N (+ve Z)} \rightarrow \text{(same magnitude, opposite direction)}$$

$$W_{23}^r = 1470.9 \text{ N (+ve X)}$$

$$W_{23}^a = 2020.7 \text{ N (-ve Y)}$$

b) Forces acting on (3) from (2):

$$W_{23}^t = W_{32}^t = 3500 \text{ N (-ve Z)}$$

$$W_{23}^r = 1470.9 \text{ N (+ve X)}$$

$$W_{23}^a = 2020.7 \text{ N (-ve Y)}$$

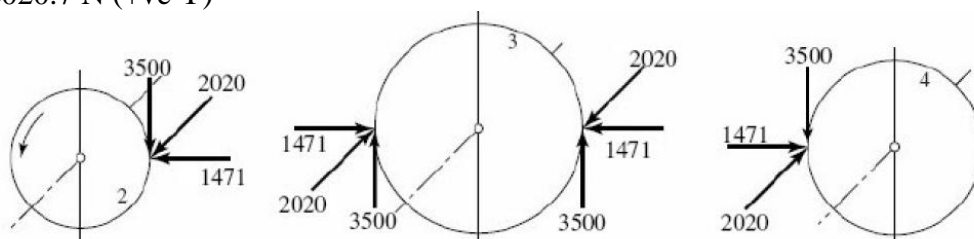
Forces acting on (3) from (4):

$$W_{43}^t r_3 = W_{23}^t r_3 \text{ (equilibrium of torques about Y axis)}$$

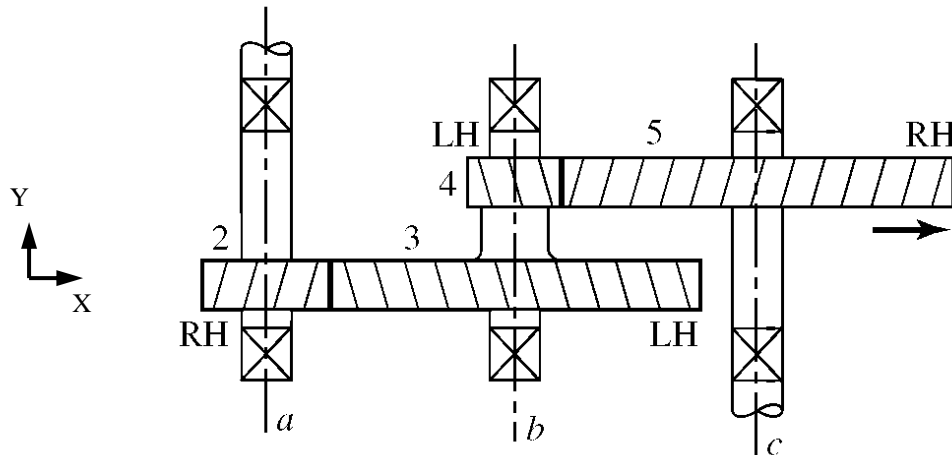
$$W_{43}^t = 3500 \text{ N (-ve Z)}$$

$$W_{43}^r = 1470.9 \text{ N (-ve X)}$$

$$W_{43}^a = 2020.7 \text{ N (+ve Y)}$$



2- A gear train is composed of four helical gears with the three axes in a single plane, as shown in the figure. The gears have a normal pressure angle of 20° and 30° helix angle. Shaft b is an idler and the transmitted load acting on gear 3 is 2250 N. The gears on shaft b have 14 and 54 teeth with a normal module of 3 mm. Find the forces and moments exerted by gears 3 and 4 on shaft b.



Gear 3

$$m = m_t = m_n / \cos \psi = 3.46 \text{ mm}$$

$$d_3 = m_t N_3 = 3.46 \times 54 = 187 \text{ mm}$$

$$W_{23}^t = 2250 \text{ N} \quad (-ve Z)$$

$$W_{23}^a = 2250 \tan 30^\circ = 1299 \text{ N} \quad (-ve Y)$$

$$W_{23}^r = 2250 \tan 22.8^\circ = 945.8 \text{ N} \quad (+ve X)$$

All forces are translated to the shaft with same magnitudes to the center of the gear accompanied with torque T_3 and bending moment M_{z3}

$$T_3 = 2250 \times 0.187/2 = 210.4 \text{ N.m (cw about +Y)}$$

$$M_{z3} = 1299 \times 0.187/2 = 121.46 \text{ N.m (ccw about +Z)}$$

Gear 4

$$d_4 = m_t N_4 = 3.46 \times 14 = 48.44 \text{ mm}$$

$$T_4 = T_3$$

$$W_{43}^t = 8.7 \text{ kN} \quad (-ve Z)$$

$$W_{43}^a = 8.7 \tan 30^\circ = 5 \text{ kN} \quad (+ve Y)$$

$$W_{43}^r = 8.7 \tan 22.8^\circ = 3.66 \text{ kN} \quad (-ve X)$$

All forces are translated to the shaft with same magnitudes to the center of the gear accompanied with torque T_4 and bending moment M_{z4}

$$T_4 = 210.4 \text{ N.m (ccw about +Y)}$$

$$M_{z4} = 5000 \times 0.04844/2 = 121 \text{ N.m (ccw about +Z)}$$

