

Tut 8 Design

Worm gears

$$\bullet P_x(\text{worm}) = P_t(\text{gear})$$

$$\bullet \lambda_{\text{worm}} = \omega_{\text{gear}}$$

$$\bullet d_G = \frac{N_G P_t}{\pi}$$

$$\bullet L = P_x N_w$$

$$\bullet \tan \lambda = \frac{L}{\pi d_w}$$

$$\bullet v_s = \frac{v_w}{\cos \lambda}$$

$$\bullet v_w = \omega_w r_w$$

$$\bullet v_g = \omega_w \frac{N_w}{N_g} \cdot r_g$$

$$\bullet W_{wt} = -W_{ga} = W_x = W \cos(\phi_n \sin \lambda + \mu \cos \lambda)$$

$$W_{wr} = -W_{gr} = W_y = W \sin \phi_n$$

$$W_{wa} = -W_{gt} = W_z = W (\cos \phi_n \cos \lambda - \mu \sin \lambda)$$

$$\bullet \text{Efficiency} = \eta = \frac{\cos \phi_n - \mu \tan \lambda}{\cos \phi_n + \mu \cot \lambda} \quad (\text{Not given})$$

$$\bullet \eta = \frac{H_o}{H}$$

$$\bullet H = H_o + H_L$$

$$\bullet H_o = W_{tg} \cdot v_{tg} \quad \left. \begin{array}{l} * H_o = W_{tg} \cdot v_{tg} \\ * H_L = \mu W \cdot v_s \end{array} \right\} \text{Not given}$$

$$\bullet H_L = \mu W \cdot v_s$$

$$\bullet W_{tg} = \beta (K_s d_g^{0.8} F_e K_m K_v)$$

$$\bullet \beta = 0.0131$$

$$\bullet K_s - K_m - K_v \rightarrow \text{tables}$$

$$\bullet d_g \rightarrow \text{gear diam}$$

$$\bullet F_e \rightarrow \text{smaller of } \frac{2}{3} d_w \text{ or } F_g$$

Direction of Forces: • get type of worm (right/left)

• use (right/left) hand rule on worm to get W_{wa}

Tut 9 Design

Bearings:

Let $F_{eq} = F_r$

$$\bullet \text{ get } C_R = k_A F_{eq} \left[\frac{L_D n_D}{L_R n_R 6.84} \right]^{1/a} \left[\frac{1}{\left(\ln \frac{1}{R} \right)^{1/1.17a}} \right] \quad (\text{only this equation given})$$

* $L_D \rightarrow$ life in hours

$L_R = 500 \text{ h}$

* $n_D \rightarrow$ rpm

$n_R = \frac{100}{3} \text{ rpm}$

* $R \rightarrow$ reliability

* $a \rightarrow$ 3 ball bearing or $\frac{10}{3}$ roller bearing

* $k_A = 1.2$

• From table choose bearing with $C > C_R$ calculated

• Calculate e from table using $\frac{F_a}{C_0}$

$$\bullet \frac{F_a}{F_r} \begin{cases} \leq e & F_{eq} = F_r \\ > e & F_{eq} = X F_r + Y F_a \end{cases} \quad (X \text{ and } Y \text{ from table using } e)$$

Tut 10

• check tut 10 for tables (tables given)

Taper

• get case, calculate $F_{Ar}, F_{Br}, F_{Ar}, F_{Br}$ (let $\gamma = 1.5$)

$$\bullet \text{ Make same check } \frac{F_a}{F_r} \begin{cases} \leq e & F_{eq} = F_r \\ > e & F_{eq} = 0.4 F_r + Y F_a \end{cases}$$

• then get C_R using same equation

Tut 11 Design

Journal bearing

$$* S = \left(\frac{r}{c}\right)^2 \frac{\mu N}{P}$$

- $r = d/2$
- c : clearance
- $\mu \rightarrow$ graph

\Rightarrow • N : rev/s Not rpm

$$* P = \frac{W}{l \cdot d} \rightarrow \text{radial force}$$

$l \cdot d \rightarrow$ area

\uparrow Not given

$$* T_{var} = \frac{\tau_{CH} \Delta T}{P}$$

• τ and C_H given

• $T_{var} \rightarrow$ graph

$$* T_{av} = T_i + \frac{\Delta T}{2}$$

$$* \text{Power loss} = H = (T)(\omega)$$

$$= \left(\frac{f}{2} W r\right) (2\pi N)$$

Not given

get f from $\rightarrow \left(\frac{r}{c}\right) f \rightarrow$ graph

Tut 12 Clutches

Uniform wear

$$F = \frac{\pi P_a d (D-d)}{2}$$

$$T = \frac{f}{4} F (D+d) * m$$

Uniform pressure

$$F = \frac{\pi P_a (D^2 - d^2)}{4}$$

$$T = \frac{\pi}{12} f P_a (D^3 - d^3) * m$$

All given $\left\{ \begin{array}{l} \text{Force} \\ \text{Torque} \end{array} \right.$

$\rightarrow m$: number of friction surfaces

P_a : maximum pressure (greater in uniform wear)

T : Torque (greater in uniform pressure)

Tut 13 Design

Disk brakes

Uniform wear

Uniform pressure

Force

$$F = (\theta_2 - \theta_1) p_{\max} r_i (r_o - r_i)$$

$$F = \frac{1}{2} (\theta_2 - \theta_1) p (r_o^2 - r_i^2)$$

Torque

$$T = \frac{1}{2} (\theta_2 - \theta_1) \int p_{\max} r_i (r_o^2 - r_i^2)$$

$$T = \frac{1}{3} (\theta_2 - \theta_1) \int p (r_o^3 - r_i^3)$$

NB: θ in rad

• equiv. radius: $r_e = \frac{r_i + r_o}{2}$

• Force location: $r_f = \frac{\cos \theta_1 - \cos \theta_2}{\theta_2 - \theta_1} \frac{r_i + r_o}{2}$ } Not given

Band brake

Torque: $T = (P_1 - P_2) r$

$$\frac{P_1}{P_2} = e^{\int \theta}$$

• θ : angle of contact in rad

• $P_1 > P_2$

Tut 14 Drum Brake

Moment due Friction: $M_f = \frac{\int p a b r}{\sin \theta_a} \left[r (1 - \cos \theta_2) - \frac{a}{2} \sin^2 \theta_2 \right]$

Moment due Normal Force: $M_N = \frac{p a b r a}{\sin \theta_a} \left[\frac{\theta_2}{2} - \frac{1}{4} \sin 2\theta_2 \right]$

Torque: $T = \frac{\int p a b r^2 (\cos \theta_1 - \cos \theta_2)}{\sin \theta_{\max}}$

$F = \begin{cases} \frac{M_N - M_F}{c} & \text{self locking} \\ \frac{M_N + M_F}{c} & \text{Normal case} \end{cases}$ } Not given

Tut 15 Design

Belt drive

$$\bullet \frac{P_1}{P_2} = e^{f\theta} \quad (\text{neglecting centrifugal force})$$

$$\bullet \frac{P_1 - mv^2}{P_2 - mv^2} = e^{f\theta}$$

$$\bullet \alpha_{\max} = \frac{\text{Force}}{\text{Area}} = \frac{P_1}{wt}$$

$$m = wt + \rho \quad (\text{mass per unit length})$$

For initial tightening

$$P_i = \frac{P_1 + P_2}{2}$$