

# Algorithm

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## The Steps for analyzing Algorithm:

- time
- space
- network transformation
- power consumption
- cpu registers

## Recursion :

Recursion is the process of defining a problem (or the solution to a problem) in terms of (a simpler version) itself.

### Law of Recursive:

- A recursive algorithm must have a base case (when to stop)
- A recursive algorithm must move toward the base case
- A recursive algorithm must call itself recursively

### Code:

#### Example 1:

```
def count_down(n):  
    print(n,end=' ')  
    if n>0:  
        count_down(n-1)
```

#### Example 2:

```
def sum_list(list):  
    if len(list)==0:  
        return 0  
    return list[0]+sum_list(list[1:])
```

#### Example 3:

Convert decimal to different base

```
def tostr(n,base):  
    digits='0123456789ABCDEF'  
    if n<base:
```

```

    return digits[n]
return tostr(n // base,base) + digits[n % base]

```

**Example 4:****Check Palindrome**

- Recursive:

```

def pallidnrome_recursive(num):
    s=str(num)
    if len(s) < 1:
        return True
    else:
        if s[0] == s[-1]:
            return pallidnrome_recursive(s[1:-1])
        else:
            return False

```

- Second Way:

```

def reverseDigits(num) :

    rev_num = 0;
    while (num > 0) :
        rev_num = rev_num * 10 + num % 10
        num = num // 10

    return rev_num

# Function to check if n is Palindrome
def isPalindrome(n) :

    # get the reverse of n
    rev_n = reverseDigits(n);

    # Check if rev_n and n are same or not.
    if (rev_n == n) :
        return 1
    else :
        return 0

```

**Example 5:****Fibonacci sequence:**

- Recursive:

```

def fib_recursive(num):
    if num <=1:
        return num
    return fib(num-1)+fib(num-2)

```

- Loop:

```

def fib_loop(num):
    n1,n2=0,1
    count=0
    if num==0:
        return 0
    elif num==1:

```

```

    return 1
else:
    while count < num:
        nth=n1+n2
        n1=n2 # swap
        n2=nth # swap
        count +=1
    return n1

```

Example 6(Check if the item in the node list):

```

def search(item,node):
    if node.item==item:
        return True
    elif node==None:
        return False
    else:
        return search(item,node.rest)

```

Stack(LIFO):

Common Data Structure Operations

Data Structure	Time Complexity								Space Complexity
	Average				Worst				Worst
	Access	Search	Insertion	Deletion	Access	Search	Insertion	Deletion	Worst
Array	$O(1)$	$O(n)$	$O(n)$	$O(n)$	$O(1)$	$O(n)$	$O(n)$	$O(n)$	$O(n)$
Stack	$O(n)$	$O(n)$	$O(1)$	$O(1)$	$O(n)$	$O(n)$	$O(1)$	$O(1)$	$O(n)$
Queue	$O(n)$	$O(n)$	$O(1)$	$O(1)$	$O(n)$	$O(n)$	$O(1)$	$O(1)$	$O(n)$
Singly-Linked List	$O(n)$	$O(n)$	$O(1)$	$O(1)$	$O(n)$	$O(n)$	$O(1)$	$O(1)$	$O(n)$
Doubly-Linked List	$O(n)$	$O(n)$	$O(1)$	$O(1)$	$O(n)$	$O(n)$	$O(1)$	$O(1)$	$O(n)$
Skip List	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(n)$	$O(n)$	$O(n)$	$O(n)$	$O(n \log(n))$
Hash Table	N/A	$O(1)$	$O(1)$	$O(1)$	N/A	$O(n)$	$O(n)$	$O(n)$	$O(n)$
Binary Search Tree	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(n)$	$O(n)$	$O(n)$	$O(n)$	$O(n)$
Cartesian Tree	N/A	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	N/A	$O(n)$	$O(n)$	$O(n)$	$O(n)$
B-Tree	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(n)$
Red-Black Tree	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(n)$
Splay Tree	N/A	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	N/A	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(n)$
AVL Tree	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(n)$
KD Tree	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(n)$	$O(n)$	$O(n)$	$O(n)$	$O(n)$

Figure 1: Common Data Structure Operation

Stack Array:

```

# Stack class implemented with array
class Stack:
    """Implements an efficient last-in first-out Abstract Data Type using a Python List"""

    # capacity is max number of Nodes, init_items is optional List parameter for initialization
    # if the length of the init_items List exceeds capacity, raise IndexError
    def __init__(self, capacity, init_items=None):
        """Creates an empty stack with a capacity"""
        self.capacity = capacity # capacity of stack
        self.items = [None]*capacity # array for stack
        self.num_items = 0 # number of items in stack

```

```

if init_items is not None:      # if init_items is not None, initialize stack
    if len(init_items) > capacity:
        raise IndexError
    else:
        self.num_items = len(init_items)
        self.items[:self.num_items] = init_items

def __eq__(self, other):
    return ((type(other) == Stack)
            and self.capacity == other.capacity
            and self.items[:self.num_items] == other.items[:other.num_items]
            )

def __repr__(self):
    return ("Stack({!r}, {!r})".format(self.capacity, self.items[:self.num_items]))

def is_empty(self):
    '''Returns True if the stack is empty, and False otherwise
    MUST have O(1) performance'''
    return self.num_items == 0

def is_full(self):
    '''Returns True if the stack is full, and False otherwise
    MUST have O(1) performance'''
    return self.num_items==self.capacity

def push(self, item):
    '''If stack is not full, pushes item on stack.
    If stack is full when push is attempted, raises IndexError
    MUST have O(1) performance'''
    if self.num_items==self.capacity:
        raise IndexError("The Stack is Full")
    self.items[self.num_items]=item
    self.num_items +=1
    # print(self.items.__repr__())
    # return self.items[self.num_items-1]

def pop(self):
    '''If stack is not empty, pops item from stack and returns item.
    If stack is empty when pop is attempted, raises IndexError
    MUST have O(1) performance'''
    if self.num_items==0:
        raise IndexError("Index out of range")
    self.num_items -=1
    # print(self.items[self.num_items].__repr__())
    return self.items[self.num_items]

def peek(self):
    '''If stack is not empty, returns next item to be popped (but does not remove the item)
    If stack is empty, raises IndexError
    MUST have O(1) performance'''

```

```

if self.num_items==0:
    raise IndexError
# print(self.items[self.num_items-1].__repr__())
return self.items[self.num_items-1]

def size(self):
    '''Returns the number of elements currently in the stack, not the capacity
    MUST have O(1) performance'''
    return self.num_items

```

## Stack Node List:

```

# NodeList is one of
# None or
# Node(value, rest), where rest is reference to the rest of the list
class Node:
    def __init__(self, value, rest):
        self.value = value      # object reference stored in Node
        self.rest = rest       # reference to NodeList
    def __eq__(self, other):
        return ((type(other) == Node)
            and self.value == other.value
            and self.rest == other.rest
        )
    def __repr__(self):
        return ("Node({!r}, {!r})".format(self.value, self.rest))

class Stack:
    """Implements an efficient last-in first-out Abstract Data Type using a node list"""

    # top is the top Node of stack
    def __init__(self, top=None):
        self.top = top          # top node of stack
        self.num_items = 0      # number of items in stack
        node = top              # set number of items based on input
        while node is not None:
            self.num_items += 1
            node = node.rest

    def __eq__(self, other):
        return ((type(other) == Stack)
            and self.top == other.top
        )

    def __repr__(self):
        return ("Stack({!r})".format(self.top))

    def is_empty(self):
        '''Returns True if the stack is empty, and False otherwise
        MUST have O(1) performance '''
        return self.num_items==0

    def push(self, item):
        '''Pushes item on stack.
        MUST have O(1) performance'''
        new_stack=Node(item,self.top)

```

```

self.rest=self.top
self.top=new_stack
self.num_items += 1

def pop(self):
    '''If stack is not empty, pops item from stack and returns item.
       If stack is empty when pop is attempted, raises IndexError
       MUST have O(1) performance'''
    if self.top is None:
        raise IndexError
    self.num_items -=1
    temp=self.top.value
    self.top.value=None
    self.top=self.top.rest
    return temp

def peek(self):
    '''If stack is not empty, returns next item to be popped (but does not remove the item)
       If stack is empty, raises IndexError
       MUST have O(1) performance'''
    if self.num_items==0:
        raise IndexError
    return self.top.value

def size(self):
    '''Returns the number of elements currently in the stack, not the capacity
       MUST have O(1) performance'''
    return self.num_items

```

## Queue(FIFO):

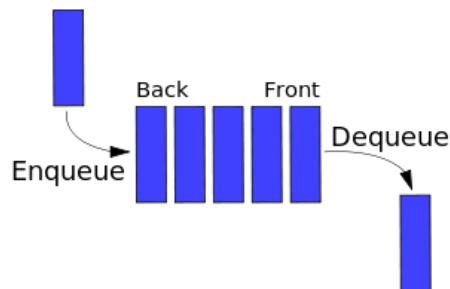


Figure 2: Queue

## Array:

# Queue ADT - circular array implementation

```

class Queue:
    """Implements an efficient first-in first-out Abstract Data Type using a Python List"""

    def __init__(self, capacity, init_items=None):
        """Creates a queue with a capacity and initializes with init_items"""
        self.capacity= capacity          # capacity of queue
        self.items = [None]*capacity     # array for queue
        self.num_items = 0                # number of items in queue

```

```

self.front = 0          # front index of queue (items removed from front)
self.rear = 0           # rear index of queue (items enter at rear)
if init_items is not None: # if init_items is not None, initialize queue
    if len(init_items) > capacity:
        raise IndexError
    else:
        self.num_items = len(init_items)
        self.items[:self.num_items] = init_items
        self.rear = self.num_items % self.capacity # % capacity addresses length=capacity

def __eq__(self, other):
    return ((type(other) == Queue)
            and self.capacity == other.capacity
            and self.get_items() == other.get_items()
            )

def __repr__(self):
    return ("Queue({!r}, {!r})".format(self.capacity, self.get_items()))

# get_items returns array (Python list) of items in Queue
# first item in the list will be front of queue, last item is rear of queue
def get_items(self):
    if self.num_items == 0:
        return []
    if self.front < self.rear:
        return self.items[self.front:self.rear]
    else:
        return self.items[self.front:] + self.items[:self.rear]

def is_empty(self):
    """Returns true if the queue is empty and false otherwise
    Must be O(1)"""
    return self.num_items==0

def is_full(self):
    """Returns true if the queue is full and false otherwise
    Must be O(1)"""
    return self.num_items==self.capacity

def enqueue(self, item):
    """enqueues item, raises IndexError if Queue is full
    Must be O(1)"""
    if self.is_full():
        raise IndexError
    self.items[self.rear]=item
    self.rear=(self.rear+1)%self.capacity # give the location which next time we need to be
    self.num_items += 1

def dequeue(self):
    """dequeues and returns item, raises IndexError if Queue is empty
    Must be O(1)"""
    if self.is_empty():
        raise IndexError
    value=self.items[self.front]
    self.front=(self.front+1)%self.capacity
    self.num_items -=1

```

```

    return value

def size(self):
    """Returns the number of items in the queue
    Must be  $O(1)$ """
    return self.num_items

```

## NodeList:

```

# NodeList version of ADT Queue

# Node class for use with Queue implemented with linked list
# NodeList is one of
# None or
# Node(value, rest), where rest is the rest of the list
class Node:
    def __init__(self, value, rest):
        self.value = value      # value
        self.rest = rest       # NodeList
    def __eq__(self, other):
        return ((type(other) == Node)
                and self.value == other.value
                and self.rest == other.rest
                )
    def __repr__(self):
        return ("Node({!r}, {!r})".format(self.value, self.rest))

class Queue:
    def __init__(self):
        self.rear = None      # rear NodeList
        self.front = None     # front NodeList
        self.num_items = 0    # number of items in Queue

    def __eq__(self, other):
        return ((type(other) == Queue)
                and self.get_items() == other.get_items()
                )

    def __repr__(self):
        return ("Queue({!r}, {!r})".format(self.rear, self.front))

# get_items returns array (Python list) of items in Queue
# first item in the list will be front of queue, last item is rear of queue
def get_items(self):
    items = []
    front = self.front
    while front is not None:
        items.append(front.value)
        front = front.rest
    if self.rear is not None:
        rear_items = []
        rear = self.rear
        while rear is not None:
            rear_items.append(rear.value)
            rear = rear.rest

```



```

        rear_items.reverse()
        items.extend(rear_items)
    return items

def is_empty(self):
    """Returns true if the queue is empty and false otherwise
    Must be  $O(1)$ """
    return self.num_items==0

def enqueue(self, item):
    """enqueues item, adding it to the rear NodeList
    Must be  $O(1)$ """

    que=Node(item,self.rear)

    self.rear=que

    self.num_items+=1

def dequeue(self):
    """dequeues item, removing first item from front NodeList
    If front NodeList is empty, remove items from rear NodeList
    and add to front NodeList until rear NodeList is empty
    If front NodeList and rear NodeList are both empty, raise IndexError
    Must be  $O(1)$  - general case"""
    if self.is_empty():
        raise IndexError
    self.num_items -= 1
    if self.front is not None:
        temp=self.front.value
        self.front=self.front.rest
        return temp
    if self.front is None:
        i=self.rear
        while i is not None:
            temp=i.value
            i=i.rest
            self.front=Node(temp,self.front)
            self.rear=self.rear.rest
        temp = self.front.value
        self.front = self.front.rest
        return temp

def size(self):
    """Returns the number of items in the queue
    Must be  $O(1)$ """
    return self.num_items

```

## Doubly Link List:

```

class Node:
    """Node for use with doubly-linked list"""
    def __init__(self, item, next=None, prev=None):

```

```
self.item = item # item held by Node
self.next = next # reference to next Node
self.prev = prev # reference to previous Node

class OrderedList:
    """A doubly-linked ordered list of integers,
    from lowest (head of list, sentinel.next) to highest (tail of list, sentinel.prev)"""
    def __init__(self, sentinel=None):
        """Use only a sentinel Node. No other instance variables"""
        self.sentinel = Node(None)
        self.sentinel.next = self.sentinel
        self.sentinel.prev = self.sentinel

    def is_empty(self):
        """Returns back True if OrderedList is empty"""
        return self.sentinel.next==self.sentinel

    def add(self, item):
        """Adds an item to OrderedList, in the proper location based on ordering of items
        from lowest (at head of list) to highest (at tail of list)
        If item is already in list, do not add again (no duplicate items)"""
        cur=self.sentinel.next
        while cur is not self.sentinel and item >cur.item:
            cur=cur.next
        if cur.item != item:
            temp=Node(item)
            temp.prev=cur.prev
            temp.next=cur
            cur.prev.next=temp
            cur.prev=temp

    def remove(self, item):
        """Removes an item from OrderedList. If item is removed (was in the list) returns True
        If item was not removed (was not in the list) returns False"""
        cur=self.sentinel
        if self.is_empty():
            return False
        else:
            while cur.next != self.sentinel:
                if cur.next.item == item:
                    cur.next=cur.next.next
                    cur.next.prev=cur
                    return True
                else:
                    cur=cur.next
            return False

    def index(self, item):
        """Returns index of an item in OrderedList (assuming head of list is index 0).
        If item is not in list, return None"""
        if self.is_empty():
            raise IndexError
```

```

    cur=self.sentinel.next
    num_item =0
    while cur.item != item:
        cur=cur.next
        num_item +=1
    return num_item

def pop(self, index):
    """Removes and returns item at index (assuming head of list is index 0).
    If index is negative or >= size of list, raises IndexError"""
    cur = self.sentinel.next
    num_itemes = 0
    if self.is_empty():
        raise IndexError
    if index < 0:
        raise IndexError

    while cur != self.sentinel and num_itemes < index:
        cur = cur.next
        num_itemes += 1
    if cur == self.sentinel:
        raise IndexError
    else:
        ret_val = cur.item
        cur.next.prev = cur.prev
        cur.prev.next = cur.next
        return ret_val

def search(self, item):
    """Searches OrderedList for item, returns True if item is in list, False otherwise recursion"""
    def helper(cur, values):
        if cur == self.sentinel:
            return False
        if cur.item > values:
            return False
        elif cur.item == values:
            return True
        else:
            return helper(cur.next, values)
    cur=self.sentinel.next
    return helper(cur, item)

def python_list(self):
    """Return a Python list representation of OrderedList, from head to tail
    For example, list with integers 1, 2, and 3 would return [1, 2, 3]"""
    list=[]
    cur=self.sentinel.next
    while cur is not self.sentinel:
        list.append(cur.item)
        cur=cur.next
    return list

def python_list_reversed(self):
    """Return a Python list representation of OrderedList, from tail to head, using recursion

```

*For example, list with integers 1, 2, and 3 would return [3, 2, 1] recursion"""*

```
def helper(cur):
    if cur.next == self.sentinel:
        return [cur.item]
    else:
        return helper(cur.next)+[cur.item]
cur=self.sentinel.next
return helper(cur)
```

```
def size(self):
    """Returns number of items in the OrderedList. O(n) is OK recursion"""
    def helper(cur):
        if cur == self.sentinel:
            return 0
        return helper(cur.next)+1
    cur=self.sentinel
    return helper(cur.next)
```

## Binary Tree:

	Insert	search	min	max	Transversals	height
Big O	log(n)	log(n)	log(n)	log(n)	O(n)	O(n)

## Three type of trees:

- Full: leaf with no children or with to leaves
- Complete: fill up top to bottom and left to right
- Perfect: all leaves and nodes are at the same level

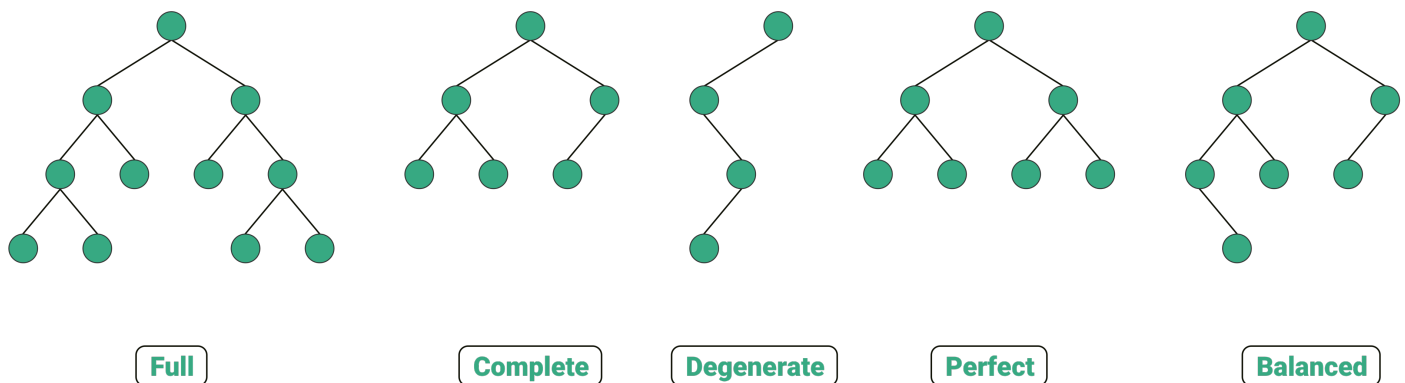


Figure 3: Trees

**Traversal:**

- Pre Order : n l r
- In Order : l n r
- Post Order: l r n

**In OrderList:**

```
def inorder_list(self):
    # return Python list of BST keys representing in-order traversal of BST (LVR-->left visit right)
    def _inorder(current, list):
        if current != None:
            _inorder(current.left, list)
            list.append(current.key)
            _inorder(current.right, list)

        return list

    return _inorder(self.root, [])
```

**PreOrder:**

```
def preorder_list(self):
    # return Python list of BST keys representing pre-order traversal of BST (VLR-> Visit Left Right)
    def _preorder(current, list):
        if current != None:
            list.append(current.key)
            _preorder(current.left, list)
            _preorder(current.right, list)
        return list

    return _preorder(self.root, [])
```

**Level order list:**

```
def level_order_list(self):
    # return Python list of BST keys representing level-order traversal of BST
    # You MUST use your queue_array data structure from lab 3 to implement this method
    q = Queue(25000) # Don't change this!
    list1 = []
    if self.root == None:
        return None

    q.enqueue(self.root) # adding whole root q Stack

    while q.is_empty() == False:
        root = q.dequeue()
        list1.append(root.key)
        if root.left != None:
            q.enqueue(root.left)
        if root.right != None:
            q.enqueue(root.right)

    return list1
```

## Calculate the Hight:

```
def height(self,node):
    if node==None:
        return 0
    left=self.height(node.left)
    right=self.height(node.right)
    return 1 + max(left,right)
```

## Insertion:

```
def insert(self, key, data=None): # inserts new node w/ key and data
    # If an item with the given key is already in the BST,
    # the data in the tree will be replaced with the new data
    # Example creation of node: temp = TreeNode(key, data)
    def _insert(key,cur_node,data):
        if key < cur_node.key:
            if cur_node.left == None:
                cur_node.left=TreeNode(key,data)
            else:
                _insert(key,cur_node.left,data)
        elif key> cur_node.key:
            if cur_node.right==None:
                cur_node.right=TreeNode(key,data)
            else:
                _insert(key,cur_node.right,data)
        else:
            cur_node.data=data # update the data
            return cur_node

    if self.root==None:
        self.root=TreeNode(key,data)
    else:
        self.root=_insert(key,self.root,data)
```

## Search:

```
def search(self, key):
    # returns True if key is in a node of the tree, else False
    def _search(key,current_node):
        if key==current_node.key:
            return True
        elif key < current_node.key and current_node.left !=None:
            return _search(key, current_node.left)
        elif key>current_node.key and current_node.right !=None:
            return _search(key, current_node.right)
        return False
    if self.root != None:
        return _search(key,self.root)
    else:
        return False
```

## Min:

```
def find_min(self):
    # returns a tuple with min key and data in the BST
```

```
# returns None if the tree is empty
if self.is_empty():
    return None
def _min(current):
    if current is None:
        return None
    if current.left is None:
        return current.key, current.data
    return _min(current.left)

return _min(self.root)
```

## Max:

```
def find_max(self): # returns a tuple with max key and data in the BST
    # returns None if the tree is empty
    if self.is_empty():
        return None
    def _max(current):
        if current is None:
            return None
        if current.right is None:
            return current.key, current.data
        return _max(current.right)

    return _max(self.root)
```

## Sorting:

Name	Time Complexity (Best)	Time Complexity (Average)	Time Complexity (Worst)	Space Complexity	Stability
Bubble Sort	$\Omega(n)$	$\Theta(n^2)$	$O(n^2)$	$O(1)$	Stable
Selection Sort	$\Omega(n^2)$	$\Theta(n^2)$	$O(n^2)$	$O(1)$	Unstable
Insertion Sort	$\Omega(n)$	$\Theta(n^2)$	$O(n^2)$	$O(1)$	Stable
Merge Sort	$\Omega(n \log(n))$	$\Theta(n \log(n))$	$O(n \log(n))$	$O(n)$	Stable
Quick Sort	$\Omega(n \log(n))$	$\Theta(n \log(n))$	$O(n^2)$	$O(\log(n))$	Unstable
Heap Sort	$\Omega(n \log(n))$	$\Theta(n \log(n))$	$O(n \log(n))$	$O(1)$	Unstable
Counting Sort	$\Omega(n+k)$	$\Theta(n+k)$	$O(n+k)$	$O(k)$	Stable
Radix Sort	$\Omega(nk)$	$\Theta(nk)$	$O(nk)$	$O(n+k)$	Stable

Figure 4: Sorting Table:

[Summery with animation](#)

### Bubble Sort:

```
def bubble_sort(A):
    for k in range(len(A)):
        flag=0 # check if one time run but we did not swap anything for code efficiency
        for i in range(len(A)-k-1):
            if A[i]>A[i+1]:
                A[i],A[i+1]=A[i+1],A[i]
                flag=1
        if flag==0:
            break
```



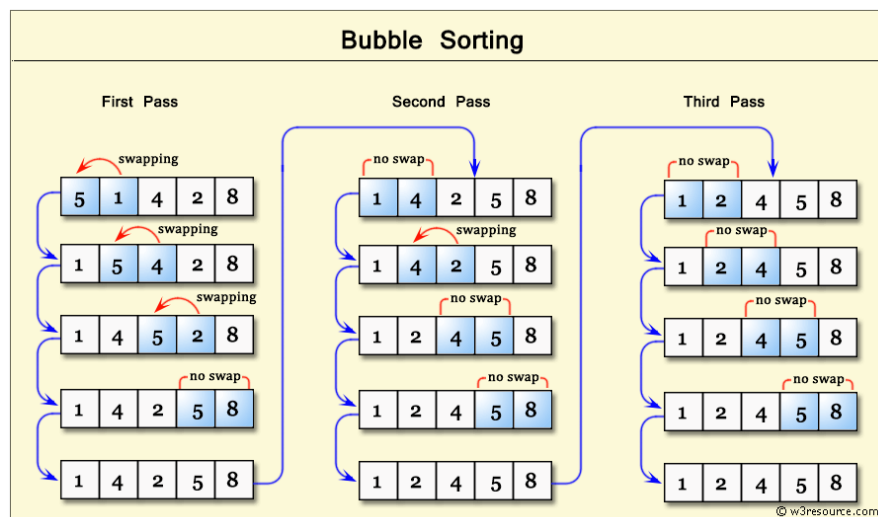


Figure 5: Bubble Sort

## Insertion Sort:

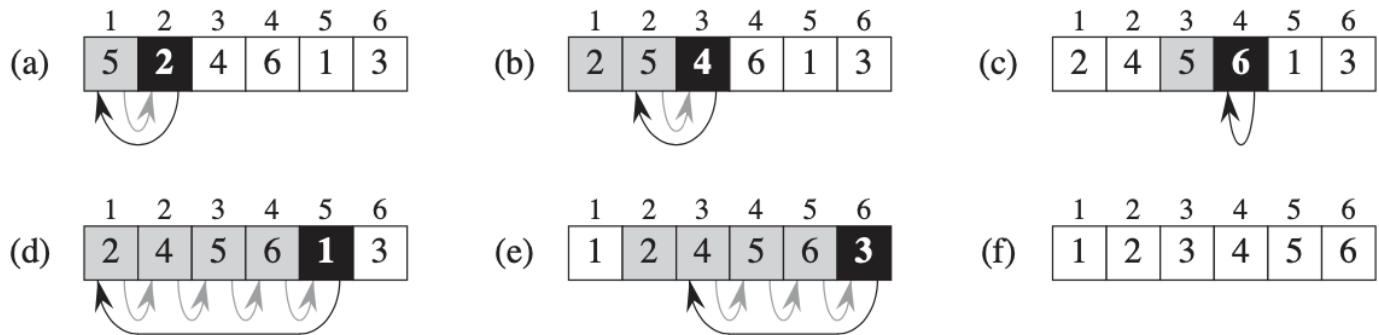


Figure 6: Insertion Sort

## Code:

```
def insertion_sort(alist):
    com = 0 # How many comparison the code do
    for i in range (1, len (alist)):
        value = alist[i]
        j = i - 1
        while j >= 0:
            com += 1
            if value < alist[j]:
                alist[j + 1] = alist[j]
                alist[j] = value
                j = j - 1
            else:
                break
    return com
```

The  $\theta(n)$  steps. Each steps have  $\theta(n)$  swaps.

## Selection Sort:

- Find the minimum value in the list
- Swap it with the value in the first position
- Repeat the steps above for the remainder of the list (starting at the second position and advancing each time)

## Code:

```
def selection_sort(A):
    # Traverse through all array elements
    for i in range(len(A)):

        # Find the minimum element in remaining
        # unsorted array
        min_idx = i
        for j in range(i+1, len(A)):
            if A[min_idx] > A[j]:
                min_idx = j

        # Swap the found minimum element with
        # the first element
```

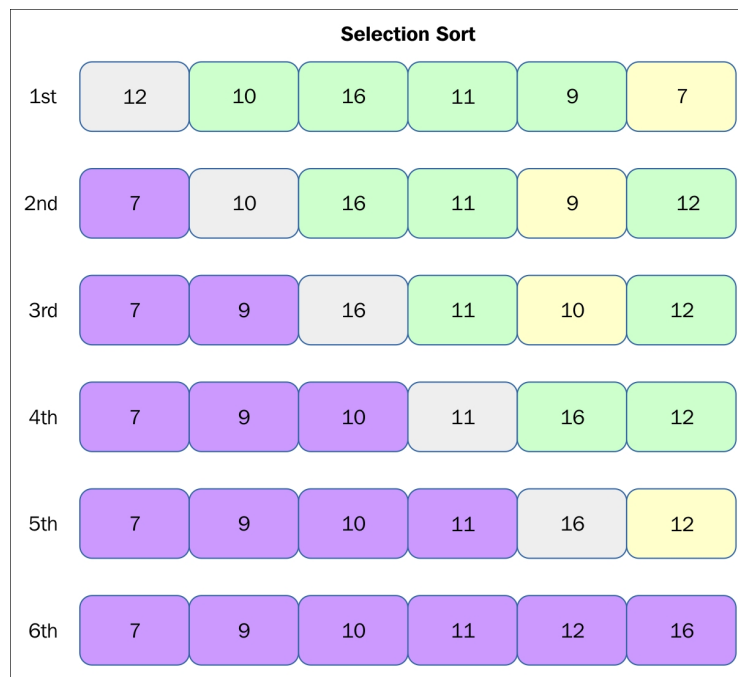


Figure 7: Selection Sort:

```

A[i], A[min_idx] = A[min_idx], A[i]
return A

```

## Merge Sort:

### Code:

```

def mergeSort(myList):
    if len(myList) > 1:
        mid = len(myList) // 2
        left = myList[:mid]
        right = myList[mid:]

        # Recursive call on each half
        mergeSort(left)
        mergeSort(right)

        # Two iterators for traversing the two halves
        i = 0
        j = 0

        # Iterator for the main list
        k = 0

        while i < len(left) and j < len(right):
            if left[i] < right[j]:
                # The value from the left half has been used
                myList[k] = left[i]
                # Move the iterator forward
                i += 1
            else:
                myList[k] = right[j]

```

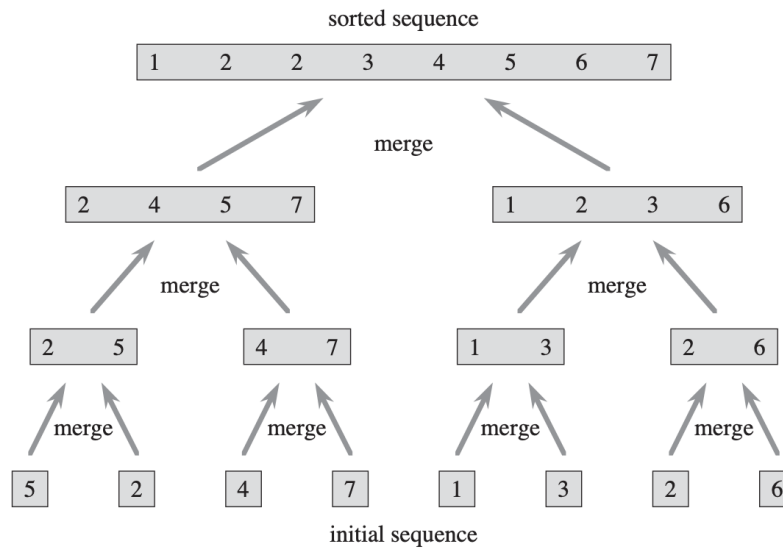


Figure 8: Merge Sort

```

        j += 1
        # Move to the next slot
        k += 1

# For all the remaining values
while i < len(left):
    myList[k] = left[i]
    i += 1
    k += 1

while j < len(right):
    myList[k]=right[j]
    j += 1
    k += 1

```

```

myList = [54,26,93,17,77,31,44,55,20]
mergeSort(myList)
print(myList)

```

The complexity  $\theta(n)$ .

$$T(n) = c_1 + 2T\left(\frac{n}{2}\right) + c.n$$

## Quick Sort:

The time complexity in best way is  $O(n \log(n))$  and the worst case scenario is when is whole list already sorted so the time complexity is  $O(n^2)$ .

### Code:

```

def partition(arr,low,high):
    i = ( low-1 )           # index of smaller element
    pivot = arr[high]       # pivot

    for j in range(low , high):

```

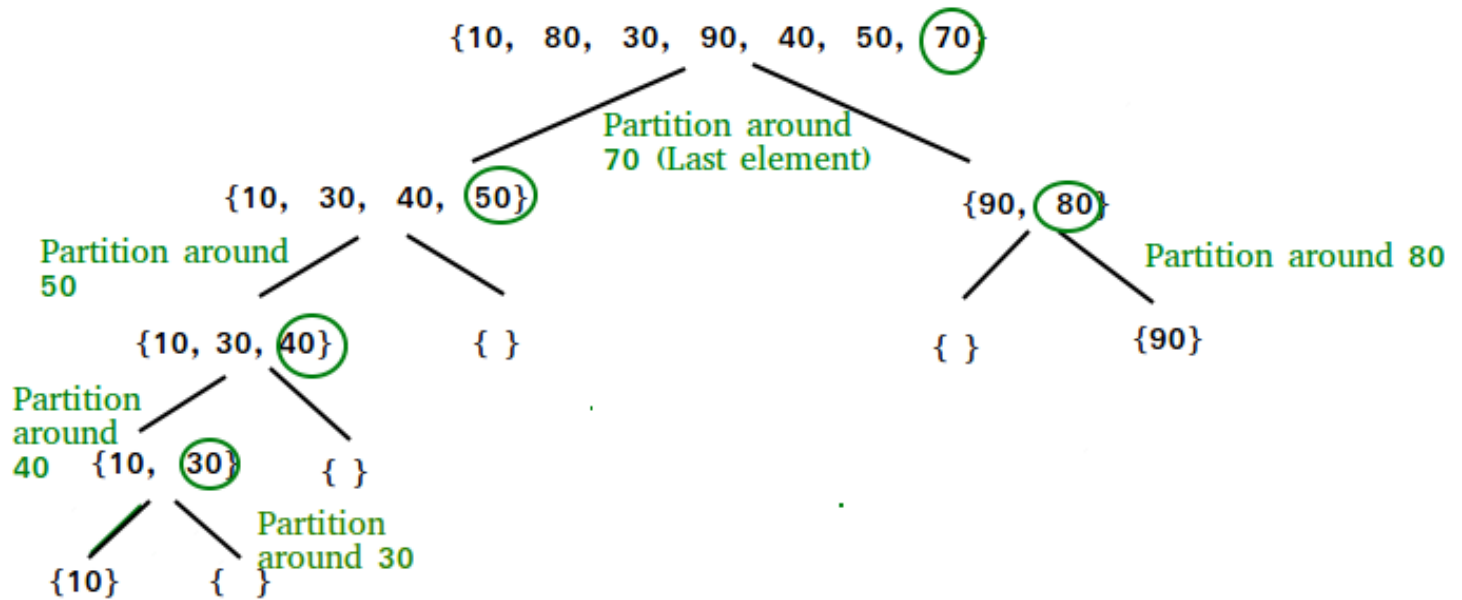


Figure 9: Quick Sort

```

# If current element is smaller than or
# equal to pivot
if arr[j] <= pivot:

    # increment index of smaller element
    i = i+1
    arr[i],arr[j] = arr[j],arr[i]

arr[i+1],arr[high] = arr[high],arr[i+1]
return ( i+1 )

# The main function that implements QuickSort
# arr[] --> Array to be sorted,
# low --> Starting index,
# high --> Ending index

# Function to do Quick sort
def quickSort(arr,low,high):
    if low < high:

        # pi is partitioning index, arr[pi] is now
        # at right place
        pi = partition(arr,low,high)

        # Separately sort elements before
        # partition and after partition
        quickSort(arr, low, pi-1)
        quickSort(arr, pi+1, high)

```

## Heap Sort:

### [Reference Book](#)

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===== »»»> 676994c7ad62f4f2c1ba875ae8c76e3852d02f72 if a node is at index i:

- its left child is at  $2*i$ .
- its right child is at  $2*i+1$ .
- its parent is at  $\lfloor \frac{i}{2} \rfloor$ .

**Max Heap:** it is a complete binary and all node have greater than descending.

**Min Heap:** it is a complete binary and all node have less than descending.

### Insertion:

The time of insertion is  $O(1)$  to  $O(\log(n))$ .

### Deletion:

The time of deletion is  $O(\log(n))$ .

By deletion and saving the element we will get sorted list.

### Code:

```
class MaxHeap:

    def __init__(self, capacity=50):
        """Constructor creating an empty heap with default capacity = 50 but allows heaps
        of other capacities to be created."""
        self.heap = [None]*(capacity+1)    # index 0 not used for heap
        self.size = 0                      # empty heap

    def enqueue(self, item): # nlog(n)
        """inserts "item" into the heap
        Raises IndexError if there is no room in the heap"""
        if self.is_full():
            raise IndexError
        self.size +=1
        self.heap[self.size]=item # Insert to the last element in the list
        self.perc_up(self.size)

    def peek(self):
        """returns max without changing the heap
        Raises IndexError if the heap is empty"""
        if self.is_empty():
            raise IndexError
        return self.heap[1] # index one becuse we start from one not from index zero

    def dequeue(self): # nlog(n)
        """returns max and removes it from the heap and restores the heap property
        Raises IndexError if the heap is empty"""
        if self.is_empty():
            raise IndexError
```

```

max=self.heap[1] # save the top element as the max
self.heap[1]=self.heap[self.size] # Replace the last element with the root
self.heap[self.size]=max # Bring the max to the end of array
self.size -= 1
self.heap.pop()
self.perc_down(1) # perc down the root element(max) down
return max

def contents(self):
    """returns a list of contents of the heap in the order it is stored internal to the heap.
    (This may be useful for in testing your implementation.)
    If heap is empty, returns empty list []"""
    if self.is_empty():
        return []

    return self.heap[1:self.size+1]

def build_heap(self, alist):
    """Discards the items in the current heap and builds a heap from
    the items in alist using the bottom up method.
    If the capacity of the current heap is less than the number of
    items in alist, the capacity of the heap will be increased to accommodate the items in alist"""

    i = 0
    self.size = len(alist)
    while i < len(alist):
        if i > self.get_capacity() - 1:
            self.heap.append(alist[i]) # We need to append because the capacity of list finish
        else:
            self.heap[i + 1] = alist[i] # i+1 because we start at index 1 and index 0 is zero
            i += 1
    i = self.size
    while i > 0:
        self.perc_down(i)
        i -= 1

    # ----- Second Way -----#
    # self.size = 0
    # for i in range(len(alist)):
    #     if i < len(self.heap) - 1:
    #         self.heap[i + 1] = alist[i] # taking values from alist and assigning them into the heap
    #         self.size += 1 # counting size again
    #     else:
    #         self.heap.append(alist[i]) # if we've passed capacity, it's okay we'll just keep adding
    #         self.size += 1
    # for i in range(self.size, 0, -1): # starting from the bottom, we want to perc everything down
    #     self.perc_down(i)

def is_empty(self):
    """returns True if the heap is empty, False otherwise"""
    return self.size == 0

```

```

def is_full(self):
    """returns True if the heap is full, False otherwise"""
    return self.size == self.get_capacity()

def get_capacity(self):
    """This is the maximum number of a entries the heap can hold, which is
    1 less than the number of entries that the array allocated to hold the heap can hold"""
    return len(self.heap)-1

def get_size(self):
    """the actual number of elements in the heap, not the capacity"""
    return self.size

def perc_down(self, i): #log(n)
    """where the parameter i is an index in the heap and perc_down moves the element stored
    at that location to its proper place in the heap rearranging elements as it goes."""

    done = False
    while not done and 2 * i <= self.size: # at least one child
        child1 = 2 * i
        child2 = child1 + 1
        if child2 <= self.size and self.heap[child1] < self.heap[child2]: # child2 > child1
            if self.heap[i] < self.heap[child2]: # child2 > parent
                self.heap[i], self.heap[child2] = self.heap[child2], self.heap[i] # swap the element
                i = child2 #change index to child 2
            else:
                done = True
        else: # one child or child1 is smaller
            if self.heap[i] < self.heap[child1]: # child 1 is greater
                self.heap[i], self.heap[child1] = self.heap[child1], self.heap[i]
                i = child1
            else:
                done = True

def perc_up(self, i):
    """where the parameter i is an index in the heap and perc_up moves the element stored
    at that location to its proper place in the heap rearranging elements as it goes."""

    while (i) // 2 >= 1:
        if self.heap[i] > self.heap[i // 2]: # Check the current element with parent
            self.heap[i],self.heap[i//2]=self.heap[i//2],self.heap[i] # Swap the elements
        i =i// 2

def heap_sort_ascending(self, alist):
    """perform heap sort on input alist in ascending order
    This method will discard the current contents of the heap, build a new heap using
    the items in alist, and mutate alist to put the items in ascending order"""

```



```

self.build_heap (alist)
while self.size > 0:
    maxValue = self.dequeue ()    # Pop the root elements
    alist[self.size] = maxValue   # add to end of the least becuae of maximum at root

```

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## Hash Map:

```
class MyHashTable:
```

```

def __init__(self, table_size=11):
    self.table_size = table_size
    self.hash_table = [[] for _ in range(table_size)] # List of lists implementation
    self.num_items = 0
    self.num_collisions = 0
def __repr__(self):
    return "{}".format(self.hash_table)

def insert(self, key, value):
    """Takes a key, and an item. Keys are valid Python non-negative integers.
    If key is negative, raise ValueError exception
    The function will insert the key-item pair into the hash table based on the
    hash value of the key mod the table size (hash_value = key % table_size)"""
    if key < 0:
        raise ValueError
    hash_value = key % self.table_size
    flag = True
    i = 0
    if self.hash_table[hash_value] == []: # Check if the place I want to add is empty or not
        self.hash_table[hash_value].append ((key, value))
        self.num_items += 1
    else:
        while i < len (self.hash_table[hash_value]):
            if self.hash_table[hash_value][i][0] == key: # We already have this key
                self.hash_table[hash_value][i] = (key, value)
                flag = False
                break
            i += 1
        if flag: # We don't have the key
            self.hash_table[hash_value].append ((key, value))
            self.num_collisions += 1

        self.num_items += 1

if self.load_factor () > 1.5:

    old_hash = self.hash_table
    new_value = 2 * self.table_size + 1
    self.hash_table = [[] for _ in range (new_value)]
    self.table_size = 2 * self.table_size + 1

```

```

        for i in range (len (old_hash)):
            for j in old_hash[i]:
                new_hash = j[0] % new_value
                self.hash_table[new_hash] = j
                self.num_collisions -= 1

def get_item(self, key):
    """Takes a key and returns the item from the hash table associated with the key.
    If no key-item pair is associated with the key, the function raises a LookupError exception."""

    hash_value = key % self.table_size
    for i in range (len (self.hash_table[hash_value])):
        if self.hash_table[hash_value][i][0] == key:
            return self.hash_table[hash_value][i][1]
    raise LookupError

def remove(self, key):
    """Takes a key, removes the key-item pair from the hash table and returns the key-item pair.
    If no key-item pair is associated with the key, the function raises a LookupError exception.
    (The key-item pair should be returned as a tuple)"""
    hash_value = key % self.table_size

    for i in range(len(self.hash_table[hash_value])):
        if self.hash_table[hash_value][i][0] == key:

            self.num_items -=1
            return self.hash_table[hash_value].pop(i)

    raise LookupError

def load_factor(self):
    """Returns the current load factor of the hash table"""
    return self.num_items/self.table_size

def size(self):
    """Returns the number of key-item pairs currently stored in the hash table"""
    return self.num_items

def collisions(self):
    """Returns the number of collisions that have occurred during insertions into the hash table"""
    return self.num_collisions
===== >>>> 676994c7ad62f4f2c1ba875ae8c76e3852d02f72

```