Algorithm

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Book

Lecture Video for the Book Good LectureTutorial(Java)

The Steps for analyzing Algorithm:

- \bullet time
- space
- network transformation
- power consumption
- cpu registers

Recursion:

Recursion is the process of defining a problem (or the solution to a problem) in terms of (a simpler version) itself.

Law of Recursive:

- A recursive algorithm must have a base case (when to stop)
- A recursive algorithm must move toward the base case
- A recursive algorithm must call itself recursively

Code:

Example 1:

```
def count_down(n):
    print(n,end='')
    if n>0:
        count_down(n-1)

Example 2:
def sum_list(list):
    if len(list)==0:
        return 0
    return list[0]+sum_list(list[1:])
```

Example 3:

Convert decimal to different base

```
def tostr(n,base):
   digits='0123456789ABCDEF'
   if n<base:</pre>
```

```
return digits[n]
  return tostr(n // base,base) + digits[n % base]
Example 4:
Check Palindrome
  • Recursive:
def pallidnrome_recursive(num):
    s=str(num)
    if len(s) < 1:
        return True
    else:
        if s[0] == s[-1]:
            return pallidnrome_recursive(s[1:-1])
        else:
            return False
  • Second Way:
def reverseDigits(num) :
    rev_num = 0;
    while (num > 0) :
        rev_num = rev_num * 10 + num % 10
        num = num // 10
    return rev_num
# Function to check if n is Palindrome
def isPalindrome(n) :
    # get the reverse of n
    rev_n = reverseDigits(n);
    \# Check if rev_n and n are same or not.
    if (rev_n == n) :
        return 1
    else :
        return 0
Example 5:
Fibonacci sequence:
  • Recursive:
def fib_recursive(num):
    if num <=1:
        return num
    return fib(num-1)+fib(num-2)
  • Loop:
def fib_loop(num):
    n1, n2=0, 1
    count=0
    if num==0:
        return 0
    elif num==1:
```

```
return 1
    else:
        while count <num:
            nth=n1+n2
            n1=n2 # swap
            n2=nth # swap
            count +=1
        return n1
Example 6(Check if the item in the node list):
def search(item, node):
  if node.item==item:
    return True
  elif node==None:
    return False
  else:
     returnsearch(item, node.rest)
```

Stack(LIFO):

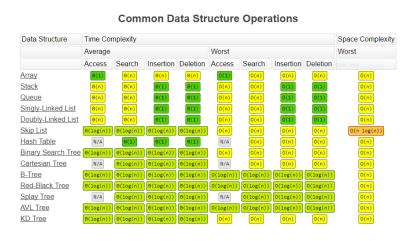


Figure 1: Common Data Structure Operation

Stack Array:

```
# Stack class implemented with array
class Stack:
    """Implements an efficient last-in first-out Abstract Data Type using a Python List"""
    # capacity is max number of Nodes, init_items is optional List parameter for initialization
    # if the length of the init_items List exceeds capacity, raise IndexError
    def __init__(self, capacity, init_items=None):
        """Creates an empty stack with a capacity"""
        self.capacity = capacity
                                        # capacity of stack
        self.items = [None]*capacity
                                        # array for stack
        self.num_items = 0
                                        # number of items in stack
                                        # if init_items is not None, initialize stack
        if init_items is not None:
            if len(init_items) > capacity:
                raise IndexError
            else:
```

```
self.num_items = len(init_items)
            self.items[:self.num_items] = init_items
def __eq__(self, other):
   return ((type(other) == Stack)
        and self.capacity == other.capacity
        and self.items[:self.num_items] == other.items[:other.num_items]
def __repr__(self):
   return ("Stack({!r}, {!r})".format(self.capacity, self.items[:self.num_items]))
def is_empty(self):
    '''Returns True if the stack is empty, and False otherwise
      MUST have O(1) performance'''
   return self.num items == 0
def is_full(self):
    {\tt '''} \textit{Returns True if the stack is full, and False otherwise}
       MUST have O(1) performance'''
   return self.num_items==self.capacity
def push(self, item):
    '''If stack is not full, pushes item on stack.
       If stack is full when push is attempted, raises IndexError
       MUST have O(1) performance'''
   if self.num items==self.capacity:
       raise IndexError("The Stack is Full")
   self.items[self.num_items]=item
   self.num_items +=1
    # print(self.items.__repr__())
    # return self.items[self.num_items-1]
def pop(self):
    '''If stack is not empty, pops item from stack and returns item.
       If stack is empty when pop is attempted, raises IndexError
       MUST have O(1) performance'''
   if self.num_items==0:
        raise IndexError("Index out of range")
   self.num_items -=1
    # print(self.items[self.num_items].__repr__())
   return self.items[self.num_items]
def peek(self):
    '''If stack is not empty, returns next item to be popped (but does not remove the item)
       If stack is empty, raises IndexError
      MUST have O(1) performance'''
   if self.num_items==0:
       raise IndexError
    # print(self.items[self.num_items-1].__repr__())
   return self.items[self.num_items-1]
```

```
def size(self):
        '''Returns the number of elements currently in the stack, not the capacity
           MUST have O(1) performance'''
        return self.num_items
Stack Nodel List:
# NodeList is one of
# None or
# Node(value, rest), where rest is reference to the rest of the list
class Node:
    def __init__(self, value, rest):
        self.value = value
                                # object reference stored in Node
                                # reference to NodeList
        self.rest = rest
    def __eq__(self, other):
        return ((type(other) == Node)
          and self.value == other.value
          and self.rest == other.rest
    def __repr__(self):
        return ("Node({!r}, {!r})".format(self.value, self.rest))
class Stack:
    """Implements an efficient last-in first-out Abstract Data Type using a node list"""
    # top is the top Node of stack
    def __init__(self, top=None):
        self.top = top
                                    # top node of stack
        self.num_items = 0
                                    # number of items in stack
        node = top
                                    # set number of items based on input
        while node is not None:
            self.num items += 1
            node = node.rest
    def __eq__(self, other):
        return ((type(other) == Stack)
          and self.top == other.top
    def __repr__(self):
        return ("Stack({!r})".format(self.top))
    def is_empty(self):
        '''Returns True if the stack is empty, and False otherwise
           MUST have O(1) performance '''
        return self.num_items==0
    def push(self, item):
        '''Pushes item on stack.
           MUST have O(1) performance'''
        new_stack=Node(item,self.top)
        self.rest=self.top
        self.top=new_stack
        self.num_items += 1
```

```
def pop(self):
    '''If stack is not empty, pops item from stack and returns item.
       If stack is empty when pop is attempted, raises IndexError
       MUST have O(1) performance'''
    if self.top is None:
        raise IndexError
    self.num_items -=1
    temp=self.top.value
    self.top.value=None
    self.top=self.top.rest
    return temp
def peek(self):
    '''If stack is not empty, returns next item to be popped (but does not remove the item)
       If stack is empty, raises IndexError
       MUST have O(1) performance'''
    if self.num_items==0:
        raise IndexError
    return self.top.value
def size(self):
    '''Returns the number of elements currently in the stack, not the capacity
       MUST have O(1) performance'''
    return self.num_items
```

Queue(FIFO):

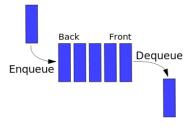


Figure 2: Queue

Array:

```
# Queue ADT - circular array implementation
class Queue:
    """Implements an efficient first-in first-out Abstract Data Type using a Python List"""
    def __init__(self, capacity, init_items=None):
        """Creates a queue with a capacity and initializes with init_items"""
                                        # capacity of queue
        self.capacity= capacity
        self.items = [None]*capacity
                                        # array for queue
        self.num_items = 0
                                        # number of items in queue
        self.front = 0
                                        # front index of queue (items removed from front)
        self.rear = 0
                                        # rear index of queue (items enter at rear)
        if init_items is not None:
                                        # if init_items is not None, initialize queue
            if len(init_items) > capacity:
                raise IndexError
            else:
```

```
self.num_items = len(init_items)
            self.items[:self.num_items] = init_items
            self.rear = self.num_items % self.capacity # % capacity addresses length=capacity
def __eq__(self, other):
   return ((type(other) == Queue)
        and self.capacity == other.capacity
        and self.get_items() == other.get_items()
def __repr__(self):
   return ("Queue({!r}, {!r})".format(self.capacity, self.get_items()))
# get_items returns array (Python list) of items in Queue
# first item in the list will be front of queue, last item is rear of queue
def get items(self):
   if self.num items == 0:
       return []
   if self.front < self.rear:</pre>
        return self.items[self.front:self.rear]
   else:
        return self.items[self.front:] + self.items[:self.rear]
def is_empty(self):
    """Returns true if the queue is empty and false otherwise
   Must be 0(1)"""
   return self.num_items==0
def is full(self):
    """Returns true if the queue is full and false otherwise
   Must be O(1)"""
   return self.num_items==self.capacity
def enqueue(self, item):
    """enqueues item, raises IndexError if Queue is full
   Must be O(1)"""
   if self.is_full():
        raise IndexError
   self.items[self.rear]=item
   self.rear=(self.rear+1)%self.capacity # give the location which next time we need to be
   self.num_items += 1
def dequeue(self):
    """dequeues and returns item, raises IndexError if Queue is empty
   Must be 0(1)"""
   if self.is empty():
       raise IndexError
   value=self.items[self.front]
   self.front=(self.front+1)%self.capacity
   self.num_items -=1
   return value
def size(self):
   """Returns the number of items in the queue
  Must be O(1)"""
  return self.num_items
```

NodeList:

```
# NodeList version of ADT Queue
# Node class for use with Queue implemented with linked list
# NodeList is one of
# None or
# Node(value, rest), where rest is the rest of the list
class Node:
    def __init__(self, value, rest):
        self.value = value
                                # value
        self.rest = rest
                                # NodeList
    def __eq__(self, other):
        return ((type(other) == Node)
         and self.value == other.value
          and self.rest == other.rest
    def __repr__(self):
        return ("Node({!r}, {!r})".format(self.value, self.rest))
class Queue:
   def __init__(self):
        self.rear = None
                            # rear NodeList
        self.front = None
                           # front NodeList
        self.num_items = 0 # number of items in Queue
   def __eq__(self, other):
        return ((type(other) == Queue)
            and self.get_items() == other.get_items()
        )
    def __repr__(self):
        return ("Queue({!r}, {!r})".format(self.rear, self.front))
    # get_items returns array (Python list) of items in Queue
    # first item in the list will be front of queue, last item is rear of queue
    def get_items(self):
        items = []
        front = self.front
        while front is not None:
            items.append(front.value)
            front = front.rest
        if self.rear is not None:
            rear items = []
            rear = self.rear
            while rear is not None:
                rear_items.append(rear.value)
                rear = rear.rest
            rear_items.reverse()
            items.extend(rear_items)
        return items
    def is_empty(self):
        """Returns true if the queue is empty and false otherwise
```

```
Must be 0(1)"""
   return self.num_items==0
def enqueue(self, item):
    """enqueues item, adding it to the rear NodeList
   Must be 0(1)"""
   que=Node(item,self.rear)
   self.rear=que
   self.num_items+=1
def dequeue(self):
    """dequeues item, removing first item from front NodeList
   If front NodeList is empty, remove items from rear NodeList
   and add to front NodeList until rear NodeList is empty
   If front NodeList and rear NodeList are both empty, raise IndexError
   Must be O(1) - general case"""
   if self.is_empty():
       raise IndexError
   self.num_items -= 1
   if self.front is not None:
        temp=self.front.value
        self.front=self.front.rest
        return temp
   if self.front is None:
        i=self.rear
        while i is not None:
            temp=i.value
            i=i.rest
            self.front=Node(temp,self.front)
            self.rear=self.rear.rest
        temp = self.front.value
        self.front = self.front.rest
        return temp
def size(self):
    """Returns the number of items in the queue
   Must be O(1)"""
   return self.num_items
```

Doubly Link List:

```
class Node:
    """Node for use with doubly-linked list"""
    def __init__(self, item, next=None, prev=None):
        self.item = item # item held by Node
        self.next = next # reference to next Node
        self.prev = prev # reference to previous Node

class OrderedList:
    """A doubly-linked ordered list of integers,
```

```
from lowest (head of list, sentinel.next) to highest (tail of list, sentinel.prev)"""
def __init__(self, sentinel=None):
    """Use only a sentinel Node. No other instance variables"""
    self.sentinel = Node(None)
    self.sentinel.next = self.sentinel
    self.sentinel.prev = self.sentinel
def is_empty(self):
    """Returns back True if OrderedList is empty"""
    return self.sentinel.next==self.sentinel
def add(self, item):
    """Adds an item to OrderedList, in the proper location based on ordering of items
    from lowest (at head of list) to highest (at tail of list)
    If item is already in list, do not add again (no duplicate items)"""
    cur=self.sentinel.next
    while cur is not self.sentinel and item >cur.item:
        cur=cur.next
    if cur.item != item:
        temp=Node(item)
        temp.prev=cur.prev
        temp.next=cur
        cur.prev.next=temp
        cur.prev=temp
def remove(self, item):
    """Removes an item from OrderedList. If item is removed (was in the list) returns True
    If item was not removed (was not in the list) returns False"""
    cur=self.sentinel
    if self.is_empty():
        return False
    else:
        while cur.next != self.sentinel:
            if cur.next.item == item:
                cur.next=cur.next.next
                cur.next.prev=cur
                return True
            else:
                cur=cur.next
        return False
def index(self, item):
    """Returns index of an item in OrderedList (assuming head of list is index 0).
    If item is not in list, return None"""
    if self.is_empty():
        raise IndexError
    cur=self.sentinel.next
    num item =0
    while cur.item != item:
        cur=cur.next
        num_item +=1
    return num_item
```

```
def pop(self, index):
    """Removes and returns item at index (assuming head of list is index 0).
    If index is negative or >= size of list, raises IndexError"""
    cur = self.sentinel.next
    num_itemes = 0
    if self.is_empty():
        raise IndexError
    if index < 0:</pre>
        raise IndexError
    while cur != self.sentinel and num_itemes < index:</pre>
        cur = cur.next
        num_itemes += 1
    if cur == self.sentinel:
        raise IndexError
    else:
        ret_val = cur.item
        cur.next.prev = cur.prev
        cur.prev.next = cur.next
        return ret_val
def search(self, item):
    """Searches OrderedList for item, returns True if item is in list, False otherwise recursion
    def helper(cur, values):
        if cur == self.sentinel:
            return False
        if cur.item> values:
            return False
        elif cur.item == values:
            return True
        else:
            return helper(cur.next, values)
    cur=self.sentinel.next
    return helper(cur,item)
def python_list(self):
    """Return a Python list representation of OrderedList, from head to tail
    For example, list with integers 1, 2, and 3 would return [1, 2, 3]"""
    list=[]
    cur=self.sentinel.next
    while cur is not self.sentinel:
        list.append(cur.item)
        cur=cur.next
    return list
def python_list_reversed(self):
    """Return a Python list representation of OrderedList, from tail to head, using recursion
    For example, list with integers 1, 2, and 3 would return [3, 2, 1] recursion"""
    def helper(cur):
        if cur.next ==self.sentinel:
            return [cur.item]
        else:
```

```
return helper(cur.next)+[cur.item]
cur=self.sentinel.next
return helper(cur)

def size(self):
    """Returns number of items in the OrderedList. O(n) is OK recursion"""
    def helper(cur):
        if cur == self.sentinel:
            return 0
        return helper(cur.next)+1
    cur=self.sentinel
    return helper(cur.next)
```

Binary Tree:

	Insert	search	min	max	Transversals	height
Big O	log(n)	log(n)	log(n)	log(n)	O(n)	O(n)

Three type of trees:

- Full: leaf with no children or with to leaves
- Complete: fill up top to bottom and left to right
- Perfect: all leaves and nodes are at the same level

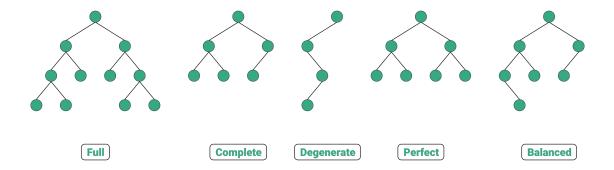


Figure 3: Trees

```
Traversal:
```

```
• Pre Order : nlr
  • In Order : lnr
  • Post Order: lrn
In OrderedList:
def inorder_list(self): # return Python list of BST keys representing in-order traversal of BST (LVR-
    def _inorder(current,list):
        if current != None:
            _inorder(current.left,list)
            list.append(current.key)
            _inorder(current.right,list)
        return list
    return _inorder(self.root,[])
PreOreder:
def preorder_list(self): # return Python list of BST keys representing pre-order traversal of BST (
      def _preorder(current,list):
          if current !=None:
              list.append(current.key)
              _preorder(current.left,list)
              _preorder(current.right,list)
          return list
      return _preorder(self.root,[])
Level order list:
def level_order_list(self): # return Python list of BST keys representing level-order traversal of B
    # You MUST use your queue_array data structure from lab 3 to implement this method
    q = Queue(25000) # Don't change this!
    list1 = []
    if self.root == None:
        return None
    q.enqueue(self.root) # adding whole root q Stack
    while q.is_empty()==False:
        root=q.dequeue()
        list1.append(root.key)
        if root.left != None:
            q.enqueue(root.left)
        if root.right != None:
            q.enqueue(root.right)
    return list1
Calculate the Hight:
def height(self,node):
  if node==None:
    return 0
```

```
left=self.height(node.left)
  right=self.height(node.right)
  return 1 + max(left,right)
Insertion:
def insert(self, key, data=None): # inserts new node w/ key and data
        # If an item with the given key is already in the BST,
        # the data in the tree will be replaced with the new data
        # Example creation of node: temp = TreeNode(key, data)
        def _insert(key,cur_node,data):
            if key <cur_node.key:</pre>
                if cur node.left == None:
                    cur_node.left=TreeNode(key,data)
                    _insert(key,cur_node.left,data)
            elif key> cur_node.key:
                if cur_node.right==None:
                    cur_node.right=TreeNode(key,data)
                else:
                    _insert(key,cur_node.right,data)
            else:
                cur_node.data=data # update the data
            return cur_node
        if self.root==None:
            self.root=TreeNode(key,data)
        else:
            self.root=_insert(key,self.root,data)
Search:
def search(self, key): # returns True if key is in a node of the tree, else False
      def _search(key,current_node):
          if key==current_node.key:
              return True
          elif key < current_node.key and current_node.left !=None:</pre>
              return _search(key, current_node.left)
          elif key>current_node.key and current_node.right !=None:
              return _search(key, current_node.right)
          return False
      if self.root != None:
          return _search(key,self.root)
      else:
          return False
Min:
def find_min(self): # returns a tuple with min key and data in the BST
      # returns None if the tree is empty
      if self.is_empty():
          return None
      def _min(current):
          if current is None:
              return None
          if current.left is None:
```

```
return current.key, current.data
return _min(current.left)

return _min(self.root)

Max:

def find_max(self): # returns a tuple with max key and data in the BST
    # returns None if the tree is empty
    if self.is_empty():
        return None
    def _max(current):
        if current is None:
            return None
        if current.right is None:
            return _max(current.right)

return _max(self.root)
```

Sorting:

Name	Time Complexity (Best)	Time Complexity (Average)	Time Complexity (Worst)	Space Complexity	Stability
Bubble Sort	Ω(n)	Θ(n²)	O(n²)	O(1)	Stable
Selection Sort	$\Omega(n^2)$	Θ(n²)	O(n²)	O(1)	Unstable
Insertion Sort	Ω(n)	Θ(n²)	O(n²)	O(1)	Stable
Merge Sort	Ω(n log(n))	Θ(n log(n))	O(n log(n))	O(n)	Stable
Quick Sort	Ω(n log(n))	Θ(n log(n))	O(n²)	O(log(n))	Unstable
Heap Sort	Ω(n log(n))	Θ(n log(n))	O(n log(n))	O(1)	Unstable
Counting Sort	Ω(n+k)	⊖(n+k)	O(n+k)	O(k)	Stable
Radix Sort	Ω(nk)	Θ(nk)	O(nk)	O(n+k)	Stable

Figure 4: Sorting Table:

Summery with animation

Bubble Sort:

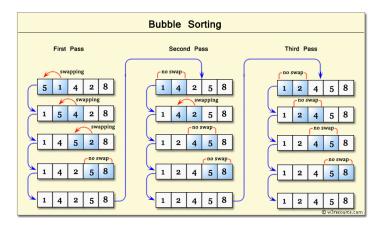


Figure 5: Bubble Sort

Insertion Sort:

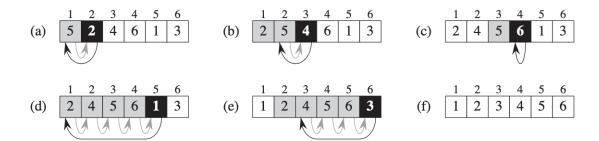


Figure 6: Insertion Sort

Code:

The $\theta(n)$ steps. Each steps have $\theta(n)$ swaps.

Selection Sort:

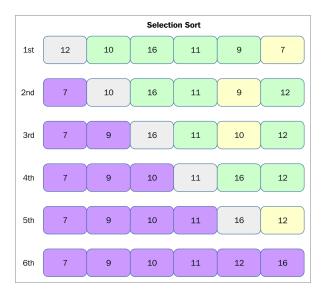


Figure 7: Selection Sort:

• Find the minimum value in the list

- Swap it with the value in the first position
- Repeat the steps above for the remainder of the list (starting at the second position and advancing each time)

Code:

```
def selection_sort(A):
    # Traverse through all array elements
    for i in range(len(A)):

    # Find the minimum element in remaining
    # unsorted array
    min_idx = i
    for j in range(i+1, len(A)):
        if A[min_idx] > A[j]:
            min_idx = j

# Swap the found minimum element with
    # the first element
    A[i], A[min_idx] = A[min_idx], A[i]
    return A
```

Merge Sort:

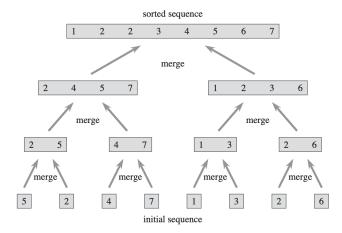


Figure 8: Merge Sort

Code:

```
def mergeSort(myList):
    if len(myList) > 1:
        mid = len(myList) // 2
        left = myList[:mid]
        right = myList[mid:]

# Recursive call on each half
        mergeSort(left)
        mergeSort(right)

# Two iterators for traversing the two halves
    i = 0
    j = 0
```

```
# Iterator for the main list
        k = 0
        while i < len(left) and j < len(right):
             if left[i] < right[j]:</pre>
               # The value from the left half has been used
               myList[k] = left[i]
               # Move the iterator forward
               i += 1
             else:
                 myList[k] = right[j]
                 j += 1
             # Move to the next slot
             k += 1
        # For all the remaining values
        while i < len(left):
             myList[k] = left[i]
             i += 1
             k += 1
        while j < len(right):</pre>
             myList[k]=right[j]
             j += 1
             k += 1
myList = [54,26,93,17,77,31,44,55,20]
mergeSort(myList)
print(myList)
The complexity \theta(n).
T(n) = c_1 + 2T(\frac{n}{2}) + c.n
```

Quick Sort:

The time complexity in best way is O(nlog(n)) and the worst case scenario is when is whole list already sorted so the time complexity is $O(n^2)$.

Code:

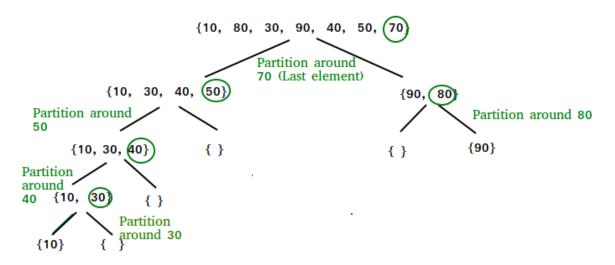


Figure 9: Quick Sort

```
# The main function that implements QuickSort
# arr[] --> Array to be sorted,
# low --> Starting index,
# high --> Ending index

# Function to do Quick sort
def quickSort(arr,low,high):
    if low < high:

        # pi is partitioning index, arr[p] is now
        # at right place
        pi = partition(arr,low,high)

        # Separately sort elements before
        # partition and after partition
        quickSort(arr, low, pi-1)
        quickSort(arr, pi+1, high)</pre>
```

Heap Sort:

Reference Book

if a node is at index i:

- its left child is at **2*i**.
- its right child is at **2*i+1**.
- its parent is at $\left[\frac{i}{2}\right]$.

Max Heap: it is a complete binary and all node have greater than descending.

Min Heap: it is a complete binary and all node have less than descending.

Insertion:

The time of insertion is O(1) to O(log(n)).

Deletion:

The time of deletion is $O(\log(n))$.

By deletion and saving the element we will get sorted list.

Code:

```
class MaxHeap:
```

```
def __init__(self, capacity=50):
    """Constructor creating an empty heap with default capacity = 50 but allows heaps of other co
    self.heap = [None]*(capacity+1)
                                        # index 0 not used for heap
    self.size = 0
                                        # empty heap
def enqueue(self, item): # nlog(n)
    """inserts "item" into the heap
    Raises IndexError if there is no room in the heap"""
    if self.is full():
        raise IndexError
    self.size +=1
    self.heap[self.size]=item # Insert to the last element in the list
    self.perc_up(self.size)
def peek(self):
    """returns max without changing the heap
    Raises IndexError if the heap is empty"""
    if self.is_empty():
        raise IndexError
    return self.heap[1] # index one because we start from one not from index zero
def dequeue(self): # nlog(n)
    """returns max and removes it from the heap and restores the heap property
       Raises IndexError if the heap is empty"""
    if self.is_empty():
        raise IndexError
    max=self.heap[1] # save the top element as the max
    self.heap[1]=self.heap[self.size] # Replace the last element with the root
    self.heap[self.size]=max # Bring the max to the end of array
    self.size -= 1
    self.heap.pop()
    self.perc_down(1) # perc down the root element(max) down
    return max
def contents(self):
    """returns a list of contents of the heap in the order it is stored internal to the heap.
    (This may be useful for in testing your implementation.)
    If heap is empty, returns empty list []"""
    if self.is_empty():
        return []
    return self.heap[1:self.size+1]
```

```
def build_heap(self, alist):
    """Discards the items in the current heap and builds a heap from
    the items in alist using the bottom up method.
   If the capacity of the current heap is less than the number of
    items in alist, the capacity of the heap will be increased to accommodate the items in alist'
   i = 0
   self.size = len(alist)
   while i < len(alist):</pre>
       if i > self.get_capacity() - 1:
            self.heap.append(alist[i]) # We need to append because the capacity of list finish
           self.heap[i + 1] = alist[i] # i+1 because we start at index 1 and index 0 is zero
   i = self.size
   while i > 0:
       self.perc_down(i)
       i -= 1
   # -----#
   # self.size = 0
    # for i in range(len(alist)):
         if i < len(self.heap) - 1:
             self.heap[i + 1] = alist[i] # taking values from alist and assigning them into the
    #
             self.size += 1 # counting size again
    #
             self.heap.append(alist[i]) # if we've passed capacity, it's okay we'll just keep a
    #
             self.size += 1
    # for i in range(self.size, 0, -1): # starting from the bottom, we want to perc everything of
         self.perc_down(i)
def is_empty(self):
    """returns True if the heap is empty, False otherwise"""
   return self.size == 0
def is_full(self):
    """returns True if the heap is full, False otherwise"""
   return self.size == self.get_capacity()
def get_capacity(self):
    """This is the maximum number of a entries the heap can hold, which is
    1 less than the number of entries that the array allocated to hold the heap can hold"""
   return len(self.heap)-1
def get_size(self):
    """the actual number of elements in the heap, not the capacity"""
   return self.size
def perc_down(self, i): #log(n)
```

```
"""where the parameter i is an index in the heap and perc_down moves the element stored
   at that location to its proper place in the heap rearranging elements as it goes."""
   done = False
   while not done and 2 * i <= self.size: # at least one child
       child1 = 2 * i
       child2 = child1 + 1
       if child2 <= self.size and self.heap[child1] < self.heap[child2]: # two children and chi
            if self.heap[i] < self.heap[child2]: # Compare biggest child with the parent
                self.heap[i], self.heap[child2] = self.heap[child2], self.heap[i] # swap the elem
                i = child2 #change index to child 2
            else.
               done = True
       else: # one child or child1 is smaller
            if self.heap[i] < self.heap[child1]: # child 1 is greater</pre>
                self.heap[i], self.heap[child1] = self.heap[child1], self.heap[i]
            else:
               done = True
def perc_up(self, i):
    """where the parameter i is an index in the heap and perc_up moves the element stored
    at that location to its proper place in the heap rearranging elements as it goes."""
   while (i) // 2 >= 1:
       if self.heap[i] > self.heap[i // 2]: # Check the current element with parent
            self.heap[i],self.heap[i/2]=self.heap[i/2],self.heap[i] # Swap the elements
       i = i// 2
def heap_sort_ascending(self, alist):
    """perform heap sort on input alist in ascending order
    This method will discard the current contents of the heap, build a new heap using
    the items in alist, and mutate alist to put the items in ascending order"""
   self.build_heap (alist)
   while self.size > 0:
       maxValue = self.dequeue ()
                                   # Pop the root elements
       alist[self.size] = maxValue # add to end of the least because of maximum at root
```