Algorithm

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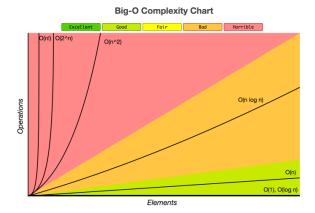
Book

Lecture Video for the Book

Good LectureTutorial(Java)

The Steps for analyzing Algorithm:

- time
- space
- network transformation
- power consumption
- cpu registers



Common Data Structure Operations

Data Structure	Time Complexity							Space Complexity	
	Average				Worst				Worst
	Access	Search	Insertion	Deletion	Access	Search	Insertion	Deletion	
Array	0(1)	0(n)	0(n)	0(n)	0(1)	0(n)	0(n)	0(n)	0(n)
Stack	0(n)	0(n)	0(1)	0(1)	0(n)	0(n)	0(1)	0(1)	0(n)
Queue	0(n)	0(n)	0(1)	0(1)	0(n)	0(n)	0(1)	0(1)	0(n)
Singly-Linked List	0(n)	0(n)	0(1)	0(1)	0(n)	0(n)	0(1)	0(1)	0(n)
Doubly-Linked List	0(n)	0(n)	0(1)	0(1)	0(n)	0(n)	0(1)	0(1)	0(n)
Skip List	0(log(n))	0(log(n))	0(log(n))	O(log(n))	0(n)	0(n)	0(n)	0(n)	O(n log(n))
Hash Table	N/A	0(1)	0(1)	0(1)	N/A	0(n)	0(n)	0(n)	0(n)
Binary Search Tree	0(log(n))	0(log(n))	0(log(n))	0(log(n))	0(n)	0(n)	0(n)	0(n)	0(n)
Cartesian Tree	N/A	0(log(n))	0(log(n))	O(log(n))	N/A	0(n)	0(n)	0(n)	0(n)
B-Tree	0(log(n))	0(log(n))	0(log(n))	O(log(n))	0(log(n))	0(log(n))	0(log(n))	0(log(n))	0(n)
Red-Black Tree	0(log(n))	0(log(n))	0(log(n))	O(log(n))	0(log(n))	0(log(n))	0(log(n))	0(log(n))	0(n)
Splay Tree	N/A	0(log(n))	O(log(n))	O(log(n))	N/A	0(log(n))	0(log(n))	0(log(n))	0(n)
AVL Tree	0(log(n))	0(log(n))	0(log(n))	0(log(n))	0(log(n))	0(log(n))	0(log(n))	0(log(n))	0(n)
KD Tree	0(log(n))	0(log(n))	0(log(n))	0(log(n))	0(n)	0(n)	0(n)	0(n)	0(n)

Recursion:

Recursion is the process of defining a problem (or the solution to a problem) in terms of (a simpler version) itself.

Law of Recursive:

• A recursive algorithm must have a base case (when to stop)

- A recursive algorithm must move toward the base case
- A recursive algorithm must call itself recursively

```
Example 1:
def count_down(n):
  print(n,end='')
  if n>0:
    count_down(n-1)
Example 2:
def sum_list(list):
  if len(list)==0:
    return 0
 return list[0]+sum_list(list[1:])
Example 3:
Convert decimal to different base
def tostr(n,base):
  digits='0123456789ABCDEF'
  if n<base:</pre>
    return digits[n]
  return tostr(n // base,base) + digits[n % base]
Example 4:
Check Palindrome
  • Recursive:
def pallidnrome_recursive(num):
    s=str(num)
    if len(s) < 1:
        return True
    else:
        if s[0] == s[-1]:
            return pallidnrome_recursive(s[1:-1])
        else:
            return False
  • Second Way:
def reverseDigits(num) :
    rev_num = 0;
    while (num > 0) :
        rev_num = rev_num * 10 + num % 10
        num = num // 10
    return rev_num
# Function to check if n is Palindrome
def isPalindrome(n) :
    # get the reverse of n
    rev_n = reverseDigits(n);
```

```
# Check if rev_n and n are same or not.
    if (rev_n == n) :
        return 1
    else :
        return 0
Example 5:
Fibonacci sequence:
  • Recursive:
def fib_recursive(num):
    if num <=1:
        return num
    return fib(num-1)+fib(num-2)
  • Loop:
def fib_loop(num):
    n1, n2=0, 1
    count=0
    if num==0:
        return 0
    elif num==1:
        return 1
    else:
        while count <num:
            nth=n1+n2
            n1=n2 # swap
            n2=nth # swap
            count +=1
        return n1
Example 6(Check if the item in the node list):
def search(item, node):
  if node.item==item:
    return True
  elif node==None:
    return False
  else:
    returnsearch(item,node.rest)
Stack(LIFO):
Stack Array:
# Stack class implemented with array
class Stack:
    """Implements an efficient last-in first-out Abstract Data Type using a Python List"""
    # capacity is max number of Nodes, init_items is optional List parameter for initialization
    # if the length of the init_items List exceeds capacity, raise IndexError
    def __init__(self, capacity, init_items=None):
        """Creates an empty stack with a capacity"""
        self.capacity = capacity
                                       # capacity of stack
        self.items = [None]*capacity
                                        # array for stack
```

Data Structure Time Complexity Space Complexity Average Worst Worst Access Search Insertion Deletion Access Search Insertion Deletion Array Stack 0(n) Queue Θ(n) Θ(n) 0(n) Singly-Linked List Θ(n) Θ(n) Doubly-Linked List Θ(n) Θ(n) 0(n) Skip List 0(log(n) Hash Table N/A Θ(1) N/A Binary Search Tree 0(log(n) Cartesian Tree N/A N/A B-Tree Θ(log(n)) (log(n)) (log(n) Red-Black Tree (log(n) (log(n)) Splay Tree Θ(log(n)) (log(n)) (log(n)) **AVL Tree** $\Theta(\log(n)) \quad \Theta(\log(n)) \quad \Theta(\log(n))$ Θ(log(n)) (log(n)) KD Tree

Common Data Structure Operations

Figure 1: Common Data Structure Operation

```
self.num_items = 0
                                    # number of items in stack
   if init_items is not None:
                                    # if init_items is not None, initialize stack
        if len(init_items) > capacity:
            raise IndexError
        else:
            self.num_items = len(init_items)
            self.items[:self.num_items] = init_items
def __eq__(self, other):
   return ((type(other) == Stack)
        and self.capacity == other.capacity
        and self.items[:self.num_items] == other.items[:other.num_items]
        )
def __repr__(self):
   return ("Stack({!r}, {!r})".format(self.capacity, self.items[:self.num_items]))
def is_empty(self):
    '''Returns True if the stack is empty, and False otherwise
       MUST have O(1) performance'''
   return self.num items == 0
def is_full(self):
    '''Returns True if the stack is full, and False otherwise
       MUST have O(1) performance'''
   return self.num_items==self.capacity
def push(self, item):
    '''If stack is not full, pushes item on stack.
       If stack is full when push is attempted, raises IndexError
       MUST have O(1) performance'''
    if self.num_items==self.capacity:
```

```
raise IndexError("The Stack is Full")
        self.items[self.num_items]=item
        self.num_items +=1
        # print(self.items.__repr__())
        # return self.items[self.num_items-1]
    def pop(self):
        '''If stack is not empty, pops item from stack and returns item.
           If stack is empty when pop is attempted, raises IndexError
           MUST have O(1) performance'''
        if self.num items==0:
            raise IndexError("Index out of range")
        self.num items -=1
        # print(self.items[self.num_items].__repr__())
        return self.items[self.num items]
    def peek(self):
        '''If stack is not empty, returns next item to be popped (but does not remove the item)
           If stack is empty, raises IndexError
           MUST have O(1) performance'''
        if self.num_items==0:
           raise IndexError
        # print(self.items[self.num_items-1].__repr__())
        return self.items[self.num_items-1]
    def size(self):
        '''Returns the number of elements currently in the stack, not the capacity
           MUST have O(1) performance'''
        return self.num_items
Stack Nodel List:
# NodeList is one of
# Node(value, rest), where rest is reference to the rest of the list
class Node:
    def __init__(self, value, rest):
        self.value = value
                                # object reference stored in Node
        self.rest = rest
                                # reference to NodeList
    def __eq__(self, other):
        return ((type(other) == Node)
          and self.value == other.value
          and self.rest == other.rest
    def __repr__(self):
        return ("Node({!r}, {!r})".format(self.value, self.rest))
class Stack:
    """Implements an efficient last-in first-out Abstract Data Type using a node list"""
    # top is the top Node of stack
    def __init__(self, top=None):
        self.top = top
                                    # top node of stack
```

```
self.num_items = 0
                                # number of items in stack
                                # set number of items based on input
   node = top
   while node is not None:
        self.num_items += 1
       node = node.rest
def __eq__(self, other):
   return ((type(other) == Stack)
      and self.top == other.top
   )
def __repr__(self):
   return ("Stack({!r})".format(self.top))
def is_empty(self):
    '''Returns True if the stack is empty, and False otherwise
       MUST have O(1) performance '''
   return self.num_items==0
def push(self, item):
    '''Pushes item on stack.
      MUST have O(1) performance'''
   new_stack=Node(item,self.top)
   self.rest=self.top
   self.top=new_stack
   self.num_items += 1
def pop(self):
    '''If stack is not empty, pops item from stack and returns item.
       If stack is empty when pop is attempted, raises IndexError
       MUST have O(1) performance'''
   if self.top is None:
       raise IndexError
   self.num items -=1
   temp=self.top.value
   self.top.value=None
   self.top=self.top.rest
   return temp
def peek(self):
    '''If stack is not empty, returns next item to be popped (but does not remove the item)
       If stack is empty, raises IndexError
       MUST have O(1) performance'''
   if self.num_items==0:
        raise IndexError
   return self.top.value
def size(self):
    '''Returns the number of elements currently in the stack, not the capacity
       MUST have O(1) performance'''
   return self.num_items
```

Queue(FIFO):

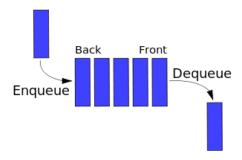


Figure 2: Queue

Array:

```
# Queue ADT - circular array implementation
class Queue:
    """Implements an efficient first-in first-out Abstract Data Type using a Python List"""
    def __init__(self, capacity, init_items=None):
        """Creates a queue with a capacity and initializes with init_items"""
        self.capacity= capacity
                                       # capacity of queue
        self.items = [None]*capacity
                                      # array for queue
        self.num_items = 0
                                        # number of items in queue
        self.front = 0
                                        # front index of queue (items removed from front)
        self.rear = 0
                                        # rear index of queue (items enter at rear)
        if init items is not None:
                                        # if init items is not None, initialize queue
            if len(init_items) > capacity:
                raise IndexError
            else:
                self.num_items = len(init_items)
                self.items[:self.num_items] = init_items
                self.rear = self.num_items % self.capacity # % capacity addresses length=capacity
    def __eq__(self, other):
        return ((type(other) == Queue)
            and self.capacity == other.capacity
            and self.get_items() == other.get_items()
            )
    def __repr__(self):
        return ("Queue({!r}, {!r})".format(self.capacity, self.get_items()))
    # get items returns array (Python list) of items in Queue
    # first item in the list will be front of queue, last item is rear of queue
    def get_items(self):
        if self.num_items == 0:
            return []
        if self.front < self.rear:</pre>
            return self.items[self.front:self.rear]
        else:
            return self.items[self.front:] + self.items[:self.rear]
    def is_empty(self):
```

```
"""Returns true if the queue is empty and false otherwise
   Must be 0(1)"""
   return self.num_items==0
def is_full(self):
    """Returns true if the queue is full and false otherwise
   Must be 0(1)"""
   return self.num_items==self.capacity
def enqueue(self, item):
    """enqueues item, raises IndexError if Queue is full
    Must be 0(1)"""
   if self.is_full():
        raise IndexError
   self.items[self.rear]=item
   self.rear=(self.rear+1)%self.capacity # give the location which next time we need to be
   self.num_items += 1
def dequeue(self):
    """dequeues and returns item, raises IndexError if Queue is empty
   Must be O(1)"""
   if self.is_empty():
       raise IndexError
   value=self.items[self.front]
   self.front=(self.front+1)%self.capacity
   self.num_items -=1
   return value
def size(self):
   """Returns the number of items in the queue
  Must be 0(1)"""
  return self.num_items
```

NodeList:

```
# NodeList version of ADT Queue
# Node class for use with Queue implemented with linked list
# NodeList is one of
# None or
# Node(value, rest), where rest is the rest of the list
class Node:
    def __init__(self, value, rest):
        self.value = value
                                # value
                                # NodeList
        self.rest = rest
    def __eq__(self, other):
        return ((type(other) == Node)
          and self.value == other.value
          and self.rest == other.rest
    def __repr__(self):
        return ("Node({!r}, {!r})".format(self.value, self.rest))
class Queue:
   def __init__(self):
```

```
# rear NodeList
   self.rear = None
   self.front = None # front NodeList
   self.num_items = 0 # number of items in Queue
def __eq__(self, other):
   return ((type(other) == Queue)
        and self.get_items() == other.get_items()
def __repr__(self):
   return ("Queue({!r}, {!r})".format(self.rear, self.front))
# get_items returns array (Python list) of items in Queue
# first item in the list will be front of queue, last item is rear of queue
def get_items(self):
   items = []
   front = self.front
   while front is not None:
        items.append(front.value)
        front = front.rest
   if self.rear is not None:
       rear_items = []
        rear = self.rear
        while rear is not None:
            rear_items.append(rear.value)
           rear = rear.rest
        rear_items.reverse()
        items.extend(rear_items)
   return items
def is_empty(self):
    """Returns true if the queue is empty and false otherwise
   Must be 0(1)"""
   return self.num_items==0
def enqueue(self, item):
    """enqueues item, adding it to the rear NodeList
    Must be O(1)"""
   que=Node(item, self.rear)
    self.rear=que
   self.num_items+=1
def dequeue(self):
    """dequeues item, removing first item from front NodeList
    If front NodeList is empty, remove items from rear NodeList
    and add to front NodeList until rear NodeList is empty
    If front NodeList and rear NodeList are both empty, raise IndexError
   Must be O(1) - general case"""
   if self.is_empty():
        raise IndexError
   self.num_items -= 1
   if self.front is not None:
```

```
temp=self.front.value
        self.front=self.front.rest
       return temp
   if self.front is None:
        i=self.rear
       while i is not None:
            temp=i.value
            i=i.rest
            self.front=Node(temp,self.front)
            self.rear=self.rear.rest
        temp = self.front.value
        self.front = self.front.rest
        return temp
def size(self):
    """Returns the number of items in the queue
   Must be 0(1)"""
   return self.num_items
```

Doubly Link List:

```
class Node:
    """Node for use with doubly-linked list"""
   def __init__(self, item, next=None, prev=None):
       self.item = item # item held by Node
       self.next = next # reference to next Node
       self.prev = prev # reference to previous Node
class OrderedList:
    """A doubly-linked ordered list of integers,
    from lowest (head of list, sentinel.next) to highest (tail of list, sentinel.prev)"""
   def __init__(self, sentinel=None):
        """Use only a sentinel Node. No other instance variables"""
       self.sentinel = Node(None)
       self.sentinel.next = self.sentinel
       self.sentinel.prev = self.sentinel
   def is_empty(self):
        """Returns back True if OrderedList is empty"""
       return self.sentinel.next==self.sentinel
   def add(self, item):
        """Adds an item to OrderedList, in the proper location based on ordering of items
        from lowest (at head of list) to highest (at tail of list)
        If item is already in list, do not add again (no duplicate items)"""
       cur=self.sentinel.next
       while cur is not self.sentinel and item >cur.item:
            cur=cur.next
       if cur.item != item:
           temp=Node(item)
           temp.prev=cur.prev
           temp.next=cur
```

```
cur.prev.next=temp
        cur.prev=temp
def remove(self, item):
    """Removes an item from OrderedList. If item is removed (was in the list) returns True
    If item was not removed (was not in the list) returns False"""
    cur=self.sentinel
    if self.is_empty():
        return False
    else:
        while cur.next != self.sentinel:
            if cur.next.item == item:
                cur.next=cur.next.next
                cur.next.prev=cur
                return True
            else:
                cur=cur.next
        return False
def index(self, item):
    """Returns index of an item in OrderedList (assuming head of list is index 0).
    If item is not in list, return None"""
    if self.is_empty():
        raise IndexError
    cur=self.sentinel.next
    num_item =0
    while cur.item != item:
        cur=cur.next
        num item +=1
    return num_item
def pop(self, index):
    """Removes and returns item at index (assuming head of list is index 0).
    If index is negative or >= size of list, raises IndexError"""
    cur = self.sentinel.next
    num_itemes = 0
    if self.is_empty():
        raise IndexError
    if index < 0:</pre>
        raise IndexError
    while cur != self.sentinel and num_itemes < index:</pre>
        cur = cur.next
        num_itemes += 1
    if cur == self.sentinel:
        raise IndexError
    else:
        ret_val = cur.item
        cur.next.prev = cur.prev
        cur.prev.next = cur.next
        return ret_val
```

```
def search(self, item):
    """Searches OrderedList for item, returns True if item is in list, False otherwise recursion"""
   def helper(cur, values):
        if cur == self.sentinel:
            return False
        if cur.item> values:
            return False
        elif cur.item == values:
            return True
        else:
            return helper(cur.next, values)
    cur=self.sentinel.next
   return helper(cur,item)
def python_list(self):
    """Return a Python list representation of OrderedList, from head to tail
   For example, list with integers 1, 2, and 3 would return [1, 2, 3]"""
   cur=self.sentinel.next
   while cur is not self.sentinel:
        list.append(cur.item)
        cur=cur.next
   return list
def python_list_reversed(self):
    """Return a Python list representation of OrderedList, from tail to head, using recursion
    For example, list with integers 1, 2, and 3 would return [3, 2, 1] recursion"""
   def helper(cur):
        if cur.next ==self.sentinel:
            return [cur.item]
        else:
            return helper(cur.next)+[cur.item]
   cur=self.sentinel.next
   return helper(cur)
def size(self):
    """Returns number of items in the OrderedList. O(n) is OK recursion"""
   def helper(cur):
        if cur == self.sentinel:
            return 0
        return helper(cur.next)+1
   cur=self.sentinel
   return helper(cur.next)
```

Binary Tree:

	Insert	search	min	max	Transversals	height
Big O	log(n)	log(n)	log(n)	log(n)	O(n)	O(n)

Three type of trees:

- Full: leaf with no children or with to leaves
- Complete: fill up top to bottom and left to right
- Perfect: all leaves and nodes are at the same level

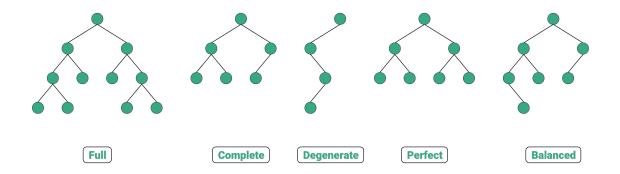


Figure 3: Trees

Traversal:

Pre Order : n l rIn Order : l n rPost Order: l r n

In OrderedList:

```
_preorder(current.left,list)
              _preorder(current.right,list)
          return list
      return _preorder(self.root,[])
Level order list:
def level_order_list(self):
  # return Python list of BST keys representing level-order traversal of BST
  # You MUST use your queue_array data structure from lab 3 to implement this method
    q = Queue(25000) # Don't change this!
    list1 = []
    if self.root == None:
        return None
    q.enqueue(self.root) # adding whole root q Stack
    while q.is empty()==False:
        root=q.dequeue()
        list1.append(root.key)
        if root.left != None:
            q.enqueue(root.left)
        if root.right != None:
            q.enqueue(root.right)
    return list1
Calculate the Hight:
def height(self,node):
  if node==None:
    return 0
  left=self.height(node.left)
  right=self.height(node.right)
  return 1 + max(left,right)
Insertion:
def insert(self, key, data=None): # inserts new node w/ key and data
        # If an item with the given key is already in the BST,
        # the data in the tree will be replaced with the new data
        # Example creation of node: temp = TreeNode(key, data)
        def _insert(key,cur_node,data):
            if key <cur_node.key:</pre>
                if cur_node.left == None:
                    cur_node.left=TreeNode(key,data)
                    _insert(key,cur_node.left,data)
            elif key> cur_node.key:
                if cur_node.right==None:
                    cur_node.right=TreeNode(key,data)
                else:
                    _insert(key,cur_node.right,data)
            else:
                cur_node.data=data # update the data
```

```
return cur_node
        if self.root==None:
            self.root=TreeNode(key,data)
        else:
            self.root=_insert(key,self.root,data)
Search:
def search(self, key):
# returns True if key is in a node of the tree, else False
      def search(key,current node):
          if key==current_node.key:
              return True
          elif key < current_node.key and current_node.left !=None:</pre>
              return _search(key, current_node.left)
          elif key>current_node.key and current_node.right !=None:
              return _search(key, current_node.right)
          return False
      if self.root != None:
          return _search(key,self.root)
      else:
          return False
Min:
def find_min(self):
  # returns a tuple with min key and data in the BST
  # returns None if the tree is empty
      if self.is empty():
          return None
      def min(current):
          if current is None:
              return None
          if current.left is None:
              return current.key, current.data
          return _min(current.left)
      return _min(self.root)
Max:
def find_max(self): # returns a tuple with max key and data in the BST
      # returns None if the tree is empty
      if self.is_empty():
          return None
      def max(current):
          if current is None:
              return None
          if current.right is None:
              return current.key, current.data
          return _max(current.right)
      return _max(self.root)
```

Sorting:

Name	Time Complexity (Best)	Time Complexity (Average)	Time Complexity (Worst)	Space Complexity	Stability
Bubble Sort	Ω(n)	Θ(n²)	O(n²)	O(1)	Stable
Selection Sort	$\Omega(n^2)$	Θ(n²)	O(n²)	O(1)	Unstable
Insertion Sort	Ω(n)	Θ(n²)	O(n²)	O(1)	Stable
Merge Sort	Ω(n log(n))	Θ(n log(n))	O(n log(n))	O(n)	Stable
Quick Sort	Ω(n log(n))	Θ(n log(n))	O(n²)	O(log(n))	Unstable
Heap Sort	Ω(n log(n))	Θ(n log(n))	O(n log(n))	O(1)	Unstable
Counting Sort	Ω(n+k)	⊖(n+k)	O(n+k)	O(k)	Stable
Radix Sort	Ω(nk)	Θ(nk)	O(nk)	O(n+k)	Stable

Figure 4: Sorting Table:

Summery with animation

Bubble Sort:

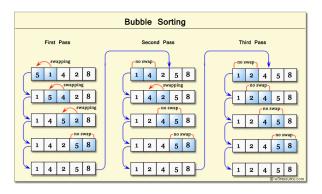


Figure 5: Bubble Sort

Insertion Sort:

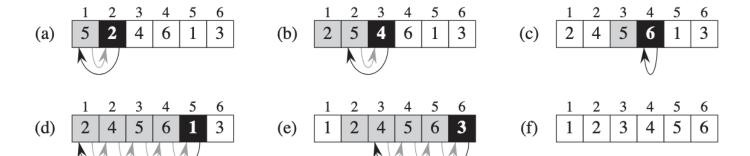


Figure 6: Insertion Sort

Code:

```
def insertion_sort(alist):
    com = 0 # How many comparison the code do
    for i in range (1, len (alist)):
        value = alist[i]
        j = i - 1
        while j >= 0:
        com += 1
        if value<alist[j]:
            alist[j + 1] = alist[j]
        alist[j] = value
        j = j - 1
        else:
            break
    return com</pre>
```

The $\theta(n)$ steps. Each steps have $\theta(n)$ swaps.

Selection Sort:

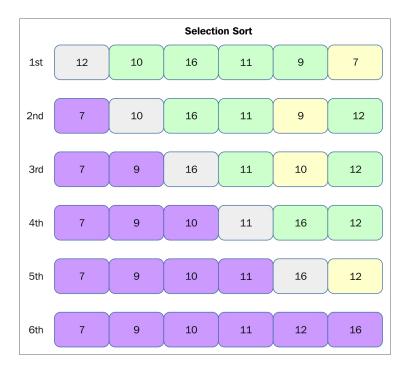


Figure 7: Selection Sort:

- Find the minimum value in the list
- Swap it with the value in the first position
- Repeat the steps above for the remainder of the list (starting at the second position and advancing each time)

Code:

```
def selection_sort(A):
    # Traverse through all array elements
    for i in range(len(A)):
        # Find the minimum element in remaining
        # unsorted array
        min_idx = i
        for j in range(i+1, len(A)):
            if A[min_idx] > A[j]:
                min_idx = j
        # Swap the found minimum element with
        # the first element
        A[i], A[min_idx] = A[min_idx], A[i]
    return A
Merge Sort:
```

```
def mergeSort(myList):
    if len(myList) > 1:
        mid = len(myList) // 2
        left = myList[:mid]
        right = myList[mid:]
```

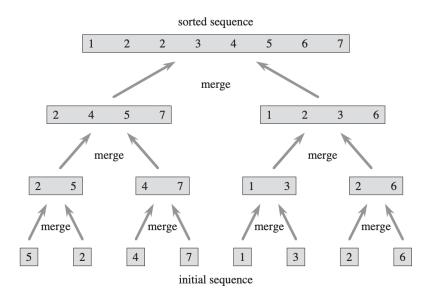


Figure 8: Merge Sort

```
# Recursive call on each half
mergeSort(left)
mergeSort(right)
# Two iterators for traversing the two halves
i = 0
j = 0
# Iterator for the main list
k = 0
while i < len(left) and j < len(right):
    if left[i] < right[j]:</pre>
      # The value from the left half has been used
      myList[k] = left[i]
      # Move the iterator forward
      i += 1
    else:
        myList[k] = right[j]
        j += 1
    # Move to the next slot
    k += 1
# For all the remaining values
while i < len(left):</pre>
    myList[k] = left[i]
    i += 1
    k += 1
while j < len(right):</pre>
    myList[k]=right[j]
    j += 1
    k += 1
```

```
myList = [54,26,93,17,77,31,44,55,20] mergeSort(myList) print(myList) The complexity \theta(n). T(n) = c_1 + 2T(\frac{n}{2}) + c.n
```

Quick Sort:

The time complexity in best way is O(nlog(n)) and the worst case scenario is when is whole list already sorted so the time complexity is $O(n^2)$.

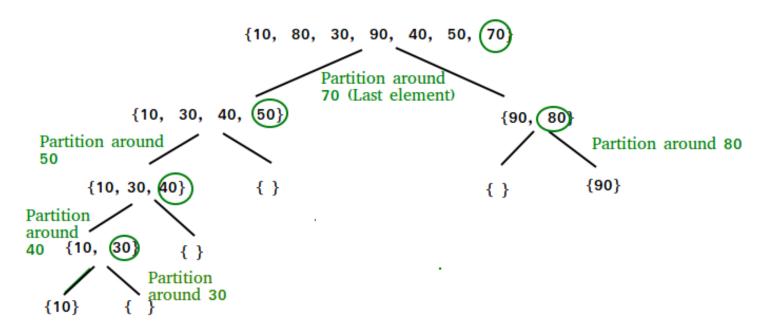


Figure 9: Quick Sort

```
def partition(arr,low,high):
   i = (low-1)
                        # index of smaller element
   pivot = arr[high]
                          # pivot
   for j in range(low , high):
        # If current element is smaller than or
        # equal to pivot
            arr[j] <= pivot:</pre>
            # increment index of smaller element
            i = i+1
            arr[i],arr[j] = arr[j],arr[i]
   arr[i+1],arr[high] = arr[high],arr[i+1]
   return ( i+1 )
# The main function that implements QuickSort
# arr[] --> Array to be sorted,
```

```
# low --> Starting index,
# high --> Ending index

# Function to do Quick sort

def quickSort(arr,low,high):
    if low < high:

        # pi is partitioning index, arr[p] is now
        # at right place
        pi = partition(arr,low,high)

        # Separately sort elements before
        # partition and after partition
        quickSort(arr, low, pi-1)
        quickSort(arr, pi+1, high)</pre>
```

Heap Sort:

Reference Book

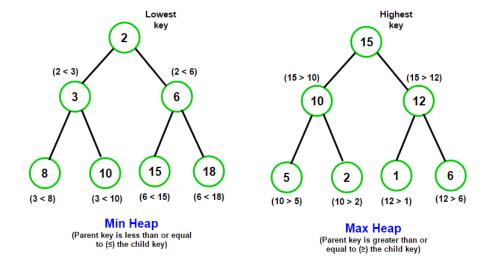


Figure 10: Type of Heap

BigO: Heap enqueue, dequeue, perc_up, perc_down are O(log(n)), build heap is O(n).

- its left child is at **2*i**.
- its right child is at **2*i+1**.
- its parent is at $\left[\frac{i}{2}\right]$.

Max Heap: it is a complete binary and all node have greater than descending.

Min Heap: it is a complete binary and all node have less than descending.

```
class MaxHeap:
```

```
def __init__(self, capacity=50):
"""Constructor creating an empty heap with default capacity = 50 but allows heaps
of other capacities to be created."""
       self.heap = [None]*(capacity+1)
                                            # index 0 not used for heap
       self.size = 0
                                             # empty heap
   def enqueue(self, item): # nlog(n)
        """inserts "item" into the heap
       Raises IndexError if there is no room in the heap"""
       if self.is_full():
            raise IndexError
       self.size +=1
       self.heap[self.size] = item # Insert to the last element in the list
       self.perc_up(self.size)
   def peek(self):
        """returns max without changing the heap
       Raises IndexError if the heap is empty"""
       if self.is_empty():
```

```
raise IndexError
   return self.heap[1] # index one because we start from one not from index zero
def dequeue(self): # nloq(n)
    """returns max and removes it from the heap and restores the heap property
      Raises IndexError if the heap is empty"""
   if self.is_empty():
       raise IndexError
   max=self.heap[1] # save the top element as the max
   self.heap[1]=self.heap[self.size] # Replace the last element with the root
   self.heap[self.size] = max # Bring the max to the end of array
   self.size -= 1
   self.heap.pop()
   self.perc_down(1) # perc down the root element(max) down
def contents(self):
    """returns a list of contents of the heap in the order it is stored internal to the heap.
    (This may be useful for in testing your implementation.)
   If heap is empty, returns empty list []"""
   if self.is_empty():
       return []
   return self.heap[1:self.size+1]
def build heap(self, alist):
    """Discards the items in the current heap and builds a heap from
    the items in alist using the bottom up method.
   If the capacity of the current heap is less than the number of
    items in alist, the capacity of the heap will be increased to accommodate the items in alist"""
   i = 0
   self.size = len(alist)
   while i < len(alist):</pre>
       if i > self.get_capacity() - 1:
           self.heap.append(alist[i]) # We need to append because the capacity of list finish
       else:
           self.heap[i + 1] = alist[i] # i+1 becuase we start at index 1 and index 0 is zero
       i += 1
   i = self.size
   while i > 0:
       self.perc down(i)
       i -= 1
    # -----#
    \# self.size = 0
    # for i in range(len(alist)):
         if i < len(self.heap) - 1:
    #
             self.heap[i + 1] = alist[i] # taking values from alist and assigning them into the heap
             self.size += 1 # counting size again
    #
         else:
```

```
self.heap.append(alist[i]) # if we've passed capacity, it's okay we'll just keep adding
              self.size += 1
    # for i in range(self.size, 0, -1): # starting from the bottom, we want to perc everything down
          self.perc_down(i)
def is_empty(self):
    """returns True if the heap is empty, False otherwise"""
   return self.size == 0
def is_full(self):
    """returns True if the heap is full, False otherwise"""
   return self.size == self.get_capacity()
def get_capacity(self):
    """This is the maximum number of a entries the heap can hold, which is
    1 less than the number of entries that the array allocated to hold the heap can hold"""
   return len(self.heap)-1
def get_size(self):
    """the actual number of elements in the heap, not the capacity"""
   return self.size
def perc_down(self, i): #log(n)
    """where the parameter i is an index in the heap and perc_down moves the element stored
    at that location to its proper place in the heap rearranging elements as it goes."""
   done = False
    while not done and 2 * i <= self.size: # at least one child
        child1 = 2 * i
        child2 = child1 + 1
        if child2 <= self.size and self.heap[child1] < self.heap[child2]: # child2 > child1
            if self.heap[i] < self.heap[child2]: # child2 > parent
                self.heap[i], self.heap[child2] = self.heap[child2], self.heap[i] # swap the element
                i = child2 #change index to child 2
            else:
                done = True
        else: # one child or child1 is smaller
            if self.heap[i] < self.heap[child1]: # child 1 is greater</pre>
                self.heap[i], self.heap[child1] = self.heap[child1], self.heap[i]
                i = child1
            else:
                done = True
def perc_up(self, i):
    """where the parameter i is an index in the heap and perc_up moves the element stored
    at that location to its proper place in the heap rearranging elements as it goes."""
   while (i) // 2 >= 1:
```

```
if self.heap[i] > self.heap[i // 2]: # Check the current element with parent
                self.heap[i],self.heap[i/2]=self.heap[i/2],self.heap[i] # Swap the elements
            i = i// 2
    def heap_sort_ascending(self, alist):
        """perform heap sort on input alist in ascending order
        This method will discard the current contents of the heap, build a new heap using
        the items in alist, and mutate alist to put the items in ascending order"""
        self.build_heap (alist)
        while self.size > 0:
            maxValue = self.dequeue ()
                                         # Pop the root elements
            alist[self.size] = maxValue # add to end of the least because of maximum at root
Hash Map:
Everything time complexity is O(1)
class MyHashTable:
    def __init__(self, table_size=11):
        self.table_size = table_size
        self.hash_table = [[] for _ in range(table_size)] # List of lists implementation
        self.num_items = 0
        self.num_collisions = 0
    def __repr__(self):
        return "{}".format(self.hash_table)
    def insert(self, key, value):
        """Takes a key, and an item. Keys are valid Python non-negative integers.
        If key is negative, raise ValueError exception
        The function will insert the key-item pair into the hash table based on the
        hash value of the key mod the table size (hash_value = key % table_size)"""
        if key < 0:
            raise ValueError
        hash_value = key % self.table_size
        flag = True
        i = 0
        if self.hash_table[hash_value] == []: # Check if the place I want to add is empty or not
            self.hash_table[hash_value].append ((key, value))
            self.num_items += 1
        else:
            while i < len (self.hash_table[hash_value]):</pre>
                if self.hash_table[hash_value][i][0] == key: # We already have this key
                    self.hash_table[hash_value][i] = (key, value)
                    flag = False
                    break
                i += 1
            if flag: # We don't have the key
                self.hash_table[hash_value].append ((key, value))
                self.num_collisions += 1
                self.num_items += 1
```

```
if self.load_factor () > 1.5:
        old_hash = self.hash_table
        new_value = 2 * self.table_size + 1
        self.hash_table = [[] for _ in range (new_value)]
        self.table_size = 2 * self.table_size + 1
        for i in range (len (old_hash)):
            for j in old_hash[i]:
                new_hash = j[0] % new_value
                self.hash_table[new_hash] = j
                self.num_collisions -= 1
def get_item(self, key):
    """Takes a key and returns the item from the hash table associated with the key.
    If no key-item pair is associated with the key, the function raises a LookupError exception."""
   hash_value = key % self.table_size
   for i in range (len (self.hash_table[hash_value])):
        if self.hash_table[hash_value][i][0] == key:
            return self.hash_table[hash_value][i][1]
   raise LookupError
def remove(self, key):
    """Takes a key, removes the key-item pair from the hash table and returns the key-item pair.
    If no key-item pair is associated with the key, the function raises a LookupError exception.
    (The key-item pair should be returned as a tuple)"""
   hash_value = key % self.table_size
   for i in range(len(self.hash_table[hash_value])):
        if self.hash_table[hash_value][i][0] == key:
            self.num_items -=1
            return self.hash_table[hash_value].pop(i)
   raise LookupError
def load_factor(self):
    """Returns the current load factor of the hash table"""
   return self.num_items/self.table_size
def size(self):
    """Returns the number of key-item pairs currently stored in the hash table"""
   return self.num_items
def collisions(self):
    """Returns the number of collisions that have occurred during insertions into the hash table"""
```

return self.num_collisions