

# Genetics and Evolution Assignment Two

Hadis Ahmadian  
400211524

## Libraries :

first we need to import the libraries that we need:

**matplotlib** for drawing graphs.

```
In [1]: import matplotlib.pyplot as plt
```

## Drwing the logistic map :

the below code calculates the value that N converges to in 500 generations for all  $0 < r < 4$  and  $N = 0.5$

the logistic map shows the value wich N converges to, per each r. we can see that for  $r \geq 3$  N does not converge to a certain value and here is were chaos stars. the chaos will get more as the value of r gets closer to 4.

I will explain more detail about the value of convergence for each range of r next parts.

below you can see the logistic map.

```
In [2]: n=0.5

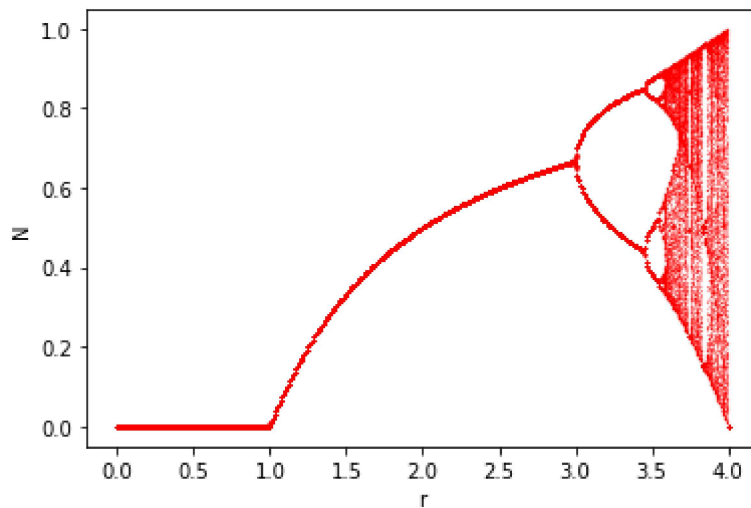
x=[]
y=[]

for j in range (401):
    r=j/100
    n=0.5
    for i in range(500):
        n=r*(n-(n*n))
        if i>100:
            x.append(r)
            y.append(n)

plt.scatter(x, y,s=0.01,color="red")

plt.xlabel('r')
plt.ylabel('N')

plt.show()
```



## pop\_itter\_plot function :

this function recives N and r and draws the graph of N per generation for 60 generation, we'll use it to see what does N converge to for diffrent amounts for r. the function calculates N of each generation in a loop (using  $n=r*(n-(n^2))$ ) and saves N of each generation and draws the graph.

```
In [3]: def pop_itter_plot(n,r):
        x=[]
        y=[]

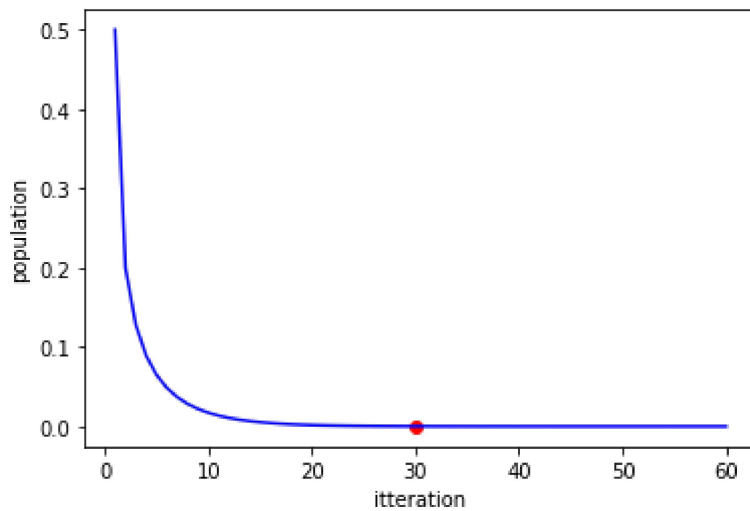
        for i in range(60):
            x.append(i+1)
            y.append(n)
            n=r*(n-(n*n))
        plt.plot(x, y,color="blue")
        plt.xlabel('itteration')
        plt.ylabel('population')
        return plt
```

we're going to test above function with N=0.5 for 1st generation and diffrent amounts of r.

1)  $0 < r < 1$

we can see that for  $r=0.8$  (and all r if  $0 < r < 1$ ) the N will converge to 0.

```
In [4]: n=0.5
        r=0.8
        p=pop_itter_plot(n,r)
        p.scatter([30],[0],color="red")
        p.show()
```

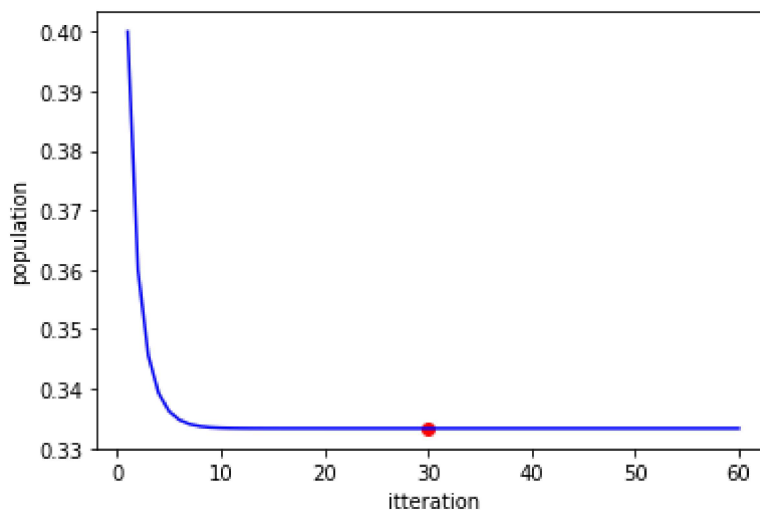


2)  $1 < r < 2$

we can see that for  $r=1.5$  (and all  $r$  if  $1 < r < 2$ ) the  $N$  will converge to a number. it is proven that the number is  $(r-1)/r$

In [5]:

```
n=0.4
r=1.5
p=pop_itter_plot(n,r)
p.scatter([30],[ (r-1)/r],color="red")
p.show()
```

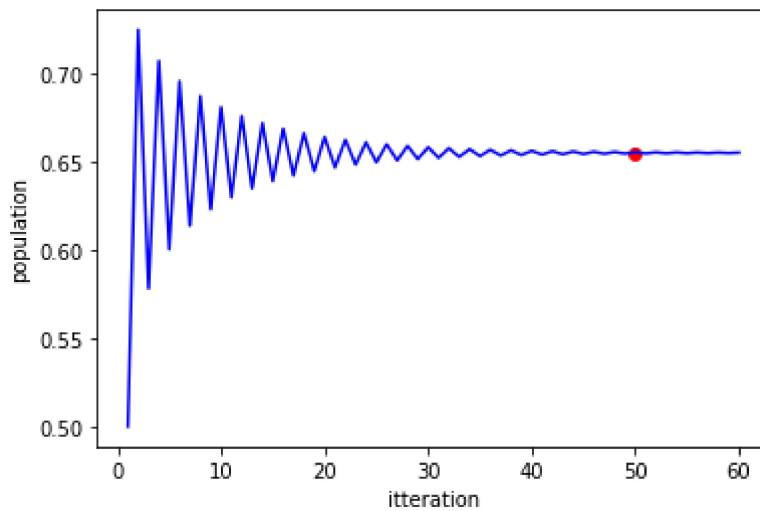


3)  $2 < r < 3$

we can see that for  $r=2.9$  (and all  $r$  if  $2 < r < 3$ ) the  $N$  will converge to a number, however not in the same shape as the last part, it increases and decreases for a while until it finally converges. it is proven that the number witch it converges to is  $(r-1)/r$

In [6]:

```
n=0.5
r=2.9
p=pop_itter_plot(n,r)
p.scatter([50],[ (r-1)/r],color="red")
p.show()
```

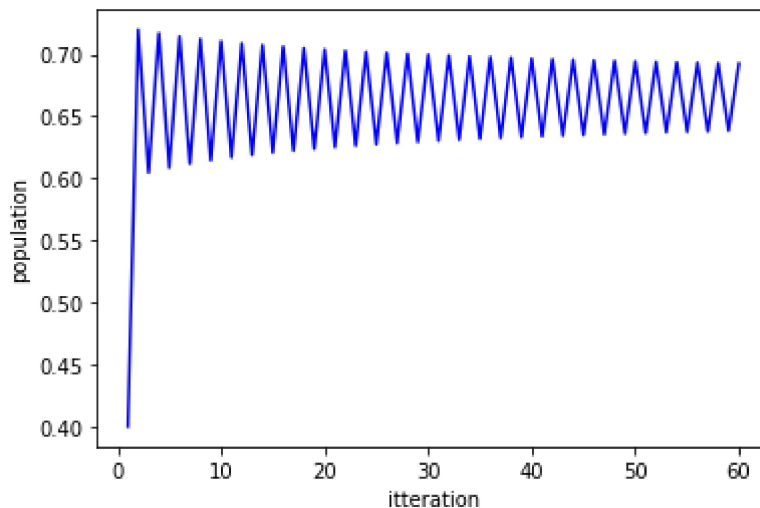


4)  $r \geq 3$

for  $r \geq 3$  we can see that  $N$  will not converge to a certain value over generations. so  $r=3$  is the **threshold**. and it's when the chaos begins.

In [7]:

```
n=0.4  
r=3  
pop_itter_plot(n,r).show()
```



it is also important to say that the higher the  $r$  ( in range 3 to 4) the more fluctuation  $N$  will have (its value will be less stable over generations, for bigger  $r$  values)

In [8]:

```
n=0.4  
r=3.9  
pop_itter_plot(n,r).show()
```

