

## CORRECTION EXERCICE 2 TD 3

1.  $L_1 = \{a^n b^n / n > 0\}$

$G = (\{S\}, \{a, b\}, S, R)$

$R = \{S \rightarrow aSb | ab\}$

ab : le plus petit mot  
accepté par  $L_1$

2.  $L_2 = \{a^n b^{2n} / n \geq 0\}$

$G = (\{S\}, \{a, b\}, S, R)$

$R = \{S \rightarrow aSbb | \varepsilon\}$

$\varepsilon$  : le plus petit mot  
accepté par  $L_2$

3.  $L_3 = \text{le langage des mots palindromes sur } \{a, b\}$

$$G = (\{S\}, \{a, b\}, S, R)$$

$$R = \{ S \rightarrow aSa \mid bSb \mid a \mid b \mid \varepsilon \}$$

4.  $L_4 = \{ a^n b^m c^n / m \geq 0, n \geq 1 \}$

$$G = (\{S\}, \{a, b, c\}, S, R)$$

$$R = \{ S \rightarrow aSc \mid aAc \\ A \rightarrow Ab \mid \varepsilon \}$$

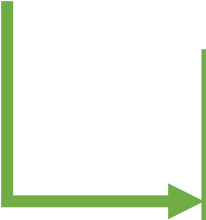
ac : le plus petit mot  
accepté par  $L_4$




$$5. L_5 = \{a^m b^n c^p / m+n = p\}$$

$$G = (\{S\}, \{a, b, c\}, S, R)$$

$$R = \{ S \rightarrow aSc \mid A \\ A \rightarrow bAc \mid \varepsilon \}$$

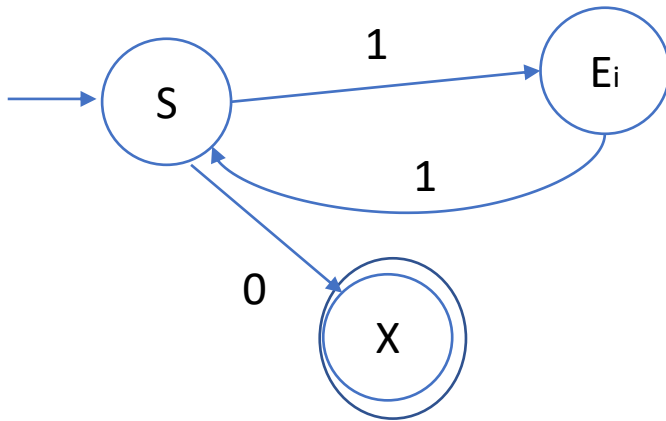




$$c^p = c^{n+m} = c^n c^m$$

$$a^m b^n c^p = a^m b^n c^n c^m$$

# CORRECTION EXERCICE 3 TD 3



D'une manière générale :

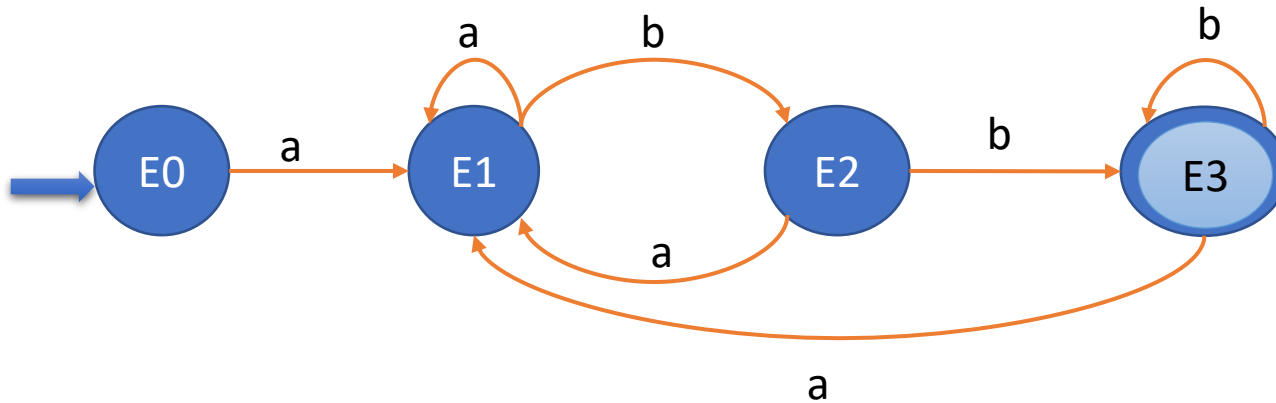
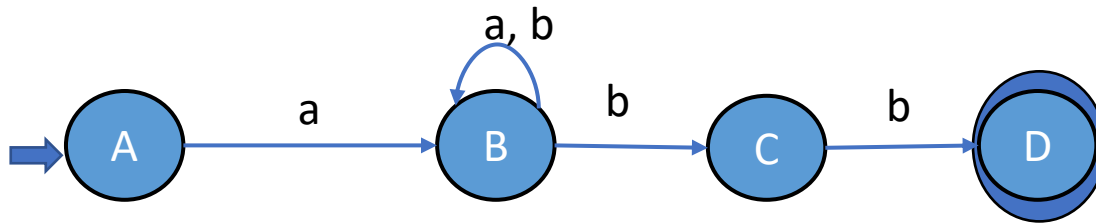
$N1 \longrightarrow t_1 t_2 N2$



$N1 \longrightarrow t_1 N_i$

$N_i \longrightarrow t_2 N2$

# CORRECTION EXERCICE 4 TD 3



|            | a        | b            |
|------------|----------|--------------|
| {A} = E0   | {B} = E1 | -            |
| {B} = E1   | {B} = E1 | {B,C} = E2   |
| {B,C} = E2 | E1       | {B,C,D} = E3 |
| E3         | E1       | E3           |

$G = \langle E0, N = \{E0, E1, E2, E3\}, T = \{a, b\},$   
 $R = \{E0 \rightarrow aE1, E1 \rightarrow aE1 \mid bE2, E2 \rightarrow aE1 \mid bE3,$   
 $E3 \rightarrow aE1 \mid bE3 \mid \epsilon\} \rangle$