

Computer Graphics and Image Processing  
CSE 955

Computer Graphics and Image Processing Laboratory  
CSE 956

Caution:

Sudden CT

1st July, 2025 - 1st Class

$$\left\{ \frac{8-3}{12-3} = \frac{5}{9} \right\}_{NS} \quad \text{02.07.25 - 2nd Class}$$

## Image processing

Image information:

signal → frequency  
 (main component) → amplitude

image → signal

Spatial domain → amplitude

Why need image transformation?

Application:

DFT → Discrete Fourier Transformation

DCT → (math) Cosine

DFT, DCT difference

real part

real and complex part

DCT performs better image compression than DFT

$$C(u) = \alpha(u) \sum_{x=0}^{n-1} f(x) \cos\left(\frac{(2x+1)u\pi}{2N}\right)$$

$$\alpha(k) = \begin{cases} \sqrt{\frac{1}{N}} & \text{if } k=0 \\ \sqrt{\frac{2}{N}} & \text{otherwise} \end{cases}$$

## Homework:

C(1), C(2) .... C(7) ?

$$C(0) = \sqrt{\frac{1}{8}} \sum_{x=0}^7 f(x) \cos \left\{ \frac{(2x+1) \cdot 0 \cdot \pi}{2N} \right\}$$

$$= \sqrt{\frac{1}{8}} \sum_{x=0}^7 f(x) \cos 0^\circ$$

$$= \sqrt{\frac{1}{8}} \left\{ f(0) + f(1) + f(3) + \dots + f(7) \right\}$$

$$= \sqrt{\frac{1}{8}} \left\{ 20 + 12 + 18 + 56 + 83 + 10 + 109 + 114 \right\}$$

DDA (Digital  
(Line Drawing algorithm)

## Math:

1. Enter two endpoints.  $(x_1, y_1), (x_2, y_2)$

2. Calculate,  $m = \frac{\Delta y}{\Delta x} = \frac{y_2 - y_1}{x_2 - x_1}$   
while (endpoints != endpoints)

3. if ( $m < 1$ )

```
{
    x_{k+1} = x_k + 1
    y_{k+1} = y_k + m
    y = roundup(y_{k+1})
    print(x_{k+1}, y)
}
```

else if ( $m > 1$ )

```
{
    y_{k+1} = y_k + 1
    x_{k+1} = x_k + \frac{1}{m}
    x' = roundup(x_{k+1})
    print(x', y_{k+1})
}
```

else ( $m = 1$ ) {  
    x++ } print (x, y)  
    y++ }

## Math(DDA)

$$(2,3), (12,8) \quad m = \frac{8-3}{12-2} = \frac{5}{10} = 0.5$$

$(2,3)$  initial coordinates (iii)

$(3,3.5) \rightarrow (3,4)$  (iv)

$(4,4) \rightarrow (4,4)$  (v)

$(5,4.5) \rightarrow (5,5)$  (vi)

$(6,5) \rightarrow (6,5)$  (vii)

$(7,5.5) \rightarrow (7,6)$  (viii)

$(8,6) \rightarrow (8,6)$  (ix)

$(9,6.5) \rightarrow (9,7)$  (x)

$(10,7) \rightarrow (10,7)$  (xi)

$(11,7.5) \rightarrow (11,8)$  (xii)

$(12,8) \rightarrow (12,8)$  (xiii)

### Disadvantage:

→ Simple, not efficient

→ fraction, takes much time

Then came,

Bresenham line algorithm.

\* Advantages of DCT.

\* Hadamard transform. (important for exam)

Hadamard transform example.  $A \leftrightarrow B$

u u advantage

# Digital Image Processing:

To A3 (A3)

## Steps:

- i) Problem domain
- ii) Image acquisition  
(using camera, scanner)
- iii) Image enhancement.  
(by modifying / editing)
- iv) Image restoration
- v) Color image processing
- vi) Wavelet and Multi-resolution processing.

- 8.8 =  $\frac{2}{\delta t} =$
- vii) Image compression,  $\frac{1}{f}$  lossy
  - viii) Morphological Image Processing.
  - ix) Image segmentation.
  - x) Image representation and Description.
  - xi) Object recognition
- (E.P) ← (E.P.E)  
(E.P.E) ← (E.R.F)  
(E.R.F) ← (E.S)  
(E.S) ← (E.O)  
(E.O) ← (E.O.D)  
(E.O.D) ← (E.F.U)  
(E.F.U) ← (E.S.I)

## Components of Image processing System:

- i) Image sensors.
- ii) Specialized Image Processing Hardware.
- iii) Computer

Inputs for algos ←  
shift down exist noise off ←  
new genes ←  
multiple soil samples ←

To expert system  
(noise not important), no expert - break off →

→ A. algos need not break off

algos → N N

⇒ What is color?

: primary colors

⇒ Physical properties of light

: color of light

⇒ Color model

→ RGB

→ CMY

→ HSI

*	W	B	R	G	I	S	Color
1.0	1.0	0.0	0.0	0.0	0.0	0.0	Black

⇒ Conversion from RGB to HSI

(Equation - George Zet)

⇒ Relationship between pixels.

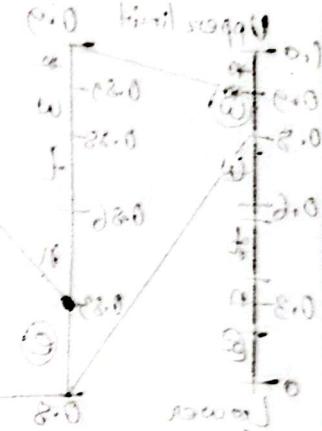
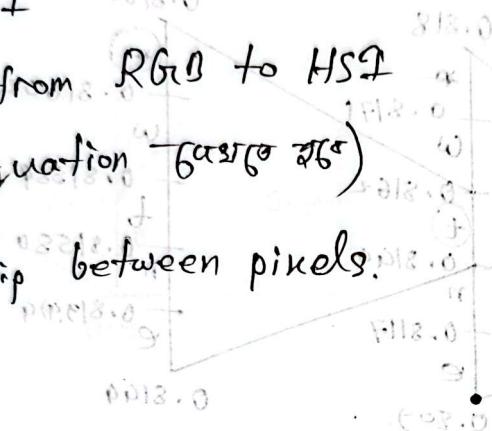


Image Processing Idea:

Image Compression:

⇒ Huffman code

Arithmetic encoding  
Arithmetic Coding → Arithmetic decoding.

Original → Source reduction

Arithmetic Coding - Example

Source → 0.518, 0.518, 0.518

0.518, 0.518, 0.518 → 0.518, 0.518, 0.518

\* Exercise.

bit wise arithmetic with source

⇒ Bit plane slicing

to high order bit to low order bit

0.518, 0.518

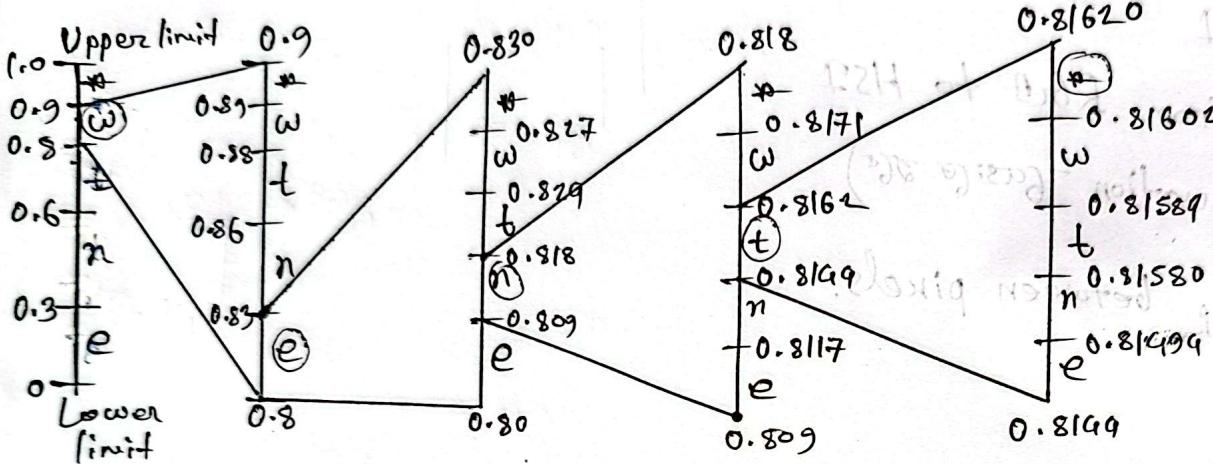
?

11218, 0

## Arithmetic encoding:

Q. Encode the msg "Went\*" — find codeword

Symbols :	e	n	t	w	*
Probability:	0.3	0.3	0.2	0.1	0.1



Range of symbols = Lower limit + d (probability of symbols)

$$d = \text{Upper limit} - \text{Lower limit}$$

Final range:

$$0.81602 - 0.81620 \rightarrow \text{codeword } \underline{\text{01010}}$$

Hence the arithmetic codeword is  $0.81602 - 0.81620$

$$\text{Generation tag} = \frac{\text{Upper limit of codeword} + \text{Lower limit of codeword}}{2}$$

$$= \frac{0.81602 + 0.81620}{2}$$

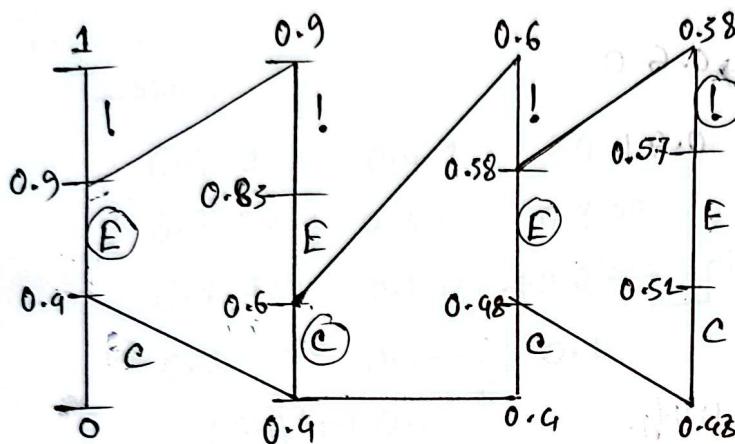
$$= 0.81611$$

## Arithmetic decoding:

Decode message 0.572, given the coding model

$$p(c) = 0.9, p(e) = 0.5, p(!) = 0.1$$

Ans:



$$(px1.0) + (px1.0) + (ex0.0) + (ex0.0) + (ix0.0) =$$

length of S.R =

$$(1)_{(0.9)} \times 1.0 + \dots + (1)_{(0.0)} \times 0.0 =$$

$$(1)_{(0.9)} \times 1.0 + \dots + (1)_{(0.0)} \times 0.0 =$$

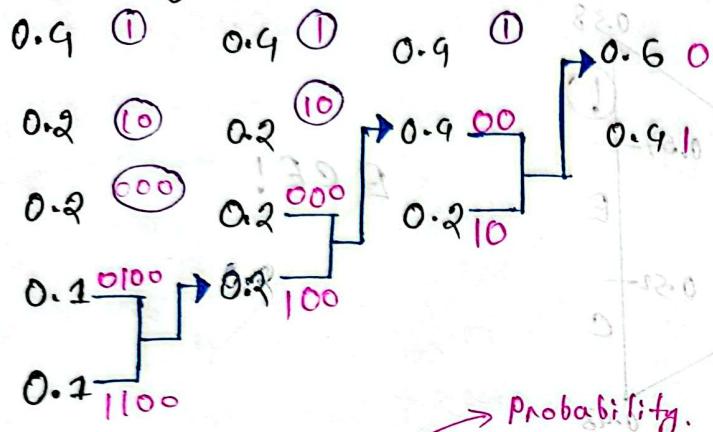
1.000

$$\frac{1}{1} = 1 \text{ (approx)}$$

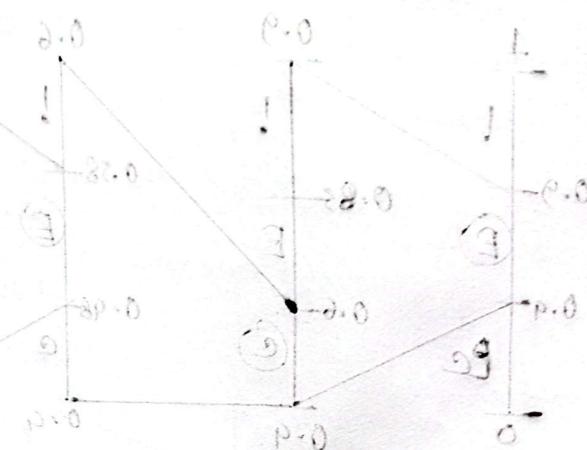
$$\frac{1.000}{1.000}$$

## Huffman Coding:

Symbol →  $S_0, S_1, S_2, S_3, S_4$  } Sort them in decreasing  
 Probability → 0.9 0.2 0.2 0.1 0.1 } order if they are not.



→ Probability.



$$\text{Length, } L_i = \sum_{i=1}^n p_i(L)$$

$$\begin{aligned}
 &= (0.9 \times 1) + (0.2 \times 2) + (0.2 \times 3) + (0.1 \times 4) + (0.1 \times 4) \\
 &= 2.2 \text{ bits/pixel.}
 \end{aligned}$$

$$\text{Entropy } (\mu) = \sum_{i=1}^m p_i \log_2 \left( \frac{1}{p_i} \right)$$

$$\begin{aligned}
 &= 0.9 \times \log_2 \left( \frac{1}{0.9} \right) + \dots + 0.1 \times \log_2 \left( \frac{1}{0.1} \right) \\
 &= 2.121
 \end{aligned}$$

$$\text{Efficiency, } \eta = \frac{\mu}{L_i}$$

$$= \frac{2.121}{2.2}$$

$$= 0.96$$

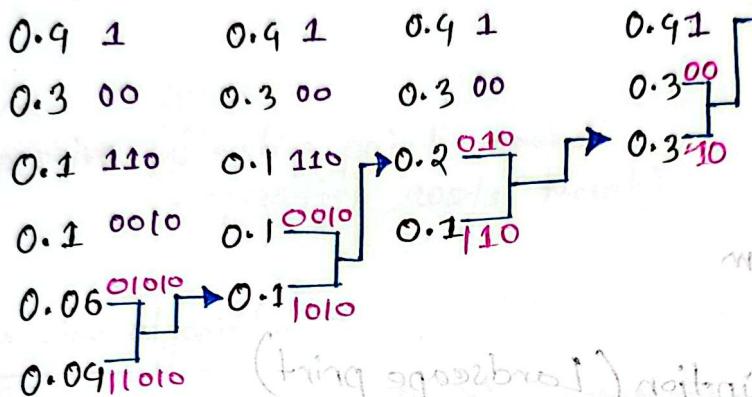
$$\text{Redundancy, } (Y) = 1 - \eta$$

DGI (Digital Gray Image)

$$= 1 - 0.96$$

$$= 0.04$$

Symbol      Probability

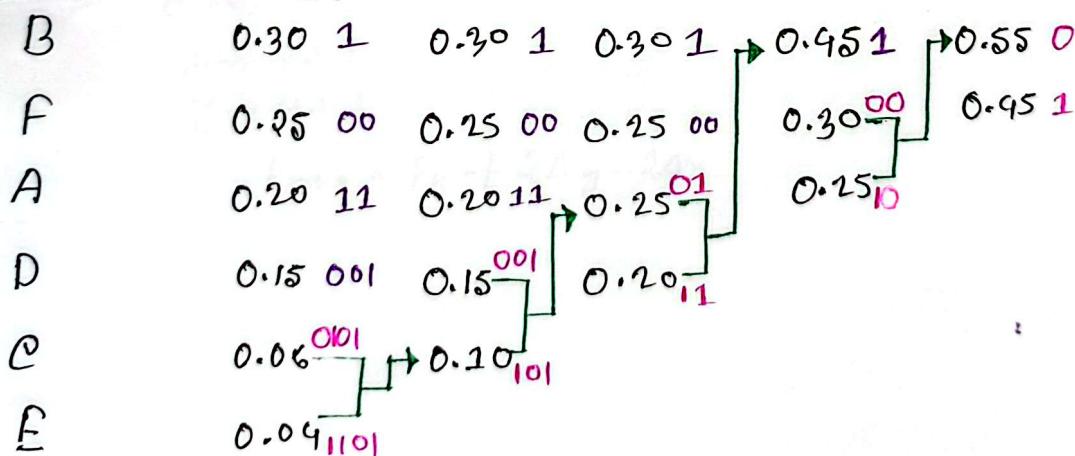


$$L_{avg} = (0.9 \times 1) + (0.3 \times 2) + (0.1 \times 3) + (0.1 \times 4) + (0.06 \times 5)$$

+ (0.09 \times 5)

$$= 2.2 \text{ bits/pixel. } \approx 3 \text{ bits/pixel.}$$

Symbol      Probability



$$L_{avg} = (0.30 \times 1) + (0.25 \times 2) + (0.20 \times 3) + (0.15 \times 3) + (0.06 \times 4)$$

$$+ (0.09 \times 4)$$

$$= 2.05 \text{ bits/pixel.}$$

# DCT → Discrete Cosine Transformation:

## CGIPLab (report guideline)

Front page

Report title

Objective

Necessary tools

Description

Algorithm

Pseudocode

Activity diagram

Source code

Output description (Landscape print)

Result (explanation) (Calculation)

Limitation of code

Conclusion: Problem faced.

Conclusion: Analysis done

Reference (IEEE format)

①

DDA

0 20.0 420.0 100.0 100.0 100.0

1 20.0 0 20.0 0 20.0 0 30.0

2 20.0 100.0 100.0 100.0 100.0

3 20.0 100.0 100.0 100.0 100.0

4 20.0 100.0 100.0 100.0 100.0

5 20.0

(px20.0) + (ex21.0) + (ex22.0) + (px23.0) + (ex24.0) = pva  
(px20.0) +

done / std 20.0 =

1. Choice (CMY-HSI) / HSI-CMY / RGB-HSI / RGB-CMY
2. You have chosen this one ---- (3108) (0105)
3. Enter the CMY values
4. HSI will be [HSI] - PE A (01008) → (01-81) 8 = 01 → 8x8 = 8

DDA line draw (0105)  
 ↳ expensive (floating point, round operation costs much)

Deriving (3108)  
Bresenham line algorithm:

Decision parameter - (P) - decides upper or lower pixel.

initializing (pixel at start)

$$P_0 = S_p + S_e$$

$P \rightarrow$  minus < 0  
 $x \rightarrow x+1$   
 $y \rightarrow$  unchanged

$$P_{k+1} = P_k + 2\Delta y$$

else (thickness, pixel size) improved now b/w if  
 $x \rightarrow x+1$   
 $y \rightarrow y+1$

$$P_{k+2} = P_k + 2\Delta y - 2\Delta x$$

examples, stories bring-bit a  
 of expanding radius, iteration of

bottom  
boundary  
and fit

(10) computer graphics  
 P.S. digital I/O's

two endpoints,

$$(20, 10) \quad (30, 18)$$

$$P_0 = 2\Delta y - \Delta x$$

$$= 2(18 - 10) - (30 - 20)$$

$$= 2 \times 8 - 10$$

$$= 6$$

$$(20, 10)$$

$$P_0 = 6 \rightarrow (21, 11)$$

$$P_1 = 2 \rightarrow (22, 12)$$

$$P_2 = -2 \rightarrow (23, 12)$$

$$P_3 = 14 \rightarrow (24, 13)$$

$$P_4 = 10 \rightarrow (25, 14)$$

$$(26, 15)$$

$$(27, 16)$$

$$(28, 16)$$

$$(29, 17)$$

$$(30, 18)$$

### Circle drawing algorithm:

$$x^2 + y^2 = r^2$$

circle — 8 way symmetric.

ellipse — 16 way symmetric

\* Eight-way symmetry: (necessity — requires less computation time)

### Mid-point circle algorithm.

Initial decision parameter —  $P_0$ .

Circle Plot starting  $(0, n)$

CGP-Graphics: 2.9

Question :-

notice quadrant if there

\* Midpoint Ellipse Algorithm → ~~more info~~

\* Polygon filling:

i) Boundary fill algorithm ii)

\* C-Curve: break in  $90^\circ$

\* Koch-curve:

break middle part in  $60^\circ$

\* The Sierpinsky Gasket

\* Area filling algorithm.

→ Boundary fill → uses stack.

    → 4-connected → problem (can't color fully some structure)

    → 8-connected

Solves this problem.

→ Flood fill (color diff.

whereas same in boundary fill)

\* Aliasing and Anti-aliasing problems: ~~without memory~~

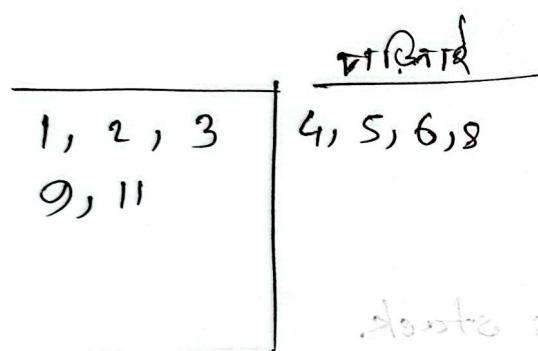
(pixel-breaking)

\* Unequal brightness  $\Rightarrow$  aliasing problem  $\Rightarrow$   $16^\circ$ ,

~~anti-aliasing solution D~~

- Unweighted filtering
- Super-sampling.
- Character display.
  - ↳ Bitmap font
  - ↳ Outline font.

## Picket fence problem: (definition)



Chapter 9, 5. (two dimension)  
6, 8 (three dimension)

## Chapter Four:

⇒ What is transformation?

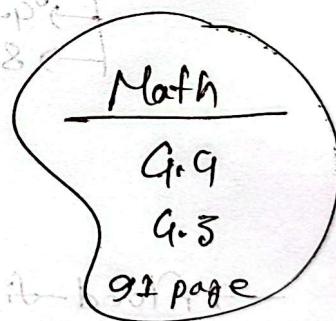
⇒ Translation.

figure: 9.2

⇒ Rotation.

⇒ Scaling.

⇒ Mirror reflection.



## 9.2 Composite transformation

(sum up of  
previous points)

⇒ Instance transformation.