

Basic Data Structures

1. Array
2. String
3. Stack
4. Queue
5. Linked List

Array, Records, Pointers

AI-1 Array Traversing

LA :- Linear Array, lower bound LB, up. b. UB

1. Initialize Set $K = LB$ $K \leq UB$
2. Repeat step 3. and 4. while
3. Apply Process to $LA[K]$
4. Set $K = K + 1$
End of Step 2 loop
5. End.

Insert And Delete

length

Al-2 Insert ($LA, N, k, ITEM$)
 $\rightarrow k \leq N$ position of item.

1. Set $j = N$.
2. Repeat Step 3 and 4 with j, k .
3. [Move j th element] Set $LA[j+1] = LA[j]$
Set $j = j-1$
- 4.
5. Insert element $LN[k] = ITEM$.
6. Set $N = N+1$
7. EXIT

Time complexity

AL-3 Delete (LA, N, k, ~~Item~~)

1. Set Item = LA[k]

2 Repeat for $j = k$ to $N-1$;

Set LA[j] = LA[j+1]

End of loop

3. Set $N = N-1$

4. Exit.

Linked List → Dynamically Allocated
→ Size can be vary at run time.

Diff between Array
and Linked List

Li. Array

- Deletion and insertion are difficult
- insertion requires data movement
- space wasted
- can not be reduced to rearrangement
- To avoid each element same time is required.
- consecutive memory location
- we can reach there directly

linked List

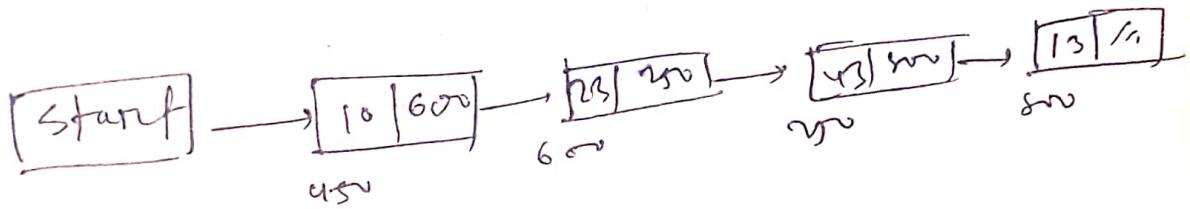
- easy
- don't
- not
- can
- different time
- may or not
- to reach particular node, you need to go through all those nodes that come before that node

Q) Why linked list is better?

- It is relatively expensive to insert and delete elements in an array. Since an array usually occupies a block of memory space, one cannot simply double or triple the size of an array when additional space is required. On the other hand, in a linked list, in memory each element contains a link or pointer which contains the address of the next element. Thus successive elements in the list need not occupy adjacent space in memory. This will make it easier to insert or delete elements in the list.

Single Linked List

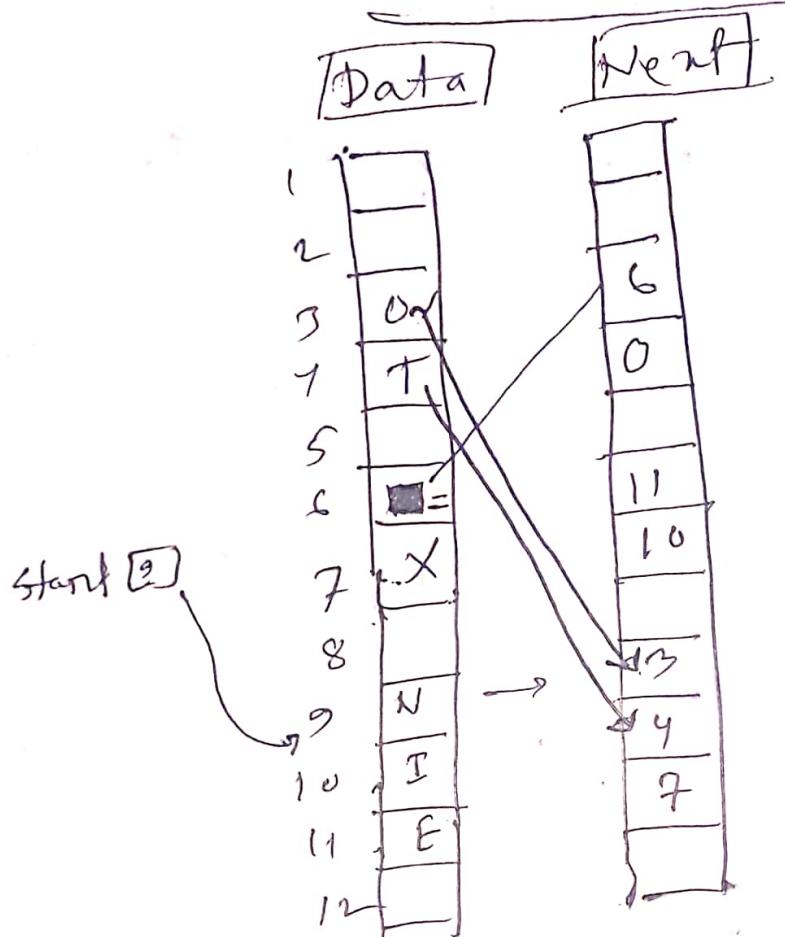
info | link



implementation of single linked list

```
struct node {  
    type1 member1;  
    type2 member2;  
    struct node *link;  
};
```

Representation of linked list in a memory



Here, $\text{start} = 9$; $\text{Data}[9] = 'N'$ is the 1st character.
 $\text{Next}[9] = 3$
 $\text{Next}[3] = 6$
 $\text{Next}[6] = 11$
 $\text{Next}[11] = 7$
 $\text{Next}[7] = 10$
 $\text{Next}[10] = 4$
 $\text{Next}[4] = 0$, Null value, list has ended.

$\text{Data}[0] = 'O'$ is the 2nd character.
 $\text{Data}[6] = '='$ is the 3rd character.
 $\text{Data}[11] = 'E'$ is the 7th character.
 $\text{Data}[7] = 'X'$ is the 8th character.
 $\text{Data}[10] = 'T'$ is the 6th character.
 $\text{Data}[4] = 't'$ is the 3rd character.

Traversing a linked list

1. Set PTR = START.

2. while PTR \neq NULL

 ① Apply process to Info [PTR]

 ② Set PTR = Link [PTR] (PTR now points to next)

End of loop

3. End.

Print

1. Set PTR = start.

2. while PTR \neq null

 ① write Info [PTR]

 ② Set PTR = Link [PTR]

End of loop,

3. End.

Searching

unsorted list

1. Set PTR = START.

2. while PTR \neq NULL

 ① If item = INFO[PTR], then
 set LOC = PTR, and exit.

 ② Else, set PTR = LINK[PTR]

 end of loop.

3. (search is unsuccessful) set LOC = NULL

4. Exit.

Overflow and Underflow.

AVAIL = NULL and

→ Overflow: when there is an insertion

→ Underflow: when START = NULL,
there is a deletion.

Sorted List

1. Set PTR = START
2. while PTR ≠ NULL
 if item = info[PTR],
 Set loc = PTR, and exit.
 Set loc = PTR, and exit.
 Else if item < info[PTR].
 Set PTR = link[PTR]
 Else set loc = NULL and exit
3. Set loc = NULL.
4. Exit.

Insertion

$$f: \mathbb{C}^d \rightarrow \mathbb{C}^{(1)}$$

↓ ↓ ↓ ↓
Insertion in the empty list at the end between the list nodes

~~Schweck~~

1. Inserting at the beginning of the list

Ins FIRST (INFO, Link, statct, avail, Item)

1. If $avail = nuk$, write: overflow and exit

1. If $\text{avail} = \emptyset$
2. [Remove first node from $\text{avail} \rightarrow$]

3. ~~Set Info[men]~~ =
Set men = Avail and Avail = link[men]

3. `leftInfo[New] = leftItem`
 \Rightarrow `l = start`

3. Set $in[0] =$
 $link[0] = start$

4. Set unk to start = new.

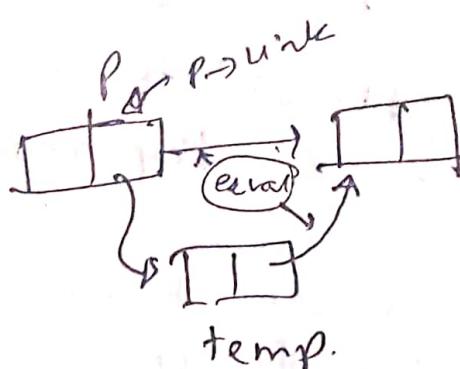
5. set start = new

6. Ent.

2 Inserting after a given node

1. If avail = null, write: overflow, exit
2. (Remove first node from avail list)
Set New = Avail, Avail = Link(Avail)
3. Set Info[New] = item
4. If loc = null.
 - (a) Set Link[New] = start
 - (b) Set start = New
 else,
 - (a) Set Link[New] = Link[loc]
 - (b) Link[loc] = New

5. Exit



$$\begin{cases} \text{temp} \rightarrow \text{link} = \\ p \rightarrow \text{link} \\ p \rightarrow \text{link} = \text{temp} \end{cases}$$

inserting into a sorted linked list.

2 → 5 → 7 → 10 → 15

insert 9 = 2 → 5 → 9 → 7 → 10 → 15

Algorithm:

- ① If linked list is empty then make the node as head and return it.
- ② If the value of the node to be inserted is smaller than the value of the head node, then insert the node at the start and make it head.
- ③ In a loop, find the appropriate node after ~~the~~ which the input node (9) is to be inserted. To find the appropriate node start from the head, keep moving until you reach a node hn (10 in the diagram). The node before hn is (7).
- ④ Insert the node (9) after the appropriate node (7).

Deleting

To delete a node from the linked list, we need to do following steps.

- ① find the previous node of the node to be deleted.
 - ② change the next of the previous node and set $\text{prev_node} \rightarrow \text{next}$
= $\text{node}_{\text{to_delete}} \rightarrow \text{next}$
 - ③ free the memory of the node to be deleted.

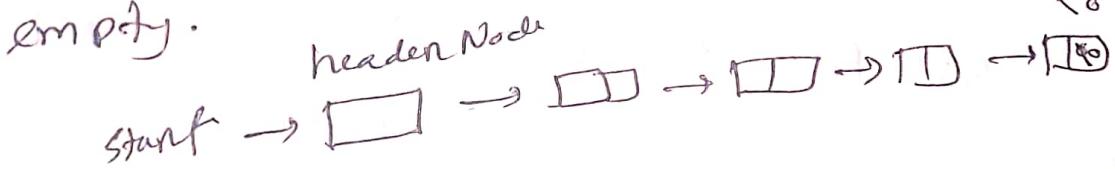
time complexity $O(n)$

Header linked list

① Grounded Header linked list

It is a list whose last node contains the null pointer. In the header linked list, the start pointer always points to the header node.

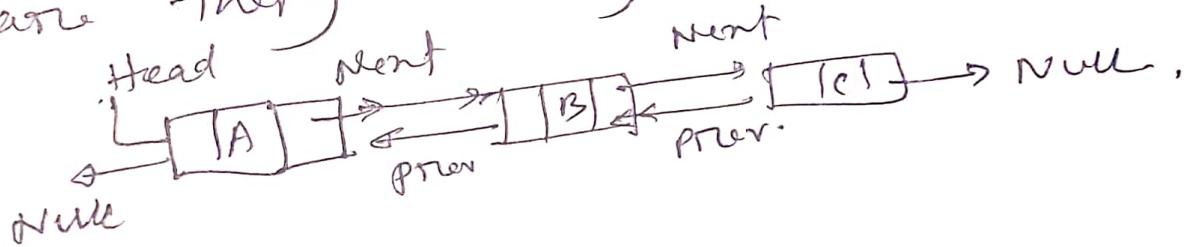
$\text{start} \rightarrow \text{next} = \text{NULL}$ indicates that the grounded header linked list is empty.



② circular
last node b points back to the header node.

Two way linked list

A ~~dot~~ doubly linked list contains an extra point, typically called previous pointers together with next pointers and data which are there in singly linked list.



Sub: Mainly used on laptop
Data and it is also removed
Stacks, Queue, Recursion

back button

Time Date: / /

- Stacks follow LIFO (last in first out)
- Abstract datatypes containing element in linear order.
- Operations are allowed only at the ends.
- Insertion, deletion allowed only one end.
- last in first out.

push operation

push (stack, TOP, MAXSTK, ITEM)

① if TOP = SIZE, print: overflow and return

② set TOP = TOP + 1

③ set stack [TOP] = ITEM

④ Return.

pop (stack, TOP, ITEM)

① if TOP = 0, print underflow and return

② set ITEM = STACK [TOP]

③ set TOP = TOP - 1

④ Return.

Use of Stack

Polish notation

1924, ¹⁹²⁴ Polish mathematician Jan Lukasiewicz

* Infix $P + Q \wedge R + S * T / (u - v)$

$$\begin{aligned}
 \text{infix} \rightarrow \text{prefix} &= P + \underline{Q \wedge R} + S * T / E - u v \\
 &= P + [\underline{Q R}] + \underline{S * T} / E - u v \\
 &= P + [\wedge Q R] + [\underline{* S T}] / E - u v \\
 &= + [P \wedge Q R] + [\vee * S T - u v] \\
 &= + + P \wedge Q R / * S T - u v
 \end{aligned}$$

→ Postfix $P + \underline{Q^1 R} + \underline{S * T / (u-v)}$

$$= P + [Q R^1] + [S T *] / [u v -]$$

$$= [P Q R^1 +] + [S T * u v -].$$

$$= P Q R^1 + S T * u v - / + .$$

postfix \rightarrow Infix

$$\underline{P Q R^1} + \underline{S T * u v - / +}$$

$$= \underline{P} \underline{Q^1 R} + \underline{S T * T} (u-v) / +$$

$$= \underline{P + Q^1 R} \underline{S * T / u - v} +$$

$$= P + Q^1 R + S * T / u - v .$$

prefix \rightarrow Infix

$$+ + P \underline{Q^1 R} / \underline{S T - u v} .$$

$$= + + \underline{P} \underline{Q^1 R} / \underline{S * T} (u-v)$$

$$= + \underline{P + Q^1 R} \underline{S * T / u - v} .$$

$$= P + Q^1 R + S * T / u - v .$$

An.

Postfix \rightarrow Prefix

$$\begin{aligned}
 & \underbrace{P \cdot Q \cdot R}_{\uparrow} + \underbrace{S \cdot T}_{\uparrow} \cdot \underbrace{U \cdot V}_{\uparrow} - / + \\
 & = \underbrace{P \cdot \underbrace{Q \cdot R}_{\uparrow}}_{\uparrow} + \underbrace{S \cdot T}_{\uparrow} \cdot \underbrace{U \cdot V}_{\uparrow} - / + \\
 & = \underbrace{+ \cdot P \cdot Q \cdot R}_{\uparrow} / \underbrace{+ S \cdot T \cdot U \cdot V}_{\uparrow} - + \\
 & = + + P \cdot Q \cdot R / + S \cdot T \cdot U \cdot V - .
 \end{aligned}$$

prefix \rightarrow postfix $+ + P \cdot Q \cdot R / + S \cdot T \cdot U \cdot V -$

$$\begin{aligned}
 & = + + \underbrace{P \cdot Q \cdot R}_{\uparrow} / \underbrace{S \cdot T \cdot U \cdot V}_{\uparrow} - \\
 & = + \underbrace{P \cdot Q \cdot R}_{\uparrow} + \underbrace{S \cdot T \cdot U \cdot V}_{\uparrow} - / \\
 & = P \cdot Q \cdot R + S \cdot T \cdot U \cdot V - / + \\
 & = \dots
 \end{aligned}$$

Evaluating Postfix Expression using Stack

Steps:

1. Create a stack to store operands
2. Scan the given expression and the
 - ① If the element is number, push it into the stack
 - ② If the element is an operator, pop operands for the operator from the stack. Evaluate the operation and the push the result back to the stack
 - ③ When stack is empty, the result is obtained

Example:

Let the given expression be $231 * 9 - 5$

① Scan '2' \rightarrow push.

②. '3' \rightarrow push, '23'.

③. '1' \rightarrow '231'

④ ' * ' \rightarrow pop, 3, 1, $2 * 3$ again push. stack '23'

⑤ ' + ' \rightarrow pop 2, 3. $2 + 3 = 5$ push - stack '5'

⑥ '9' \rightarrow push, '59'.

⑦ ' - ' \rightarrow pop '59' $5 - 9 = -4$. Ans.

Infix to Postfix conversion

Step-0 Tokenize the infix expression, i.e. store each element of an infix expression into a list

Step 1: If operand (number) \rightarrow add it to postfix.

Step-2: If left paren. "(" \rightarrow push it on the stack.

Step 3: Right parn ")" , pop out and add to postfix all operators till first parenthesis. Discard both left and right parn.

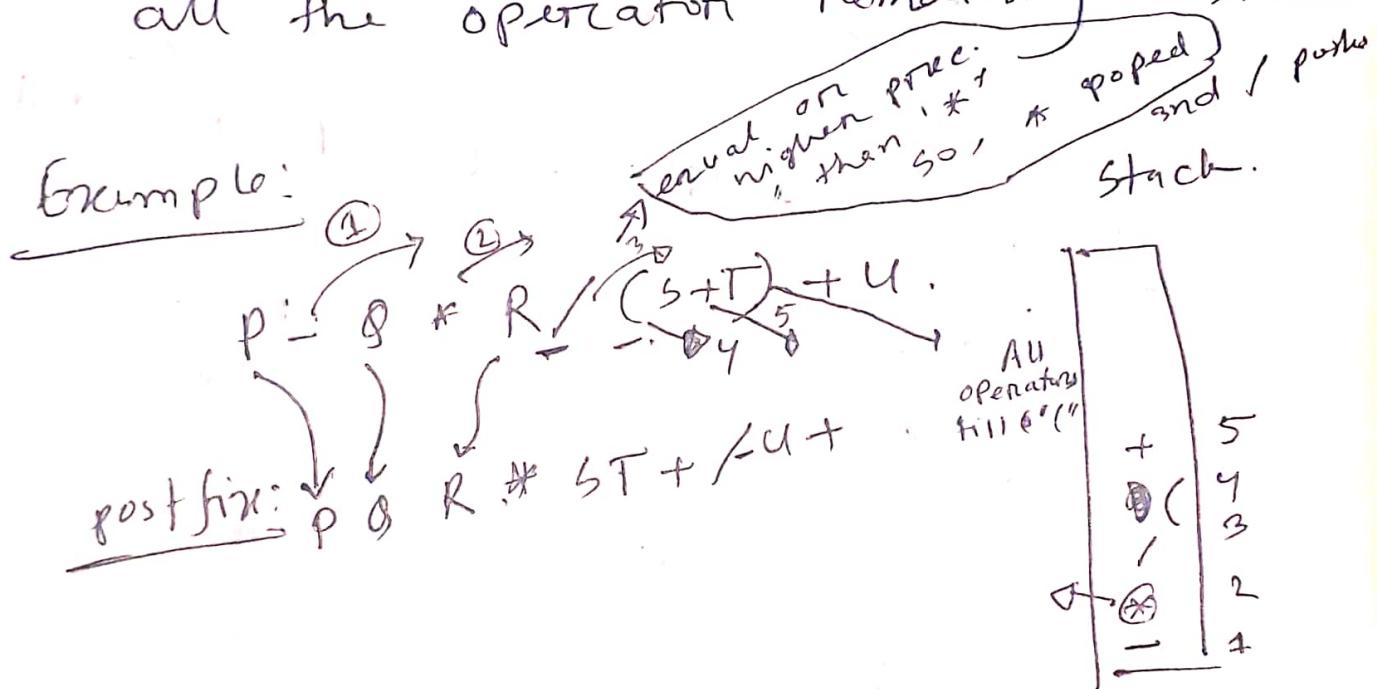
Step-4: If an operator, pop and add to postfix these operators that have higher or equal precedence than the scanned operator.

\hookrightarrow push the scanned symbol on the stack.

Step-5 If the token is an operator

After scanning all the symbol of infix. pop and add to postfix. all the operator remaining on stack

Example:

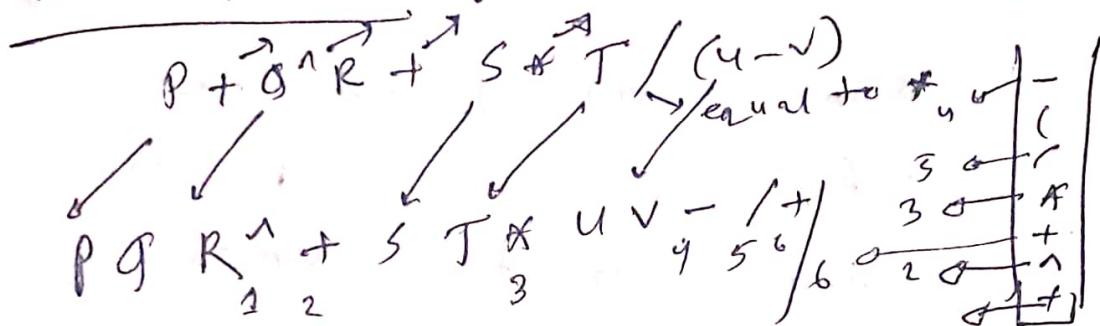


stack puts
higher on causal.
precedence
on top
doesn't allow
P allow
lower precedence

Sub:

Date:

Example-2



Example-3

$$A + (B * C - (D / E^F) * G) * H$$

poped '*'

infix	stack	postfix
A		A
+	+	A
(+ C	.A
B	+ C	AB
*	+ C *	AB
C	+ C *	AB C *
-	+ C -	AB C *
(+ C - (AB C *
D	+ C - (/	AB C * D
)	+ C - (/	AB C * D

infix	stack	postfix
E	+(-C/	ABC*DE
^	+(-C/)^	ABC^DE
F	+(-C/)^	ABC*DEF
)	+(-)	ABC*DEF^)
*	+(-#	ABC*DEF^*)
^	+(-#	ABC*DEF^*)^
)	+	ABC*DEF^*)^ -
A	+ #	ABC*DEF^*)^#
H	+ #	ABC*DEF^*)^# - H
		ABC*DEF^*)^# - H #

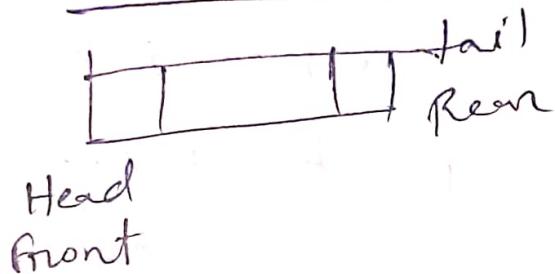
Ans.

Sub:

ADD \rightarrow last (Rear)
remove \rightarrow first (front)

Date: / /
Time: / /

Queue:



FIFO
first in
first out

Algorithm: insert
En Queue: (Queue, n, front, Rear, Item)

1. [Queue already filled ?]
If front = 1 and Rear = N, or if
FRONT = REAR + 1, then write overflow
2. [Find of Rear]
If front = Null, then set front = 1, Rear = 1
Else if Rear = N, then set Rear = 1
Else Rear = Rear + 1;
(End of if structure)
3. Set Queue [Rear] = item.
4. Return.

Insertion complexity
 $O(1)$

Deletion

Delete (Queue, N, front, Rear, item)

1. [Queue already empty?]

if front = null, then: Underflow

2. Set item = Queue[front]

3. front = front + 1;
(Find the new value of front)

if front = Rear,

Set front = null, Rear = null.

Else if front = N,

Set front = 1

Else, Set front = front + 1

deletion complexity

$\delta(n)$

Sub:

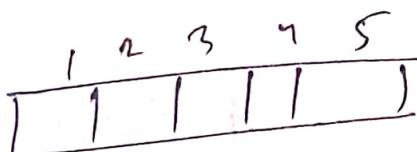
Day				
Name:		Date:	/ /	

Example:

① Initially empty:

front = 0

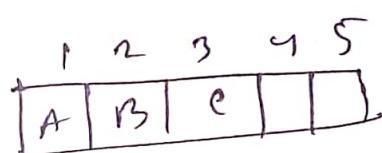
rear = 0



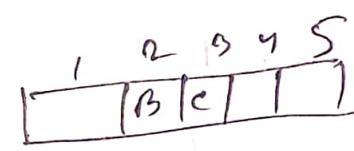
② A, B, C inserted

front 1

rear 3

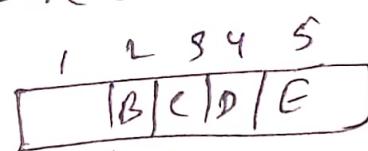


③ A deleted (dequeue)



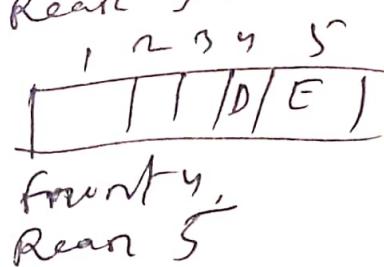
front 2
rear 3

④ D, E inserted (enqueue)



front 2
rear 5

⑤ B, D, E deleted



front 4
rear 5

⑥ F inserted



front 4
rear 1

Sub:

Day

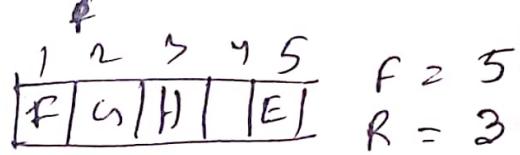
Time:

Date: / /

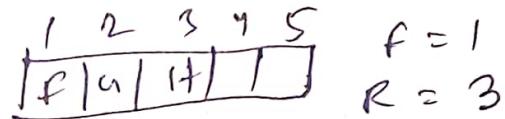
7. D deleted



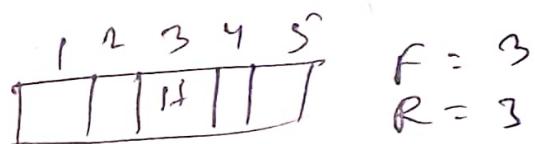
8. G, H inserted



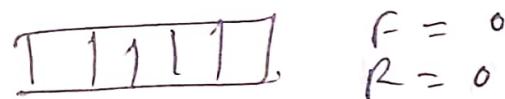
9. E deleted



10. F, G deleted



11. D, H in



→