

Ch-7

MTBF - mean-time between failure

MTBF $\rightarrow \infty$; SW availability $\rightarrow 100\%$

MTBF $\rightarrow 0$; " " $\rightarrow 0\%$

never fails

- code contains faults
but that part is
never executed

fails every time

\rightarrow may have only
1 fault

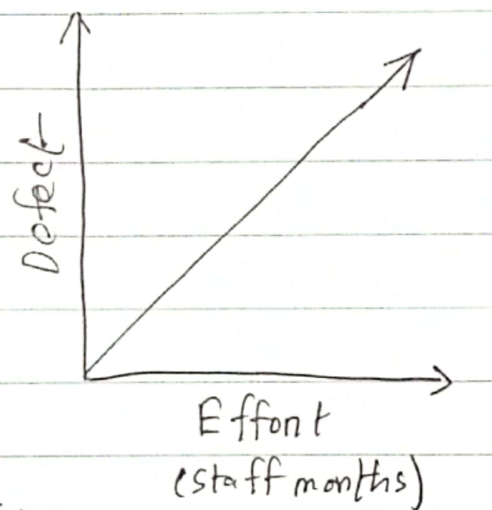
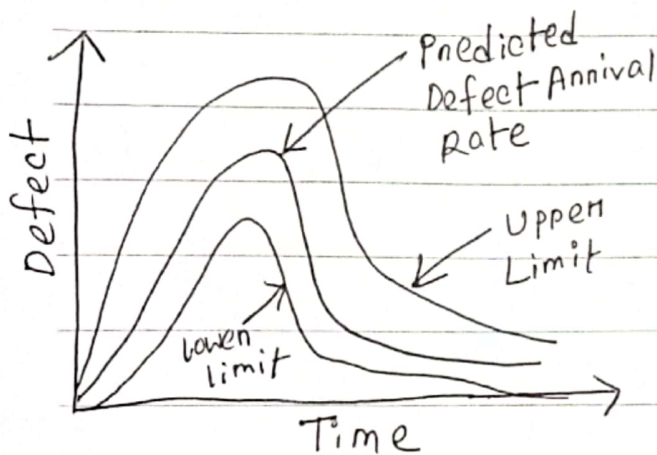


Fig: Defect arrival rates

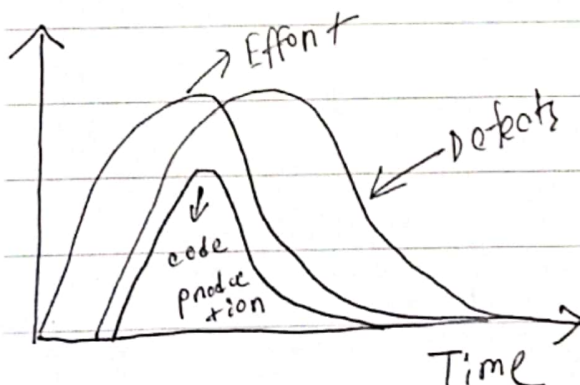


Fig: Defect vs staffing

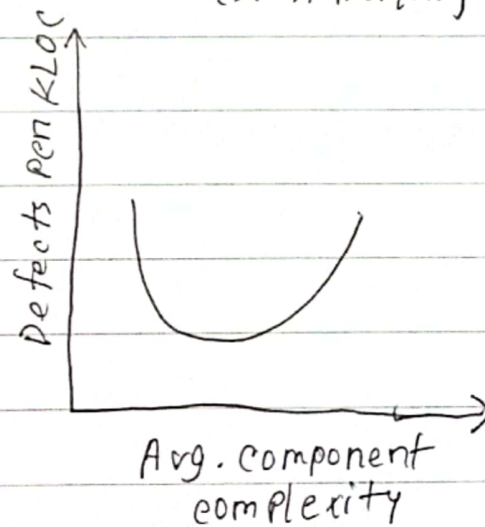
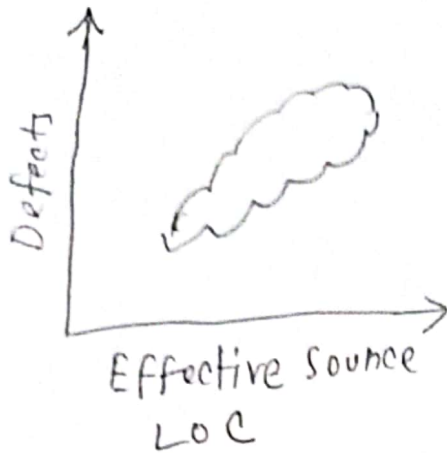
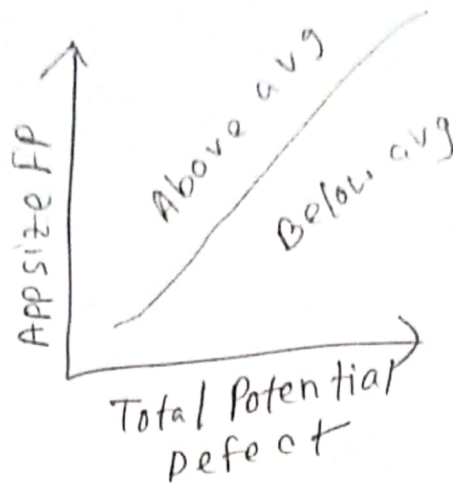


Fig: Bathtub chart



→ Defect Density
vs system size



→ Defect vs FP

* 2 distributed function:

→ 1) PDF (Probability distribution ^{ion} ~~st~~ function)
→ defect arrival $f(t)$

2) CDF (Cumulative distribution function)

$$F(t) = \frac{\text{total no. of defects to arrive}}{\text{time}}$$

$$= \frac{f(t)}{t} = \frac{d}{dt} f(t)$$

$$f(t) = m(t/c)^{m-1} e^{-(t/c)^m} / t$$

$$F(t) = 1 - e^{-(t/c)^m}$$

Exponential: $m = 1$ } Rayleigh: $m = 2$

Hence, $c = \sqrt{2} t_m$

$t_m \rightarrow t$ at which $f(t) = \max$

$$f(t) = K \left[(1/t_m)^{\sim} t e^{-(1/2 t_m^{\sim}) t^{\sim}} \right]$$

$$F(t) = K \left[1 - e^{-(1/2 t_m^{\sim}) t^{\sim}} \right]$$

Ex: week	1	2	3	4	5	6	7	8	9
Defects	20	41	48	52	62	59	52	44	33

40% (pointing to week 5)

$t_m = 5$, total no. of defects,

$$K = \frac{20 + 41 + 48 + 52 + 62}{0.4} \approx 557$$

$$\therefore f(t) = 557 \left[(1/5)^{\sim} t e^{-(1/50) t^{\sim}} \right]$$

$$= 557 \left[(t/25) e^{-(t^{\sim}/50)} \right]$$

$$F(t) = 557 \left[1 - e^{-(t^{\sim}/50)} \right]$$

Method 2: $f(1) = 20$, $t = 1$, $t_m = 5$

$$20 = K \left[(1/25) e^{-(1/50)} \right]$$

$$\rightarrow 20 \times 25 = K e^{-(1/50)}$$

$$\rightarrow 500 = \frac{k}{e^{1/50}}$$

$$\therefore k = 510$$

$$\therefore f(t) = 510 \left[(t/25) e^{-(t/25)^2} \right]$$

$$= 20.4 t e^{-(t^2/50)}$$

$$F(t) = 510 \left[1 - e^{-(t^2/50)} \right]$$

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(b) You're now in system test for technovent website. Assume a neleigh curve.

Month	1	2	<u>3</u>	4	5	6
Defect	13	22	<u>25</u>	22	17	5

$$i) f(t) = k * \left[2(t/c^2) e^{-(t/c)^2} \right] ; c = \sqrt{2} t_m$$

$$= k * \left[2(t/2t_m^2) e^{-(t^2/2t_m^2)} \right]$$

$$\text{Hence, } t_m = 3, k = \frac{13+22+25}{0.33} = 181.82$$

$$\therefore f(t) = 181 \left[2(t/18) e^{-(t^2/18)} \right]$$

$$= \frac{1801}{9} t e^{-(t^2/18)}$$

$$F(t) = 181 \left[1 - e^{-(t^2/18)} \right]$$

① End of month 3:

Defect removal efficiency =

$$\frac{\text{no. of defects resolved}}{\text{total no. of defects}}$$

$$= \frac{13 + 22 + 25}{13 + 22 + 25 + 22 + 17 + 5}$$

$$= 57.7\%$$

↳ DRE → Defect Removal Efficiency

$$DRE = \frac{E}{E + D}$$

E → no. of defects found before delivery

D → " " " after " "