

Lecture-1

Monday

DAY:

TIME:

DATE: 7 / 8 / 23

Salim
Sir

TOPIC NAME: Equation Solving Method

$$\# \quad 27x + 6y - z = 85$$

$$6x + 15y + 2z = 72$$

$$x + y + 54z = 110$$

$$D = \begin{bmatrix} 27 & 6 & -1 \\ 6 & 15 & 2 \\ 1 & 1 & 54 \end{bmatrix} = 19893$$

$$D_x = \begin{bmatrix} 85 & 6 & -1 \\ 72 & 15 & 2 \\ 110 & 1 & 54 \end{bmatrix} = 48250$$

$$D_y = \begin{bmatrix} 27 & 85 & -1 \\ 6 & 72 & 2 \\ 1 & 110 & 54 \end{bmatrix} = 71078$$

$$D_2 = \begin{bmatrix} 27 & 6 & 85 \\ 6 & 15 & 72 \\ 1 & 1 & 110 \end{bmatrix} = 38313$$

$$x = \frac{D_x}{D}$$

$$= 2.425$$

$$y = \frac{D_y}{D}$$

$$= 3.573$$

$$z = \frac{D_2}{D}$$

$$= 1.925$$

1-211029

Topic Name:

badiam pmt 03 with 03

DAY:

TIME:

DATE:

Gauss-Seidel iteration method: $\begin{cases} 5x + 3y + z = 85 \\ 3x + 5y + z = 72 \\ x + y + 5z = 110 \end{cases}$ First iteration:

$$x = \frac{1}{27} (85 - 6y - z) \quad \text{--- (i)}$$

$$y = \frac{1}{15} (72 - 6x - 2z) \quad \text{--- (ii)}$$

$$z = \frac{1}{54} (110 - x - y) \quad \text{--- (iii)}$$

Put $y=0, z=0$ in (i)

$$x = \frac{85}{27} = 3.148 = x^{(1)} = \text{First approximation}$$

put $x=3.148, z=0$ in (ii)

$$y = \frac{1}{15} (72 - 6 \times 3.148 - 2 \times 0) = 3.54 = y^{(1)} = \text{First approximation}$$

put $x=3.148, y=3.54$ in (iii)

$$z = \frac{1}{54} (110 - 3.148 - 3.54) = 1.91 = z^{(1)} = \text{First approximation}$$

TOPIC NAME:

DAY:

TIME:

DATE: / /

Second Iteration:

$$x^{(2)} = \frac{1}{27} (85 - 6y^{(1)} + z^{(1)}) = 2.43$$

$$y^{(2)} = \frac{1}{15} (72 - 6x^{(2)} - 2z^{(1)}) = 3.57$$

$$z^{(2)} = \frac{1}{54} (110 - 6y^{(2)} - z^{(2)}) = 1.92$$

} Second
approximation

Third Iteration:

$$x^{(3)} = \frac{1}{27} (85 - 6y^{(2)} + z^{(2)}) = 2.426$$

$$y^{(3)} = \frac{1}{15} (72 - 6x^{(3)} - 2z^{(2)}) = 3.57$$

$$z^{(3)} = \frac{1}{54} (110 - 6y^{(3)} - z^{(3)}) = 1.926$$

* Iteration କେବଳ ୩ ଟଙ୍କାମେ steps, କାହାରୁ

-ଥାରିଲେ minimum 3-step's

* Error କେବଳ ୩ଟଙ୍କାମେ 1st, 2nd ଓ 3rd ଏବଂ

ମାତ୍ର ଦିନ୍ୟେ ଯାହାର କେବଳ ୨୦୫ ଟଙ୍କାମେ

* Point ଏବଂ ପର ଟାଙ୍କା କେବଳ ମାତ୍ର ଦିନ୍ୟେ ୨୦୦, କାହାରୁ

-ଥାରିଲେ ।

Salim Sir

Numerical Integration

Simpson's One Third Rule

Lecture-2

DAY: Monday

TIME:

DATE: 14/8

Solve integration:

$$\int_{4}^{5.2} \log x \, dx = (11.8 + 10.1 + 8.9) \frac{1}{3} - 8x$$

$$\int \log x \, dx = \log x \int 1 \, dx - \int \left\{ \frac{d}{dx} \log x \int 1 \, dx \right\} \, dx$$

$$\begin{aligned} \int_{4}^{5.2} \log x \, dx &= x \log x - \int \frac{1}{x} x \, dx \\ &= x \log x - \int 1 \, dx \end{aligned}$$

$$= x \log x - x \quad \text{Hence, } b = 5.2, a = 4$$

$$\int_{4}^{5.2} \log x = [x \log x - x]_{4}^{5.2}$$

$$= (5.2 \log 5.2 - 5.2) - (4 \log 4 - 4)$$

Step $n = \frac{\text{Upper limit} - \text{Lower limit}}{n}$

$n = \frac{5.2 - 4}{10} = 0.12$

* n এবং Δx এর মুক্তি করে নির্ণয় করা হবে।

অন্যান্য ।

GOOD LUCK

Engineering

Project

TOPIC NAME:

LAST DAY:

TIME:

DATE: / /

Steps: $x_0 = 4 = LL$, $y_0 = \log_e x$

$$x_1 = 4 + 0.2x_0, y_1 = 1.3862$$

$$x_2 = x_0 + 0.2x_1, y_2 = 1.4350$$

$$x_3 = x_0 + 0.2x_2, y_3 = 1.4816$$

$$x_4 = x_0 + 0.2x_3, y_4 = 1.5260$$

$$x_5 = x_0 + 0.2x_4, y_5 = 1.5686$$

$$x_6 = x_0 + 0.2x_5, y_6 = 1.6094$$

$$x_7 = x_0 + 0.2x_6, y_7 = 1.6486$$

$$= UL$$

$$\int_{4.0}^{5.2} \log_e x \, dx = h \left[\frac{1}{2} (y_0 + y_6) + (y_1 + y_2 + y_3 + y_4 + y_5) \right]$$

$$= 1.8271$$

\Rightarrow slide এর নির্ভর কোনো প্রশ্ন নেওয়া + স্বাধীন কোর্স

প্রশ্ন করুন, Next class এ নিখুঁত নির্ভর করে \rightarrow marks থামাও।

\Rightarrow এইসব নির্ভর কোর্স Rule এর Assignment থামাও।
+ যাকি কৌণ্ডী প্রশ্ন

Lecture-3

DAY: Monday

TIME:

DATE: 21/8

TOPIC NAME: Spot Test

⇒ Spot Test: Compute the general equation

→ Trapezoidal

→ Simpson's 1/3 Rule

→ Simpson's 3/8 Rule

Lecture-4

Salim
site

Method of Factorization

From the relation $A = LU$, we get -

$$\begin{bmatrix} 1 & 0 & 0 \\ l_{21} & 1 & 0 \\ l_{31} & l_{32} & 1 \end{bmatrix} \times \begin{bmatrix} U_{11} & U_{12} & U_{13} \\ 0 & U_{22} & U_{23} \\ 0 & 0 & U_{33} \end{bmatrix} = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix}$$

*** Find out the factors of matrix X.

GOOD LUCK™

TOPIC NAME:

DAY: 12

TIME:

DATE: / /

$$\begin{array}{ccc|ccc} 1 & 0 & 0 & U_{11} & U_{12} & U_{13} \\ l_{21} & 1 & 0 & 0 & U_{22} & U_{23} \\ l_{31} & l_{32} & 1 & 0 & 0 & U_{33} \end{array} \quad \begin{array}{l} 1 \times U_{11} + 0 \times 0 + 0 \times 0 = U_{11} = a_{11} - \textcircled{1} \\ 1 \times U_{12} + 0 \times 0 + 0 \times 0 = U_{12} = a_{12} - \textcircled{2} \\ 1 \times U_{13} + 0 \times 0 + 0 \times 0 = U_{13} = a_{13} - \textcircled{3} \end{array}$$

$$\left[\begin{array}{ccc|ccc} 1 & 8 & 9 & U_{11} & U_{12} & U_{13} \\ 8 & 0 & 1 & 0 & 1 & 0 \\ 9 & 1 & 8 & 0 & 0 & 1 \end{array} \right] \quad \begin{array}{l} U_{11} \times l_{21} = a_{21} \\ \Rightarrow l_{21} = \frac{a_{21}}{a_{11}} = \textcircled{4} \end{array}$$

$$U_{12} \times l_{21} + U_{22} = a_{22} - \textcircled{5}$$

$$l_{21} \times U_{13} + U_{23} = a_{23}$$

$$\rightarrow a_{12} \times l_{21} + U_{22} = a_{22} - \textcircled{5}$$

$$\rightarrow l_{21} \times a_{13} + U_{23} = a_{23} - \textcircled{6}$$

$$l_{31} \times U_{11} = a_{31}$$

$$\rightarrow l_{31} = \frac{a_{31}}{a_{11}} - \textcircled{7}$$

$$l_{31} \times U_{12} + l_{32} \times U_{22} = a_{32} - \textcircled{8}$$

$$l_{31} \times U_{13} + l_{32} \times U_{23} + U_{33} = a_{33} - \textcircled{9}$$

Lecture-5

DAY: Monday

TIME:

DATE: 28 / 8

Salim
Sir

TOPIC NAME: Method of Factorization

① #

$$2x + 3y + z = 9$$

②

$$x + 2y + 3z = 6$$

③

$$3x + y + 2z = 8$$

Coefficient matrix

④

$$= \frac{180}{110} = 1.636$$

$$\begin{bmatrix} 2 & 3 & 1 \\ 1 & 2 & 3 \\ 3 & 1 & 2 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 \\ l_{21} & 1 & 0 \\ l_{31} & l_{32} & 1 \end{bmatrix}$$

$$\begin{bmatrix} U_{11} & U_{12} & U_{13} \\ 0 & U_{22} & U_{23} \\ 0 & 0 & U_{33} \end{bmatrix}$$

From the matrix :

$$U_{11} = a_{11} = 2$$

$$U_{12} = a_{12} = 3$$

$$U_{13} = a_{13} = 1$$

$$U_{11} \times l_{21} = a_{21}$$

$$\Rightarrow l_{21} = \frac{1}{2}$$

$$a_{12} \times l_{21} + U_{22} = a_{22}$$

$$\Rightarrow 3 \times \frac{1}{2} + U_{22} = 2$$

$$3l_{21} + U_{22} = 2 \quad \text{--- (i)}$$

$$l_{21} \times a_{31} + U_{23} = a_{23}$$

$$\Rightarrow 3l_{21} + U_{23} = 3 \quad \text{--- (ii)}$$

$$l_{31} = \frac{a_{31}}{a_{11}} = \frac{3}{2}$$

$$l_{31} \times U_{21} + l_{32} \times U_{22} = a_{32}$$

$$\Rightarrow \frac{3}{2} U_{21} + l_{32} \times U_{22} = 1$$

$$\Rightarrow 3U_{21} + 2l_{32} \times U_{22} = 2 \quad \text{--- (iii)}$$

$$l_{31} \times U_{13} + l_{32} \times U_{23} + U_{33} = a_{33}$$

$$l_{31} + l_{32} \times U_{23} + U_{33} = 2 \quad \text{--- (iv)}$$

GOOD LUCK!!

TOPIC NAME:

DAY:

TIME:

DATE:

$$A = \begin{bmatrix} 1 & 0 & 0 \\ \frac{1}{2} & 1 & 0 \\ \frac{3}{2} & -7 & 11 \end{bmatrix} \begin{bmatrix} 2 & 3 & 1 \\ 0 & \frac{1}{2} & \frac{5}{2} \\ 0 & 0 & 18 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = 14 \begin{bmatrix} 9 \\ 6 \\ 8 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 \\ \frac{1}{2} & 1 & 0 \\ \frac{3}{2} & -7 & 11 \end{bmatrix} \begin{bmatrix} y_1 \\ y_2 \\ y_3 \end{bmatrix} = \begin{bmatrix} 9 \\ 6 \\ 8 \end{bmatrix} \Rightarrow \text{Assignment (Factorization method) } \rightarrow \text{class } 9 \text{ math.}$$

$$y_1 = 9$$

$$\frac{y_1}{2} + y_2 = 6$$

$$\frac{3y_1}{2} - 7y_2 + y_3 = 8$$

$$y_1 = 9$$

$$y_2 = \frac{3}{2}$$

$$y_3 = 5$$

Solve.

$$\begin{bmatrix} 2 & 3 & 1 \\ 0 & \frac{1}{2} & \frac{5}{2} \\ 0 & 0 & 18 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = 14 \begin{bmatrix} 9 \\ 6 \\ 8 \end{bmatrix} \Rightarrow \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 9 \\ 6 \\ 8 \end{bmatrix}$$

$$\begin{aligned} 2x + 3y + z &= 9 \\ \frac{y}{2} + \frac{5z}{2} &= \frac{3}{2} \\ \Rightarrow y + 5z &= 3 \end{aligned} \quad \begin{aligned} 18z &= 5 \\ \Rightarrow z &= \frac{5}{18} \\ \Rightarrow y &= \frac{29}{18} \end{aligned} \quad \begin{aligned} x &= \frac{35}{18} \\ &= \frac{1}{2} \end{aligned}$$

$y_{n+1} \approx y_n + h f(x_n, y_n)$

Given, $\frac{dy}{dx} = \frac{y-x}{y+x}$ with $y=1$ for, $x=0$ in five steps. Find y approximation for $x=0.1$ by Euler's method (in five steps).

Soln: Here we want the value at $x=0.1$ from $x=0$ in five steps. So, we breakup the interval 0 to 0.1 into five subintervals by introducing the points x_1, x_2, x_3, x_4, x_5 . Let $h = 0.02$. We shall find the values of y at $x = 0.02, 0.04, 0.06, 0.08$ and 0.1 successively.

$$y_1 = y_0 + h f(x_0, y_0)$$

$$= 1.02$$

$$x_0 = 0, y_0 = 1, h = 0.02$$

$$f(x_0, y_0) = 1 = 1.02$$

$$y_2 = y_1 + h f(x_1, y_1) = 1.02 + 0.02 \times \frac{1.02 - 0.02}{1.02 + 0.02}$$

$$= 1.03923$$

TOPIC NAME:

DAY:

TIME:

DATE: / /

$$Y_3 = Y_2 + h f(x_2, y_2)$$

$dt + dx = dx$

$$= 1.03923 + 0.02 \times \frac{1.03923 - 2 \times 0.02}{1.0392 - 2 \times 0.02} = 1.05751$$

$(\frac{y_2}{x_2} + dx) + (\frac{dy}{dx} + dx) dx = dy$

$$Y_4 = Y_3 + h f(x_3, y_3)$$

$$= 1.05751 + 0.02 \times \frac{1.05751 - 3 \times 0.02}{1.05751 - 3 \times 0.02} = 1.0748$$

$$Y_5 = Y_4 + h f(x_4, y_4)$$

$dt + dx = \frac{10}{x_0}$

$$= 1.0748 + 0.02 \times \frac{1.0748 - 4 \times 0.02}{1.0748 + 4 \times 0.02} = 1.0922$$

Hence $y = 1.0928$ where $x = 0.1$

\Rightarrow Modified Euler's method.

Modified

Spot Test: $7/9/23 \rightarrow$ Euler's method derivation.

$$(y_0 + \frac{dy}{dx} x_0) + 1.0 =$$

$$(y_0 + f(x_0, y_0)) + 1.0 =$$

Salim Sir

Lecture-7

DAY: Monday

TIME:

DATE: 4/9

TOPIC NAME: Runge kutta Method

$$K_1 = hF(x_0, y_0)$$

$$K_2 = hF\left(x_0 + \frac{h}{2}, y_0 + \frac{K_1}{2}\right)$$

$$K_3 = hF\left(x_0 + \frac{h}{2}, y_0 + \frac{K_2}{2}\right)$$

$$K_4 = hF(x_0 + h, y_0 + K_3)$$

$$\Delta y = \frac{1}{6} (K_1 + 2K_2 + 2K_3 + K_4)$$

$$(x_0, y_0) \text{ initial value } = p^1$$

$$x_1 = x_0 + h$$

and

$$y_1 = y_0 + \Delta y$$

$$(x_1, y_1) \text{ final value } = p^2$$

Given, $\frac{dy}{dx} = x+y$ (when $x=0$, then $y=1$)

Approximate y , when $x=0.1$ and $x=0.2$

Solⁿ:

Let us take, $h=0.1$. Hence $f(x,y) = x+y$

$$\text{Now, } K_1 = ? = hF(x_0, y_0) = 0.1(0+1) = 0.1$$

$$K_2, K_3, K_4 = ?$$

$$K_2 = hF\left(x_0 + \frac{h}{2}, y_0 + \frac{K_1}{2}\right) = 0.1(0.05 + 1.05) = 0.11$$

$$= 0.1 F\left(0 + \frac{0.1}{2}, 1 + \frac{0.1}{2}\right)$$

$$= 0.1(0.05, 1.05)$$

GOOD LUCK

TOPIC NAME :

DAY :

TIME :

DATE : / /

$$K_3 = h f \left(x_0 + \frac{h}{2}, y_0 + \frac{k_2}{2} \right)$$

$$= 0.1 (0.05, 1.055)$$

$$= 0.1105$$

$$K_4 = h f (x_0 + h, y_0 + k_3)$$

$$= 0.1 (0.1, 1.1105)$$

$$= 0.12105$$

$$\Delta y = \frac{1}{6} \times 0.66205$$

$$= 0.110341$$

$$x_1 = x_0 + h = 0 + 0.1 = 0.1$$

$$y_1 = y_0 + \Delta y = 1 + 0.110341$$

$$= 1.110341$$

2nd iteration:

$$x_0 = 0.1, y_0 = 1.110341$$

$$K_1 = h f (x_0, y_0)$$

$$= 0.1 (0.1 + 1.110341)$$

$$= 0.121034$$

$$K_2 = h f \left(x_0 + \frac{h}{2}, y_0 + \frac{k_1}{2} \right)$$

$$= 0.1 (0.15, 1.17085)$$

$$= 0.132085$$

TOPIC NAME : _____

DAY : _____
TIME : _____

DATE : / /

$$k_3 = h f(x_0 + \frac{h}{2}, y_0 + \frac{k_2}{2})$$

$$= 0.1(0.15, 1.1763)$$

$$= 0.13263$$

$$k_4 = h f(x_0 + h, y_0 + k_3)$$

$$= 0.1(0.2, 2.28664)$$

$$= 0.248664$$

$$\Delta y = \frac{1}{6} \times 0.899128 = 0.14985$$

$$x_2 = x_0 + h = 0.1 + 0.1 = 0.2$$

$$y_2 = y_0 + \Delta y = 1.110341 + 0.14985 = 1.26326$$

Lecture-8

TOPIC NAME: Inverse Matrix

DAY: Tuesday

TIME:

DATE: 5/9/23

Find the inverse, $A = \begin{bmatrix} 0 & -1 & 2 \\ 1 & 2 & 3 \\ 3 & 1 & 1 \end{bmatrix}$

$$|A| = -2$$

$$A_{11} = -1 \quad A_{12} = 8 \quad A_{13} = -5$$

$$A_{21} = 1 \quad A_{22} = -6 \quad A_{23} = 3$$

$$A_{31} = -1, A_{32} = 2, A_{33} = -1$$

$$\text{Row echelon form: } \begin{array}{ccc|ccc} 1 & -1 & 8 & -5 & 1/2 & -1/2 & 1/2 \\ 0 & 1 & -6 & 3 & -4 & 0 & 1 \\ 0 & 0 & 2 & -1 & 1 & 0 & 0 \end{array}$$

$$A^{-1} = \frac{1}{-2} \begin{bmatrix} 1 & 1 & -1 \\ 8 & -6 & 2 \\ -5 & 3 & -1 \end{bmatrix} = \begin{bmatrix} 1/2 & -1/2 & 1/2 \\ -4 & 3 & -1 \\ 5/2 & -3/2 & -1/2 \end{bmatrix}$$

Find inverse of Matrix:

- ① Gauss Jordan method
- ② Choleski method
- ③ Escalator method

Solve: 5 (from slide)

~~Salim Sir~~Curve FittingLecture-9

Monday

11/09/23

Fit a second degree parabola to the data -

x: 0 1 2 3 4

y: 1 5 10 22 38

Soln: let the parabola to be fitted to the given
 be - $y = a + bx + cx^2$. Then the normal equations -

$$\sum y = ma + b\sum x + c\sum x^2$$

$$\sum xy = a\sum x + b\sum x^2 + c\sum x^3$$

TOPIC NAME: _____ DAY: _____
 TIME: _____ DATE: / /

$$\sum x^v y = a \sum x^v + b \sum x^3 + c \sum x^4$$

$$\sum y = ma + b \sum x \quad \text{and} \quad \sum xy = a \sum x + b \sum x^v$$

$$\sum x = 10 \quad \sum y = 76$$

straight line.

$$\sum x^v = 0^v + 1^v + 2^v + 3^v$$

x	y	x^v	x^3	x^4	xy	$x^v y$
0	1	0	0	0	0	0
1	5	1	1	1	5	5
2	10	4	8	16	20	40
3	22	9	27	81	66	198
4	38	16	64	256	152	608
$\sum x = 10$	$\sum y = 76$	$\sum x^v = 30$	$\sum x^3 = 100$	$\sum x^4 = 354$	$\sum xy = 243$	$\sum x^v y = 851$

Hence, $m = 5$

$$\begin{aligned} \sum y &= ma + b \sum x \\ \Rightarrow 76 &= 5a + 10b \end{aligned}$$

$$a = -3, b = \frac{91}{10}$$

$$\sum y = m a + b \sum x + c \sum x^v$$

$$\Rightarrow 76 = 5 \times (-3) + \frac{91}{10} \times 10 + c \times 30$$

$$\Rightarrow 76 = -15 + 91 + c \times 30$$

DAY: _____

TIME: _____

DATE: / /

TOPIC NAME: _____

$$76 = 5a + 10b + 30c$$

$$243 = 10a + 30b + 100c$$

$$851 = 30a + 100b + 354c$$

Solving we get -

$$a = 10/7, b = 17/70, c = 31/14$$

#	x	\bar{x}	$\bar{v}x$	\bar{v}^2x	$\bar{v}y$	\bar{v}^2y	$\bar{v}x^2$	\bar{x}^2
	x : 0	0	0	0	3	0	4	1
	y : 10	1	1	1	1	1	1	1
		1.8	3.3	6.6	4.5	9	6.3	2.25
		2.8	5.6	11.2	10	18	12.6	4.41
		3.8	7.6	15.2	13.5	22.5	16.2	5.29
		4.8	9.6	19.2	12.5	30	20.2	6.09

$$\sum y = ma + b \sum x, \quad \sum xy = a \sum x + b \sum x^2$$

x	y	$\bar{v}x$	$\bar{v}y$	$a = m = \frac{\sum y - b \sum x}{\sum v^2x}$
0	10	0	0	$16.9 = 5a + 10b$
1	1.8	1	1.8	$47.1 = 10a + 30b$
2	3.3	4	6.6	$a = 18/25, b = 133/100$
3	4.5	9	13.5	
4	6.3	16	25.2	$y = \frac{133}{100}x + \frac{18}{25}$
$\sum x = 10$		$\sum y = 16.9$	$\sum v^2x = 30$	$\sum xy = 47.1$

Partial Differential Equation

Lecture-10

(Bala Gurusamy)

TOPIC NAME: Problems

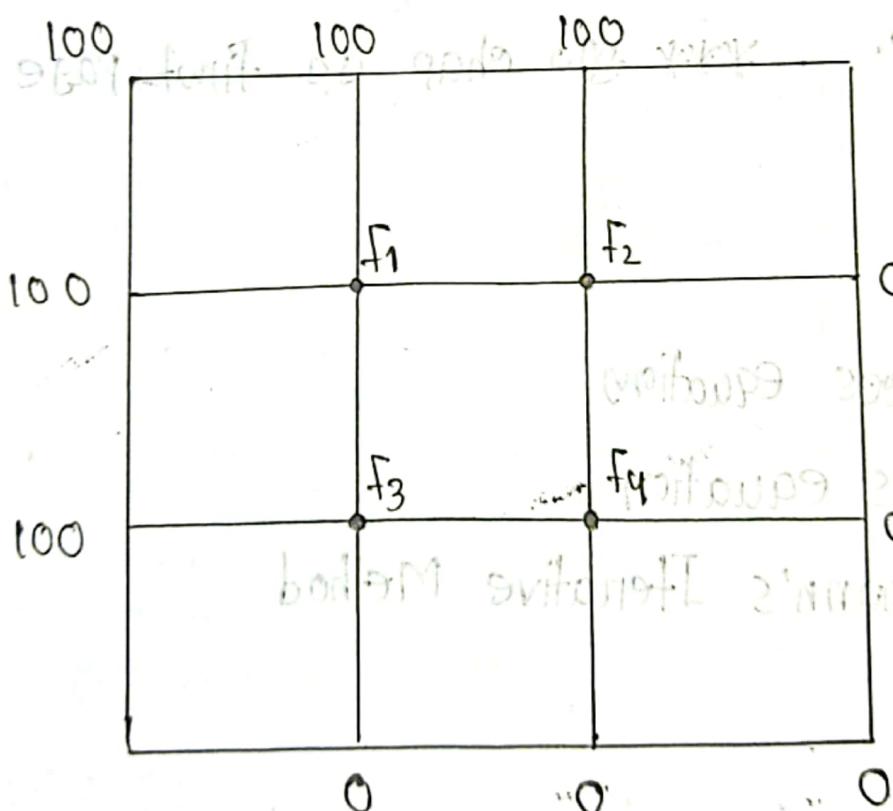
DAY: Tuesday

TIME:

DATE: 12/9/23

Consider a steel plate of size 15 cm x 15 cm. If two of the sides are held at 100°C and other two sides, are held at 0°C , what are the steady state temperatures at interior points assuming a grid size 5 cm x 5 cm.

After notes, written by Prof. Dr. K. S.



The system of equations are as follows -

$$\text{At point 1: } f_1 + f_3 - 4f_1 + 100 + 100 = 0$$

$$\text{" " 2: } f_1 + f_4 - 4f_2 + 100$$

$$\text{" " 3: } f_1 + f_4 - 4f_3 + 100$$

Observe without looking at the book.

TOPIC NAME: Partial Differential Equations
DAY: / /
TIME: / /
DATE: / /

QUESTION NO. 4: $f_3 + f_2 - 4f_1 = 0$

ANSWER: To find up to 3rd order partial derivatives.

*** What is partial differential equation, explain with example.

*** तरीका वर्णन के साथ समीकरण का परिचय दें।

Topics:

- ① PDE
- ② Laplace's equation
- ③ Poisson's equation
- ④ Liebnmann's Iterative Method

Lecture-11

TOPIC NAME : Partial Differential Equation

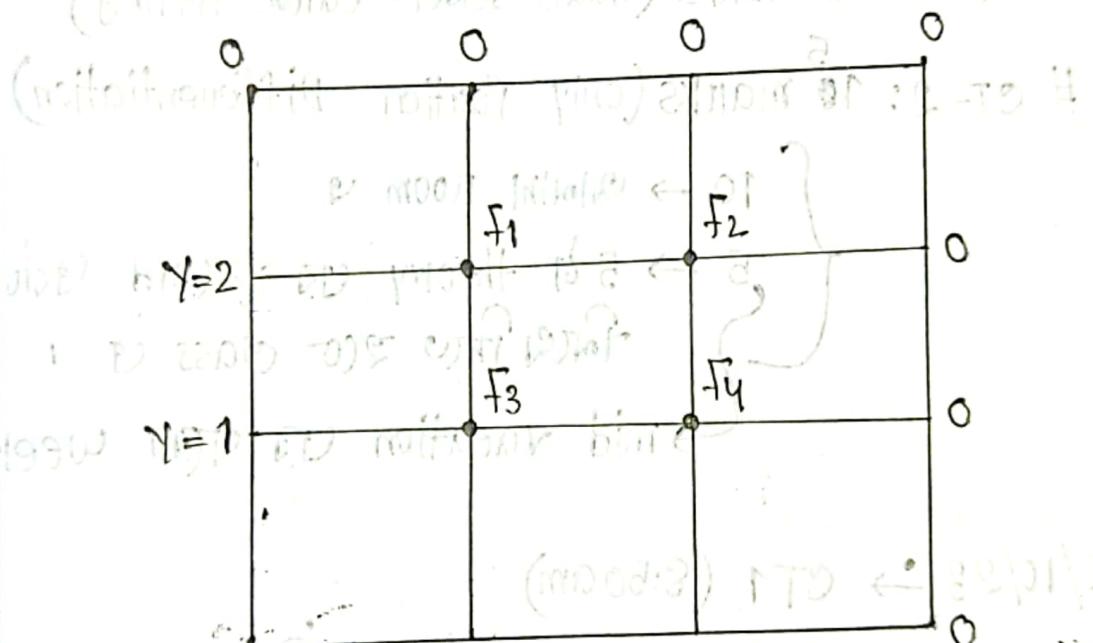
DAY: Monday

TIME:

DATE: 18/9/23

Solve the Poisson's equation -

$\nabla^2 f = 2x^2y^2$ over the square domain $0 \leq x \leq 3$ and $0 \leq y \leq 3$ with $f=0$ on the boundary and $h=1$.



at point 1:

$$0 + 0 + f_3 + f_2 - 4f_1 = 2(1)^2(2)^2$$

at point 2:

$$0 + 0 + f_1 + f_4 - 4f_2 = 2(2)^2(2)^2$$

at point 3:

$$0 + 0 + f_1 + f_4 - 4f_3 = 2(1)^2(1)^2$$

at point 4: $0 + 0 + f_2 + f_3 - 4f_4 = 2(1)^2(2)^2$

TOPIC NAME : Interpolation

DAY :

TIME :

DATE :

Some methods:

1. Benders - Schmidt method

2. Crank - Nicholson method

CT-1 : 30 marks (Gauss Seidel - Curve fitting)

CT-2: 10 marks (only Partial Differentiation)

$\left\{ \begin{array}{l} 10 \rightarrow \text{partial room } \Rightarrow \\ 5 \rightarrow 5 \text{ theory പ്രയോഗ ഫർമാ } \\ \text{നിഖേദിത്ത ഒരു ക്ലാസ് } \\ \rightarrow \text{mid vacation പ്രയോഗ week.} \end{array} \right.$

5/10/23 → CT1 (8.50 am)

16/10/23 → Partial Diff പ്രയോഗ നിഖേദി

Thru 2nd class ഏ

TOPIC NAME: Some Terms

Some Terms: Definition + example

1. Numerical Differentiation
2. Interpolation
3. Differential equation.
4. Linear algebraic equation.
5. Definition of curve fitting.
6. Polynomial equation.

* যাই রয়েছে প্রিমি মেথড এবং definition + prove
(Mainly প্রিমি মেথড এবং অন্য Page) আরো আজ্ঞা :