

# Sheet #1

## Rules

### Recall

Arrival rate  $\lambda_i = \frac{A_i}{T}$  (1) Arrivals

- # of completed jobs  $C_i$

Completion rate  $X_i = \frac{C_i}{T}$  (2)

- Busy time  $B_i$

Utilization  $U_i = \frac{B_i}{T}$  (3)

mean service time  $S_i = \frac{B_i}{C_i}$  (4)

$S_i = \frac{1}{\text{speed of device } i}$  (5)

### Operational laws

$U_i = X_i S_i$  (6)

- Job flow balance from (1) & (2)

$A_i = C_i \iff \lambda_i = X_i$  (7)

\* if a job needs several visits to device  $i$  to be performed  $v_i$  (visit ratio) then,  $X_i$  is

$X_i = X v_i$  (8)

- Job demand  $D_i = v_i S_i$  (9)

From  $U_i = X_i S_i = X v_i S_i = X D_i$  (10)

- Little's law

$Q_i = X_i R_i$  (11) mean response time  
mean customers in system

## Examples

1) During a 10 sec. observation period, 400 packets were served by a gateway whose cpu can serve 200 pps speed

② What was the utilization of the gateway cpu?

$S = \frac{1}{\text{Speed}} = 5 \times 10^{-3} \text{ sec}$

$X = \frac{C}{T} = \frac{400}{10} = 40$

$U = X S = 40 \times 5 \times 10^{-3} = 0.2$  #

2) For given system of 2 devices A & B,  $V_A = 2$ ,  $V_B = 3$ , during 10 sec., the system served 3 jobs. What was the throughput of each device?

$X = \frac{C}{T} = \frac{3}{10} = 0.3$

$X_A = X V_A = 0.3(2) = 0.6$

$X_B = X V_B = 0.3(3) = 0.9$

3) Dist. sys has a printer server with a printing speed of 60 pages per minute. The server was observed to print 500 pages over a 10 min observation period. If each job prints 5 pages on average, 5 pages/job

② What was the job completion rate?

$X_p = X v_p$

$50 = X (5) \rightarrow X = 10 \text{ jobs/min}$



4) During a 10 sec observation period, 40 requests were served by a file server. Each request requires 2 disk accesses. The average service time at the disk was 30 msec.

② What is the avg disk utilization?

$$U_d = X V_d S_d = \frac{C}{T} V_d S_d$$

$$= \frac{40}{10} (2) (0.03) = 0.24 < 1$$

5) Consider a desktop computer with one disk that serves page faults. We measured that the disk utilization is 0.8, and the mean time to handle (serve) 9 page faults is 0.01 sec. If on average 5 tasks per second arrive to the system, what is the average number of page faults per task?

$$U = X V S = \lambda V S$$

$$0.8 = (5)(V)(0.01)$$

$$V = 16 \text{ page fault / task}$$

6) A web server is monitored for 10 minutes & its CPU is observed to be busy 90%. The web server log reveals that 30,000 requests are completely processed in that period.

② What is the CPU service demand of the web server?

$$\bar{U} = \bar{X} D$$

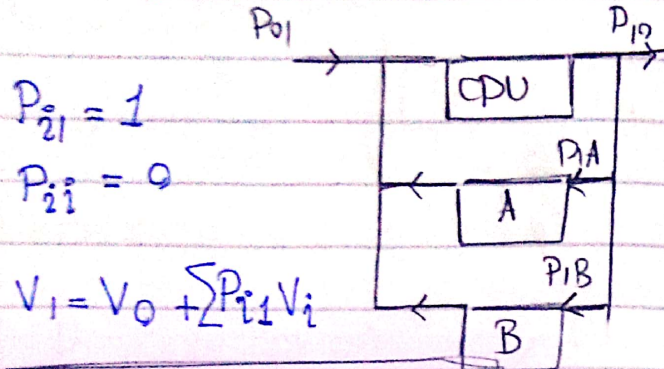
$$D = \frac{U}{X} = \frac{UT}{C} = 3 \times 10^{-4} \text{ min}$$

7) The throughput of a timesharing system was observed to be 5 jobs per sec over 10 min. If the avg number of jobs in the system was 4, what is the avg response time?

$$\bar{Q} = \bar{X} R \Rightarrow R = \frac{4}{5} = 0.8 \text{ sec}$$



## central server Model



$$P_{i1} = 1$$

$$P_{ii} = 0$$

$$V_1 = V_0 + \sum P_{i1} V_i$$

$$V_1 = 1 + V_A + V_B + \dots \quad (12)$$

$$V_A = V_1 P_{1A}, \quad V_B = P_{10} V_1$$

$$V_1 = V_{CPU} = \frac{1}{P_{10}} \quad (13)$$

$$V_A = \frac{P_{1A}}{P_{10}}, \quad V_B = \frac{P_{1B}}{P_{10}} \quad (14)$$

(i) In a time-sharing system, accounting log data produced the following user profile for user programs.

The avg think time is 7.18 sec. From the devices specs, it was determined that disk A takes 50 msec & disk B takes 30 msec per request. With 17 active users, disk A throughput was observed to be 15.7 I/O req. Per sec.

\* Each program requires 5 sec of CPU time & makes 80 I/O req to disk A and 100 I/O to disk B

i) System throughput  $X$

$$\bar{X}_A = X V_A$$

$$X = \frac{15.7}{80} = 0.19625 \text{ rps}$$

ii) The utilization of each device

$$U_A = X_A S_A = (15.7)(50 \times 10^{-3}) = 0.785$$

$$U_B = X_B S_B = X V_B S_B$$

$$= (0.19625)(100)(30 \times 10^{-3}) = 0.58875$$

$$U_{CPU} = X D_{CPU} = (0.19625)(5) = 0.98125$$

iii) visit ratio of CPU

$$V_{CPU} = 1 + V_A + V_B$$

$$= 1 + 80 + 100 = 181 \text{ visit/prog}$$

(2) consider the open queueing nw model for a file server, show in the figure ... during 1 hour

$$\text{CPU Busy time} = 1728 \text{ s} \quad C_{CPU}$$

$$\text{Disk A Busy time} = 1512 \text{ s} \quad B_A$$

$$\text{Disk B Busy time} = 2592 \text{ s} \quad B_B$$

$$\# \text{ of I/O operations to disk A} = 75,600 \quad C_A$$

$$\# \text{ of I/O op to disk B} = 86,400 \quad C_B$$

i) service demand & visit ratio for the 3 devices

$$S_i = \frac{B_i}{C_i} \Rightarrow S_A = \frac{1512}{75,600} = 0.02 \text{ sec}$$



$$S_B = \frac{B_B}{S_B} = \frac{2592}{86400} = 0.03 \text{ sec}$$

$S_{CPU}$

$$D_A = \frac{1728}{10800} = 0.16 \text{ sec}$$

$$X = \frac{C}{T} = \frac{10,800}{3600} = 3 \text{ req/sec}$$

$$X_A = \frac{C_A}{T} = \frac{2592}{3600} = 21 \text{ req/sec}$$

$$X_B = \frac{C_B}{T} = \frac{84,400}{3600} \approx 24 \text{ req/sec}$$

$$V_A = \frac{X_A}{X} = \frac{21}{3} = 7 \text{ vi/req} \leftarrow$$

$$V_B = \frac{X_B}{X} = \frac{24}{3} = 8 \text{ vi/req} \leftarrow$$

$$V_{CPU} = \frac{1}{X} (1 + V_B + V_A) = 16 / \text{req} \leftarrow$$

$$D_A = V_A S_A = 7(0.02) = 0.14 \text{ sec}$$

$$D_B = V_B S_B = 8(0.03) = 0.24 \text{ sec}$$

$$D_{CPU} = V_{CPU} S_{CPU} = 16(0.16) = 2.56 \text{ sec}$$

2) device utilization

$$U_{CPU} = \frac{B_{CPU}}{T} = \frac{1728}{3600} = 0.48$$

$$U_A = \frac{B_A}{T} = \frac{1512}{3600} = 0.42$$

$$U_B = \frac{B_B}{T} = \frac{2592}{3600} = 0.72$$