Algorithm Library

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Algorithm Library

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1 头文件

```
#include<iostream>
#include<cstdio>
#include<cmath>
#include<cstdlib>
#include<cstring>
#include<string>
#include<vector>
#include<stack>
#include<queue>
#include<set>
#include<map>
#include<algorithm>
using namespace std;
typedef long long 11;
typedef unsigned long long ull;
    暴力
\mathbf{2}
2.1 枚举
do{
        for(int i=0;i<n;++i) cout<<num[i]<<endl;</pre>
    }while(next_permutation(num,num+n)); //prev_permutation
2.2 子集生成
void print_subset(int *A,int *B,int n,int cur){
    if(cur==n){
        for(int i=0;i<n;++i) if(B[i]) printf("%d ",A[i]);</pre>

→ printf("\n");
        return;
    B[cur]=0; print_subset(A,B,n,cur+1);
    B[cur]=1; print_subset(A,B,n,cur+1);
}
2.3
     回溯
int vis[maxn];
void bt(int cur) {// (int x, int y)
    if(cur==n){
```

```
for(int i=0;i<4;++i){</pre>
        //改变
        bt(cur+dx[i])
        //恢复
    }
}
    搜索
3
3.1 dfs
int cnt, vis[maxn] [maxn];
void dfs(int x,int y,int id){
    // 判读边界
    dfs(nx,ny,id);
}
for(int i=0;i<n;++i){</pre>
    for(int j=0; j<n;++j){</pre>
        if(!vis[i][j]){
            vis[i][j]=1;
            dfs(i,j,++cnt);
            //vis[i][j]=0;
        }
    }
}
3.2 bfs
queue<int> que;
int vis[maxn];
while(que.size()) que.pop();
memset(vis,0,sizeof(vis));
que.push(0); vis[0]=1;
void bfs(){
    while(que.size()){
        int x=que.front(); que.pop();
        for(){
            vis[]=1; //每加入队列就标记
            que.push();
        }
```

```
}
}
    数据结构
4
4.1 并查集
const int maxn=1010;
int fa[maxn]; //memset(fa,-1,sizeof(fa));
findroot(int x){
    if(fa[x]==-1) return x;
    return fa[x]=findroot(fa[x]);
}
void Union(int x,int y){
    x=findroot(x); y=findroot(y);
    if(x!=y) fa[x]=y;
}
4.2 heap
vector<int> vec;
make_heap(vec.begin(),vec.end(),greater<int>());
        for(int i=k;i<n;++i){</pre>
            int x;cin>>x;
            if(*vec.begin()<x){</pre>
                 → pop_heap(vec.begin(),vec.end(),greater<int>());{
                     cout<<"before pop "<<*(vec.end()-1)<<endl;</pre>
                     vec.pop_back();
                     cout<<"after pop "<<*(vec.end()-1)<<endl;</pre>
                 }
                 cout<<"before push "<<*(vec.end()-1)<<endl;</pre>
                 vec.push_back(x);
                 → push_heap(vec.begin(),vec.end(),greater<int>());
                 cout<<"after push "<<*(vec.end()-1)<<endl;</pre>
            }
        }
        sort_heap(vec.begin(),vec.end(),greater<int>());
        cout<<*(vec.end()-1)<<endl;</pre>
```

4.3 二叉树

4.3.1 各种遍历及合成

```
struct node{
    node *lc,*rc;
    char ch;
} nodes[maxn];
void preord(node *t){
    if(t==0) return;
    printf("%d",t->id);
    preord(t->lc); preord(t->rc);
}
int cur=0,idx=0;
node * newnode(){
    nodes[cur].lc=nodes[cur].rc=0;
    nodes[cur].ch=s[idx++];
    return &nodes[cur++];
}
node *build(){
    if(idx==len) return 0;
    char ch=s[idx];
    if(ch=='#') {++idx; return 0;}
    node *t=newnode();
    t->lc=build();
    t->rc=build();
    return t;
}
char s1[maxn],s2[maxn];
node *build(int l1,int r1,int l2,int r2){
    int idx;
    node *t=newnode(); t->ch=s1[l1];
    if(idx!=12) t->1c=build(11+1,idx-12+11+1,12,idx);
    if(idx!=r2-1)t->rc=build(idx-12+11+1,r1,idx,r2);
    return t;
}
```

5 动态规划

5.1 背包

```
5.1.1 01 背包
```

```
int wei[maxn],val[maxn],dp[maxn],c;
memset(dp,0,sizeof(dp)); //若要恰好放满 则 dp[0]=0 其余为负无
→ 穷
                                 //若 c 较小, n 较大, 可调整
for(int i=0;i<n;++i){</pre>
→ i,j 的内外顺序
   for(int j=c;j>=wei[i];--j){ //完全背包的话, j 顺序反过来即
       dp[j]=max(dp[j],dp[j-wei[i]]+val[i]);
   }
}
5.1.2 多重背包
//HDU-2191
#include <cstdio>
const int maxn = 110;
int dp[maxn];
struct rice{
    int p;
    int h;
    int c;
} r[maxn];
int V;
int max(int a, int b) { return a > b ? a : b; }
void ZeroOnePack(int cost, int weight){
   for (int v = V; v >= cost; v--){
       dp[v] = max(dp[v], dp[v - cost] + weight);
   return;
}
void CompletePack(int cost, int weight){
   for (int v = cost; v \leftarrow V; v++)
       dp[v] = max(dp[v], dp[v - cost] + weight);
    }
   return;
}
void MultiplePack(int cost, int weight, int amount){
```

if (cost*amount >= V){

CompletePack(cost, weight);

```
return;
    }
    else{
        int k = 1;
        while(k<amount){</pre>
            ZeroOnePack(k * cost, k * weight);
            amount -= k;
            k *= 2;
        }
        ZeroOnePack(amount * cost, amount * weight);
    }
    return;
}
int main(){
    int c, m;
    scanf("%d", &c);
    while(c--){
        scanf("%d%d", &V, &m);
        for (int i = 1; i <= m; i++){
            scanf("%d%d%d", &r[i].p, &r[i].h, &r[i].c);
        }
        for (int v = 0; v \le V; v++){
            dp[v] = 0;
        for (int i = 0; i <= m; i++){
            MultiplePack(r[i].p, r[i].h, r[i].c);
        printf("%d\n", dp[V]);
    return 0;
}
5.2 背包-其他
//double cost bag(3d)
f[i][v][u]=max(f[i-1][v][u],f[i-1][v-a[i]][u-b[i]]+w[i])
//double cost bag(2d)
for v=V...cost
        for u=U...cost
                f[v][u]=max(f[u][v],f[u-ucost[i]][v-vcost[i]]+w[i])
//group bag
for group in groups
        for v=V...0
```

```
for i in group
                        f[v]=max(f[v],f[v-c[i]]+w[i])
//optimize
if cost[i] <=cost[j] && weight[i] == weight[j]</pre>
        remove item[j]
5.3 最长公共子序列
char s1[maxn],s2[maxn];
int dp[maxn] [maxn];
for(int i=1;i<=n1;++i){ //从 1 开始存
        for(int j=1; j<=n2;++j){</pre>
                if(s1[i]==s2[j]) dp[i][j]=dp[i-1][j-1]+1;
        else dp[i][j]=max(dp[i-1][j],dp[i][j-1]);
    }
}
int i=n1, j=n2, path[maxn], k=-1;
while(dp[i][j]){
    if(dp[i-1][j]==dp[i][j]) --i;
    else if(dp[i][j-1]==dp[i][j]) --j;
    else {
            path[++k]=i;
            --i; --j;
    }
}
for(;k;--k) cout<<s1[path[k]]<<" ";</pre>
cout<<s1[path[0]]<<endl;</pre>
5.4 最长上升子序列
int n,num[1010],dp[1010];
const int inf=10000000;
int lis(){ // nlogn 但是不能打印路径
    fill(dp,dp+n,inf);
    for(int i=0;i<n;++i){</pre>
        *lower_bound(dp,dp+n,num[i])=num[i];
    return lower_bound(dp,dp+n,inf)-dp;
}
```

```
int n,num[maxn],dp[maxn],pre[maxn]; //n ~ 能打印路径
int ans,idx;
void lis(){
    memset(pre,-1,sizeof(pre));
    for(int i=0;i<n;++i){</pre>
        dp[i]=0;
         for(int j=0; j<i; ++j){</pre>
             if(num[i]>num[j]&&dp[j]+1>dp[i]){
                 dp[i]=dp[j]+1;
                 pre[i]=j;
                 if(dp[i]>ans){
                      ans=dp[i];
                      idx=i;
                 }
             }
        }
    }
}
//safe
void lis(){
    for(int i=0;i<n;++i){</pre>
                 dp[i]=0;
                 pre[i]=-1;
        }
    for(int i=0;i<n;++i){</pre>
         for(int j=0; j<i; ++j){</pre>
             if(num[i]>num[j]&&dp[j]+1>dp[i]){
                 dp[i]=dp[j]+1;
                 pre[i]=j;
             }
        }
    }
         ans=dp[0];
         for(int i=1;i<n;++i){</pre>
                 if(dp[i]>ans){
                          ans=dp[i];
                          idx=i;
                 }
        }
}
```

```
void print(int i){
    if(pre[i]!=-1) print(pre[i]);
    printf("%d",num[i]);
}
int main(){
    while (scanf("%d", &n)==1){
        for(int i=0;i<n;++i) scanf("%d",&num[i]);</pre>
        lis();
        printf("%d\n",ans);
        print(idx);
        printf("\n");
    return 0;
}
5.5 最长公共上升
- n,m,num1[maxn],num2[maxn],pre[maxn],dp[maxn],ans,Max,last,idx;
void lcis(){
    ans=0;
   memset(dp,0,sizeof(dp));
    memset(pre,-1,sizeof(pre));
    for(int i=0;i<n;++i){</pre>
        Max=0;
        for(int j=0;j<m;++j){ //dp[j] 表示串 1 的前 i 个和串的
        → 前 j 个, 且以 num2[j] 结尾
            if(num1[i]>num2[j]) {
                Max=max(Max,dp[j]); //最大的 dp[i-1][k]
            if(num1[i] == num2[j]) {
                dp[j]=Max+1;
                pre[j]=last;
            if(dp[j]>ans){
                ans=dp[j];
                idx=j;
            }
        }
    }
void print(int idx){
    if(pre[idx]!=-1) print(pre[idx]);
```

```
printf("%d",num2[idx]);
}
5.6 maxsubsum
int max_sub_sum(int *line,int *dp,int n){
    fill(dp,dp+n,0);
    dp[0]=line[0];
    for(int i=1;i<n;++i) dp[i]=max(dp[i],dp[i-1]+line[i]);</pre>
    int res=-inf;
    for(int i=0;i<n;++i) res=max(res,dp[i]);</pre>
    return res;
}
5.7 maxsubmatsum
for(int i=0;i<n;++i) {</pre>
    for(int j=0;j<n;++j) scanf("%d",&mat[i][j]);</pre>
}
fill(tot[0],tot[0]+n,0);
for(int i=1;i<=n;++i){</pre>
    for(int j=0; j<n;++j) tot[i][j]=tot[i-1][j]+mat[i-1][j];
}
int res=-inf;
for(int i=0;i<n;++i){</pre>
    for(int j=i+1; j<=n;++j){</pre>
        for(int k=0;k<n;++k) line[k]=tot[j][k]-tot[i][k];</pre>
        res=max(res,max_sub_sum(line,dp,n));
    }
}
5.8 tsp
int solve(){ //上回到起始点,如果需要回到起始点,
    int s;
    for(s=0;s<(1<<n)-1;++s) fill(dp[s],dp[s]+n,inf);
    fill(dp[s],dp[s]+n,0);
    for(s=(1<< n)-2;s>0;--s){
        for(int u=0;u<n;++u ){</pre>
             if((s\&(1<< u))==0) continue;
            for(int v=0;v<n;++v){</pre>
                 if(s\&(1<< v)) continue;
                 \rightarrow dp[s][u]=min(dp[s][u],dp[s|(1<<v)][v]+mat[u][v]);
            }
```

```
}
    }
    s=1;
    int res=inf;
    for(int i=0;i<n;++i){</pre>
        res=min(res,dp[s][i]);
        s<<=1;
    }
    return res;
}
5.9 拆分方案数
void cnt(){
        fill(dp,dp+m+1,0); dp[0]=1; //恰好凑齐
        for(int i=0;i<n;++i){</pre>
            for(int j=m; j>=num[i]; --j){
                dp[j]=(dp[j-num[i]]+dp[j]);
            }
        }
}
    图论
6.1 tree
const int maxn=110;
int lc[maxn],rc[maxn],p[maxn]; //若节点编号严格是 1-n
int n,m;
const int maxn=1010;
struct node{
    int val;
    node *lc,*rc;
} nodes[maxn];
int cur=0;
node *newnode(int v=0){
   nodes[cur].val=v;
   nodes[cur].lc=nodes[cur].rc=0;
   return &nodes[cur++];
}
```

6.2 拓扑排序

```
const int maxn=510;
vector<int> edges[maxn],ans;
int ind[maxn],n,m,used[maxn];
int dfs(int k){ // void dfs(int k) 只输出一组值 后面 return 处
    也要修改
    if(k==n){
        for(int i=0;i<n-1;++i) printf("%d ",ans[i]);</pre>
        printf("d\n",ans[n-1]);
        return 1;
    }
    for(int i=1;i<=n;++i){</pre>
        if(!ind[i]&&!used[i]){
            used[i]=1; ans.push_back(i);
            for(int j=0;j<edges[i].size();++j)</pre>

    ind[edges[i][j]]--;

            if(dfs(k+1)) return 1;
            for(int j=0;j<edges[i].size();++j)</pre>

    ind[edges[i][j]]++;

            used[i]=0; ans.pop_back();
        }
    }
    return 0;
}
     单源最短路径
6.3
6.3.1 Bellman-Ford
const int maxm=5210,maxn=510;
struct edge{
    int u,v,c;
}edges[maxm];
int e,n,dis[maxn];
bool bellman(){
    const int inf=100000000; //不能用-1, 在判断负环时有问题
    fill(dis,dis+n,inf);
    dis[1]=0;
    for(int i=0;i<n;++i){</pre>
        for(int j=0; j < e; ++ j) {</pre>
            edge eg=edges[j];
            if(dis[eg.v]>dis[eg.u]+eg.c){
                dis[eg.v]=dis[eg.u]+eg.c;
```

```
if(i==n-1) return 1;
            }
        }
    }
    return 0;
}
                                //无负边
void bellman(){
    const int inf=100000000;
    fill(dis,dis+n,inf);
    dis[1]=0;
    while(1){
        int update=0;
        for(int i=0;i<e;++i){</pre>
            edge eg=edges[i];
            if(dis[eg.v]>dis[eg.u]+eg.c){
                dis[eg.v]=dis[eg.u]+eg.c;
                update = 1;
            }
        }
        if(!update) break;
    }
}
6.3.2 Dijkstra
struct edge{
    int to,w;
    bool operator<(const edge&b)const {return w>b.w;}
    edge(){to=w=0;}
    edge(int to,int w){this->to=to; this->w=w;}
const int maxn=1010,inf=1000000;
vector<edge> edges[maxn];
int n,dis[maxn];
priority_queue<edge> que;
void dijkstra(int s){
    while(que.size()) que.pop();
    fill(dis,dis+n+1,inf);
    que.push(edge(s,0)); dis[s]=0;
    while(que.size()){
        edge eg=que.top(); que.pop();
        int u=eg.to;
        if(eg.w!=dis[u]) continue;
```

```
for(int i=0;i<edges[u].size();++i){</pre>
           int v=edges[u][i].to;
           if(dis[v]>dis[u]+edges[u][i].w){
               dis[v]=dis[u]+edges[u][i].w;
               que.push(edge(v,dis[v]));
           }
       }
    }
}
     多源最短路径
6.4
6.4.1 Floyd
const int inf=1000000,maxn=210; //支持负边
int n,dis[maxn][maxn];
void floyd(){
                       //dis[i][i]=0; inf
    for(int k=1;k<=n;++k){</pre>
        for(int i=1;i<=n;++i){</pre>
            for(int j=1; j<=n;++j){</pre>
                dis[i][j]=min(dis[i][j],dis[i][k]+dis[k][j]);
            }
        }
          //通过检查 dis[i][i] 有没有为负的 可以判断有无负圈
    }
}
//支持打印路径
const int maxn=40;
int p,q,r;
const int inf=1000000;
map<string,int> Id;
map<int,string> Name;
struct dis{
    int len,pre;
} Dis[maxn][maxn];
void print(int u,int v){
    if(u==v){
        cout<<Name[v]; return;</pre>
    print(u,Dis[u][v].pre);

    cout<<"->("<<Dis[Dis[u][v].pre][v].len<<")"<<"->"<<Name[v];</pre>
}
```

```
for(int k=0;k< p;++k){
        for(int i=0;i<p;++i){</pre>
             for(int j=0;j<p;++j){</pre>
                 int tmp=Dis[i][k].len+Dis[k][j].len;
                 if(tmp<Dis[i][j].len){</pre>
                     Dis[i][j].len=tmp;
                     Dis[i][j].pre=Dis[k][j].pre;
                 }
            }
        }
    }
6.5 最小生成树
6.5.1 Prim
const int maxn=110,inf=10000000;
int n,dis[maxn],used[maxn],mat[maxn][maxn];
int prim(){
    memset(used,0,sizeof(used));
    fill(dis,dis+n+1,inf);
    dis[1]=0;
    int res=0;
    while(1){
        int u=-1;
        for(int v=1; v<=n; ++v){</pre>
             if(!used[v]&&(u==-1||dis[v]<dis[u])) u=v;
        if(u==-1) break;
        used[u]=1;
        res+=dis[u];
        for(int v=1; v<=n; ++v){</pre>
             dis[v]=min(dis[v],mat[u][v]); //注意不是
             \rightarrow dis[u]+mat[u][v]
        }
    return res;
}
const int maxn=30,maxm=100,inf=100000;
int vis[maxn],mat[maxn][maxn],dis[maxn];
int n;
```

```
int prim(){
    memset(vis,0,sizeof(vis));
    fill(dis,dis+n,inf);
    int res=0;
    dis[0]=0;
    while(1){
        int u=-1;
        for(int v=0;v<n;++v){</pre>
            if(!vis[v]\&\&(u==-1||dis[v]<dis[u])) u=v;
        }
        if (u==-1) break;
        vis[u]=1;
        res+=dis[u];
        for(int i=0;i<n;++i) dis[i]=min(dis[i],mat[u][i]);</pre>
    }
    return res;
}
struct edge{
    int v,1;
    bool operator<(const edge &b) const {return 1>b.1;}
    edge(int v=0,int l=inf){
        this->v=v; this->l=1;
};
priority_queue<edge> que;
int prim(){
    fill(dis,dis+n,inf);
    int res=0;
    dis[0]=0;
    memset(vis,0,sizeof(vis));
    while(que.size()) que.pop();
    que.push(edge(0,0));
    while(que.size()){
        int u=que.top().v,l=que.top().1;
        que.pop();
        if(dis[u]!=1||vis[u]) continue;
        res+=1;
        vis[u]=1;
        for(int v=0;v<n;++v) {</pre>
```

```
if(dis[v]>mat[u][v]&&!vis[v]){
                dis[v]=mat[u][v];
                que.push(edge(v,dis[v]));
            }
        }
    }
    return res;
}
6.5.2 Kruskal
const int maxn=110,maxm=5010;
int n,m,fa[maxn];
int findroot(int u){
    if(fa[u]==-1) return u;
    return fa[u]=findroot(fa[u]);
}
void Union(int u,int v){
    u=findroot(u); v=findroot(v); //上能直接 fa[u]=v;
    fa[u]=v;
}
struct edge{
    int u,v,w;
    bool operator<(const edge& b) const {return w<b.w;}</pre>
} edges[maxm];
int kruskal(){
    memset(fa,-1,sizeof(fa));
    sort(edges,edges+m);
    int res=0;
    for(int i=0;i<m;++i){</pre>
        edge eg=edges[i];
        int u=eg.u,v=eg.v;
        if(findroot(u)==findroot(v)) continue;
        res+=eg.w;
        Union(u,v);
    }
    return res;
}
```

7 数论

7.1 进制转换

```
int idx(char ch){
    if(ch>='0'&&ch<='9') return ch-'0';
    if(ch \ge 'A' \&\&ch \le 'Z') return ch - 'A' + 10;
    if(ch>='a'&&ch<='z') return ch-'a'+10;
}
char ch(int x){
    if(x<10) return '0'+x;</pre>
    else return 'A'+x-10;
}
int toten(int b,char *s){
    int res=0;
    int n=strlen(s);
    for(int i=0;i<n;++i){</pre>
        int t=idx(s[i]);
        res=res*b+t;
    return res;
}
void tob(int x,int b,char *s){
    int i=0;
    char s1[10000];
    while(x){
        s1[i++]=ch(x\%b);
        x/=b;
    }
    for(int j=0;j<i;++j) s[j]=s1[i-1-j];</pre>
   if(i==0) s[i++]='0';
    s[i]=0;
}
7.2 gcd
int gcd(int a,int b){
    if(b==0) return a;
    return gcd(b,a%b);
}
int lcm(int a, int b)
{
        return a * b / gcd(a, b);
}
```

```
int exgcd(int a,int n,int &x,int &y){
    if(n==0) {x=1; y=0; return a;}
    int res= exgcd(n,a%n,y,x);
    y=x*(a/n);
    return res;
}
7.3 改进素数筛
#include <cstdio>
#include <cstring>
const int MAXN = 100000000;
bool flag[MAXN];
int primes[MAXN / 3], pi;
int main()
{
        int i, j;
        pi = 0;
        memset(flag, false, sizeof(flag));
        for (i = 2; i < MAXN; i++)</pre>
        {
                if (!flag[i])
                         primes[pi++] = i;
                for (j = 0; (j < pi) && (i * primes[j] <
                 \hookrightarrow MAXN); j++)
                {
                         flag[i * primes[j]] = true;
                         if (i % primes[j] == 0)
                                 break;
                }
    for (i = 0; i < pi; i++)
        printf("%d\n", primes[i]);
    return 0;
}
7.4 模线性方程
int modequ(int a,int b,int n){     //ax=b (mod n)
    int d=gcd(a,n);
    if(b\%d!=0) return -1;
    a/=d; b/=d; n/=d; n=abs(n); a'x=b \pmod{n}
    int x,y;
    exgcd(a,n,x,y);
```

```
//x=(a')^(-1)b'
    int p=x*b;
    return ((p\%n)+n)\%n;
}
     中国剩余定理
7.5
11 exgcd(ll a,ll b,ll &x,ll &y){
    if(b==0) {x=1; y=0; return a;}
    11 res=exgcd(b,a%b,y,x);
    y=x*(a/b);
    return res;
}
11 M;
ll china(int n,int *a,int *m){ // x=a_i \pmod{m_i} i=1,2,...n
    11 x,y,res=0;
    M=1;
    for(int i=0;i<n;++i) M*=m[i];</pre>
    for(int i=0;i<n;++i){</pre>
        ll w=M/m[i];
        exgcd(w,(11)m[i],x,y);
        res=(res+w*x*a[i])%M;
    }
    return (res+M)%M;
}
7.6
     快速幂
int pow_mod(ll a,ll p,ll n){
    if(a==0) return 0;
    if(p==0) return 1;
    ll tmp=pow_mod(a,p/2,n);
    tmp=tmp*tmp%n;
    if(p\%2) tmp=tmp*a\%n;
    return (int) tmp;
}
    字符串
8
8.1
     字典树
const int maxnode=100010,sigma_size=10;
struct trie{
    int ch[maxnode][sigma_size],val[maxnode];
    int sz;
```

```
void init(){
        sz=1;
        memset(ch[0],0,sizeof(ch[0]));
        memset(val,0,sizeof(val));
    trie(){init();}
    bool insert(char *s){
        int ok=1;
        int u=0,n=strlen(s);
        for(int i=0;i<n;++i){</pre>
           int c=s[i]-'0';
           if(!ch[u][c]){
              memset(ch[sz],0,sizeof(ch[sz]));
              ch[u][c]=sz++;
           }
           else{
               if(val[ch[u][c]]||i==n-1) ok=0;
           u=ch[u][c];
        }
        val[u]=1;
        return ok;
    }
} ;
8.2 KMP
int kmp(char *t,char *p){
    int n=strlen(t),m=strlen(p);
    int *next=new int[m];
    next[0] = -1;
    for(int i=1,k=-1;i<m;++i){</pre>
        while (k>=0 \&\&p[k+1]!=p[i]) k=next[k];
        if(p[k+1]==p[i]) ++k;
                         //k 保存的是 p[0,1...i] 的最长的同时
       next[i]=k;
        → 是前缀和后缀的,那个前缀的最后一个字符的下标
    }
    for(int i=0,k=-1;i<n;++i){</pre>
        while (k>=0 \&\&p[k+1]!=t[i]) k=next[k];
        if(p[k+1]==t[i]) ++k; //k 保存的是 p 中已经匹配的最后一
        → 个字符的下标
        if(k==m-1) return i-m+1;
    return -1; //不匹配
```

```
}
8.3 hash
const ull B=1000000007; //实在不行 可以用两个 hash 另外用 1e9+9
bool contatin(string a,string b){
    int la=a.length(),lb=b.length();
    if(la>lb) return 0;
    ull ha=0,hb=0,t=1;
    for(int i=0;i<la;++i){</pre>
        t*=B;
        ha=ha*B+a[i];
        hb=hb*B+b[i];
    }
    for(int i=0;i+la<=lb;++i){</pre>
        if(hb==hb) return 1;
        if(i+la<lb) hb=hb*B+b[i+la]-b[i]*t;</pre>
    return 0;
}
8.4 表达式计算
8.4.1 前缀表达式
#include<cstdlib>
#include<cstdio>
using namespace std;
char s[100];
double exp(){
    scanf("%s",s);
    char c=s[0];
    if(c=='+') return exp()+exp();
    else if(c=='-') return exp()-exp();
    else if(c=='*') return exp()*exp();
    else if(c=='/') return exp()/exp();
    else return atof(s);
}
int main(){
    printf("%f\n",exp());
}
```

```
//#include<cstdlib>
//#include<cstdio>
//#include<cstring>
//#include<string>
//#include<iostream>
//#include<queue>
//#include<stack>
//#include<sstream>
//using namespace std;
//typedef long long ll;
//stack<string> stk; //这个方法有问题
//string s,s1;
//bool isnum(string str){
     return (str.size()>1)||(str[0]>='0'&&str[0]<='9');
//
//}
//bool isop(string str){
//
      char op=str[0];
      return (op=='+'||op=='-'||op=='*'||op=='/'):
//
1/7
//double getres(double a, double b, string op){
//
      if(op[0]=='+') return a+b;
     if(op[0]=='-') return a-b;
//
     if(op[0]=='*') return a*b;
//
     else return a/b;
//}
//void calu(){
     while(stk.size()>=3){
//
         string s3, s2, s1;
//
//
          s3=stk.top(); stk.pop();
          s2=stk.top(); stk.pop();
//
//
          s1=stk.top(); stk.pop();
          if(isnum(s3)&&isnum(s2)&&isop(s1)){
//
//
              double a=stod(s2), b=stod(s3);
              stk.push(to_string(getres(a,b,s1)));
//
//
//
              stk.push(s1); stk.push(s2); stk.push(s3);
//
              break;
//
          }
     }
//
//}
//int main(){
//
     while(getline(cin,s)){
          stringstream ss(s);
//
//
          while(stk.size()) stk.pop();
```

```
//
          while(ss>>s1){
//
              stk.push(s1);
//
              calu();
//
//
          printf("%f\n",stod(stk.top()));
      7
//
//
      return 0;
//}
8.4.2 中缀表达式
char s[610];
stack<char> ops;
stack<int> num;
int calu(int a,int b,char op){
    if(op=='+') return a+b;
    if(op=='-') return a-b;
    if(op=='*') return a*b;
    if(op=='/') return a/b;
    return -10000000;
}
bool higher(char op1,char op2){
    if(op2=='(') return 1;
    if((op1=='*'||op1=='/')&&(op2=='+'||op2=='-')) return 1;
    return 0;
}
int solve(){
    while(ops.size())
                         ops.pop();
    while(num.size()) num.pop();
    int n=strlen(s);
    for(int i=0;i<n;++i){</pre>
        if(s[i]=='(') ops.push(s[i]);
        else if(s[i] >= '0' \&\&s[i] <= '9'){
            int x=s[i]-'0';
            while (i+1 < n \&\&s [i+1] > = '0' \&\&s [i+1] < = '9') {
                ++i;
                x=x*10+s[i]-'0';
            }
            num.push(x);
        }else if(s[i]==')'){
           while(ops.size()&&ops.top()!='('){
               int b,a;
               b=num.top(); num.pop();
               a=num.top(); num.pop();
```

```
num.push(calu(a,b,ops.top()));
                ops.pop();
           }
           if(ops.size()&&ops.top()=='(') ops.pop();
        }else{
             char op1=s[i];
             while(ops.size()&&!higher(op1,ops.top())){
                 int b,a;
                b=num.top(); num.pop();
                a=num.top(); num.pop();
                num.push(calu(a,b,ops.top()));
                ops.pop();
            }
             ops.push(op1);
        }
    }
    return num.top();
}
     find longest shortest word
char s[210];
const int inf=10000;
bool isala(char c){ //is alaphabet
     return (c>='a'&&c<='z')||(c>='A'&&c<='Z');
}
void find_longest_shortest_word(){
    int n=strlen(s);
    int l=0,r=0,lmin,rmin,lmax,rmax;
    lmin=-1; rmin=inf;
    lmax=-1; rmax=-inf;
    while(1<n){
        while (1 \le n \& \& ! isala(s[1])) ++1;
        if(l==n) break;
        r=1+1;
        while(r<n&&isala(s[r])) ++r;</pre>
        s[r]=0;
        if(r-l<rmin-lmin) {lmin=l; rmin=r; }</pre>
        if(r-l>=rmax-lmax){lmax=l; rmax=r;}
        l=r+1;
    }
    if(lmax<0) printf("\n");</pre>
    else printf("%s\n",s+lmax);
    if(lmin<0) printf("\n");</pre>
```

```
else printf("%s\n",s+lmin);
}
void find_longest_shortest_word(string s){
    stringstream ss;
    for(int i=0;i<s.size();++i)</pre>
        if(!isala(s[i])) s[i]=' ';
        ss.clear();
    ss.str(s);
    string Max="",Min(inf,'a');
    string t;
    while(ss>>t){
        if(t.size()>=Max.size()) Max=t;
        if(t.size()<Min.size())</pre>
                                     Min=t;
    }
    cout<<Max<<endl;</pre>
    cout<<Min<<endl;</pre>
}
9
    bigint
const int maxn=210;
struct bigint{
        int dig[maxn];
        bigint(string s=""){
                 memset(dig,0,sizeof(dig));
                 if(s.size()==0) {
                         dig[0]=1;
                         dig[1]=0;
                         return ;
                 }
                 int k,i;
                 for(i=s.length()-1,k=0;i>=0;--i){
                         dig[++k]=s[i]-'0';
                 dig[0]=k;
        }
        void print(){
                 for(int i=dig[0];i>0;--i){
                         if(dig[i]==0&&dig[0]>1) --dig[0];
                         else break;
                 }
                 for(int i=dig[0];i;--i) printf("%d",dig[i]);
```

```
bigint operator+(const bigint &b)const {
                 bigint c;
                 c.dig[0]=max(dig[0],b.dig[0]);
                 for(int i=1;i<=c.dig[0];++i){</pre>
                          if(i<=dig[0]) c.dig[i]+=dig[i];</pre>
                          if(i<=b.dig[0]) c.dig[i]+=b.dig[i];</pre>
                 }
                 int x=0,i=1;
                 while(x||i<=c.dig[0]){
                          x+=c.dig[i];
                          c.dig[i]=x\%10;
                          x/=10;
                          ++i;
                 }
                 c.dig[0]=i-1;
                 return c;
        bigint operator*(const bigint& b)const{
                 bigint c;
                 c.dig[0] = dig[0] + b.dig[0] - 1;
                 for(int i=1;i<=dig[0];++i){</pre>
                          for(int j=1;j<=b.dig[0];++j){</pre>
                                   c.dig[i+j-1]+=dig[i]*b.dig[j];
                          }
                 }
                 int x=0,i=1;
                 while(i<=c.dig[0]||x){
                          x+=c.dig[i];
                          c.dig[i]=x%10;
                          x/=10;
                          ++i;
                 }
                 c.dig[0]=i-1;
                 return c;
        }
};
```