

2-6 Notes

Ratios and Proportions

Example 1: Determine whether the ratios $\frac{24}{36}$ and $\frac{12}{18}$ are equivalent ratios. Write *yes* or *no*. Justify your answer.

$$\frac{24}{36} = \frac{2}{3}$$

$$\frac{12}{18} = \frac{2}{3}$$

yes! both reduce to $\frac{2}{3}$

Exercises

Determine whether each pair of ratios are equivalent ratios. Write *yes* or *no*.

1. $\frac{1}{2}, \frac{16}{32}$

yes! $\frac{16}{32} = \frac{1}{2}$

2. $\frac{5}{8}, \frac{10}{15}$

no!
 $\frac{10}{15} = \frac{2}{3}$

3. $\frac{10}{20}, \frac{25}{49}$

$\frac{10}{20} = \frac{1}{2}$ *$\frac{25}{49}$ already reduced*
no

Means-Extremes Property of Proportions

For any numbers a, b, c , and d , if $\frac{a}{b} = \frac{c}{d}$, then $ad = bc$.

Example: Solve $\frac{x}{5} = \frac{10}{13}$.

$13x = 5(10)$
 $13x = 50$

$x = \frac{50}{13}$

Solve each proportion. If necessary, round to the nearest hundredth.

1. $\frac{-3}{x} = \frac{2}{8}$

$-24 = 2x$
 $-12 = x$

2. $\frac{4}{b-2} = \frac{4}{12}$

$12(4) = 4(b-2)$
 $48 = 4b - 8$
 $+8$
 $\frac{56}{4} = \frac{4b}{4}$
 $b = 14$

3. $\frac{1.5}{x} = \frac{12}{x}$

$1.5x = 12x$

no solution!

$x = 0$ will not work in denominator
undefined!

Use a proportion to solve each problem.

10. **MODELS** To make a model of the Guadeloupe River bed, Hermie used 1 inch of clay for 5 miles of the river's actual length. His model river was 50 inches long. How long is the Guadeloupe River?

$\frac{1''}{5 \text{ mi}} = \frac{50''}{x \text{ mi}}$

$1x = 5(50)$

$x = 250$
miles long

11. **EDUCATION** Josh finished 24 math problems in one hour. At that rate, how many hours will it take him to complete 72 problems?

$\frac{24}{1 \text{ hr}} = \frac{72}{x \text{ hrs}}$

$\frac{24x}{24} = \frac{72}{24}$

$x = 3 \text{ hrs}$

2-7 Percent of Change

Percent of Change When an increase or decrease in an amount is expressed as a percent, the percent is called the **percent of change**. If the new number is greater than the original number, the percent of change is a **percent of increase**. If the new number is less than the original number, the percent of change is the **percent of decrease**.

Example 1: Find the percent of increase.

original: 30

new: 66

Step 1: find the amount of change 36

Step 2: find the percent of increase by dividing amount of change by original number.

$$\frac{36}{30} = 1.2 \text{ or } 120\% \text{ increase}$$

Example 2: Find the percent of decrease.

new: 22 original: 48

step 1: $48 - 22 = 26$

step 2: $\frac{26}{48} = 54.17\%$

Exercises

State whether each percent of change is a percent of *increase* or a percent of *decrease*. Then find each percent of change. Round to the nearest whole percent.

1. original: 50
new: 80

$$\frac{30}{50} = .6 = 60\% \text{ increase}$$

2. original: 90
new: 100

$$\frac{10}{90} = .111 = 11.1\% \text{ increase}$$

3. original: 45
new: 20

$$\frac{25}{45} = .555 = 55.6\% \text{ decrease}$$

4. **VIDEOS** The original selling price of a new sports video was \$65.00. Due to the demand the price was increased to \$87.75. What was the percent of increase over the original price?

$$\frac{87.75 - 65}{65} = \frac{22.75}{65} = .35 = 35\% \text{ increase}$$

5. **SCHOOL** A high school paper increased its sales by 75% when it ran an issue featuring a contest to win a class party. Before the contest issue, 10% of the school's 800 students bought the paper. How many students bought the contest issue?

$$10\% \text{ of } 800 = \frac{1}{10}(800) = 80$$

$$\text{increase } 75\% \text{ of } 80 = .75(80) = 60 \text{ more sales}$$

$$80 + 60 = 140 \text{ students}$$

6. **BASEBALL** Baseball tickets cost \$15 for general admission or \$20 for box seats. The sales tax on each ticket is 8%. What is the final cost of each type of ticket,

$$15(1.08) = \$16.20$$

$$20(1.08) = \$21.60$$