

2-8 Notes (continued)**Dimensional Analysis**

Use dimensional analysis to convert each rate. Show all of your work and draw a line through the units that cancel.

RUNNING A 10K run is 10 kilometers long. If 1 meter = 1.094 yards, use dimensional analysis to find the length of the race in miles.

(Hint: 1 mi = 1760 yd)

$$\begin{array}{c}
 \text{length} \\
 \text{of run}
 \end{array}
 \times
 \begin{array}{c}
 \text{kilometers} \\
 \text{to meters}
 \end{array}
 \times
 \begin{array}{c}
 \text{meters} \\
 \text{to yards}
 \end{array}
 \times
 \begin{array}{c}
 \text{yards} \\
 \text{to miles}
 \end{array}
 =
 \begin{array}{c}
 10 \cancel{\text{km}} \\
 1 \text{ run}
 \end{array}
 \cdot
 \frac{1000 \cancel{\text{meters}}}{1 \cancel{\text{km}}}
 \cdot
 \frac{1.094 \text{ yds}}{1 \cancel{\text{meter}}}
 \cdot
 \frac{1 \text{ mile}}{1760 \cancel{\text{yds}}}
 =
 \frac{6.2 \text{ miles}}{1 \text{ run}}$$

Exercises

1. Convert 13 feet per second to miles per hour.

$$\frac{13 \cancel{\text{ft}}}{1 \cancel{\text{sec}}} \cdot \frac{3600 \cancel{\text{sec}}}{1 \text{ hr}} \cdot \frac{1 \text{ mile}}{5280 \cancel{\text{ft}}} =$$

$$\frac{8.86 \text{ miles}}{1 \text{ hr}}$$

2. Convert 40 miles per hour to feet per second.

$$\frac{40 \cancel{\text{miles}}}{1 \cancel{\text{hr}}} \cdot \frac{1 \cancel{\text{hr}}}{3600 \cancel{\text{sec}}} \cdot \frac{5280 \cancel{\text{ft}}}{1 \cancel{\text{mile}}} =$$

$$\frac{58.67 \text{ feet}}{1 \text{ sec}}$$

3. Convert 150 yards per minute to feet per day.

$$\frac{150 \cancel{\text{yds}}}{1 \cancel{\text{min}}} \cdot \frac{3 \cancel{\text{feet}}}{1 \cancel{\text{yd}}} \cdot \frac{60 \cancel{\text{min}}}{1 \cancel{\text{hr}}} \cdot \frac{24 \cancel{\text{hrs}}}{1 \text{ day}} =$$

$$\frac{648,000 \text{ feet}}{1 \text{ day}}$$

4. A car travels a distance of 100 feet in about 2.8 seconds. What is the velocity of the car in miles per hour? Round to the nearest whole number.

$$\frac{100 \cancel{\text{ft}}}{2.8 \cancel{\text{sec}}} \cdot \frac{1 \text{ mile}}{5280 \cancel{\text{ft}}} \cdot \frac{3600 \cancel{\text{sec}}}{1 \text{ hr}} =$$

$$\frac{24.35 \text{ miles}}{1 \text{ hr}}$$

5. A person is walking at a rate of 160 feet per minute. Use dimensional analysis to find the speed at feet per second.

$$\frac{160 \text{ ft}}{1 \text{ min}} \cdot \frac{1 \text{ min}}{60 \text{ sec}} = \frac{2.67 \text{ ft}}{\text{sec}}$$

6. Convert 3.82 meters per second to kilometers per hour.

$$\frac{3.82 \text{ m}}{1 \text{ sec}} \cdot \frac{1 \text{ km}}{1000 \text{ m}} \cdot \frac{60 \text{ sec}}{1 \text{ min}} \cdot \frac{60 \text{ min}}{1 \text{ hr}} = \frac{13.752 \text{ km}}{1 \text{ hr}}$$

7. Convert 15 miles per hour to inches per second.

$$\frac{15 \text{ miles}}{1 \text{ hr}} \cdot \frac{1 \text{ hr}}{60 \text{ min}} \cdot \frac{1 \text{ min}}{60 \text{ sec}} \cdot \frac{5280 \text{ ft}}{1 \text{ mile}} \cdot \frac{12 \text{ in}}{1 \text{ ft}} = \frac{264 \text{ inches}}{1 \text{ sec}}$$

8. Falcons can dive at speeds of up to 318 feet per second. Convert this speed to miles per hour.

$$\frac{318 \text{ ft}}{1 \text{ sec}} \cdot \frac{1 \text{ mile}}{5280 \text{ ft}} \cdot \frac{60 \text{ sec}}{1 \text{ min}} \cdot \frac{60 \text{ min}}{1 \text{ hr}} = \frac{216.82 \text{ miles}}{1 \text{ hr.}}$$

9. A cyclist travels 56 miles in 4 hours. What is the cyclist's speed in feet per minute?

$$\frac{56 \text{ miles}}{4 \text{ hrs}} \cdot \frac{1 \text{ hr}}{60 \text{ min}} \cdot \frac{5280 \text{ ft}}{1 \text{ mile}} = \frac{1232 \text{ feet}}{1 \text{ min.}}$$