

Key

6-6 Notes

Systems of Inequalities

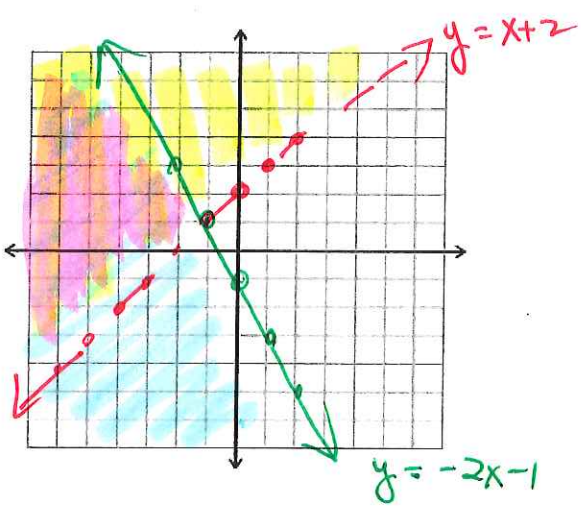
[shaded] = solution

Systems of Inequalities The solution of a **system of inequalities** is the set of all ordered pairs that satisfy both inequalities. If you graph the inequalities in the same coordinate plane, the solution is the region where the graphs overlap.

Example 1:
Solve the system of inequalities by graphing

$$y > x + 2$$

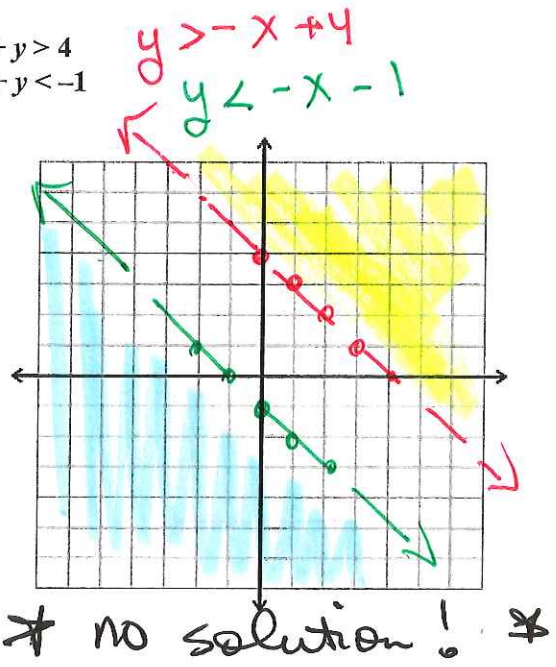
$$y \leq -2x - 1$$



Example 2:
Solve the system of inequalities by graphing.

$$x + y > 4$$

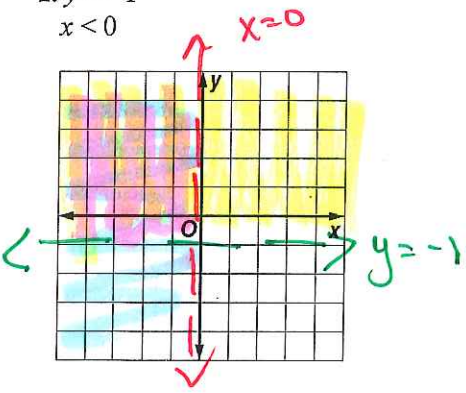
$$x + y < -1$$



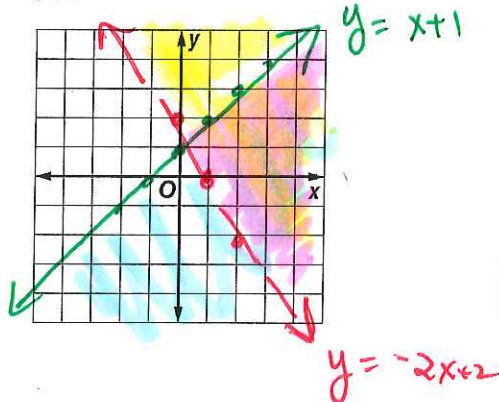
Exercises

Solve each system of inequalities by graphing. Give two ordered pairs that are solutions and two that are not solutions.

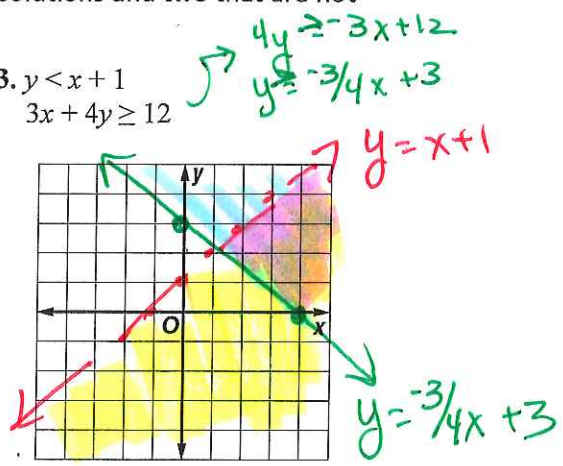
1. $y > -1$
 $x < 0$



2. $y > -2x + 2$
 $y \leq x + 1$



3. $y < x + 1$
 $3x + 4y \geq 12$



[shaded] = solution:
overlapping shaded
blue & yellow regions.

7. Business: AAA Gem Company produces necklaces and bracelets. In a 40-hour week, the company has 400 gems to use. A necklace requires 40 gems and a bracelet requires 10 gems. It takes 2 hours to produce a necklace and a bracelet requires one hour. How many of each type can be produced in a week?

Let n = the number of necklaces that will be produced
 b = the number of bracelets that will be produced.

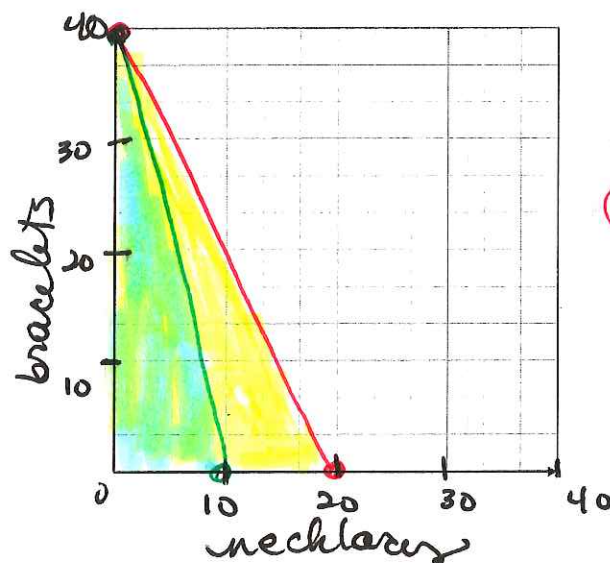
$$2n + 1b \leq 40$$

$$40n + 10b \leq 400$$

graph with intercepts

$$\begin{aligned} 2n + 1b &\leq 40 \\ 40n &= 400 \quad 1b = 40 \\ n &= 20 \quad b = 40 \end{aligned}$$

$$\begin{aligned} 40n + 10b &\leq 400 \\ 40n &= 400 \quad 10b = 400 \\ n &= 10 \quad b = 40 \end{aligned}$$



multiple answers - $\frac{\text{Intercepts}}{(0, 40)}$ max of 40 bracelets & no necklaces
 $(10, 0)$ max of 10 necklaces & no bracelets

8. RECREATION Maria had \$150 in gift certificates to use at a record store. She bought fewer than 20 recordings. Each tape cost \$5.95 and each CD cost \$8.95. How many of each type of recording might she have bought?

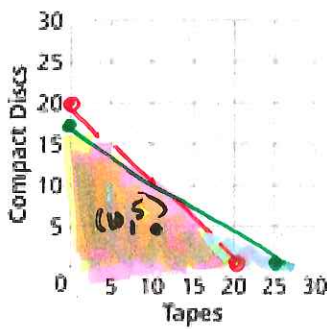
let x = tapes
 let y = CD's

$$\begin{aligned} x + y &\leq 20 \\ 5.95x + 8.95y &\leq 150 \end{aligned}$$

Graph w/ intercepts

$$\begin{aligned} x + y &\leq 20 \\ x &= 20 \quad y = 20 \end{aligned}$$

$$\begin{aligned} 5.95x + 8.95y &\leq 150 \\ 5.95x &= 150 \quad 8.95y = 150 \\ x &= 25 \quad y = 16 \end{aligned}$$



Any solution in pink region

$(10, 5)$
 10 tapes & 5 CD's
 etc.

Chapter 6
 ex: 20 tapes & no CD's
 16 CD's & no tapes