2-9 Weighted Averages

Mixture Problems Mixture Problems are problems where two or more parts are combined into a whole. They involve weighted averages. In a mixture problem, the weight is usually a price or a percent of something.

Weighted Average	The weighted average M of a set of data is the sum of the product of each number in the set and its weight divided by the sum of all the weights.

Example: COOKIES Delectable Cookie Company sells chocolate chip cookies for $6.95 per pound and white chocolate cookies for $5.95 per pound. How many pounds of chocolate chip cookies should be mixed with 4 pounds of white chocolate cookies to obtain a mixture that sells for $6.75 per pound.

Let w = the number of pounds of chocolate chip cookies

$$6.95x + 5.95(4) = 6.75(x+4)$$
$$6.95x + 23.8 = 6.75x + 27$$
$$6.95x = 6.75x + 3.2$$
$$-6.75x \quad -6.75x$$
$$\frac{.2x}{.2} = \frac{3.2}{.2} \quad x = 16$$

	Number of Pounds	Price per Pound	Total Price
Chocolate Chip	x	6.95	$6.95x$
White Chocolate	4	5.95	$5.95(4)$
Mixture	$x+4$	6.75	$6.75(x+4)$

$x = 16$ pounds choc. chips should be mixed w/ 4 lbs of white choc.

Exercises

1. SOLUTIONS How many grams of sugar must be added to 60 grams of a solution that is 32% sugar to obtain a solution that is 50% sugar?

$$.32(60) + 1(x) = .5(60+x)$$

$100\% = 1$

$32\% = .32$

$50\% = .5$

$$19.2 + x = 30 + .5x$$
$$-.5x \qquad -.5x$$
$$19 + .5x = 30$$

$$\frac{.5x}{.5} = \frac{11}{.5}$$

$$\boxed{x = 22}$$

22 gms of pure sugar needs to be added.

2. NUTS The Quik Mart has two kinds of nuts. Pecans sell for $1.55 per pound and walnuts sell for $1.95 per pound. How many pounds of walnuts must be added to 15 pounds of pecans to make a mixture that sells for $1.75 per pound?

$$1.55(15) + 1.95x = 1.75(15+x)$$
$$23.25 + 1.95x = 26.25 + 1.75x$$
$$-1.75x \qquad\qquad -1.75x$$
$$23.25 + .2x = 26.25$$

$$\frac{.2x}{.2} = \frac{3}{.2}$$

$$x = 15$$

15 lbs walnuts added to 15 lbs pecans

4. MILK Whole milk is 4% butterfat. How much skim milk with 0% butterfat should be added to 32 ounces of whole milk to obtain a mixture that is 2.5% butterfat?

$4\% = .04$

$2.5\% = .025$

let x = 0% skim milk

let y = # oz mixed or $x+32$

$$x + 32 = y$$

$$0 + .04(32) = .025y$$
$$0 + .04(32) = .025(x+32)$$
$$1.28 = .025x + .8$$
$$-.8 \qquad\qquad -.8$$
$$\frac{.48}{.025} = \frac{.025x}{.025}$$

$$\boxed{x = 19.2 \text{ oz } 0\% \text{ milk}}$$

2-9 *(continued)*
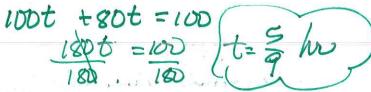
Uniform Motion Problems

Uniform Motion Problems Motion problems are another application of weighted averages. **Uniform motion problems** are problems where an object moves at a certain speed, or rate. Use the formula $d = rt$ to solve these problems, where d is the distance, r is the rate, and t is the time.

Example: DRIVING Bill Gutierrez drove at a speed of 65 miles per hour on an expressway for 2 hours. He then drove for 1.5 hours at a speed of 45 miles per hour on a state highway. What was his average speed?
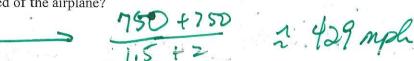
$$\frac{65(2) + 45(1.5)}{3.5 \text{ hrs}} = 56.4 \text{ mph}$$

Exercises

1. TRAVEL Mr. Anders and Ms. Rich each drove home from a business meeting. Mr. Anders traveled east at 100 kilometers per hour and Ms. Rich traveled west at 80 kilometers per hours. In how many hours were they 100 kilometers apart.

$d = rt$ $100t + 80t = 100$

$$\frac{180t}{180} = \frac{100}{180} \qquad t = \frac{5}{9} \text{ hr}$$

2. AIRPLANES An airplane flies 750 miles due west in $1\frac{1}{2}$ hours and 750 miles due south in 2 hours. What is the average speed of the airplane?

$$\frac{750 + 750}{1.5 + 2} \approx 429 \text{ mph}$$

5. CYCLING Two cyclists begin traveling in the same direction on the same bike path. One travels at 15 miles per hour, and the other travels at 12 miles per hour. When will the cyclists be 10 miles apart?

$d_1 = 15t$ difference $= 10$ miles $3t = 10$

$d_2 = 12t$ $15t - 12t = 10$ $t = 3\frac{1}{3}$ hrs

6. TRAINS Two trains leave Chicago, one traveling east at 30 miles per hour and one traveling west at 40 miles per hour. When will the trains be 210 miles apart?

$40t \quad 30t$ $30t + 40t = 210$ miles

$$\frac{70t}{70} = \frac{210}{70} \qquad t = 3 \text{ hours}$$