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Recursion

A recursive function is one that calls itself.

e.g.

```
1 void print () {
```

```
2
```

```
3     cout << mess "This is infinite recursion aka Stack  
4         overflow" << endl;
```

```
5
```

```
6     print ();
```

```
7 }
```

The above code will print the message infinite times because there is no condition to stop it. This condition is called a **base case**:

eg.

```
1 void print (int n) {
```

```
2
```

```
3
```

```
4
```

```
5
```

```
6
```

```
7
```

```
8 }
```

```
void print (int n) {  
cout << "This will stop" << endl;
```

```
return;
```

```
if (n <= 0) {
```

```
    return; }
```

```
    cout << "This will stop" << endl;
```

```
    print (n-1);
```

```
}
```

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For $n=5$, the message will be printed 5 times.

Properties of recursion:

- It must have a base case
- The recursive must change state and move towards base case.
- The recursive function must call itself

Using stack to show recursion.

- It is always a good idea to ~~make~~ make a stack and understand what is really happening.

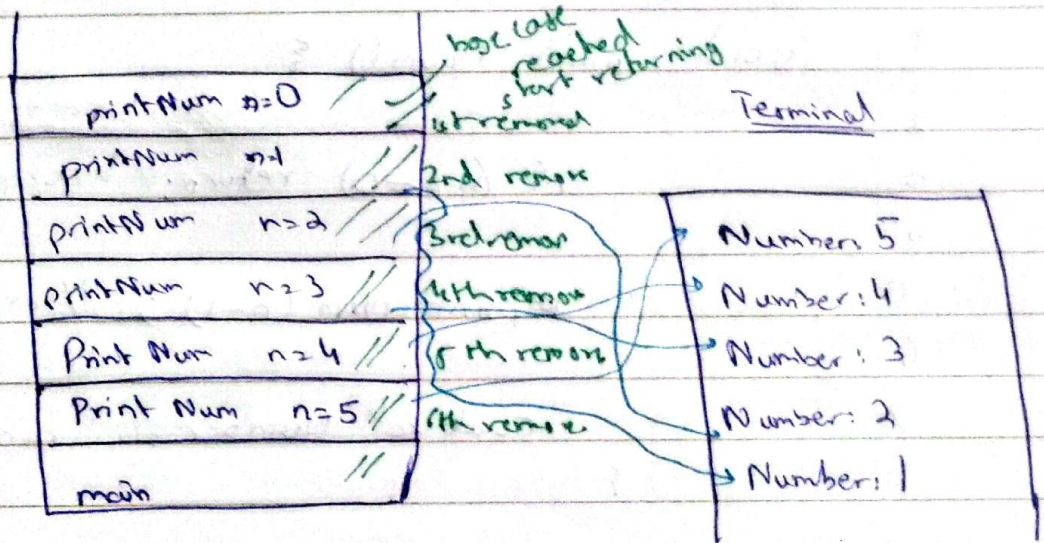
1)

```
void printNum(int n) {  
    if (n <= 0) return; // base case  
    cout << "Number: " << n << endl;  
    printNum(n-1); // recursive case  
}
```


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for $n = 5$



In this case we can see that whenever a case is called, the statement is printed with it. This is case of First in, first out.

— whatever come in first printed it's content come out first.

There can also be another case. First in, last out. SEE NEXT PAGE.

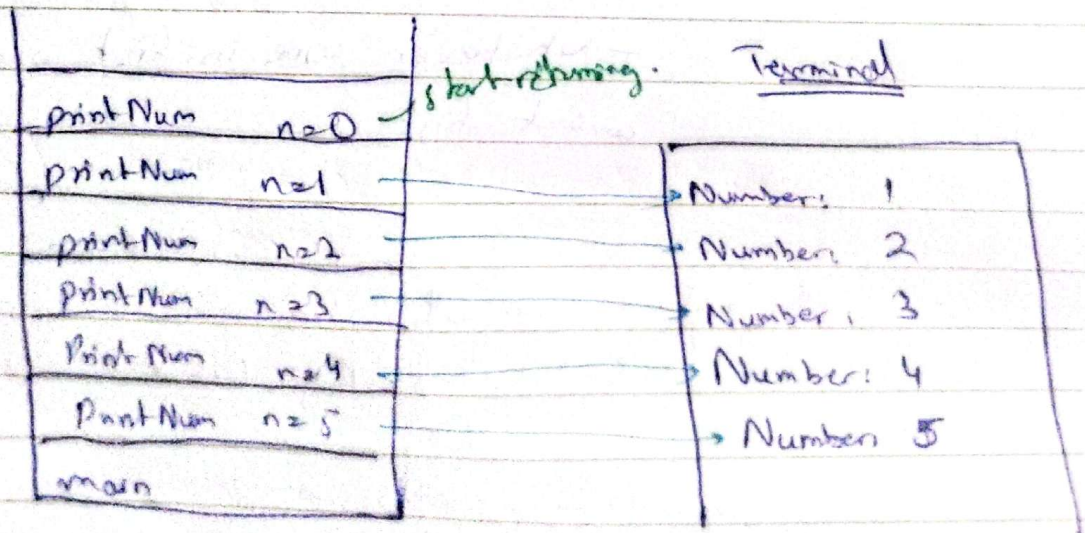
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```
1 void print Num() {  
2  
3     if (n == 0) return; // base case  
4  
5     print Num (n-1); // recursive case  
6  
7     cout << "Number: " << n << endl;  
8 }
```

- Now in this Program the statement comes after recursive case.



This is an example of First in, last out

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Now? let's see a simpler version for $n=4$, $n=0$.

```
void printNum(int n) {  
    if (n > 0) return;
```

```
    printNum(n-1); # This line ends as we have returned. now go to next line
```

```
    cout << "Number: " << n << endl;
```

- $n=1$ & 0 it is printed.

```
}
```

- when we go on $n=0$, we return and go back to $\text{print}^{\text{num}}(1)$ where $n=1$.

- when $n=0$ returns, the $\text{printNum}(1)$ does its job and ends and we go to next line and the statement is printed.

- Then after this line Number: 1 is printed the function ends and in stack we can see that we go back to $n=2$ or $\text{printNum}(2)$ and this will now print this continues like this.

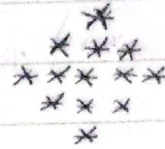
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2) Using both cases; Printing a diamond:

e.g for $n=3$:



```
void spaces (int n, int max) { // helper func
```

```
    if (n == max) { // A case so that no extra spaces  
        return; // at end are printed.  
    }
```

```
    if (n <= 0) { return }; // True base cases
```

```
    cout << "  ";
```

```
    spaces (n-1, max);
```

```
}
```

```
void triangle (int max, int n) { // helper function
```

```
    if (n >= max)
```

```
    { return; }
```

```
    cout << " * ";
```

```
    triangle (max, n+1);
```

```
}
```

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```
void printPattern (int n, int max) {
```

```
    if (n <= 0) return;
```

```
    spaces (n-1, max);
```

```
    triangle (max, n-1);
```

```
    triangle (max, n);
```

```
    cout << endl;
```

First in
First out
Upper half

```
    printPattern (n-1, max);
```

```
    spaces (n, max);
```

```
    triangle (max, n);
```

```
    triangle (max, n+1);
```

```
    if (n != max) {
```

```
        cout << endl;
```

```
    }
```

```
}
```

First in
last out.
lower half.

Yousaf