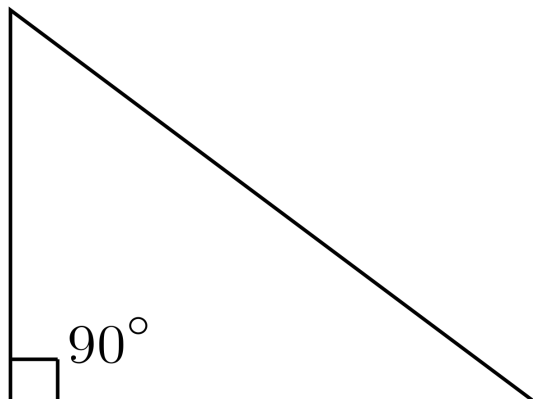


# Right Triangles

**Right Triangle:** A right triangle is a type of triangle that has one angle that measures  $90^\circ$ . Right triangles, and the relationships between their sides and angles, are the basis of trigonometry.

In a right triangle, the side that is opposite of the  $90^\circ$  angle is the longest side of the triangle, and is called the hypotenuse. The sides of a right triangle are commonly referred to with the variables  $a$ ,  $b$ , and  $c$ , where  $c$  is the hypotenuse and  $a$  and  $b$  are the lengths of the shorter sides. Their angles are also typically referred to using the capitalized letter corresponding to the side length: angle  $A$  for side  $a$ , angle  $B$  for side  $b$ , and angle  $C$  (for a right triangle this will be  $90^\circ$ ) for side  $c$ .  $h$  refers to the altitude of the triangle, which is the length from the vertex of the right angle of the triangle to the hypotenuse of the triangle. The altitude divides the original triangle into two smaller, similar triangles that are also similar to the original triangle.



## Special Right Triangles

### **$30^\circ$ $60^\circ$ $90^\circ$ triangle:**

The  $30^\circ$ - $60^\circ$ - $90^\circ$  refers to the angle measurements in degrees of this type of special right triangle. In this type of right triangle, the sides corresponding to the angles  $30^\circ$   $60^\circ$   $90^\circ$  follow a ratio of  $1:\sqrt{3}:2$ . Thus, in this type of triangle, if the length of one side and the side's corresponding angle is known, the length of the other sides can be determined using the above ratio. For example, given that the side corresponding to the  $60^\circ$  angle is 5, let  $a$  be the length of the side corresponding to the  $30^\circ$  angle,  $b$  be the length of the  $60^\circ$  side, and  $c$  be the length of the  $90^\circ$  side.

Knowing just one side of a  $30^\circ$   $60^\circ$   $90^\circ$  triangle enables you to determine the length of any of the other sides relatively easily. This type of triangle can be used to evaluate trigonometric functions for multiples of  $\pi/6$ .

### **$45^\circ$ $45^\circ$ $90^\circ$ triangle:**

The  $45^\circ$ - $45^\circ$ - $90^\circ$  triangle, also referred to as an isosceles right triangle, since it has two sides of equal lengths, is a right triangle in which the sides corresponding to the angles,  $45^\circ$   $45^\circ$   $90^\circ$ , follow a ratio of  $1:1:\sqrt{2}$ . Like the  $30^\circ$   $60^\circ$   $90^\circ$  triangle, knowing one side length allows you to determine the lengths of the other sides of a  $45^\circ$   $45^\circ$   $90^\circ$  triangle.

$45^\circ$   $45^\circ$   $90^\circ$  triangles can be used to evaluate trigonometric functions for multiples of  $\pi/4$ .