

Course: ECON 613

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Date: 02/04/2022

Project: Assignment 2

Exercise 1 OLS estimate

- Calculate the correlation between Y and X.

The correlation between Y and X is 0.143492.

- Calculate the coefficients on this regression.

The coefficient is 230.9923.

- Calculate the standard errors of β

The standard error is 509.2344.

```
Residuals:
    Min       1Q   Median       3Q      Max
-37130 -10653  -2196   6030 361786

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) 14141.18    645.23   21.92  <2e-16 ***
age          230.99     14.88   15.53  <2e-16 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 19480 on 11467 degrees of freedom
Multiple R-squared:  0.02059,    Adjusted R-squared:  0.0205
F-statistic: 241.1 on 1 and 11467 DF,  p-value: < 2.2e-16
```

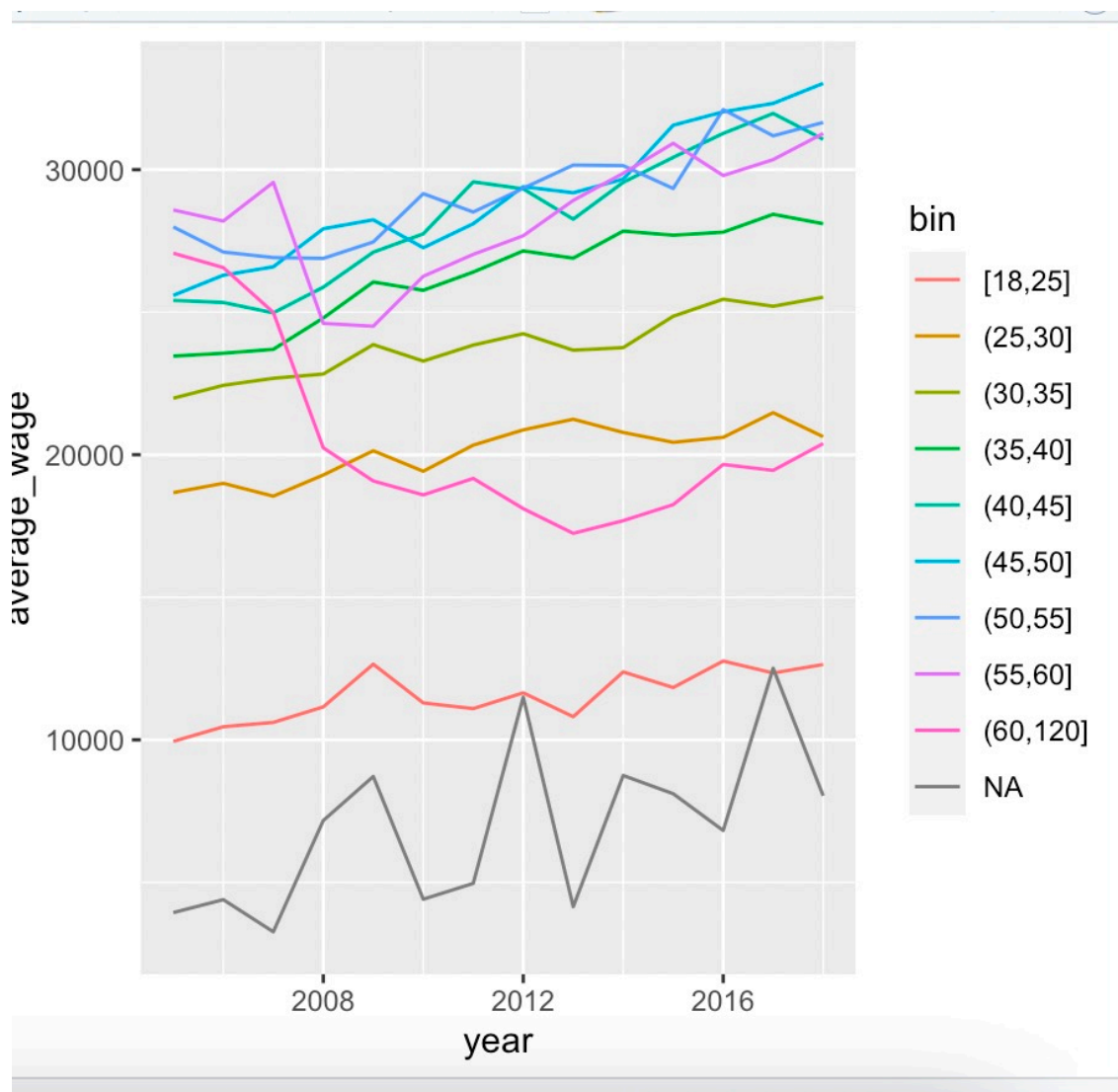
The two strategies give similar results. The accuracy increases when the number of bootstrap increases.

Exercise 2 Detrend Data

- Create a categorical variable `ag`, which bins the age variables into the following groups: “18-25”, “26- 30”, “31-35”, “36-40”, “41-45”, “46-50”, “51-55”, “56-60”, and “60+”.

Presented in R programming.

- Plot the wage of each age group across years. Is there a trend?



The wage increases when people get older, and the average wage level increases through time.

- Consider $Y_{it} = \beta X_{it} + \gamma_t + e_{it}$. After including a time fixed effect, how do the estimated coefficients change?

After including a time fixed effect, the estimated coefficient of age becomes larger.

Exercise 3 Numerical Optimization

- Exclude all individuals who are inactive.

Presented in R programming

- Write a function that returns the likelihood of the probit of being employed. You might want to write $X\beta$ first. Then, calculate $F(X\beta)$ and the log likelihood. Remember, for the probit model, $F(x)$ is the standard normal distribution function.

Presented in R programming

- Optimize the model and interpret the coefficients. You can use pre-programmed optimization packages.

```
      V1      V2      V3
55 1.087762 0.01320048 2079.099
```

From the output, we can see that the age coefficient is positive, implying that age has a positive effect for labors to be employed.

- Can you estimate the same model including wages as a determinant of labor market participation? Explain

No, I can't estimate the same model when including wages as a determinant.

Because unemployed people have no wage, and this would influence our outcome.

Exercise 4 Discrete choice

- Exclude all individuals who are inactive.

Presented in R programming

- Write and optimize the probit, logit, and the linear probability models.

Remember, for the logit model, $F(x)$ is the logistic function $\frac{\exp(x)}{1+\exp(x)}$

Presented in R programming

- Interpret and compare the estimated coefficients. How significant are they?

```
> output5[which.max(output5$V5 == min(output5$V5)), ]
      V1      V2      V3      V4      V5
3 -4.151691  8.271051  6.096356  3.766964 79563.63
```

```
> output6[which.max(output6$V5 == min(output6$V5)), ]
      V1      V2      V3      V4      V5
2 -7.712691  0.3578611  8.198586  6.674762 79563.63
```

```
> output7[which.max(output7$V5 == min(output7$V5)), ]
      V1      V2      V3      V4      V5
1 9.786648 6.747987 9.446685 1.54806 79563.63
> |
```

In all methods, age appeared to have positive and significant effects.

Exercise 5 Marginal Effects

- Compute the marginal effect of the previous probit and logit models.
- Construct the standard errors of the marginal effects.

```
> m_probit(fun <- empstat2 ~ age2 + year, data <- datind_05_to_15)
      Marginal Effect      SE
(Intercept) -8.9274778376 2.237966e-01
age2         0.0003351427 1.342062e-07
year         0.0044732472 1.113388e-04
> |
```

```
> m_logit(formula = empstat2 ~ age2 + year, data = datind_05_to_15)
      Marginal Effect      SE
(Intercept) -1.055478e+01 2.109887e-01
age2         3.668174e-04 9.415952e-08
year         5.276457e-03 1.049657e-04
~ |
```