

# MCC125 Wireless Link Project 2021- Software design

## In the Tx

- ✓ Data to symbols
- ✓ Construct the frame
- ✓ Up-sampling
- ✓ Filtering
- ✓ To the DAC (the USRP)
- ✓ Up-conversion (0-50 MHz)
- ✓ To the Transmitter HW

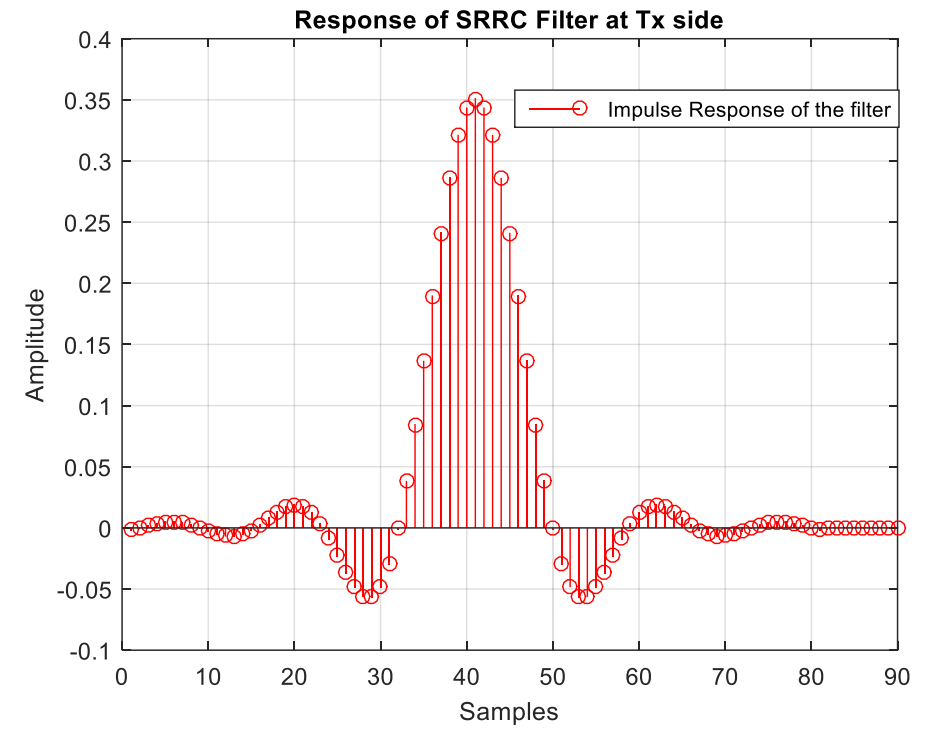
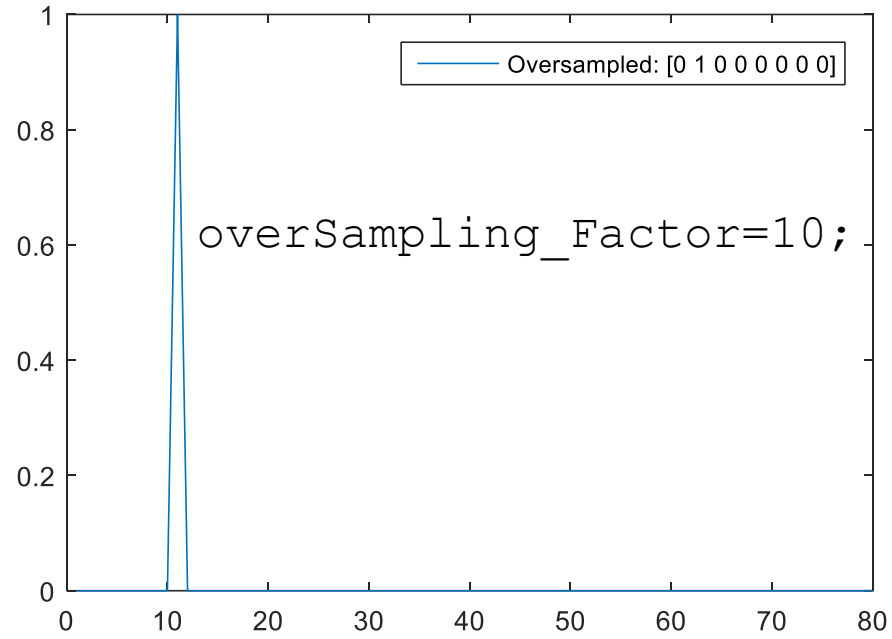
## In the Rx

- ✓ Samples received from the USRP
- ✓ Down-conversion to baseband (perhaps together with coarse frequency correction?)
- ✓ Detection of message
- ✓ Filtering
- ✓ Down sampling + timing synchronization
- ✓ Frequency and phase correction
- ✓ Symbols to data
- ✓ Display of the message

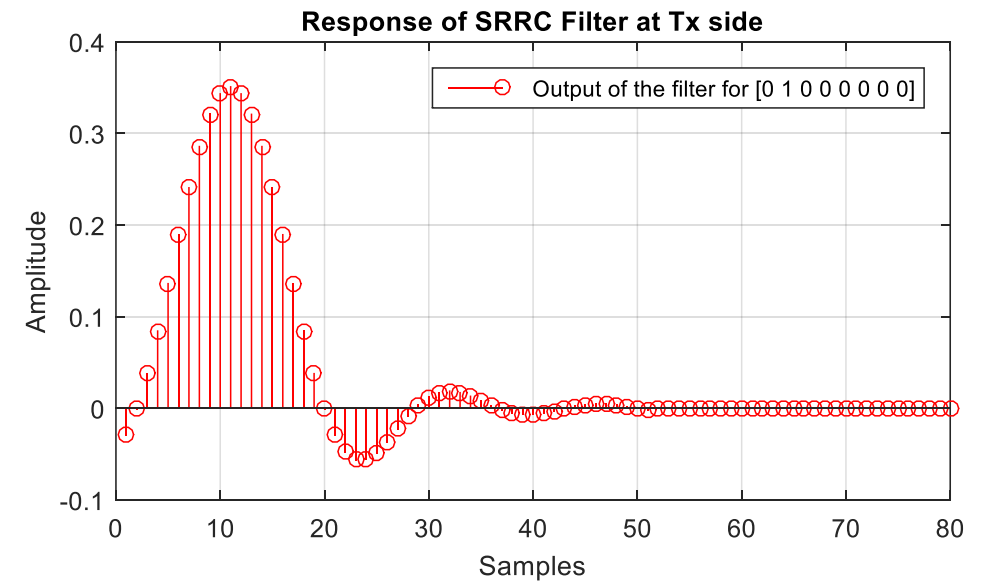
The challenge:  
the LO sources in your Tx/Rx hardware  
are not synchronized!

The steps above need not necessarily be performed in this sequence.

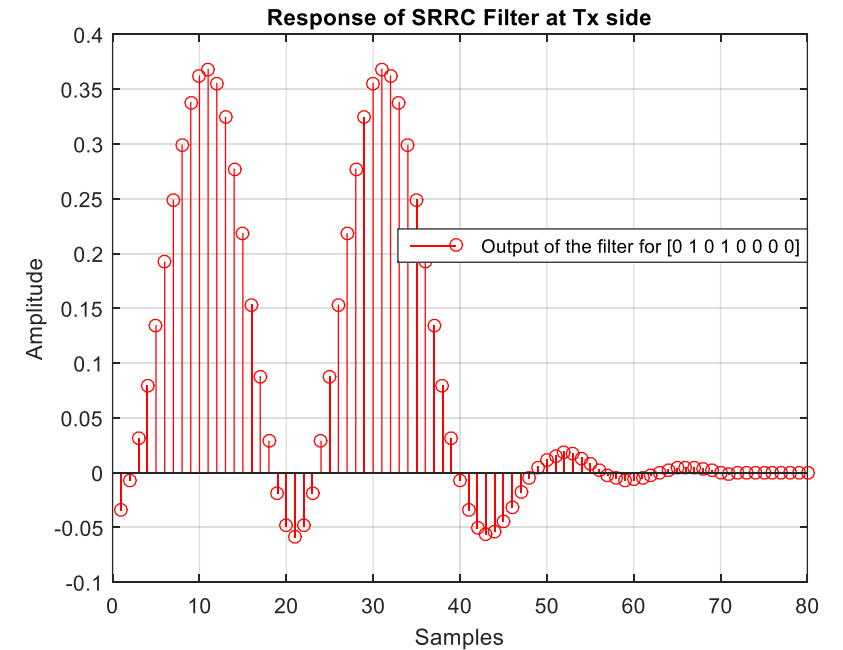
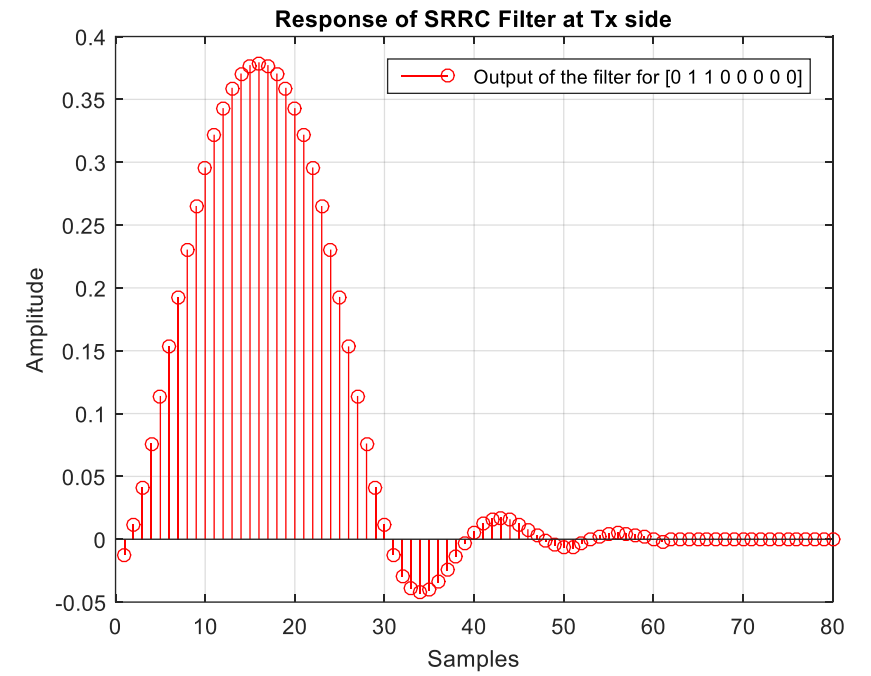
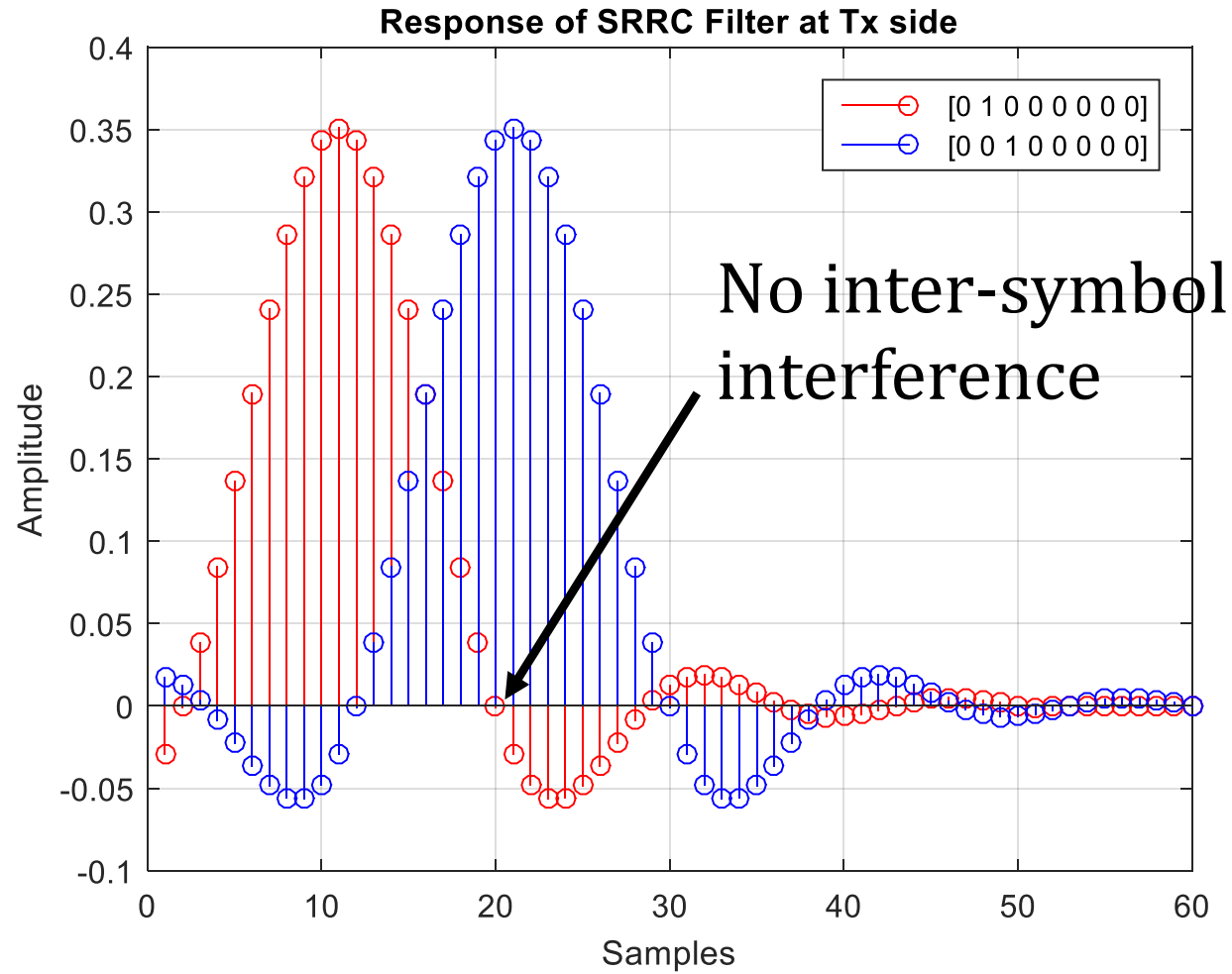
# Filtering

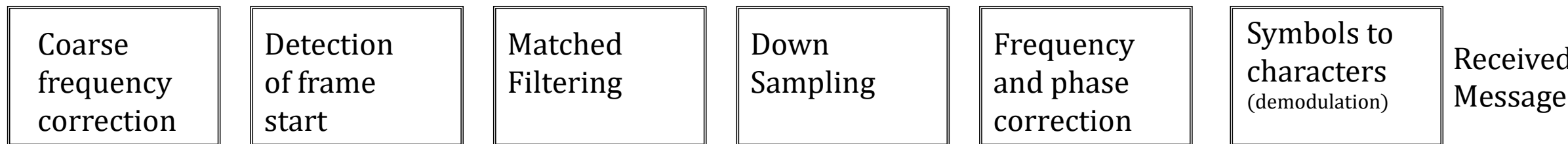
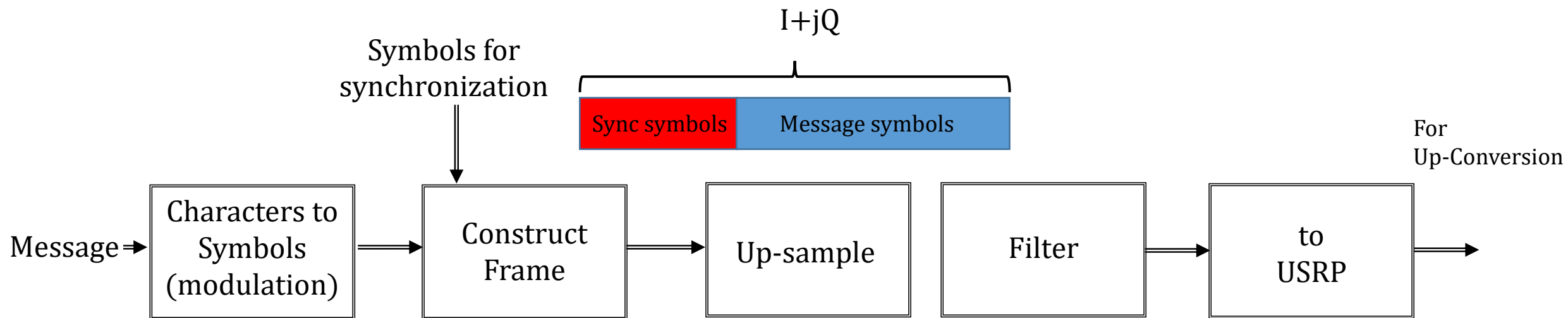


```
pt = rcosdesign(alpha,symb_span,s_per_symb);  
output_of_srrc_filter = conv(Input_bit_os,pt,'same');
```



# Filtering

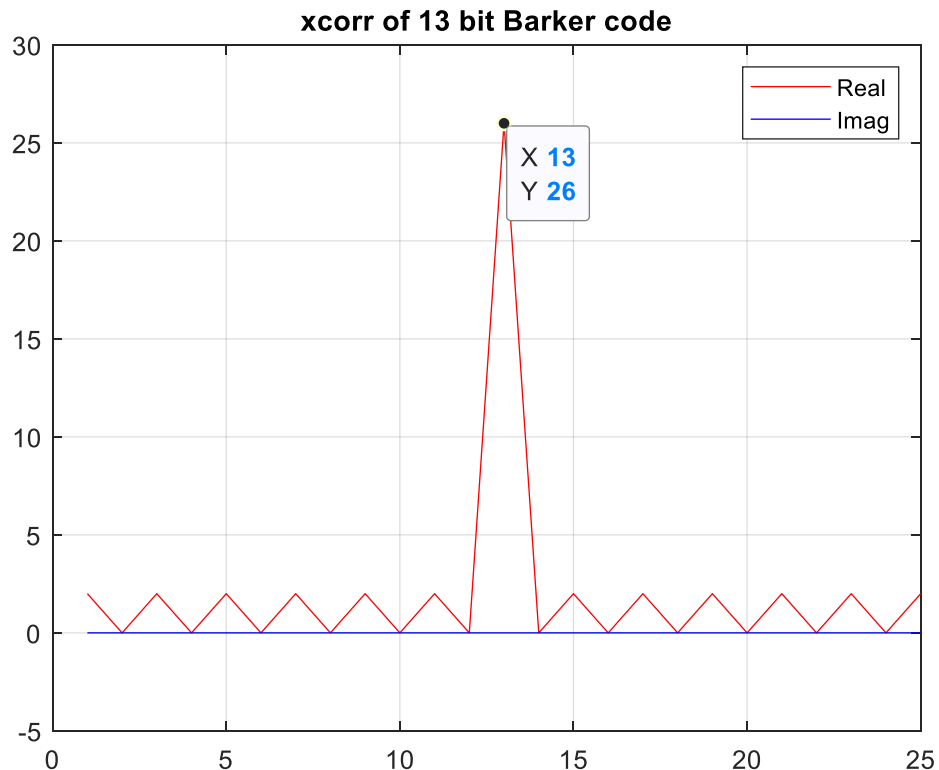




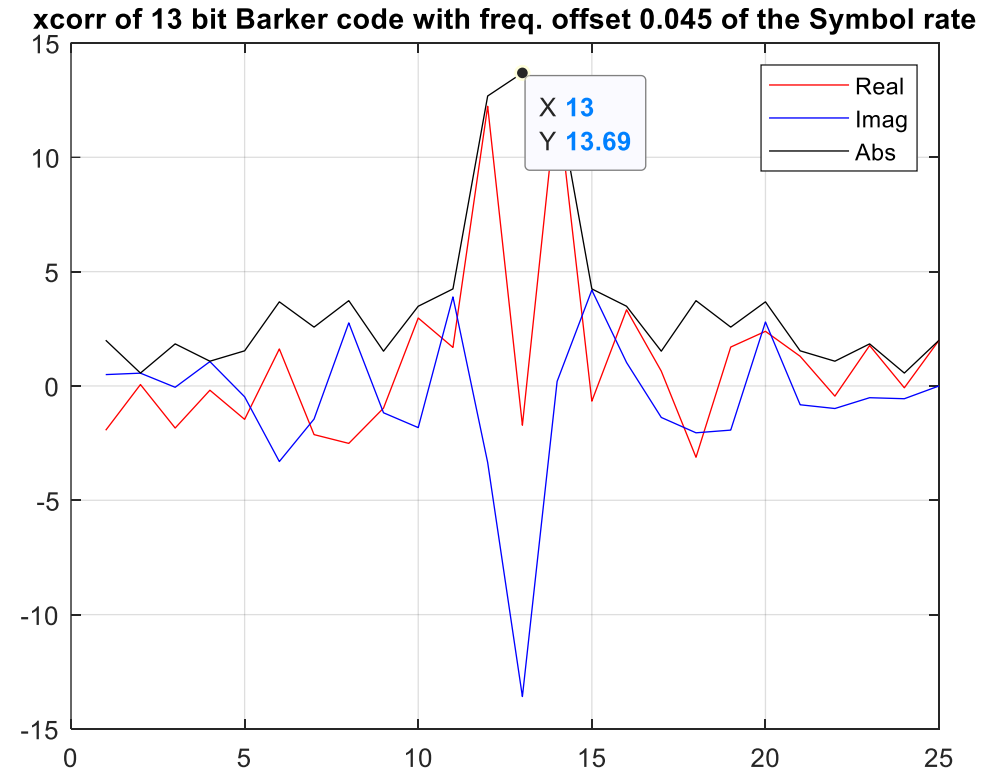
# Detection of message/frame start

- ✓ Your receiver will collect a certain number of samples and it will look for the known “Sync” symbols by correlating your received symbols with the known synchronization symbols.

```
correlation=xcorr((symb_synk),(symb_received));
```

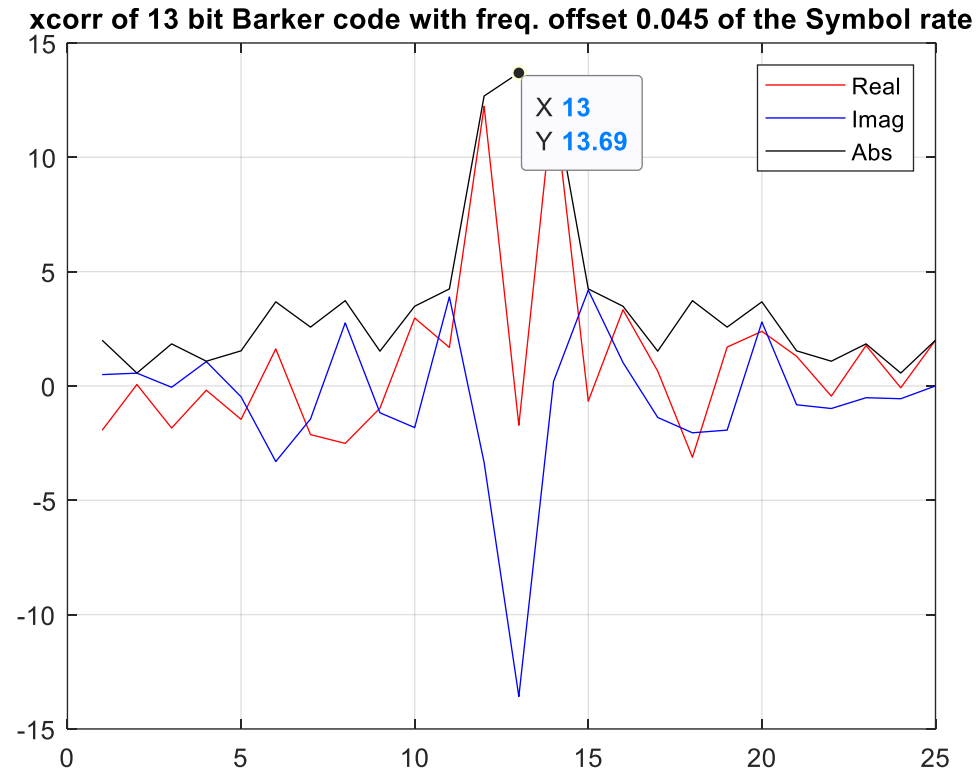


What happens if the received symbols have frequency offset?

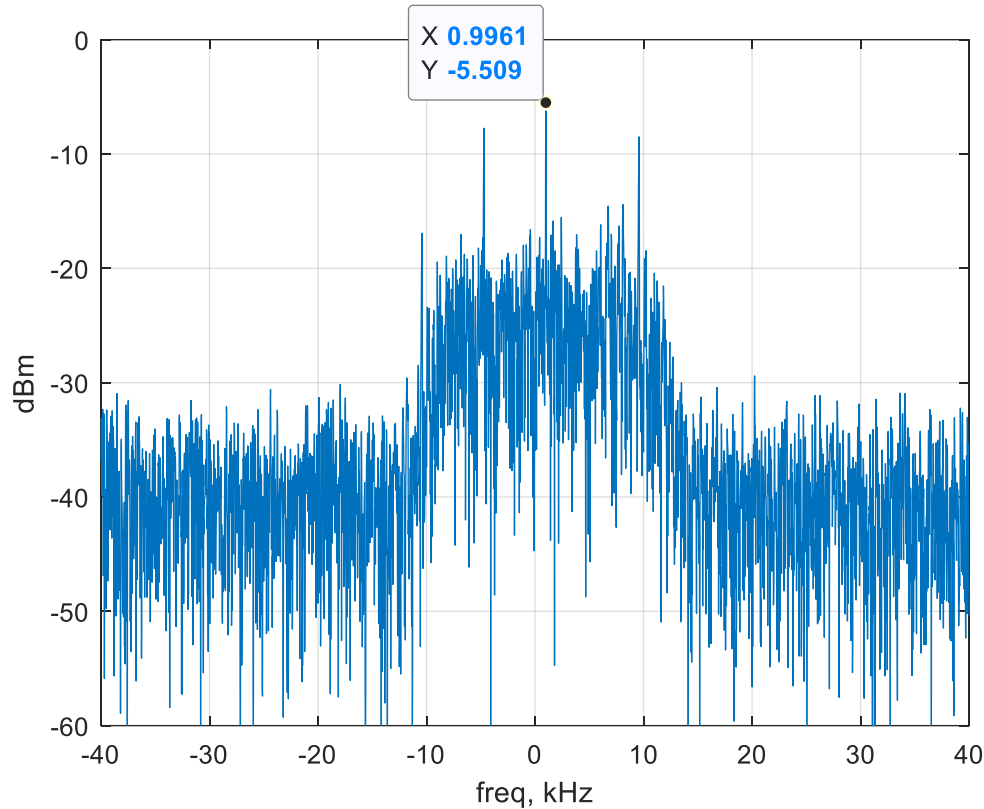


# Detection of message, frame start

Using 13 bit Barker sequence, we can tolerate frequency offset up to 0.045 of the symbol rate! Why 0.045?  
What can we do to tolerate higher frequency offset and still be able to detect the message?



# Coarse frequency correction

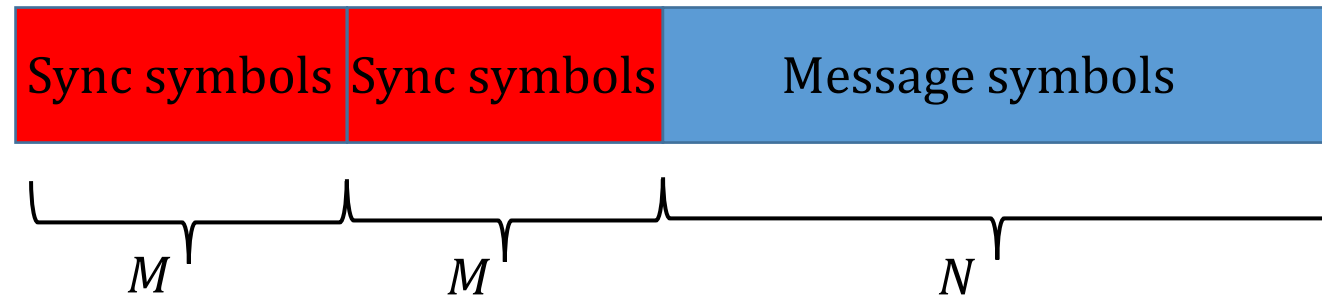


- ✓ It is a good idea to do a coarse frequency correction as a first step in the receiver.
- ✓ Due to DC offset in the DAC, the received spectrum will have a DC component, which will be located in the middle of the pass-band.
- ✓ Identifying the frequency of the DC component allows to correct for frequency offsets. This will make the detection of the message easier.
- ✓ If the DC component is not highest in the spectrum, one can enhance it by adding DC offset in the data.

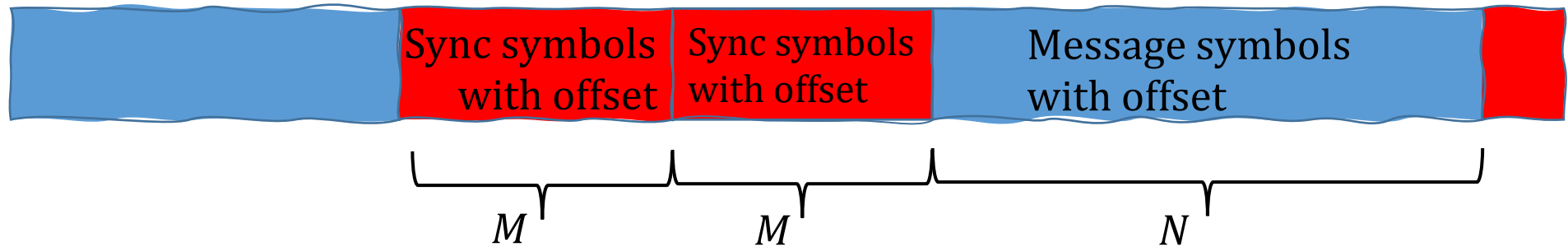


## Detecting the message in presence of arbitrary frequency offset (1)

Step 1: In the Tx you construct your frame so that the sync symbols are repeated at least 2 times.

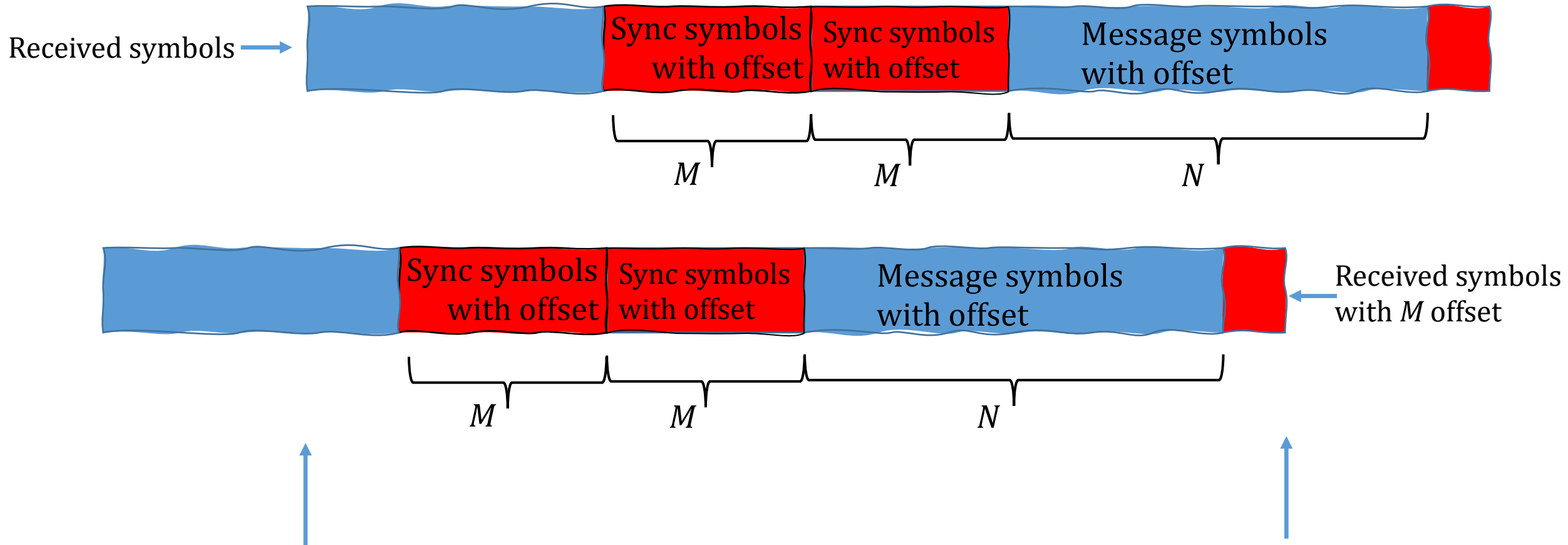


Step 2: In the Rx you receive for at least  $3M+N$  symbols.



## Detecting the message in presence of arbitrary frequency offset (2)

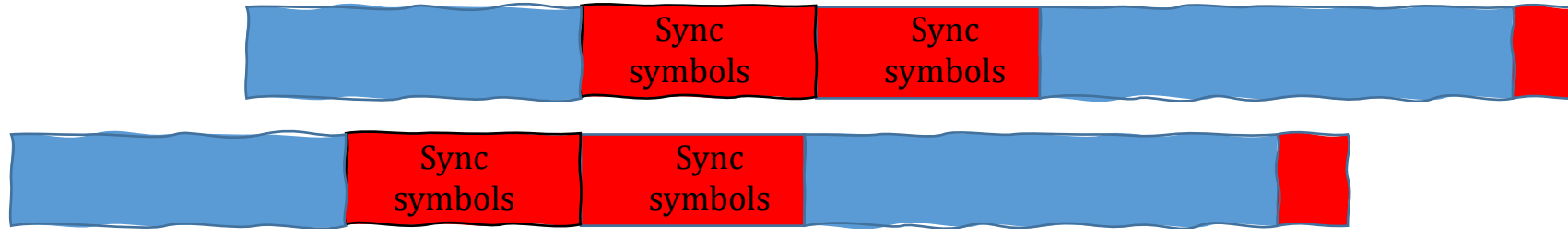
Step 3: You copy the received symbols *conjugate* them and *offset* them by  $M$  symbols



Step 4: You multiply both vectors element by element for the symbols where they overlap

## Detecting the message in presence of arbitrary frequency offset (3)

Step 4: You multiply both vectors element by element for the symbols where they overlap



Received symbol

$$\begin{array}{c} \overbrace{se^{j\theta} \cdot e^{j(\omega t_1 + \psi)}} \\ * \\ \underbrace{se^{-j\theta} \cdot e^{-j(\omega t_2 + \psi)}} \end{array}$$

Received symbol  
conjugated

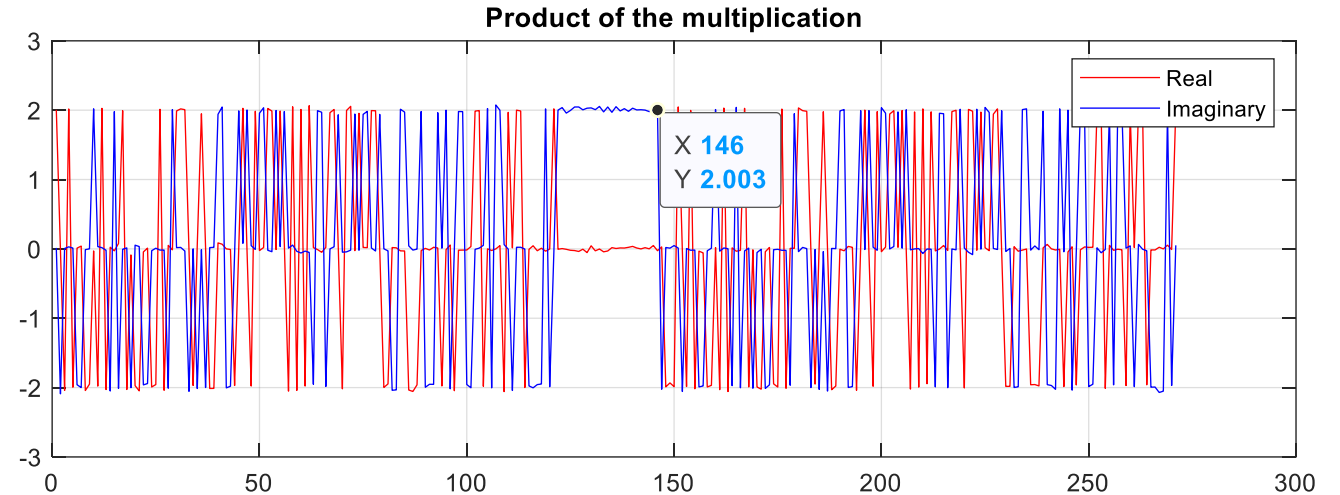
Only symbols that  
are ***the same*** will  
produce ...

$$e^{j\omega(t_1 - t_2)}$$

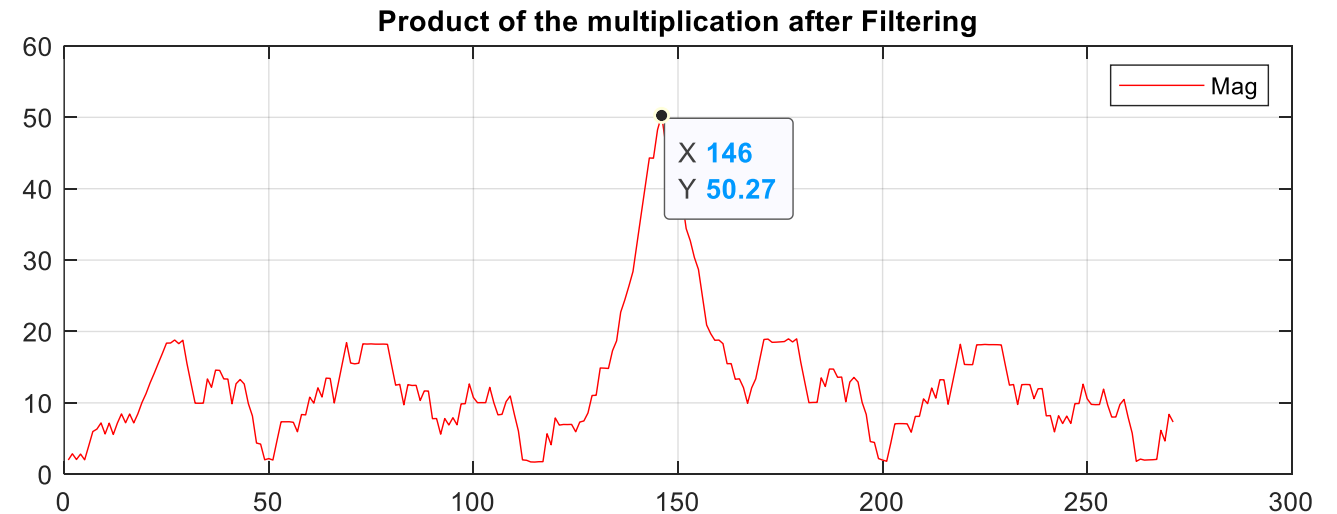
## Detecting the message in presence of arbitrary frequency offset (5)

Step 5: You filter the product of the multiplication with a window of the same length as the Sync symbols

```
Product=(conj(Rx).* (Rx_offset));
```

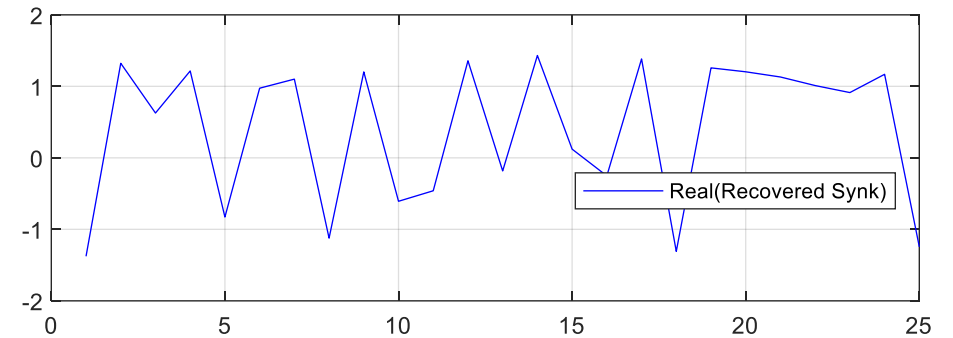
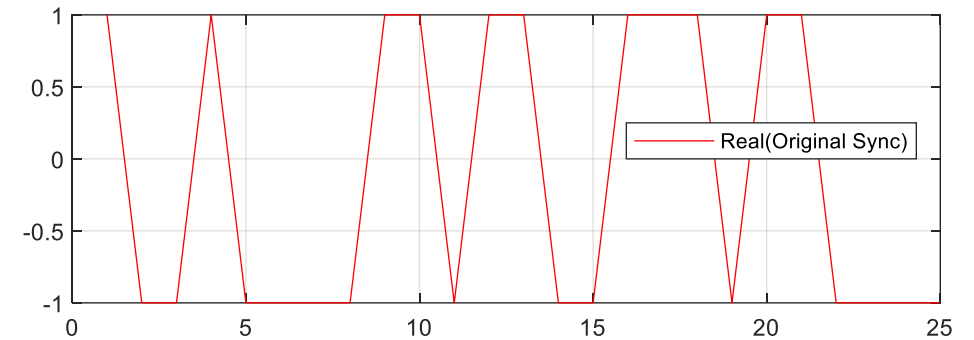
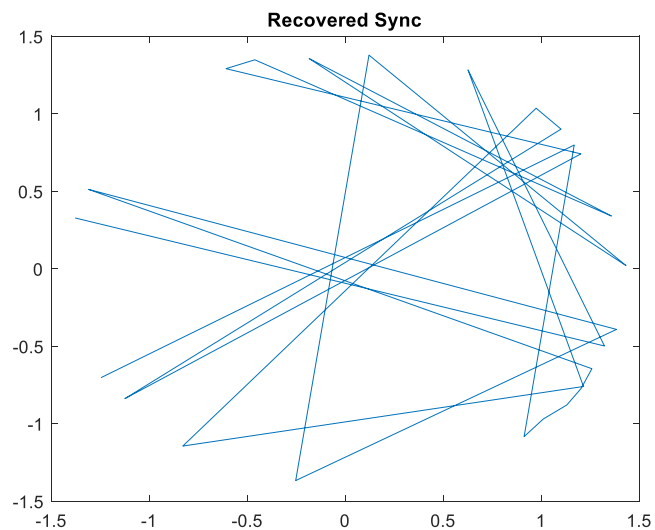
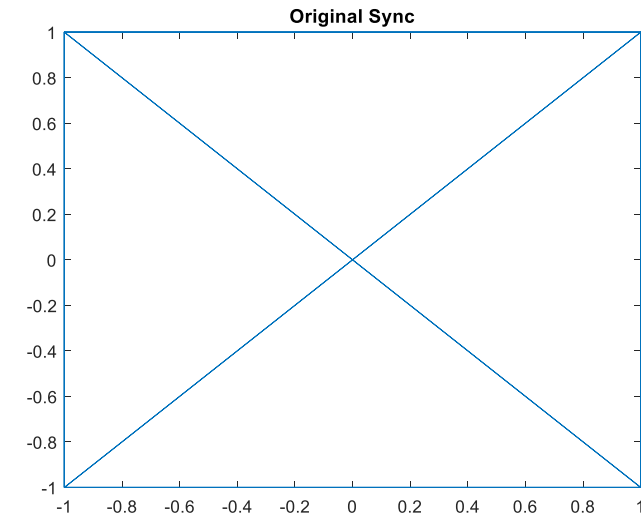


```
window = ones(1,M);  
convv = filter(window,1,Product);
```



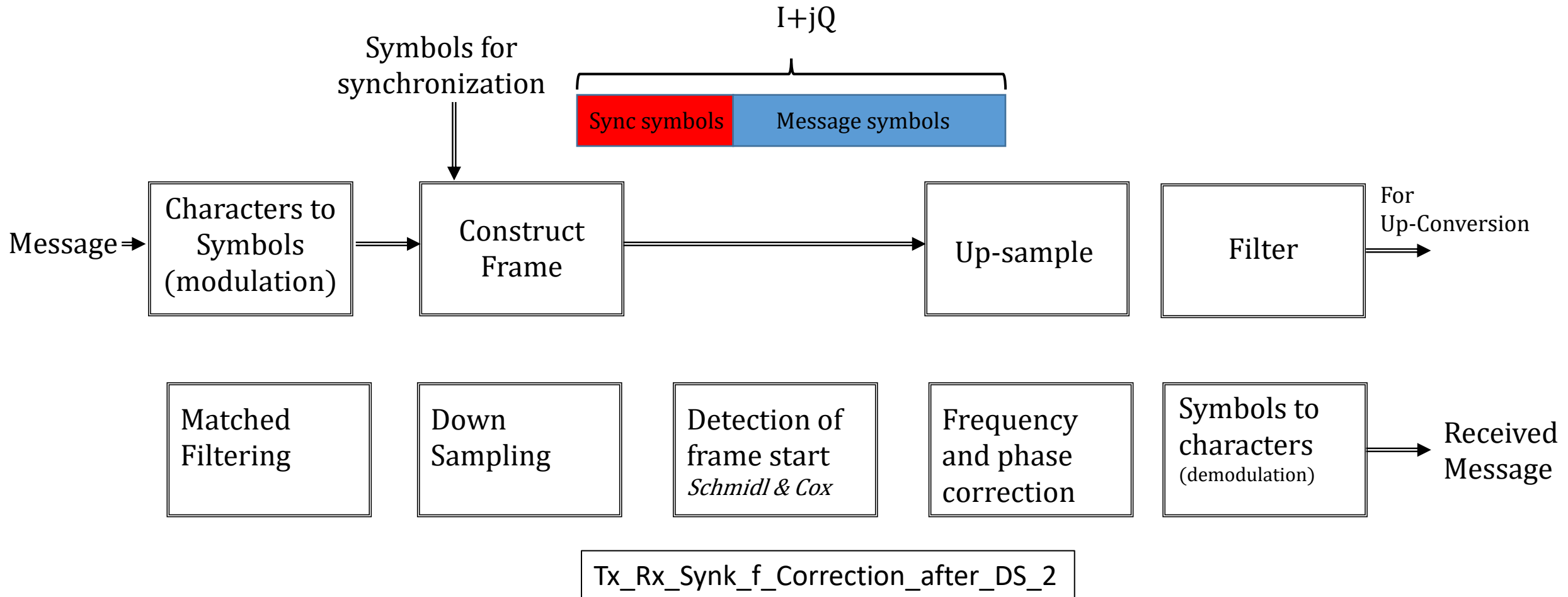
# Detecting the message in presence of arbitrary frequency offset (6)

Step 6: You can now extract the Sync Symbols and use them to find the frequency and phase offset



Find\_Message\_Start\_Schmidl\_Cox

# Frequency correction after down-sampling



## Frequency correction after down-sampling

### Frequency and phase synchronization using the known sync symbols in the frame

1. Filter the incoming signal
2. Find the message start and isolate the sync symbols – `symb_sync_received` The frequency offset estimation is based on comparing the received to the known sync symbols `symb_sync`

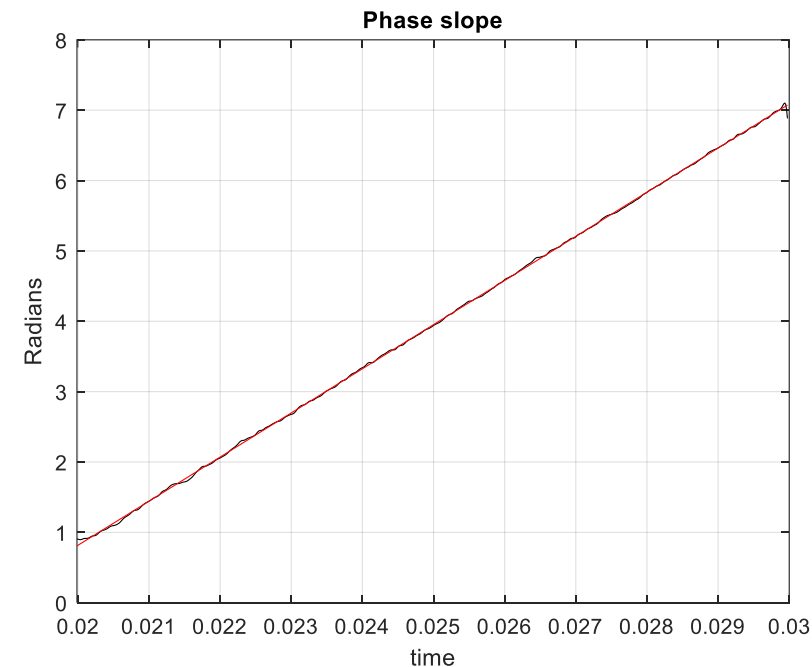
Original Sync symbols

\*

Conj(Received Sync symbols f  
with offset)

=

Complex Number with  
increasing phase slope  
proportional to the freq. offset



```
phase_slope=unwrap(angle((symb_sync_received).*conj(symb_sync_us)) );
```

## Frequency correction after down-sampling

### Frequency and phase synchronization using the known synk symbols in the frame

3. Fit a line to the phase slope: slope of the line = freq offst, value at t=0 equals the phase offset

```
p = polyfit(time_symb_synk, phase_slope, 1);  
phase_slope_fit = polyval(p, time_symb_synk);  
  
freq_offset_estimated = p(1) / (2*pi) % In Hz  
%phase_offset_estimated_deg = -360*p(2) / (2*pi) % In degrees  
phase_offset_estimated_deg = 360 * (phase_slope(1)) / (2*pi);
```

The “unwrap” function may not work on up-sampled symbols! Why?

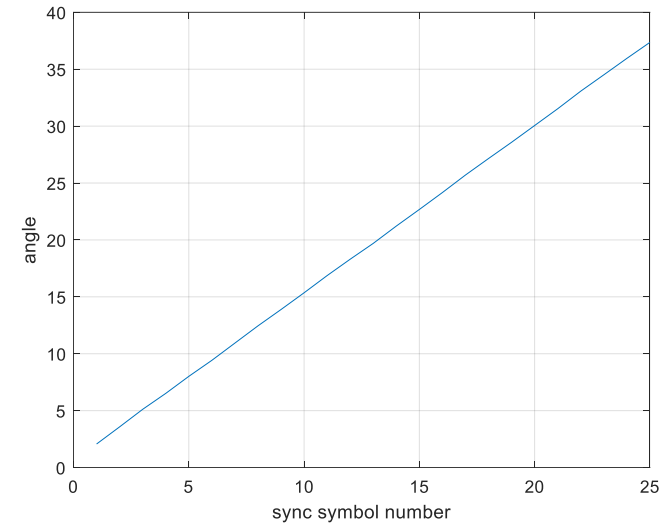
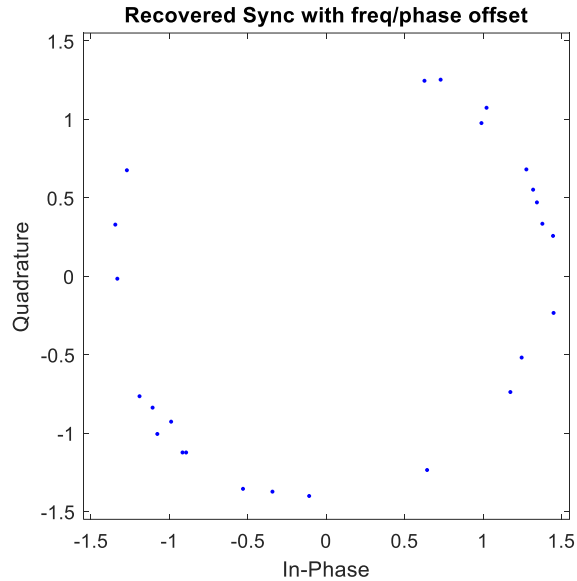
The solution is to use the same value for all the synk symbols (for example  $1+1j$ ) – the drawback is that you introduce close to DC frequency component.



# Frequency correction after down-sampling

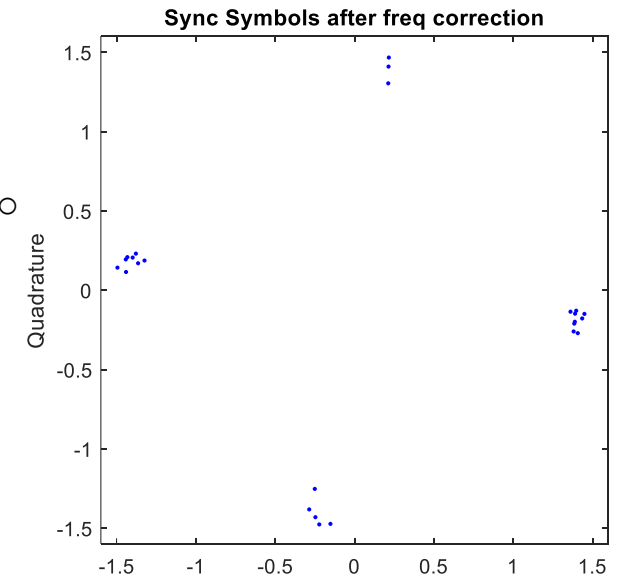
Find\_Message\_Start\_Schmidl\_Cox

```
phase_slope=unwrap(angle(simbsynk_recovered)-angle(simbsynk));
```



```
freq_offset_detected=mean(diff(phase_slope))/(2*pi)
```

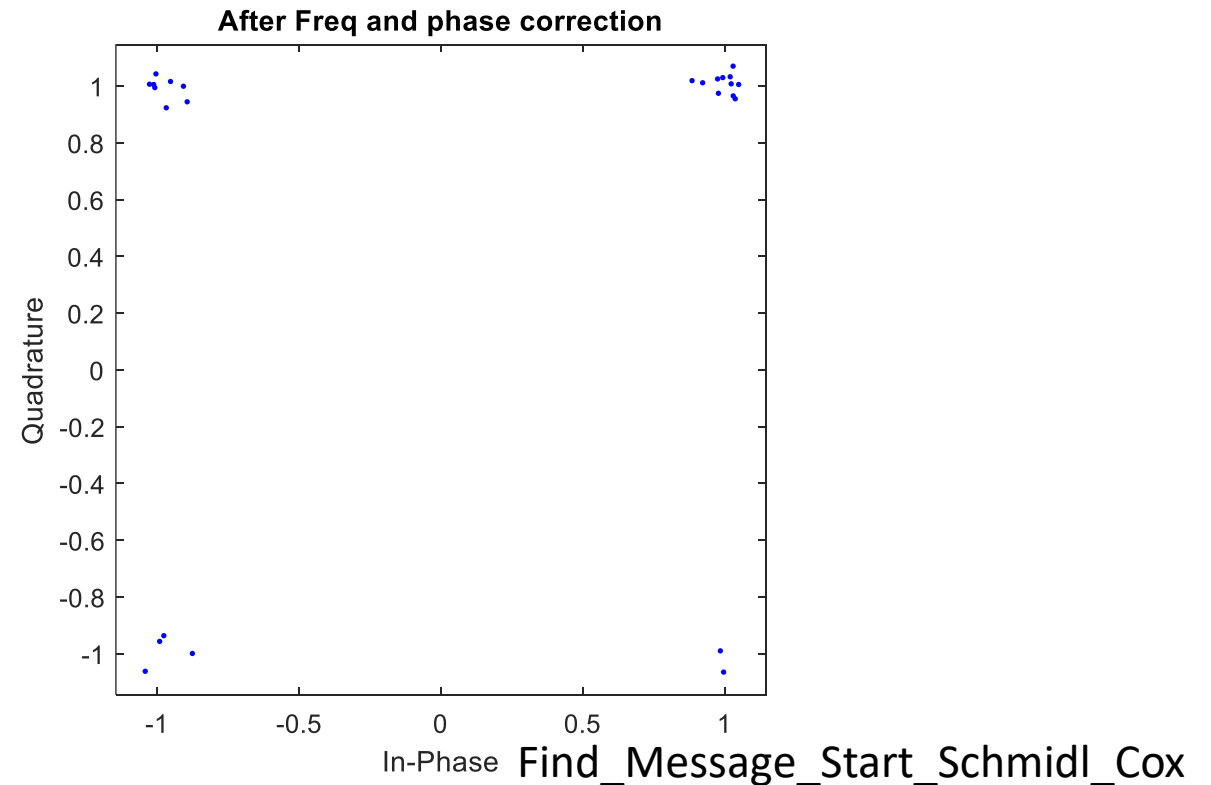
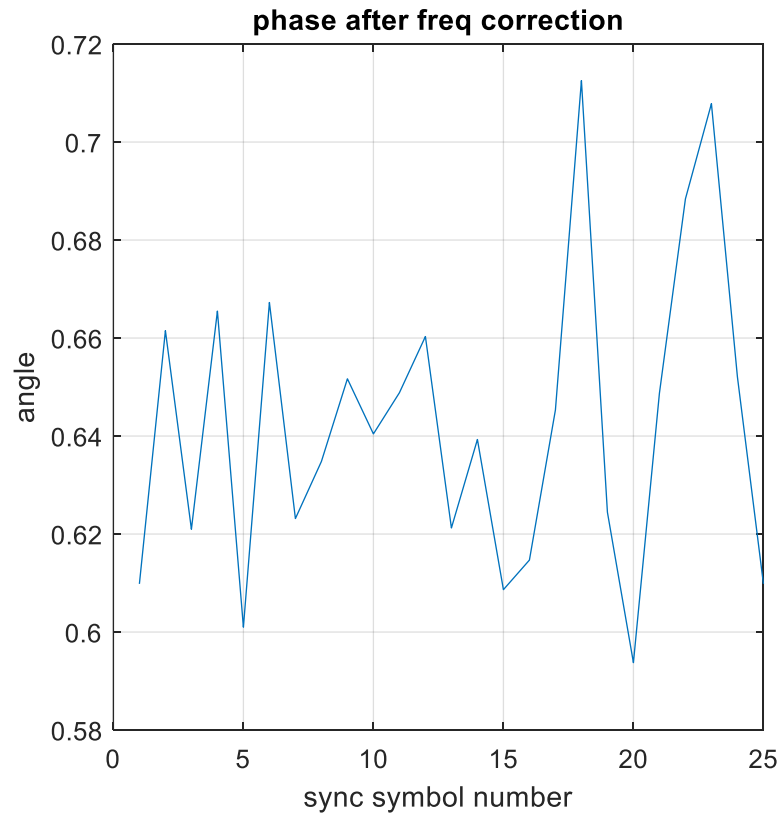
```
simbsynk_recovered=  
simbsynk_recovered.*exp(i*(2*pi*freq_offset_detected*(1:1:length(simbsynk_recovered))));
```



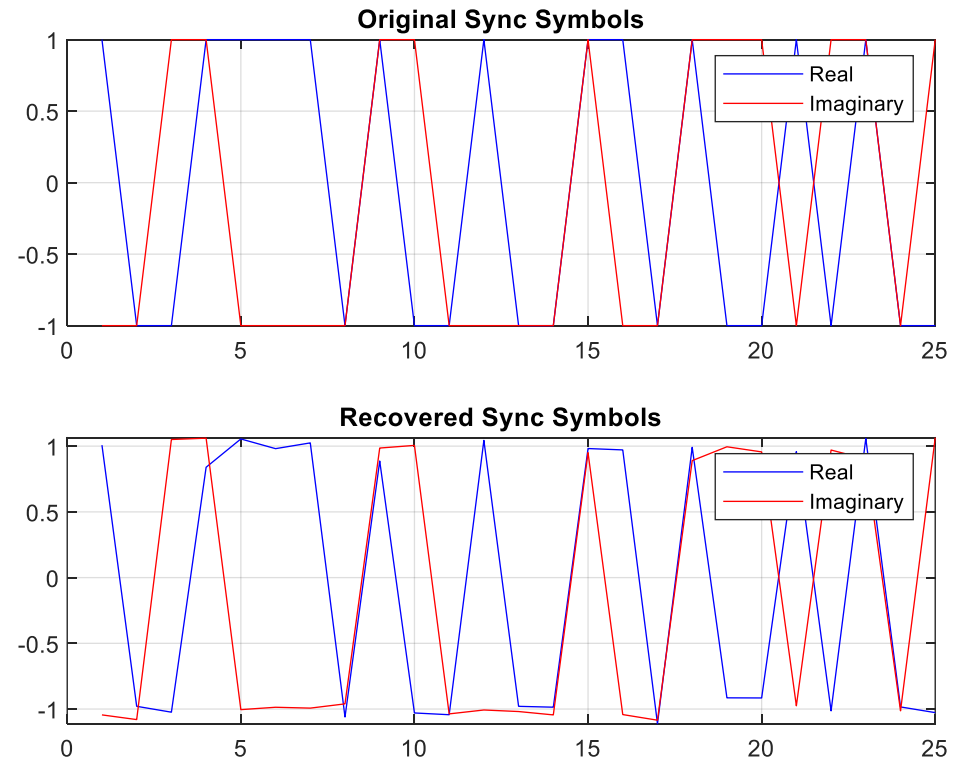
# Phase offset correction after down-sampling

Symbols already corrected for  
Freq. offset

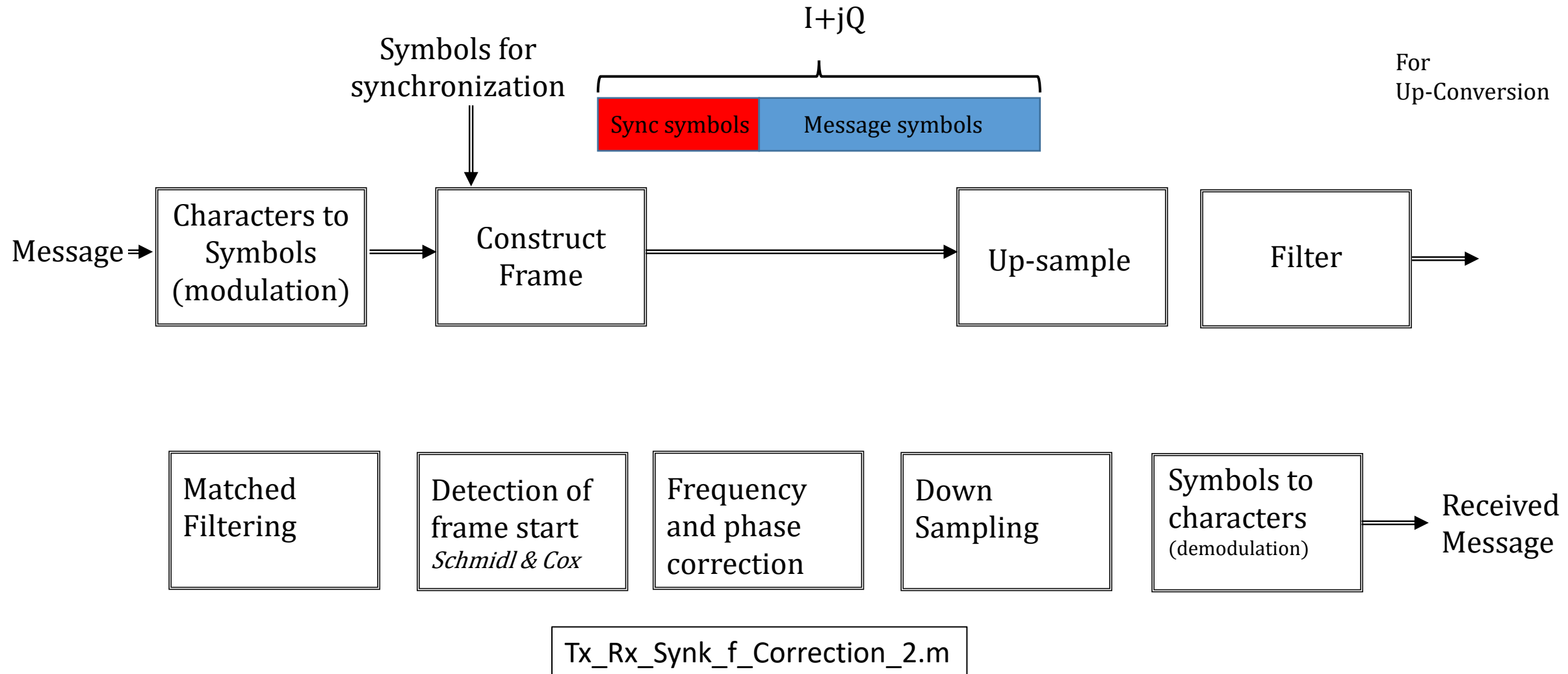
```
phase_offset=unwrap(angle(simb_synk_recovered)-angle(simb_synk));  
phase_offset_detected=mean(phase_offset/(2*pi))
```



# Verification that the Sync Symbols are recovered



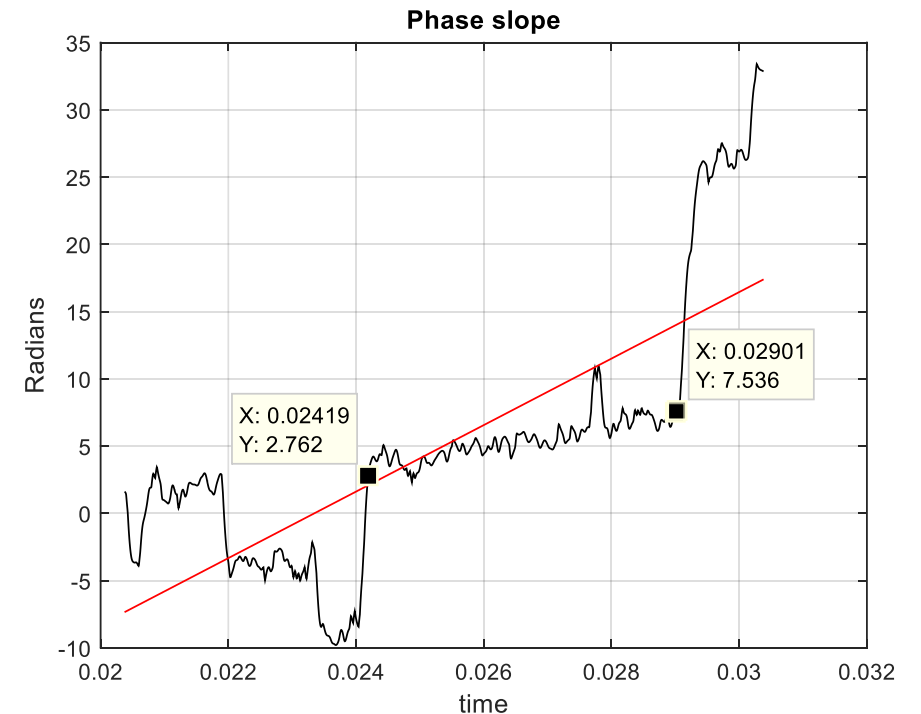
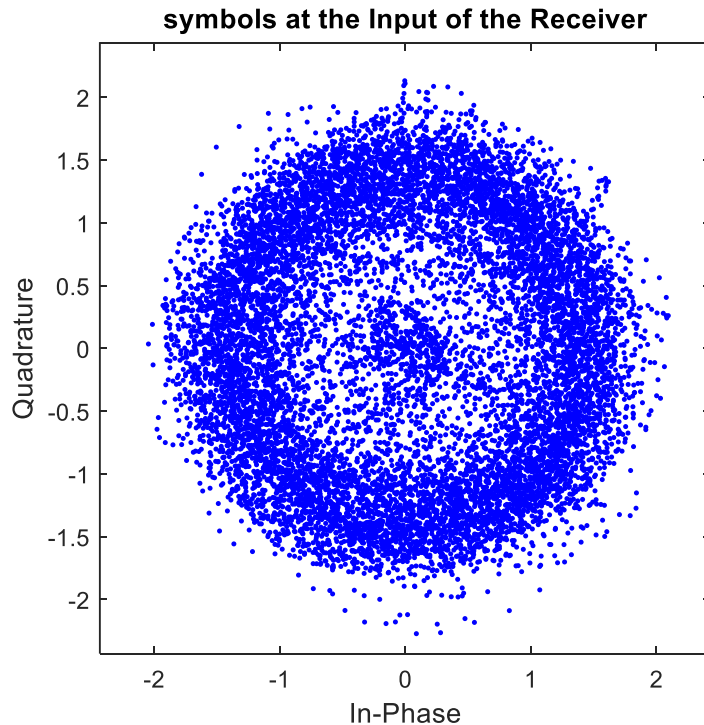
# Frequency correction before down-sampling



## Frequency correction before down-sampling

Frequency and phase synchronization using the known synk symbols in the frame

Limitations: when used on an up-sampled signal and when the synk symbols are random there will be samples close to 0, and the unwrap function will not work properly and will produce jumps in the phase slope.



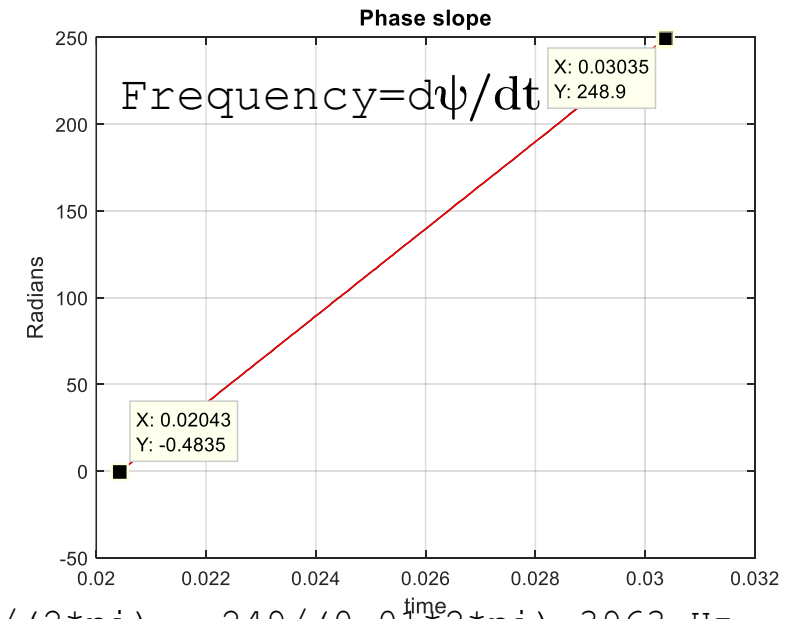
# Frequency correction before down-sampling

Frequency and phase synchronization using the known synk symbols in the frame  
(before down sampling)

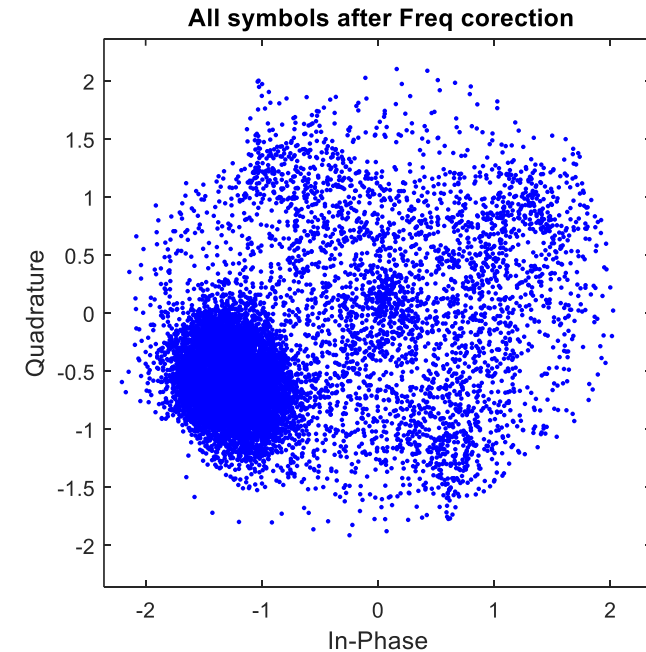
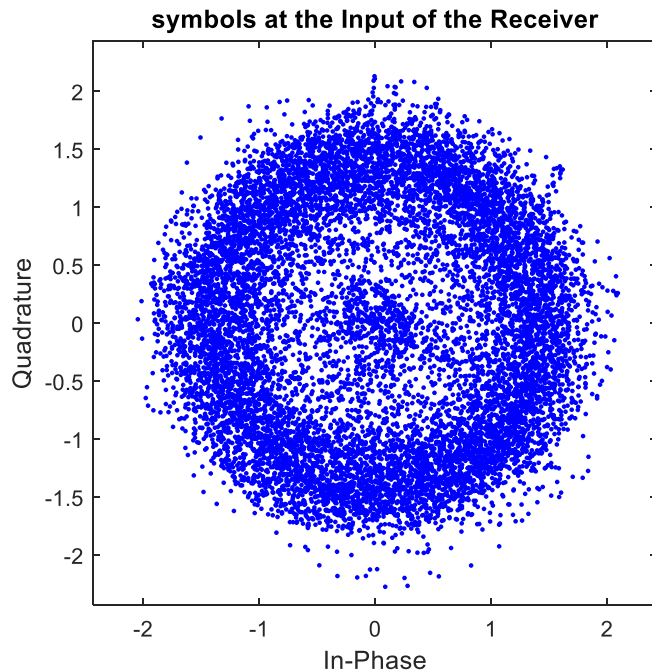
```
phase_slope=unwrap(angle(symb_synk_received)-angle(symb_synk_us));
```

Example:

```
fsymb=20e3; %Symbol rate  
s_per_symb=10; % Samples per symbol  
fs=fsymb*s_per_symb;% Sampling rate  
Phase_Offset=70; %In degrees  
SNR=10; % In dB  
Freq_Offset=4000; %In Hz
```



Frequency offset=estimated slope/(2\*pi) = 249/(0.01\*2\*pi)=3963 Hz

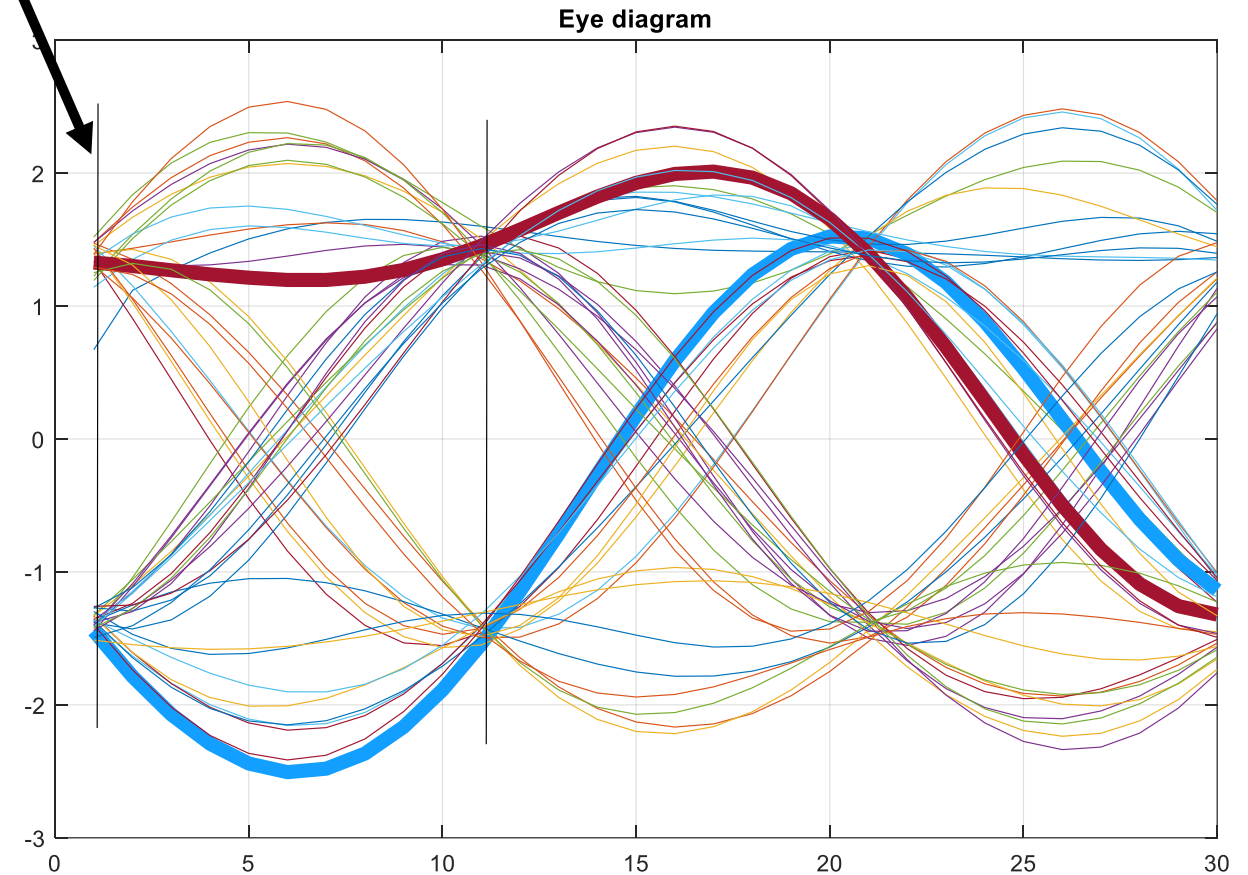
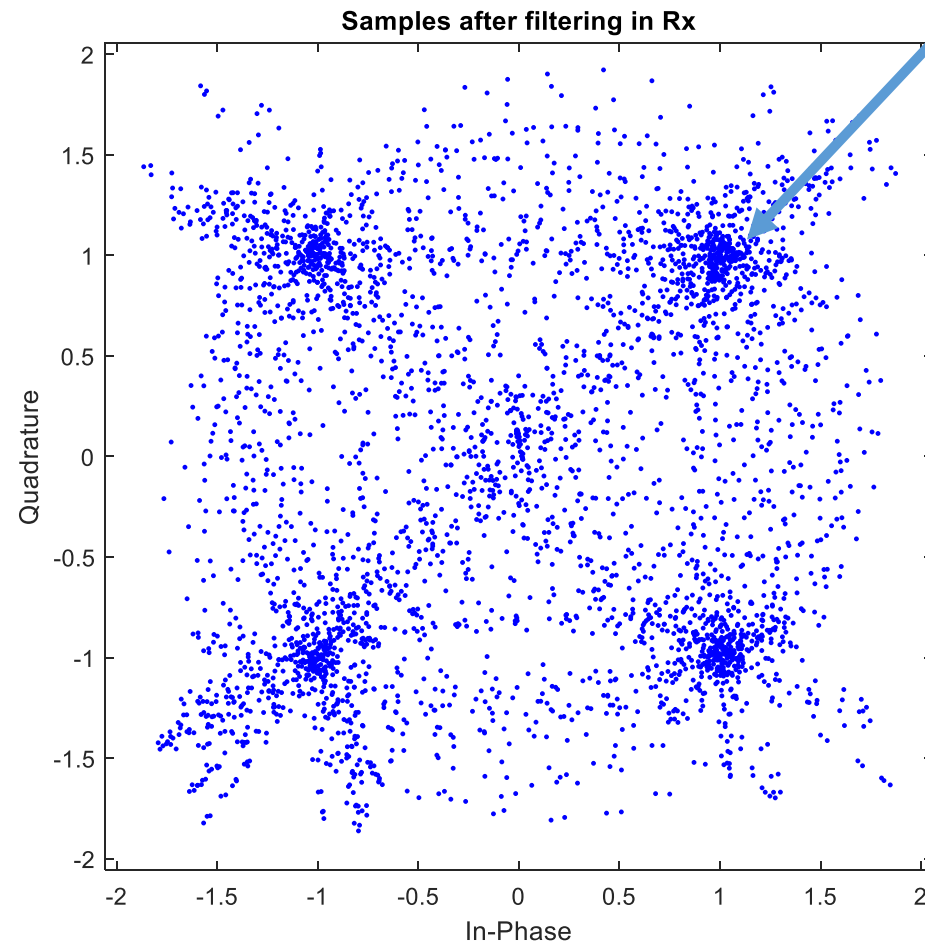


In this example all the synk symbols are 1+j1, thus the cloud

# Down sampling (timing synchronization)

We need to take only one sample per Symbol

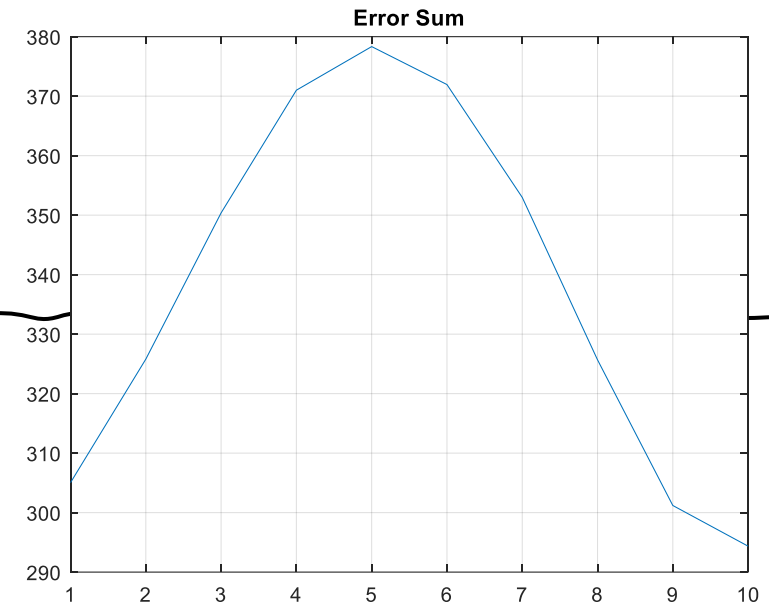
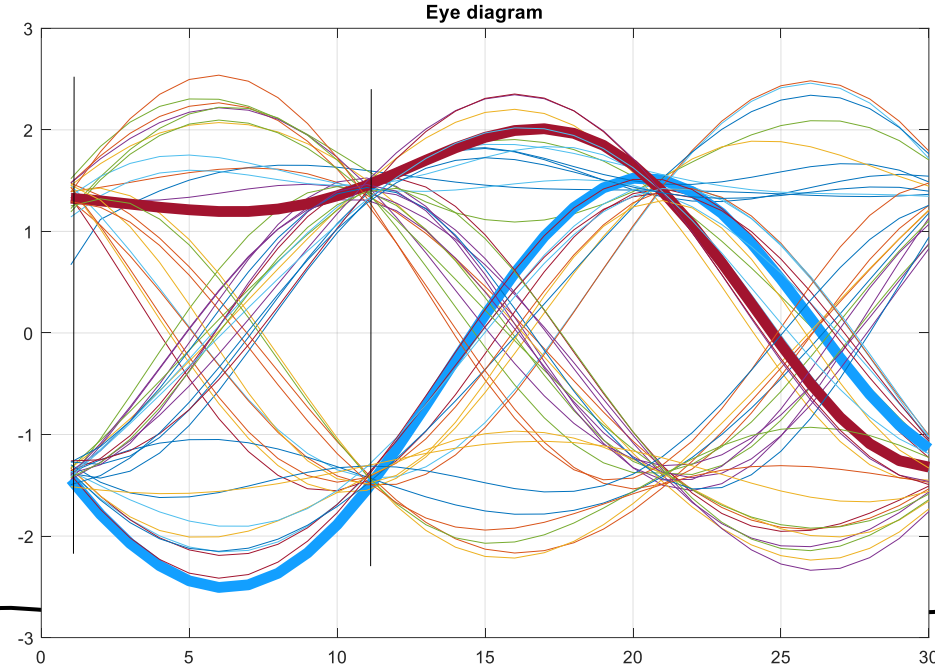
3 symbols, 10 samples/symbol



```
s_per_symb=10; % Samples per symbol
```

How to identify the sample that gives max eye opening?

# Down-sampling



```
for k=2:1:length(symb)-1;  
eI(k)=abs(real(symb(k-1))-real(symb(k+1)));  
eQ(k)=abs(imag(symb(k-1))-imag(symb(k+1)));  
e(k)=eI(k)+eQ(k);  
end  
  
error=reshape(e,s_per_symb,[]); %[s_per_symb length(symb)/s_per_symb]  
error_sum=sum(error,2);% [samples_per_symbol 1]
```

Optimum sample is found at the minimum of the error sum



# Down-sampling works even in presence of freq/phase offset

