

$$\ddot{y} - 2\dot{y} + y = u + \dot{u} \quad (1)$$

↓ (slide 41)

Show how to derive (1) from (2)

$$\begin{cases} \dot{x}_1 = x_2 \\ \dot{x}_2 = -x_1 + 2x_2 + u \\ y = x_1 + x_2 \end{cases} \quad (2)$$

Write (1) as $y = 2\int y - \iint y + \iint u + \int u$, assuming 0 initial conditions

From (2)

$$x_1 = \int x_2 \quad \text{and} \quad x_2 = -\int x_1 + 2\int x_2 + \int u$$

$$\begin{aligned} \underline{y} = x_1 + x_2 &= \int x_2 + x_2 = -\int x_1 + 2\int x_2 + \int u + \int x_1 + 2\int x_2 + \int u = \\ &= -\underline{\int x_1} + \underline{2\int x_1} + \int u - \underline{\int x_2} + \underline{2\int x_2} + \int u = \\ &= -\underline{\int y} + \underline{2\int y} + \underline{\int u} + \underline{\int u} \end{aligned}$$