Introduction to Computer Vision: Neural Networks, Image Classification, Semantic Segmentation

Navasardyan Shant



November 14, 2019

Overview

1 Image Classification Network Architectures

Semantic Segmentation

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2 Semantic Segmentation

AlexNet

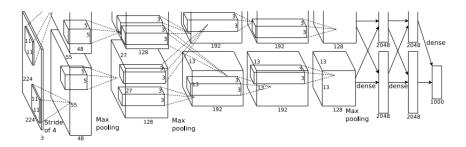


Figure: In the AlexNet architecture¹ after each convolution we have the **ReLU** activation, and after each of the first two convolutions we have **ReLU** activation, **local response normalization**. All Max-Pooling layers have the kernel size 3×3 and are done with strides 2×2 . After each fully connected layer we have the **ReLU** activation and **dropout**.

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¹Imagenet classification with deep convolutional neural networks A Krizhevsky, I Sutskever, GE Hinton - Advances in neural information processing systems, 2012

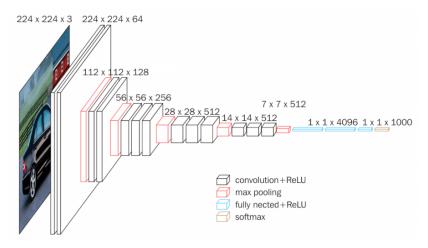


Figure: Vgg-16²

²Very deep convolutional networks for large-scale image recognition K Simonyan, A Zisserman - arXiv preprint arXiv:1409.1556, 2014

ResNet



Figure: The ResNet architecture³, dotted lines means decreasing-size residual blocks. There are two kinds of residual blocks: with and without 2-strided convolution block in the residual branch

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Question

How to pass the output of a convolutional layer as the input of a dense layer? What about the cases when we want our neural network to deal with images of arbitrary size?

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Inception v1: GoogleNet

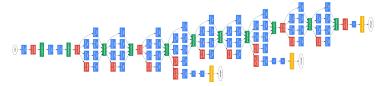


Figure: The GoogleNet architecture⁴ and the Inception Module (below) used in GoogleNet

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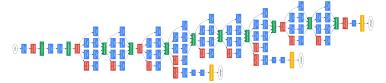
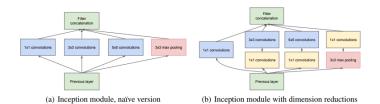


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Inception v2 and v3

The Inception $v2^5$ architecture simply is a slightly modified version of GoogleNet with **batch normalization** layers before each activation layer. In the Inception $v3^6$ architecture we are getting familiar with the idea of **factorizing** convolutions.

 $^{^5} loffe,$ Sergey and Christian Szegedy. "Batch Normalization: Accelerating Deep Network Training by Reducing Internal Covariate Shift." ArXiv abs/1502.03167 (2015): n. pag.

⁶Szegedy, Christian et al. "Rethinking the Inception Architecture for Computer Vision." 2016 IEEE Conference on Computer Vision and Pattern Recognition (CVPR) (2015): 2818-2826.

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Let we have a convolutional neural network with consequent layers F_0, F_1, \ldots, F_D (F_0, F_D are inputs and outputs of the network respectively).

Receptive Field

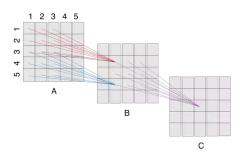
The **Receptive Field** of a layer F_k with respect to the layer F_m (m < k) is the maximal region in the layer F_m each element of which is contributed in forming one of pixels in F_D , considering only convolutional layers as contribution.

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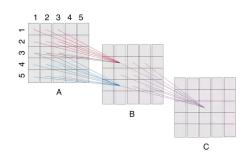
Receptive Field

The **Receptive Field** of a layer F_k with respect to the layer F_m (m < k) is the maximal region in the layer F_m each element of which is contributed in forming one of pixels in F_D , considering only convolutional layers as contribution. By receptive field of a network we mean the receptive field of its output with respect to its input.

Here is the illustration of the receptive field of the layer *C* with respect to the layer *A*. Here you can see that the whole layer *A* is this receptive field.



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Note

Although the receptive field can be referred as the "area under vision of the net", not all pixels in receptive field are "equally contributed" in formation of an output pixel. So there is a concept of effective receptive field^a.

^aYu, Fisher and Vladlen Koltun. "Multi-Scale Context Aggregation by Dilated Convolutions." CoRR abs/1511.07122 (2015): n. pag.

Inception-V3 Revisited

So the natural need arises to enlarge the size of the receptive field of the network, or keep the size of receptive field the same but decrease the number of computations. For the latter purpose the approach of *convolution factorization* is appropriate.

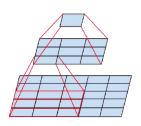
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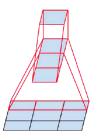
The concept of convolution factorization was introduced in the *Inception-V3* architecture. The idea is the following: in some places

- ullet replace 5 imes 5 convolution layers with two 3 imes 3 convolution layers
- replace $n \times n$ convolution layers with asymmetric consequent convolution layers of sizes $n \times 1$ and $1 \times n$.

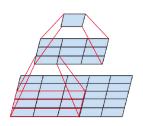
Below you can see visualizations of these convolution factorizations.



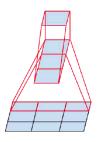
Two 3×3 convolutions replacing one 5×5 convolution



One 3×1 convolution followed by one 1×3 convolution replaces one 3×3 convolution



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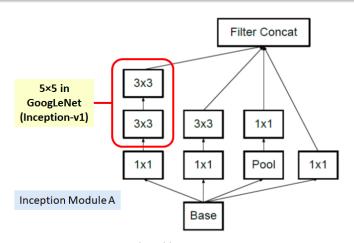


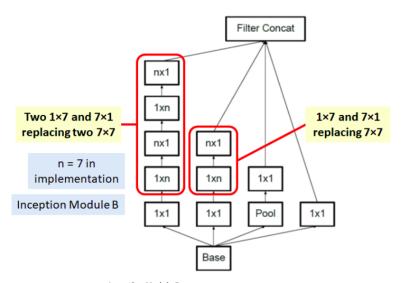
One 3×1 convolution followed by one 1×3 convolution replaces one 3×3 convolution

You can see that the receptive fields of replaced blocks are the same as before replacement.

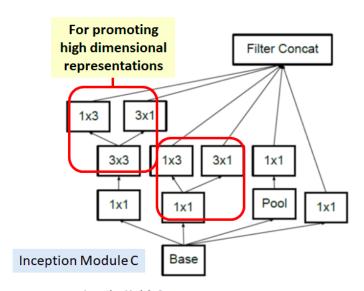
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Inception Module B using asymmetric factorization



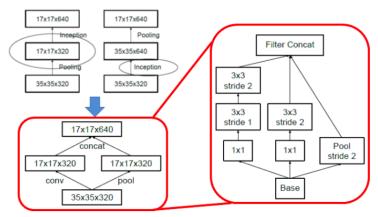
Inception Module C using asymmetric factorization

Inception-V3: Grid Size Reduction

The architecture of Inception-V3 also introduces a new size reduction method, directly in the inception block.

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Conventional downsizing (Top Left), Efficient Grid Size Reduction (Bottom Left), Detailed Architecture of Efficient Grid Size Reduction (Right)

Inception-V3

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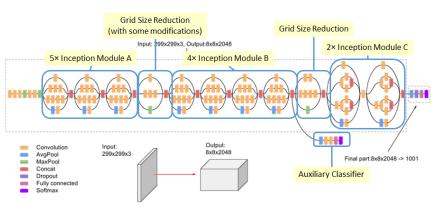


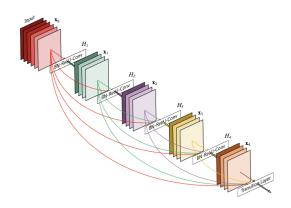
Figure: After each convolution layer we use BatchNorm and ReLU

Another architecture similar to ResNet architecture is introdused as *DenseNet*⁷. Here you can see the main block of this network, called *dense block*.

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⁷Huang, Gao et al. "Densely Connected Convolutional Networks." 2017 IEEE Conference on Computer Vision and Pattern Recognition (CVPR) (2016): 2261-2269. ○ ○ ○

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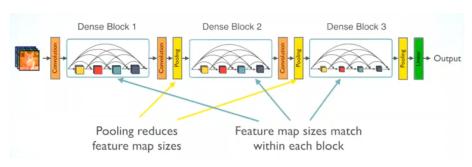


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The model SqueezeNet⁸ aims to reduce the model size and computation complexity while preserving the high accuracy. As described in the paper, there are several strategies to achieve a high accuracy with a small model:

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- downsample in deeper features instead of earlier features.

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So the SqueezeNet architecture introduces the module called **fire module**:

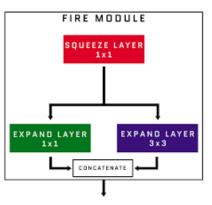
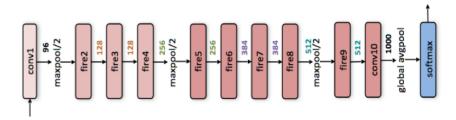


Figure: This *fire module* has three parameters. $s_{1\times 1}$ is the number of the filters of the 1×1 convolution in the "Squeeze Layer", $e_{1\times 1}$ and $e_{3\times 3}$ are the numbers of the filters of the 1×1 and 3×3 convolutions in the "Expand Layers". Each layer consists of a convolution followed by ReLU activation.

SqueezeNet

So the SqueezeNet architecture is the following:



Another small-sized network architecture is described in *MobileNet*⁹. This is a bunch of neural networks similar to each other, so we refer to all of them as *MobileNet*.

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Depthwise Separable Convolutions

In the *MobileNet* architecture the core idea is the concept of **Depthwise Separable Convolution** block. This block consists of two convolutional blocks: **depthwise** block and **pointwise** block.

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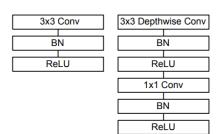
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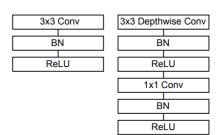
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Left: standard convolutional block. Right: depthwise separable convolutional block



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Width Multiplier

The number of filters of the pointwise 1×1 convolutions can be controlled with a hyperparameter called **width multiplier**, which is denoted by α . If in the baseline *MobileNet* architecture we have 1×1 convolution layers with numbers of filters C_1, C_2, C_3, \ldots , then in the *Mobilenet* $-\alpha$ architecture we have these numbers multiplied by α , i.e. the numbers of filters of 1×1 convolutions are $\alpha C_1, \alpha C_2, \alpha C_3, \ldots$

Overview

1 Image Classification Network Architectures

Semantic Segmentation

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Therefore, semantic image segmentation in essence is a classification of each pixel in the image.

Note

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$$L(I, P) = -\frac{1}{H \cdot W} \sum_{i,j} \sum_{k=1}^{K} GT_{i,j,k} \log(P_{i,j,k}),$$

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Note

There are also other losses for semantic segmentation about which we will discuss later in this course.

We start the investigation of semantic segmentation algorithms with FCNs - Fully Convolutional Networks¹⁰

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FCN

Fully Convolutional Networks can take inputs of arbitrary size.

At first we adapt a classifier network to the fully convolutional one. For this we can refer to each dense layer as a convolution layer with kernel size as the size of the preceding layer. Or we can just throw away the part after the last convolutional layer.

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At first we adapt a classifier network to the fully convolutional one. For this we can refer to each dense layer as a convolution layer with kernel size as the size of the preceding layer. Or we can just throw away the part after the last convolutional layer. In both cases the question arises how to **upsample** the resulting tensor to the input image size. This can be done, for example, with bilinear upsampling. Also a method called **deconvolution or transposed convolution** is used. The latter enables us also to train these upsampling parts of the network. We will talk about transposed convolutions later.

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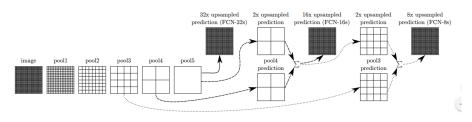


Figure: Pools are the pooling layers of some fully convolutional network, adapted from a classification network

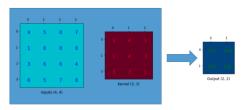
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Question: How?

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Question: How? *Answer:* By using the concept of the *convolution matrix*, which is described below.

Let's investigate a simple case, when we have a tensor X of shape 4×1 and we want to convolve it by the filter ϕ of shape $3\times 3\times 1$ (without padding and strides), the output, let's denote it by X', will be of shape $2\times 2\times 1$ as shown in the figure below:



Flattening

Let $A = (a_{ij})^{H \times W}$ be a real-valued matrix. We call the vector

$$A^f = (a_{11} \ a_{12} \ \dots \ a_{1W} \ a_{21} \ a_{22} \ \dots \ a_{2W} \ \dots \ a_{HW})$$

the flattened vector of A. The operation $A \mapsto A^f$ we call the flattening operation.

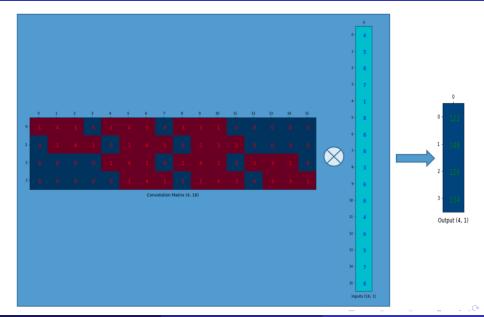
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So in the above considered case we can obtain the matrix X' firstly by obtaining its flattened version X'^f then reshape it to the shape $2\times 2\times 1$. We can obtain the vector X'^f by the following way:



As you can see, the red part of this matrix is composed of the elements of the convolution kernel. We call this matrix **the convolution matrix** of the convolution operation. Let's denote the convolution matri by $Conv(X, \phi)$.

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Exercise

Formalize the concept of the convolution matrix in case of arbitrary sizes of input, kernel and the convolution type (padding, strides).

Note

We have consider the case when input tensor is one-channeled. If it has C channels, we can obtain the result of the convolution by applying per-channel convolutions, then sum the obtained C matrices (and repeat this process C' times, when C' is the number of output filters of the convolution operation)

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Exercise

Define the concept of the convolution matrix in the general case.

Sometimes we need to do the backward operation of the convolution operation. For this we introduce the concept of transposed convolution.

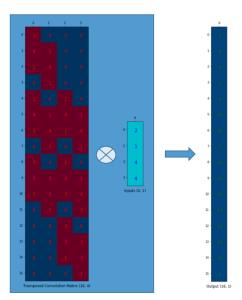
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$$Conv(X,\phi)X^f=X'^f.$$

Hence we get

$$X^f = Conv(X, \phi)^T X'^f.$$

In the image below you can see the illustration of this for our example:



Definition (Transposed Convolution)

The mapping

$$\mathit{TrConv}: \mathbb{R}^{H' \times W' \times 1} \to \mathbb{R}^{H \times W \times 1} \qquad \mathit{X'} \mapsto \mathit{Reshape}(\mathit{Conv}(\mathit{X}, \phi)^T \mathit{X'}^f),$$

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is called a **transposed convolution** with the kernel ϕ .

Note

It seems, that the matrix $Conv(X,\phi)$ depends on the tensor X, but, actually, it only depends on ϕ , the shape of X, the padding and the stride of the convolution. So, the transposed convolution is **well defined** if the kernel, padding and stride of the convolution is given (the shape of X can be obtained from the padding, the strides and the shape of X').

Note

As in case of convolutions, if the input of a transposed convolution operation has C channels, we apply the operation per-channel then sum the resulting 1-channeled outputs.

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Exercise

Determine the output shape of transposed convolution with kernel size k, padding p (from each size) and strides (s, s).

Dilated Convolutions

RefiNet

PSPNet

UNET

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