

# Word2Vec/Glove/FastText

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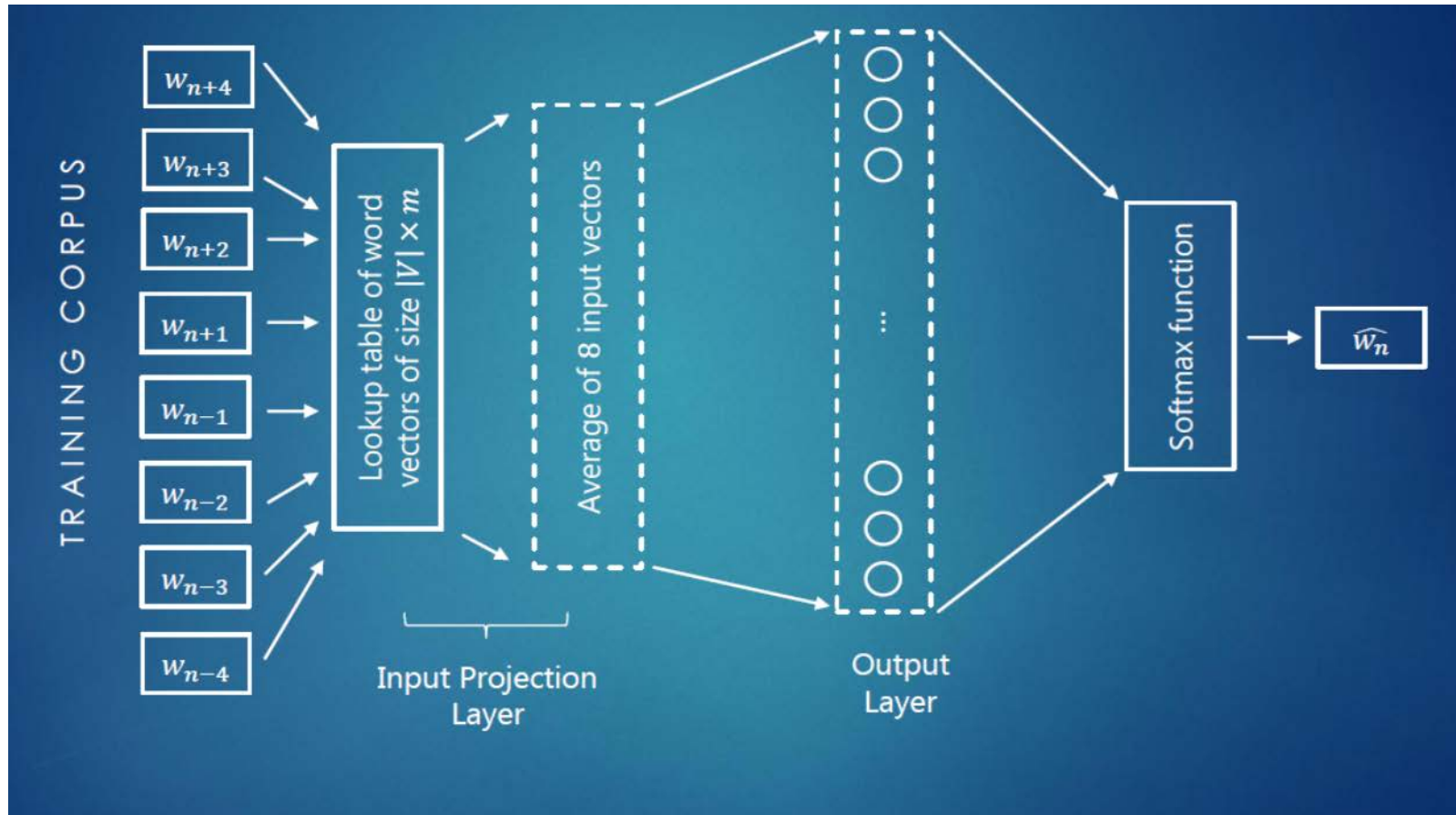
Computational Linguistics

#Semantics with Dense Vectors

Supplement Data

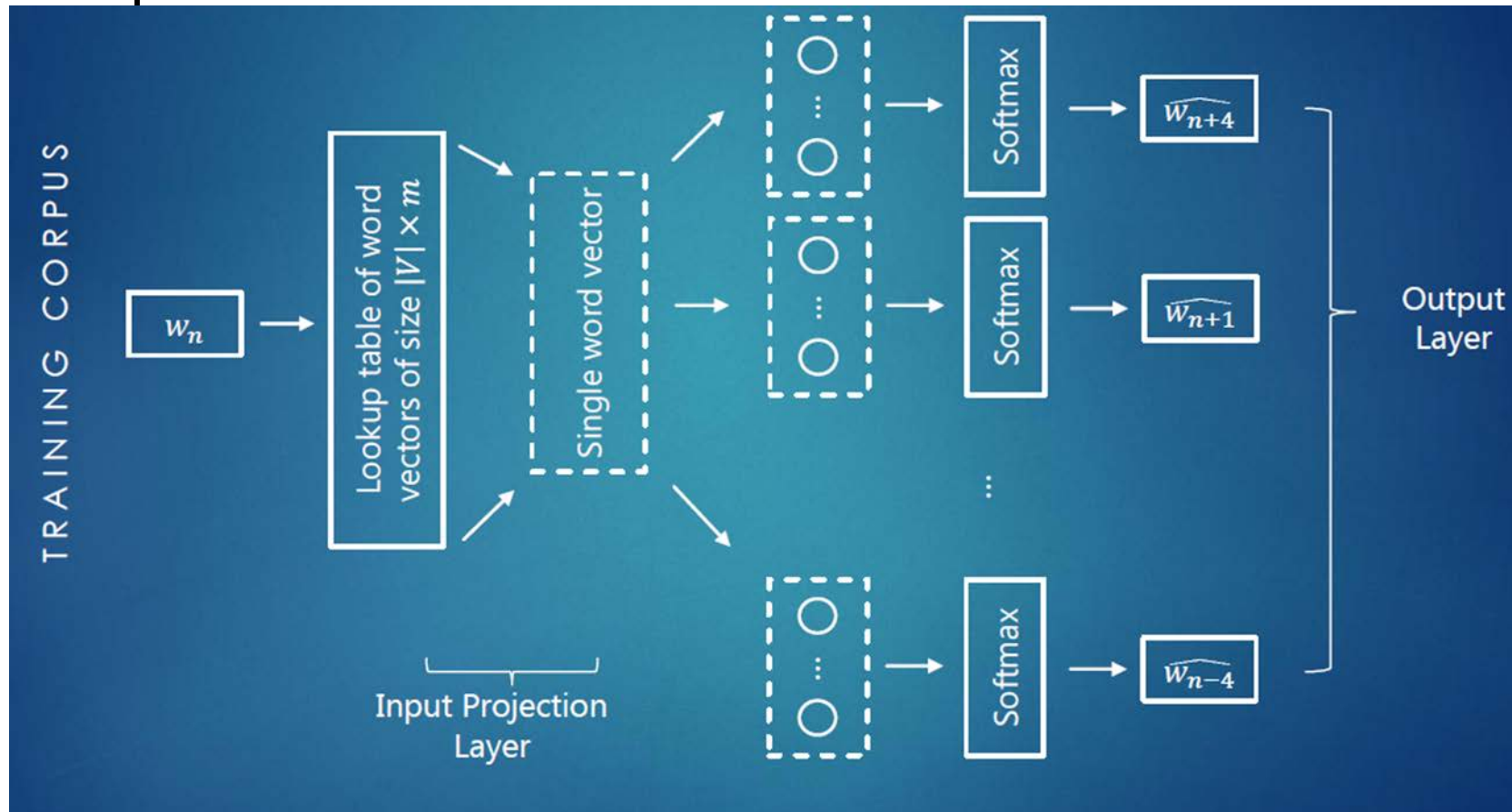
# Word2Vec

- CBOW: Continuous Bag of words

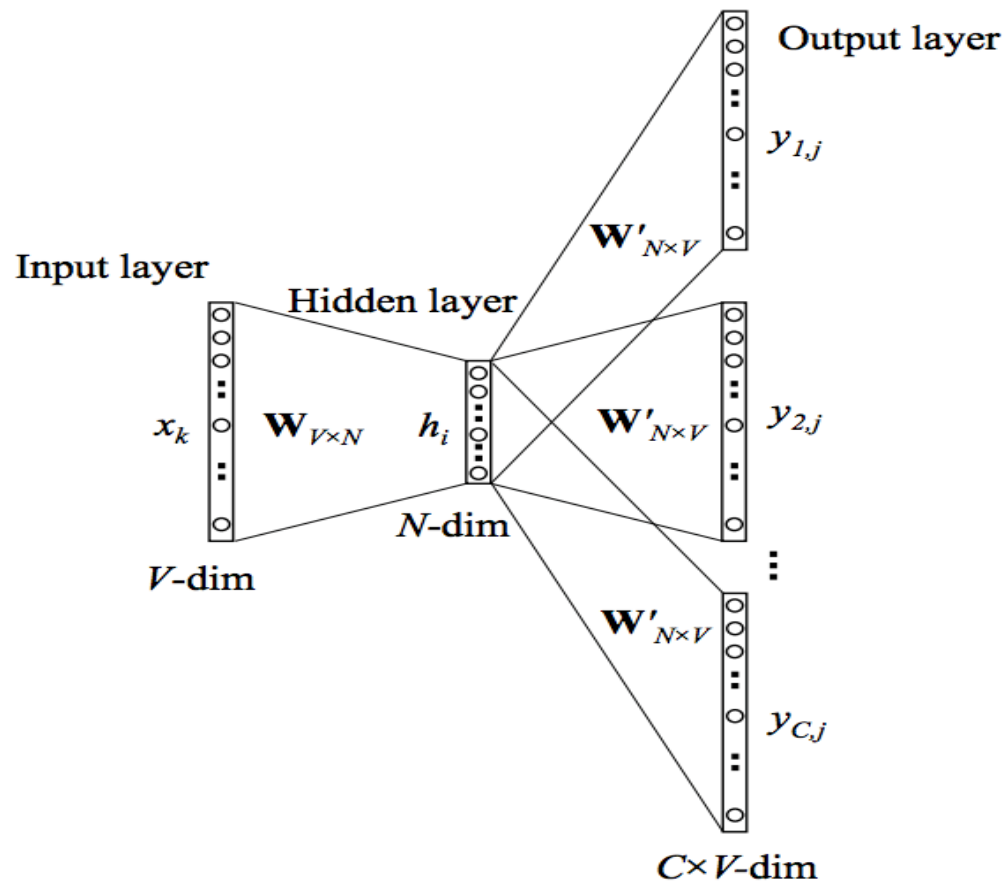


# Word2Vec

- Skip-Gram

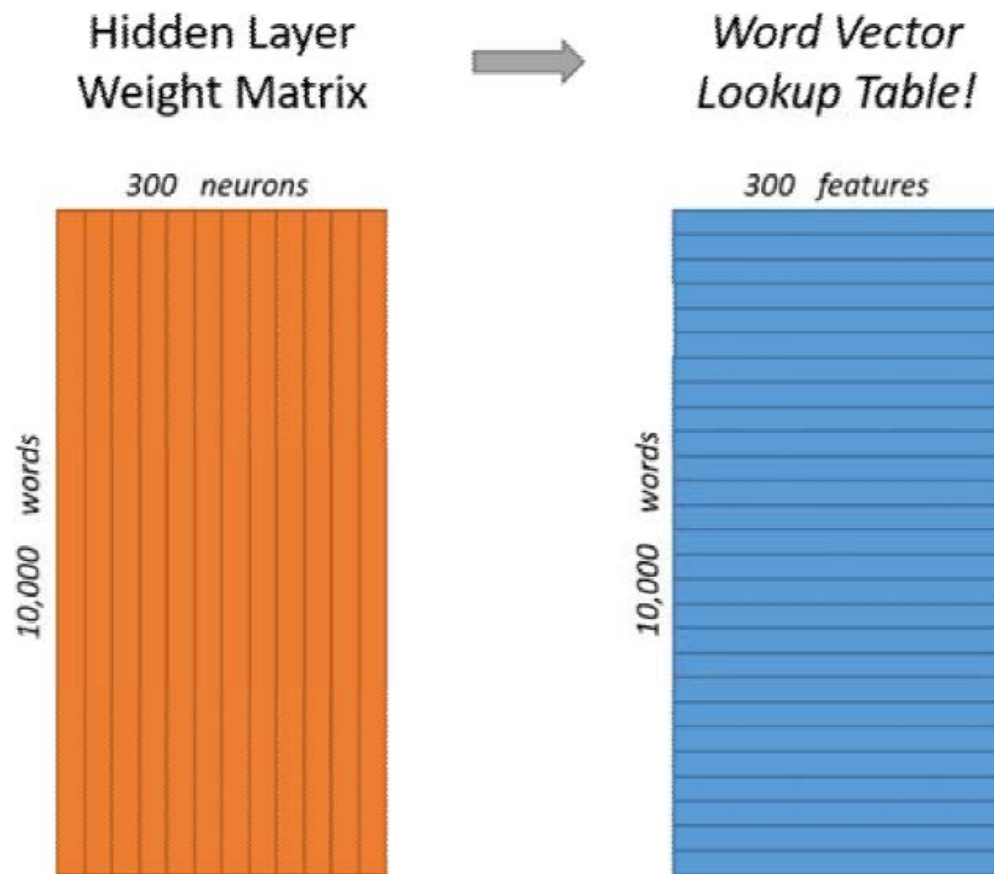


# Word2Vec 학습 패러미터(skip-gram)



# Word2Vec

- V-임베딩 단어수
- N-은닉층의 노드 개수
- 중심단어로 주변단어를 맞추거나, 주변단어로 중심단어를 맞추기 위해 가중치 행렬인  $W$ ,  $W'$ 을 조금씩 업데이트 하면서 이루어지는 구조



# Word2Vec

- 학습이 마무리되면  $W$ 의 행벡터들이 각 단어에 해당하는 임베딩이 됨

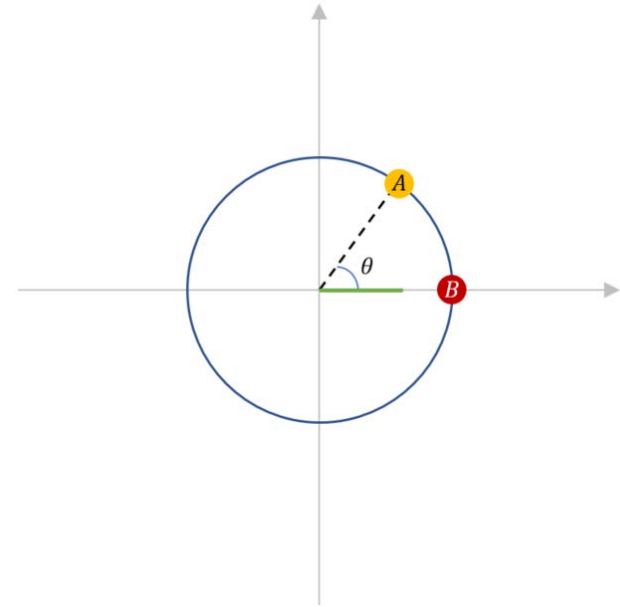
$$[0 \quad 0 \quad 0 \quad 1 \quad 0] \times \begin{bmatrix} 17 & 24 & 1 \\ 23 & 5 & 7 \\ 4 & 6 & 13 \\ 10 & 12 & 19 \\ 11 & 18 & 25 \end{bmatrix} = [10 \quad 12 \quad 19]$$

# Word2Vec 입력과 Skip-Gram

Source Text	Training Samples			
<table><tr><td>The</td><td>quick</td><td>brown</td></tr></table> fox jumps over the lazy dog. ➡	The	quick	brown	(the, quick) (the, brown)
The	quick	brown		
The <table><tr><td>quick</td><td>brown</td><td>fox</td></tr></table> jumps over the lazy dog. ➡	quick	brown	fox	(quick, the) (quick, brown) (quick, fox)
quick	brown	fox		
The quick <table><tr><td>brown</td><td>fox</td><td>jumps</td></tr></table> over the lazy dog. ➡	brown	fox	jumps	(brown, the) (brown, quick) (brown, fox) (brown, jumps)
brown	fox	jumps		
The quick brown <table><tr><td>fox</td><td>jumps</td><td>over</td></tr></table> the lazy dog. ➡	fox	jumps	over	(fox, quick) (fox, brown) (fox, jumps) (fox, over)
fox	jumps	over		

# Word2vec 학습 - 코사인 유사도

- A와 B가 겹칠 때( $\Theta = 0$ ),  
 $\cos(\Theta) = 1$
- $\cos(\Theta)$ 는 단위원 내 벡터  
들끼리의 내적과 같음
- 내적이 커진다는 것은  
두 벡터가 이루는  $\Theta$ 가  
작아지고, 유사도는 높아  
진다
- Cos인과 내적을 목적함  
수에 활용





# Word2Vec 학습(skip-gram): 목적함수

- Skip-gram: 중심단어( $c$ )가 주어졌을 때 주변단어 ( $o$ )가 나타날 확률을 최대화 하는 식으로 학습이 이루어짐

$$P(o|c) = \frac{\exp(u_o^T v_c)}{\sum_{w=1}^W \exp(u_w^T v_c)}$$

- $v$ : 입력층-은닉층을 잇는 가중치 행렬  $W$ 의 행벡터
- $u$ : 은닉층-출력층을 잇는 가중치 행렬  $W$ 의 열벡터
- 최대화:
  - 분자 지수를 키움-중심단어( $c$ )에 대한 주변단어( $o$ ) 벡터의 내적값을 높임.  $\Theta$ 를 줄여 유사도를 높임
  - 분모는 중심단어( $c$ )와 학습말뭉치 내 모든 단어를 각각 내적한 것의 총합. 분모를 줄이기 위해서는 주변에 등장하지 않은 단어와 중심단어의 내적값을 줄여야 함.  $\Theta$ 를 크게함
  - 윈도우 내에 등장하지 않는 단어에 해당하는 벡터는 중심단어 벡터와 벡터 공간상에서 멀어지게(내적을 줄임), 등장하는 주변단어 벡터는 중심단어 벡터와 가까워지게(내적을 늘림) 하는 방식으로 벡터값을 업데이트 하면서 이루어짐

# Word2Vec: 목적함수

$$\begin{aligned}\frac{\partial}{\partial v_c} \ln P(o|c) &= \frac{\partial}{\partial v_c} \ln \frac{\exp(u_o^T v_c)}{\sum_{w=1}^W \exp(u_w^T v_c)} \\&= \frac{\partial}{\partial v_c} u_o^T v_c - \frac{\partial}{\partial v_c} \ln \sum_{w=1}^W \exp(u_w^T v_c) \\&= u_o^T - \frac{1}{\sum_{w=1}^W \exp(u_w^T v_c)} \left( \sum_{w=1}^W \exp(u_w^T v_c) \cdot u_w \right) \\&= u_o^T - \sum_{w=1}^W \frac{\exp(u_w^T v_c)}{\sum_{w=1}^W \exp(u_w^T v_c)} \cdot u_w \\&= u_o^T - \sum_{w=1}^W P(w|c) \cdot u_w\end{aligned}$$

$$v_c^{t+1} = v_c^t + \alpha (u_o^T - \sum_{w=1}^W P(w|c) \cdot u_w)$$

# Word2Vec: Complexity Reduction

- 10개의 V와  $N=100$ 일 경우에,  $W, W'$ 의 계산량은 2000만( $2 \times 10^7 \times 100$ )
- Subsampling frequent words: 자주 등장하는 단어의 학습량을 확률적인 방식으로 줄임.
  - $f(w_i)$ 는 해당 단어가 말뭉치에 등장한 비율 (해당단어빈도/전체단어수)
  - $t$ 는 사용자 지정값. 보통 0.00001
  - $f(w_i)$ 가 0.01이라면  $p(w_i)$ 는 0.9684로 100번의 학습 중 96번 정도는 학습에서 제외
  - Subsampling은 학습량을 효과적으로 줄여 계산량을 감소

$$P(w_i) = 1 - \sqrt{\frac{t}{f(w_i)}}$$

# Word2Vec: Complexity Reduction

- Negative sampling:
  - 출력층의 softmax 함수는 중심단어와 나머지 모든 단어들의 내적을 한 뒤 다시 exp를 취해야함. -> 계산량이 큼
  - Softmax를 구할 때 전체 단어를 대상으로 하지 않고 일부만 뽑아 계산
  - 지정한 윈도우 사이즈 내에 등장하지 않는 단어(negative sample)를 5-20개 정도 뽑은 후 이를 정답단어와 합쳐 이것만으로 softmax를 계산.
  - 윈도우 사이즈가 5일 경우 최대 25개 단어를 대상으로만 softmax 확률을 계산하고, 패러미터 업데이트도 25개만 함
  - 윈도우 내에 등장하지 않는 어떤 단어( $w_i$ )가 negative sample로 뽑힐 확률
- 예) is:  $0.9^{(3/4)} = 0.92$  (2.2% 증가)  
Constitution:  $0.09^{(3/4)} = 0.16$   
bombastic:  $0.01^{(3/4)} = 0.032$  (220% 증가)

$$P(w_i) = \frac{f(w_i)^{3/4}}{\sum_{j=0}^n f(w_j)^{3/4}}$$

# Glove(Global Vectors for Word Representation)

- GloVe is an unsupervised learning algorithm for obtaining vector representations for words. Training is performed on aggregated global word-word co-occurrence statistics from a corpus, and the resulting representations showcase interesting linear substructures of the word vector space.
  - While methods like LSA efficiently leverage statistical information, they do relatively poorly on the word analogy task, indicating a sub-optimal vector space structure. Methods like skip-gram may do better on the analogy task, but they poorly utilize the statistics of the corpus since they train on separate local context windows instead of on global co-occurrence counts.
  - <https://nlp.stanford.edu/projects/glove/>

# Glove(Global Vectors for Word Representation)

- GloVe is essentially a log-bilinear model with a weighted least-squares objective. The main intuition underlying the model is the simple observation that ratios of **word-word co-occurrence probabilities** have the potential for encoding some form of meaning

Probability and Ratio	$k = solid$	$k = gas$	$k = water$	$k = fashion$
$P(k ice)$	$1.9 \times 10^{-4}$	$6.6 \times 10^{-5}$	$3.0 \times 10^{-3}$	$1.7 \times 10^{-5}$
$P(k steam)$	$2.2 \times 10^{-5}$	$7.8 \times 10^{-4}$	$2.2 \times 10^{-3}$	$1.8 \times 10^{-5}$
$P(k ice)/P(k steam)$	8.9	$8.5 \times 10^{-2}$	1.36	0.96

- 특정 문맥 단어가 주어졌을 때 임베딩된 두 단어벡터의 내적이 두 단어의 동시등장확률간 비율에 되게끔 임베딩
- solid*라는 문맥 단어가 주어졌을 때 *ice*와 *steam* 벡터 사이의 내적값이 8.9가 되도록
- 단어 상호간 비율 정보를 말뭉치 전체를 놓고 한꺼번에 반영하면 좀 더 정확한 임베딩이 될 것이라고 가정

# Glove(Global Vectors for Word Representation)

- Objective Function

- $P_{ik} = P(k|i)$  :  $i$ 번째 단어가 등장했을 때  $k$ 라는 문맥 단어(context word)가 등장할 조건부 확률,  
 $P(\text{solid}|\text{ice})$
- $P_{ik}/P_{jk} : P(\text{solid}|\text{ice})/ P(\text{solid}|\text{stream}) = 8.9$

$$F(w_{\text{ice}}, w_{\text{stream}}, w_{\text{solid}}) = \frac{P_{\text{ice}, \text{solid}}}{P_{\text{stream}, \text{solid}}} = \frac{P(\text{solid}|\text{ice})}{P(\text{solid}|\text{stream})} = \frac{1.9 \times 10^{-4}}{2.2 \times 10^{-5}} = 8.9$$

- Three conditions

- $w_i, w_k$  를 서로 바꾸어도 같은 값을 가져야 함
- 코퍼스 전체에서 구한 co-occurrence matrix  $X$ 는 대칭행렬(symmetric matrix)이므로 함수는 이런 특징을 포함해야 함
- Homomorphism조건을 만족해야 함

$$F(w_i, w_j, \tilde{w}_k) = \frac{P_{ik}}{P_{jk}}$$

$$F((w_i - w_j)^T \tilde{w}_k) = \frac{P_{ik}}{P_{jk}}$$

$$w_i \longleftrightarrow \tilde{w}_k$$

$$X \longleftrightarrow X^T$$

$$F(X - Y) = \frac{F(X)}{F(Y)}$$

# Glove(Global Vectors for Word Representation)

- 이러한 조건을 만족하는 함수는 지수함수, F를  $exp$ 로 치환하고 정리
- $w_i, w_k$ 를 서로 바꾸어도 식이 성립해야 하나  $\log(P_{ik})$ 가  $\log(P_{ki})$ 와 같아야 하나  $\log(X_{ik}) - \log(X_k)$ 와  $\log(X_{ki}) - \log(X_i)$ 로 달라짐.
- 따라서  $\log(X_i)$ 를 상수항( $b_i, b_k$ )로 하여 이 조건을 만족시킴
- $\log(X_{ik})$ 는 co-occurrence matrix에 로그값을 취한것.
- 이 차이를 최소한으로 하는 것이 목적함수

$$\exp(w_i^T \tilde{w}_k - w_j^T \tilde{w}_k) = \frac{\exp(w_i^T \tilde{w}_k)}{\exp(w_j^T \tilde{w}_k)}$$

$$w_i^T \tilde{w}_k = \log P_{ik} = \log X_{ik} - \log X_i$$

$$w_i^T \tilde{w}_k = \log X_{ik} - b_i - \tilde{b}_k$$

$$w_i^T \tilde{w}_k + b_i + \tilde{b}_k = \log X_{ik}$$

$$J = \sum_{i,j=1}^V (w_i^T \tilde{w}_j + b_i + \tilde{b}_j - \log X_{ij})^2$$



# Glove(Global Vectors for Word Representation) : weighted least squares regression model

$$J = \sum_{i,j=1}^V f(X_{ij}) \left( w_i^T \tilde{w}_j + b_i + \tilde{b}_j - \log X_{ij} \right)^2$$

1.  $f(0) = 0$ . If  $f$  is viewed as a continuous function, it should vanish as  $x \rightarrow 0$  fast enough that the  $\lim_{x \rightarrow 0} f(x) \log^2 x$  is finite.
2.  $f(x)$  should be non-decreasing so that rare co-occurrences are not overweighted.
3.  $f(x)$  should be relatively small for large values of  $x$ , so that frequent co-occurrences are not overweighted.

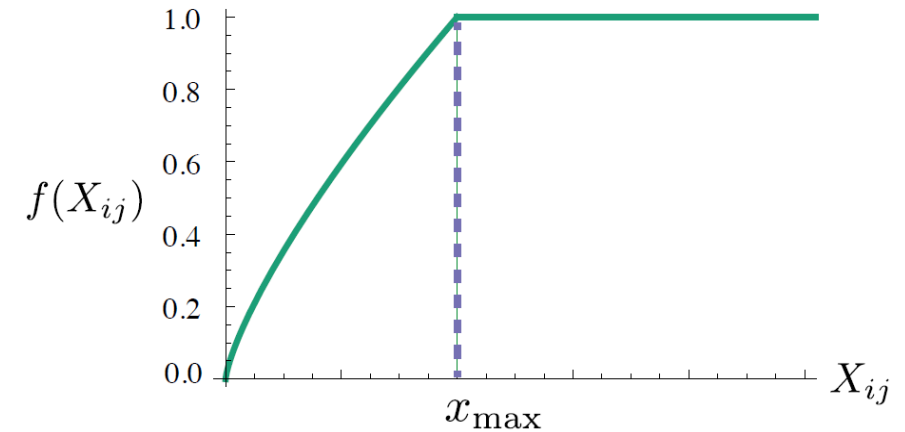


Figure 1: Weighting function  $f$  with  $\alpha = 3/4$ .

# FastText

- Facebook AI Research lab에 의한 open source
  - <https://research.fb.com/fasttext/>
  - FastText combines some of the most successful concepts introduced by the natural language processing and machine learning communities in the last few decades. These include representing sentences with **bag of words** and **bag of n-grams**, as well as using **subword information**, and **sharing information across classes** through a hidden representation.
  - It also employs a hierarchical softmax that takes advantage of the unbalanced distribution of the classes to speed up computation. These different concepts are being used for two different tasks: efficient text classification and learning word vector representations.

# General Model

- Given a word vocabulary size  $W$ , where a word is identified by its index  $w \in \{1, \dots, W\}$ , the goal is to learn a vectorial representation for each word  $w$ .
- Skip-gram model is to maximize the following log-likelihood:

$$\sum_{t=1}^T \sum_{c \in \mathcal{C}_t} \log p(w_c \mid w_t),$$

- where the context  $\mathcal{C}_t$  is the set of indices of words surrounding word  $w_t$
- one possible choice to define the probability of a context word is the softmax:

- d

$$p(w_c \mid w_t) = \frac{e^{s(w_t, w_c)}}{\sum_{j=1}^W e^{s(w_t, j)}}.$$

# General Model

- Negative Sampling

- The problem of predicting context words can be framed as a set of independent binary classification tasks
- For the word at position  $t$  we consider all context words as positive examples and sample negatives at random from the dictionary
- For a chosen context position  $c$ , using the binary logistic loss, we obtain the following negative log-likelihood:

$$\log \left( 1 + e^{-s(w_t, w_c)} \right) + \sum_{n \in \mathcal{N}_{t,c}} \log \left( 1 + e^{s(w_t, n)} \right)$$

- Where  $\mathcal{N}_{t,c}$  is a set of negative examples sampled from the vocabulary
- By denoting the logistic loss function  $\ell : x \mapsto \log(1 + e^{-x})$ , we can rewrite the objective as:

$$\sum_{t=1}^T \left[ \sum_{c \in \mathcal{C}_t} \ell(s(w_t, w_c)) + \sum_{n \in \mathcal{N}_{t,c}} \ell(-s(w_t, n)) \right]$$

# Subword Model

- By using a distinct vector representation for each word, the skipgram model ignores the internal structure of words.
  - Each word  $w$  is represented as a bag of character  $n$ -gram. FastText adds special symbols  $<$  and  $>$  at the beginning and end of words, allowing to distinguish prefixes and suffixes from other character sequences
  - Also includes  $w$  itself in the set of its  $n$ -grams, to learn a representation for each word
  - Taking the word where and  $n=3$  as an example, it will be represented by the character  $n$ -grams:
    - $<wh, whe, her, ere, re>$  and the special sequence
    - $<where>$
    - Note that the sequence  $<her>$ , corresponding to her is different from the tri-gram  $her$  from the word where.
  - In practice, they extract all the  $n$ -grams for  $n$  greater or equal 2 and smaller or equal to 6

# Subword Model

- Suppose that you are given a dictionary of *n-grams* of size  $G$ . Given a word  $w$ , let us denote by  $\mathcal{G}_w \subset \{1, \dots, G\}$ , the set of *n-grams* appearing in  $w$ .
  - Then associate a vector representation  $\mathbf{z}_g$  to each n-gram  $g$
  - The scoring function is

$$s(w, c) = \sum_{g \in \mathcal{G}_w} \mathbf{z}_g^\top \mathbf{v}_c.$$

- This simple model allows sharing the representations across words, thus allowing to learn reliable representation for rare words