

## Streams as a data structure -

2/09

$\left. \begin{array}{l} (\text{cons-stream } a \ b) \Rightarrow \text{stream, say } 's' \\ (\text{stream-car } s) \Rightarrow a \\ (\text{stream-cdr } s) \Rightarrow b \end{array} \right\} \begin{array}{l} \text{constructors} \\ \text{selectors} \end{array}$

$\text{the-empty-stream} \Rightarrow '() .$

$(\text{stream-null? } s) \Rightarrow (\text{eq? } s \ \text{the-empty-stream})$

$(\text{define } (\text{stream-enumerate } \text{low } \text{high}))$

$\text{Cif } (> \text{low } \text{high})$

$\text{the-empty-stream}$

$(\text{cons-stream } \text{low} . (\text{stream-enumerate } (+ \text{low } 1) \text{high})))$

$(\text{define } (\text{stream-filter } \text{pred } s))$

$(\text{cond } ((\text{stream-null? } s) \text{the-empty-stream})$

$((\text{pred } (\text{stream-car } s))$

$(\text{cons-stream } (\text{stream-car } s).$

$(\text{stream-filter } (\text{stream-car } s))))$

$(\text{else } (\text{stream-filter } (\text{stream-cdr } s)))) .$

$(\text{stream-car } (\text{stream-cdr } (\text{stream-filter } \text{prime?}$

$(\text{stream-enumerate } 1000000)))) .$

This is supposed to be more efficient than what we wrote earlier.

So far it looks the same as list



$(\text{cons-stream } a \ b) \Rightarrow (\text{cons } a \ (\text{delay } b))$

$(\text{stream-car } s) \Rightarrow (\text{car } s)$

$(\text{stream-cdr } s) \Rightarrow (\text{force } (\text{cdr } s))$

forces the delay.

when you pass something to a 'delay', the result is a 'promise'.

when you pass a 'delay' to 'force', it forces the promise (similar to the notion of a promise on a note). call the promise.

If we want to delay the evaluation of an expression, put it inside a lambda so that it is evaluated when it's invoked.

$(\text{delay } \langle \text{expr} \rangle) \Rightarrow (\text{lambda } () \ \langle \text{expr} \rangle)$

$(\text{force } \text{promise}) \Rightarrow (\text{promise})$

$(\text{stream-car } (\text{stream-cdr } (\text{stream-filter } \text{prime? } (\text{stream-ei } 10k \ 1M))))$

$(\text{cons } 10k \ (\text{delay } (\text{stream-ei } 10k+1 \ 1M)))$  (after shipping one step)

this is now passed to stream-filter.

is 10k a prime - applying predicate

predicate is false - goes to else branch

- applies predicate to car.

It's not being evaluated (whatever is in delay) because it wasn't called so far.

$(\text{stream-ei } 10k+1 \ 1M)$

$\Rightarrow (\text{cons } 10k+1 \ (\text{delay } (\text{stream-ei } 10k+2 \ 1M)))$



pass this to stream-filter again.

$10k+7$  - first prime  
no similar things till there

$\Rightarrow$  (cons 10007 (delay (stream-ei 10k+8 1M)))

stream-car s.

(cons 10008 (delay (stream-filter (cons 10009 1M))))

supplied to stream-cdr.in

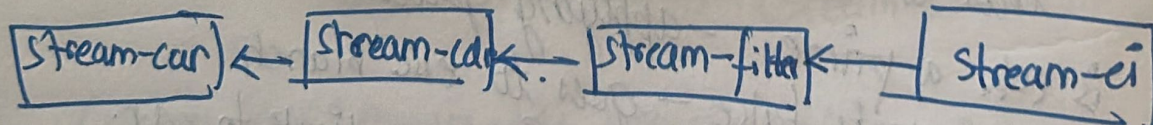
(stream-car (stream-cdr (stream-filter prime? (stream-ei 10k 1M))))

when stream-cdr forces it, calls stream-filter  
on the stream - checks the first number.  
(checks  $10k+8$  - not prime)  
(checks  $10k+9$  - prime).

stream-cdr gives out

(cons 10k+9 (delay (stream-filter (cons 10k+10 1M))))

stream-car of this? 10009



The order in which things are happening is diff  
from how the computation happens