

Chapter 3

# Memory

These slides support chapter 3 of the book

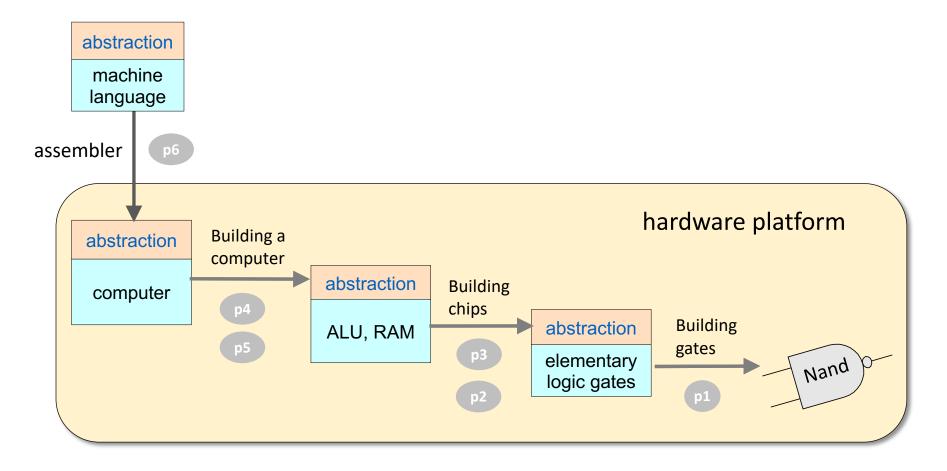
The Elements of Computing Systems

(1st and 2nd editions)

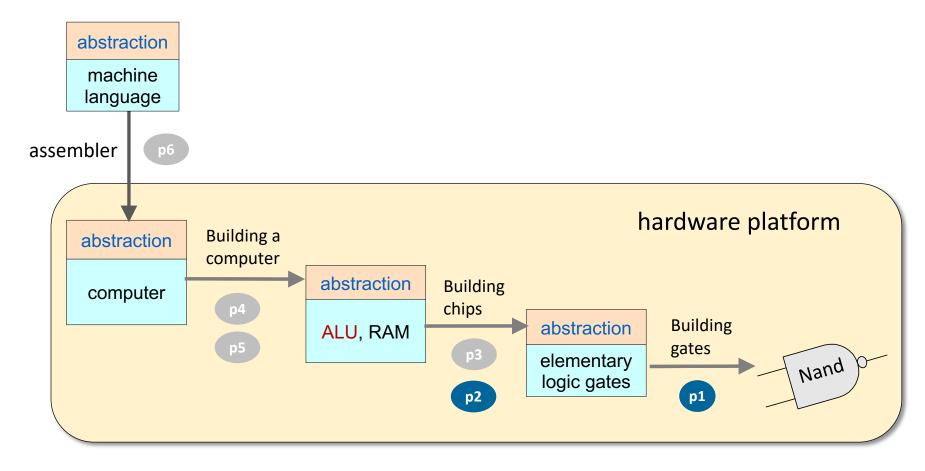
By Noam Nisan and Shimon Schocken

MIT Press

## Nand to Tetris Roadmap: Hardware



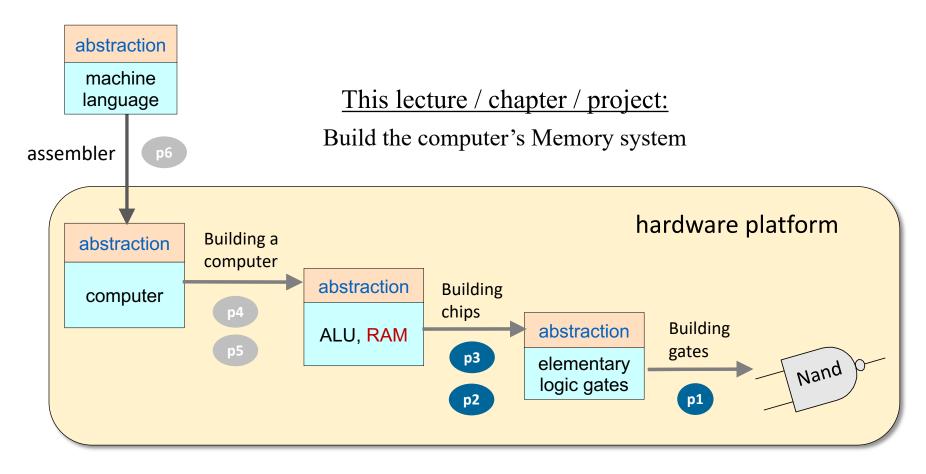
## Nand to Tetris Roadmap: Hardware



<u>Project 1</u>: Build basic logic gates

Project 2: Build the ALU

## Nand to Tetris Roadmap: Hardware



<u>Project 1</u>: Build basic logic gates

Project 2: Build the ALU

# A common theme in computer science

- We present a simple model (the simpler, the better)
- We explore the model's power:
  - What the model can do
  - What it cannot do
- We then extend the model, to make it more powerful

### Case in point:

Logic gates.

## Logic gates

Model: And, Or, Not, ...

- Simple, and powerful:
   Logic gates can realize any Boolean function, and can be combined to form powerful chips, like an ALU
- But, as a general model of computation, logic gates fall short

### **Limitations**

- Logic gates cannot store information (bits) over time
- Feedback loops are not allowed: A chip's output cannot serve as its input
- Logic gates can handle only inputs of a fixed size.

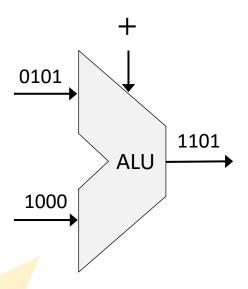
  For example, we can build an Or3 gate, and an Or4 gate, and so on, but we cannot build a single gate that computes Or for any given number of inputs

### **Extension**

Allow logic gates to be sensitive to the progression of time.

## Time-independent logic

- So far we ignored *time*
- The chip's inputs were just "sitting there" fixed and unchanging
- The chip's output was a function ("combination") of the current inputs, and the current inputs only
- This style of gate logic is sometimes called:
  - □ time-independent logic
  - □ combinational logic
- All the chips that we discussed and developed so far were combinational



ALU: The "topmost" combinational chip

## Hello, time

### Software needs:

- The hardware must be able to remember things, over time:
- The hardware must be able to do things, one at a time (sequentially):

### Hardware needs:

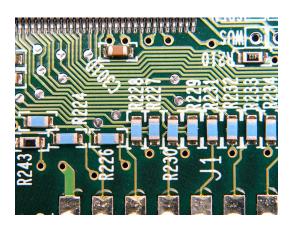
• The hardware must handle the *physical time delays* associated with *computing* and *moving* data from one chip to another.

#### Example (variables):

$$x = 17$$

#### Example (iteration):

for i in range(0, 10):
 print(i)



## Hello, time

### Software needs:

- The hardware must be able to remember things, over time:
- The hardware must be able to do things, one at a time (sequentially):

### Hardware needs:

• The hardware must handle the *physical time delays* associated with *computing* and *moving* data from one chip to another.

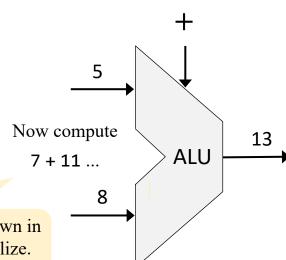
It will take some time before 7 and 11 will settle down in the input ports, and before the sum 7 + 11 will stabilize. Till then, the ALU will output nonsense.

#### Example (variables):

$$x = 17$$

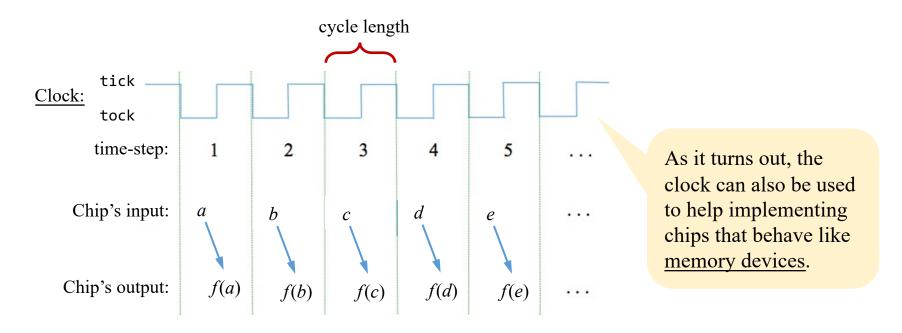
#### Example (iteration):

for i in range(0, 10):
 print(i)



## Hello, time

Solution: We can neutralize the time delays if we decide to use discrete time



- Set the *cycle length* to be slightly > than the maximum time delay, and...
- Decide to use the chips's outputs only at the end of cycles (time-steps), ignoring what happens within cycles
- Details later.

## Memory

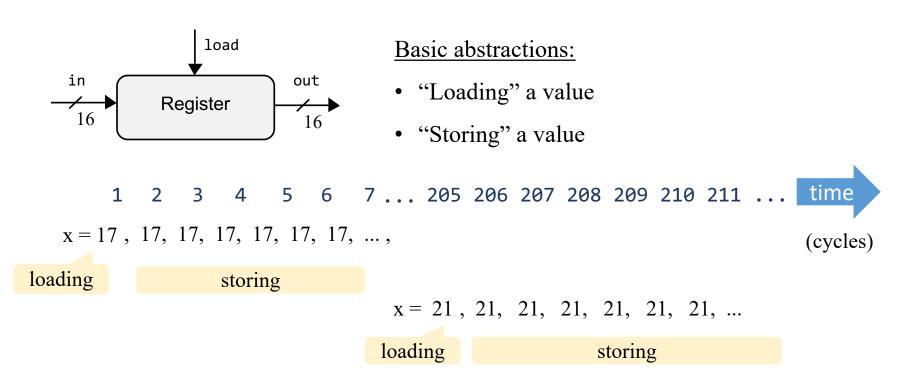
Memory: The faculty of the brain by which data or information is encoded, stored, and retrieved when needed. It is the *retention of information over time* for the purpose of influencing future action (Wikipedia)

## Memory is time-based:

We remember *now* what was committed to memory *earlier*.

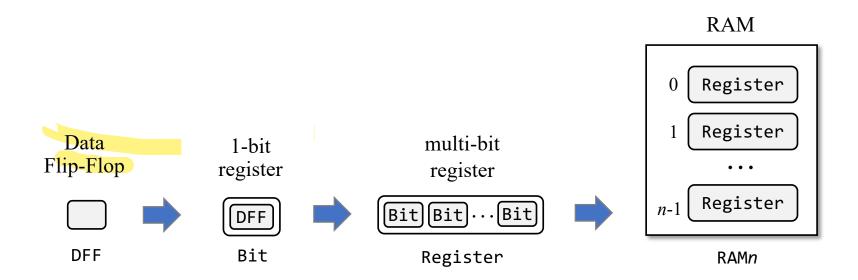


## Memory



The challenge: Building chips that realize this functionality.

## Memory



The challenge: Building chips that realize this functionality.

## Chapter 3: Memory

## **Abstraction**

- Representing time
- Clock
- Registers
- RAM
- Counters

## **Implementation**

- Data Flip Flop
- Registers
- RAM
- Project 3: Chips
- Project 3: Guidelines

# Chapter 3: Memory

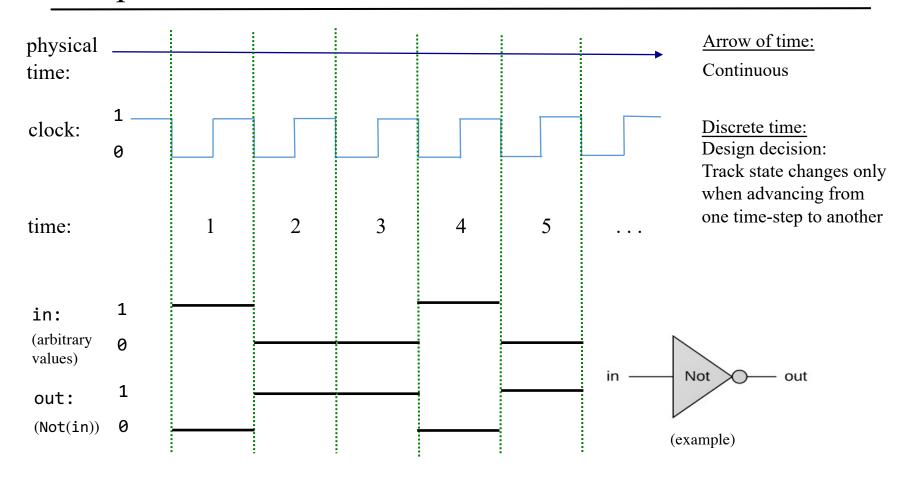
## **Abstraction**



- Clock
- Registers
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- Counters

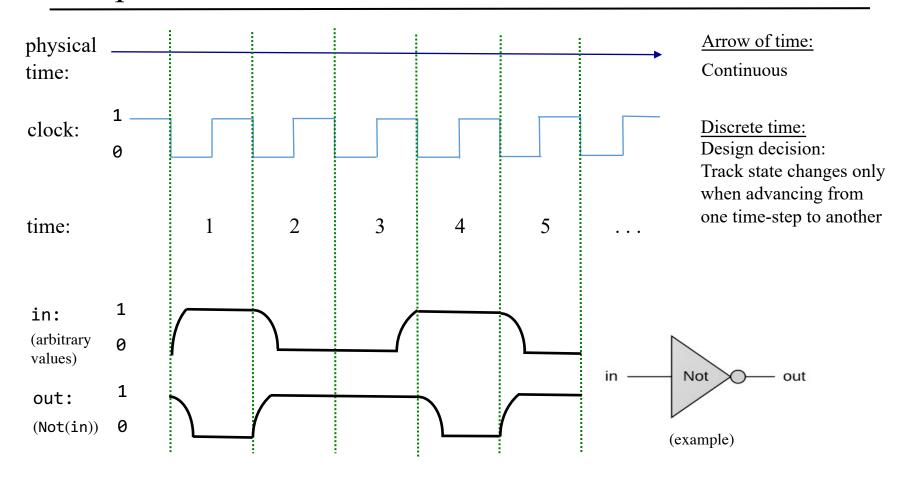
## **Implementation**

- Data Flip Flop
- Registers
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- Project 3: Guidelines



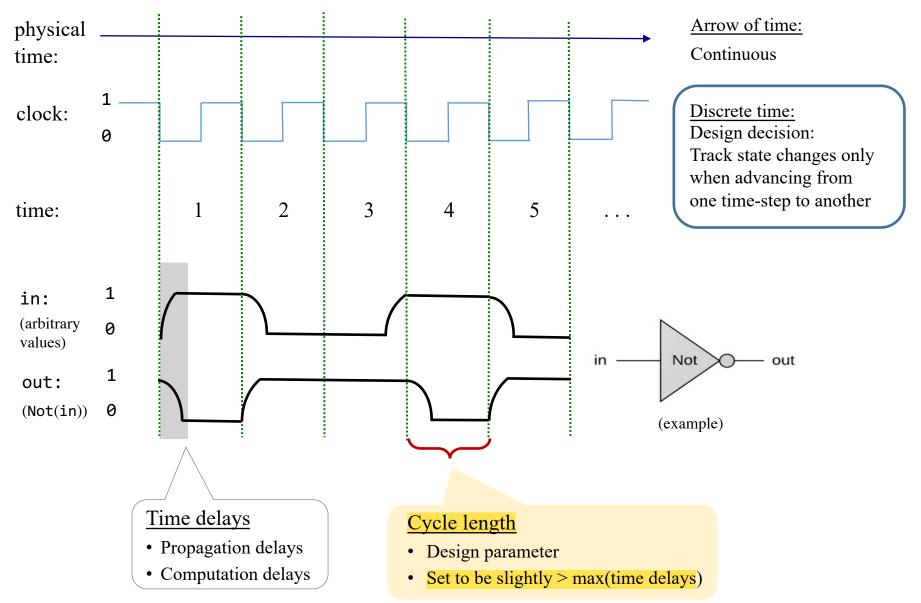
Desired / idealized behavior of the in and out signals:

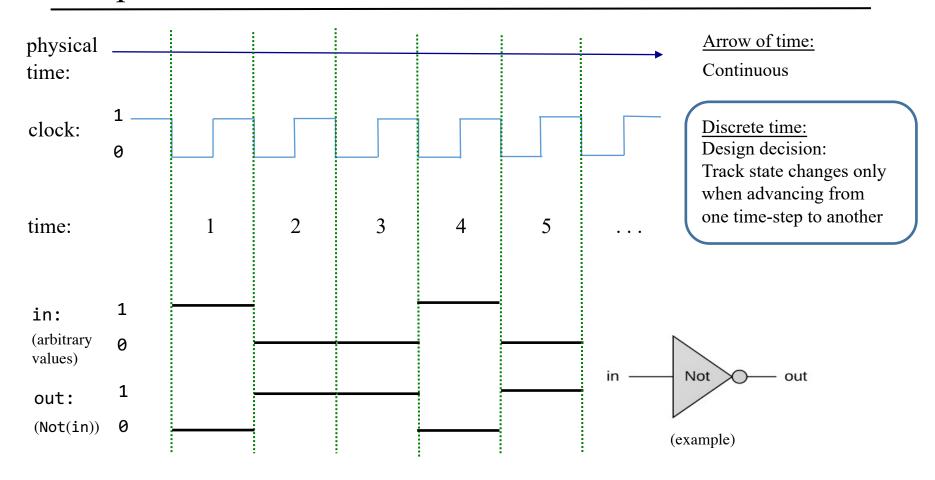
That's how we want the hardware to behave



Actual behavior of the in and out signals:

Influenced by physical time delays





## Resulting effect:

- Combinational chips react "immediately" to their inputs
- Facilitated by the decision to track changes only at cycle ends

## Chapter 3: Memory

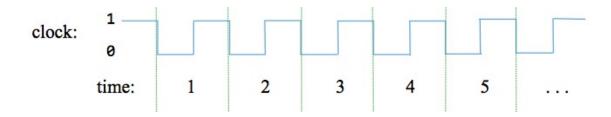
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## Clock: Simulated implementation



#### <u>Interactive simulation</u>

A clock icon can be used to generate a sequence of tick-tock signals:



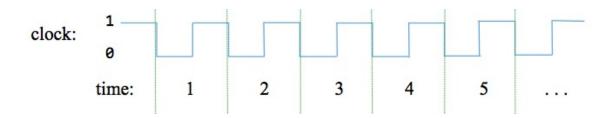


### **Script-based simulation**

"tick" and "tock" commands can be used to advance the clock:

```
// Sets inputs, advances the clock, and
// writes output values as it goes along.
set in 19,
set load 1,
tick,
output,
tock,
output,
tick, tock,
output,
...
```

## Clock: Physical implementation



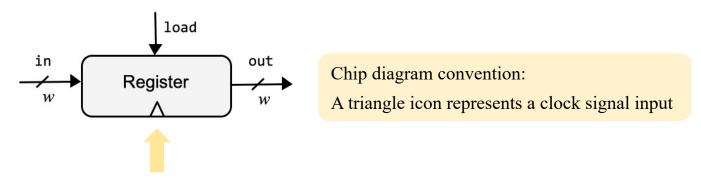
### Physical clock

• An oscillator is used to deliver an ongoing train of "tick/tock" signals



"1 MHz electronic oscillator circuit which uses the resonant properties of an internal quartz crystal to control the frequency. Provides the clock signal for digital devices such as computers." (Wikipedia)

• The oscillator's output is connected to all the time-based (clocked) chips in the computer



# Chapter 3: Memory

### **Abstraction**

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### **Implementation**

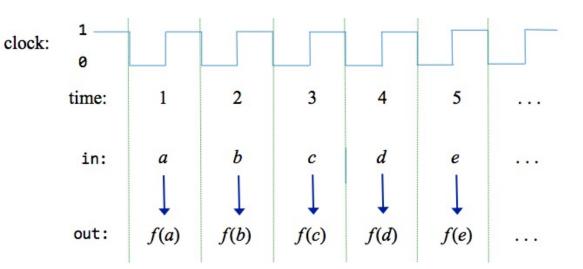
- Data Flip Flop
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# Combinational logic / Sequential logic

### Combinational logic:

The output depends on the current inputs

The clock is used to stabilize outputs

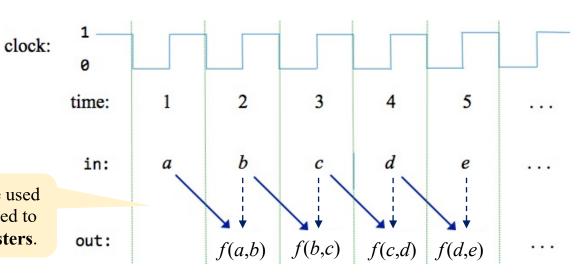


### Sequential logic:

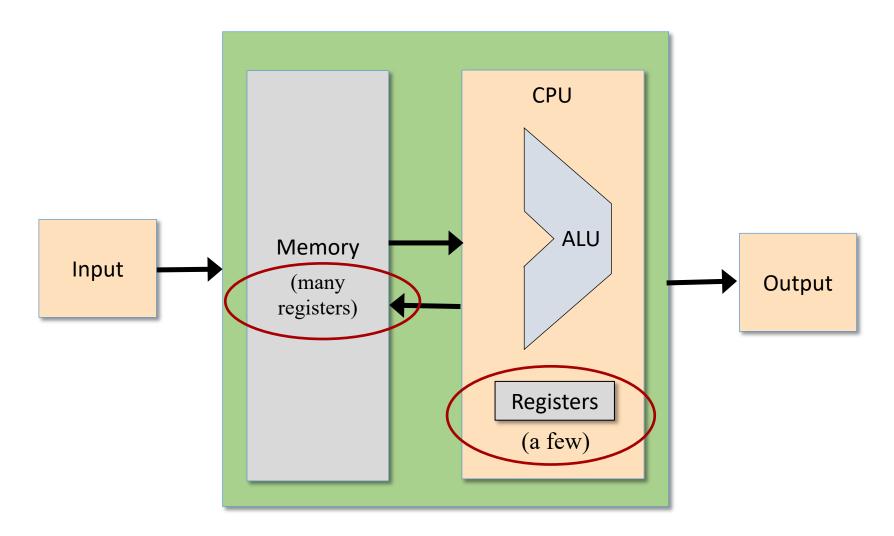
The output depends on:

- Previous inputs
- Current inputs (optionally)

This behavior can be used to build chips designed to maintain state: **Registers**.

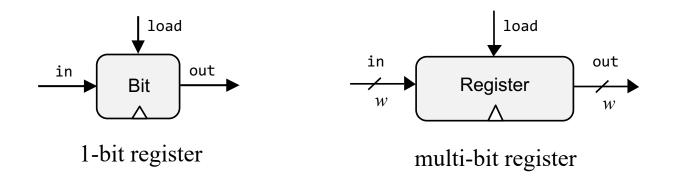


# Registers



Computer Architecture

## Registers



### Designed to:

- "Store" / "remember" / "maintain" / "persist" a value, until...
- "Instructed" to "load", and then "store", another value.

$$x = 17, 17, 17, 17, 17, 17, 17, ..., 17$$

loading

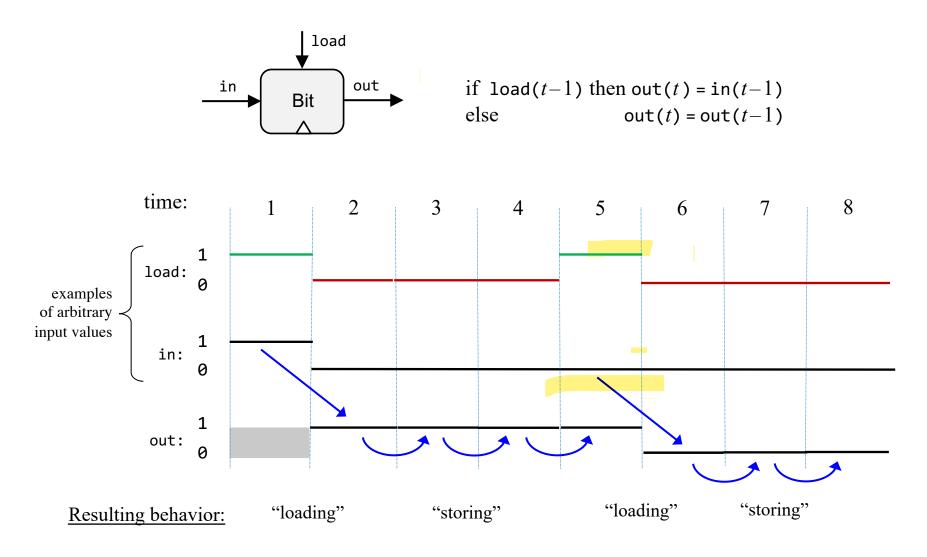
maintaining state

$$x = 21, 21, 21, 21, 21, 21, ..., 21$$

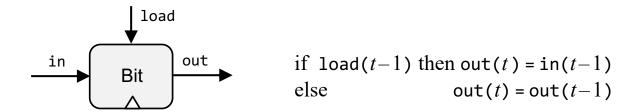
loading

maintaining state

## 1-Bit Register



## 1-Bit Register



### <u>Usage:</u> To read:

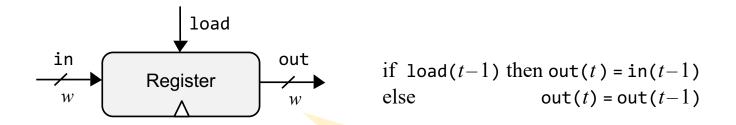
probe out (out always emits the register's state)

#### To write:

set in = v Result: The register's state becomes v;

set load = 1 From the next time-step onward, out will emit v

## Multi-bit Register



We'll focus on word width w = 16, without loss of generality

<u>Load / store behavior:</u> Exactly the same as a 1-bit register

Read / write usage: Exactly the same as a 1-bit register



# Chapter 3: Memory

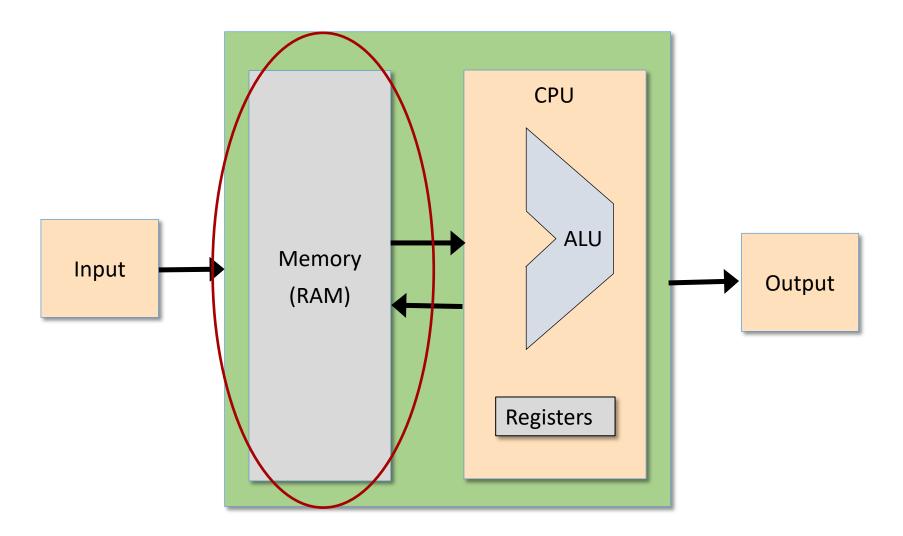
### **Abstraction**

- ✓ Representing time
- ✓ Clock
- ✓ Registers
- RAM
  - Counters

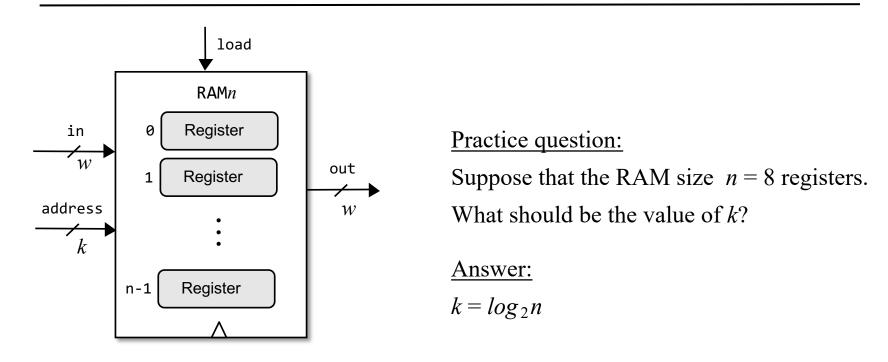
## **Implementation**

- Data Flip Flop
- Registers
- RAM
- Project 3: Chips
- Project 3: Guidelines

# Computer architecture



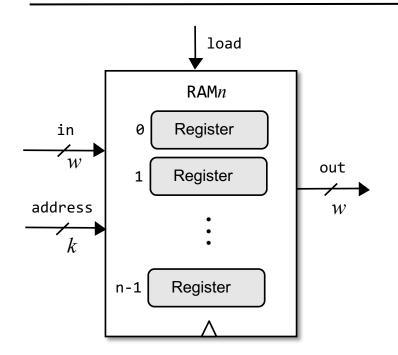
## RAM



Abstraction: A sequence of *n* addressable, *w*-bit registers, with addresses 0 to *n*-1

Word width: Typically 16, 32, 64 bits (Hack computer: w = 16)

## **RAM**



### **Behavior**

If load == 0, the RAM maintains its state

If load == 1, RAM[address] is set to the value of in

The loaded value will be emitted by out from the next time-step (cycle) onward, until the next load

(Only one RAM register is selected; All the other registers are not affected)

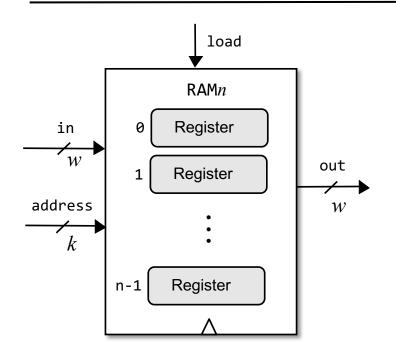
### <u>Usage:</u> To read register i:

set address = i, probe out (out always emits the value of RAM[i])

#### To write v in register i:

set address = i, set in = v, Result: RAM[i]  $\leftarrow v$ set load = 1 From the next time-step onward, out will emit v

## **RAM**



### Why "Random Access Memory"?

Irrespective of the RAM size (*n*), every randomly selected register can be accessed "instantaneously", at more or less the same speed.



# Chapter 3: Memory

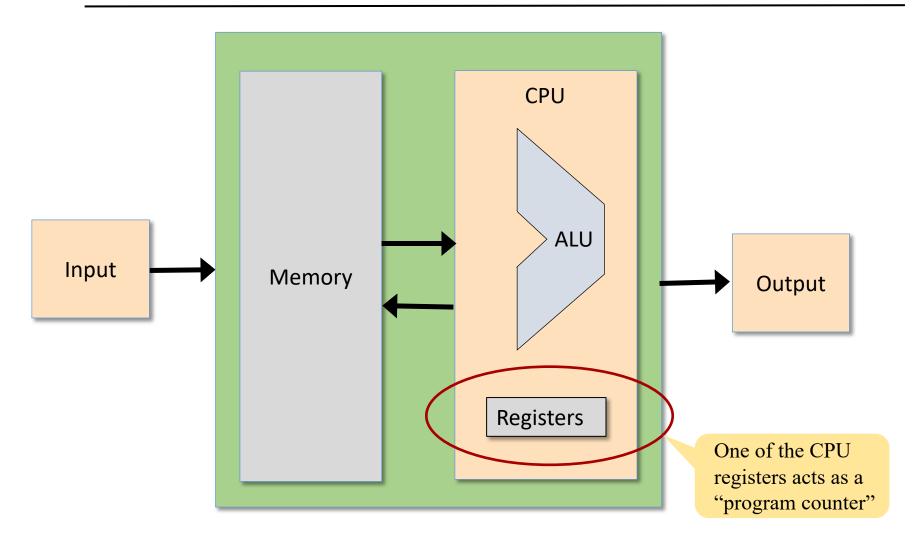
### **Abstraction**

- ✓ Representing time
- ✓ Clock
- ✓ Registers
- **✓** RAM
- Counters

## **Implementation**

- Data Flip Flop
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# Computer architecture



# Counter

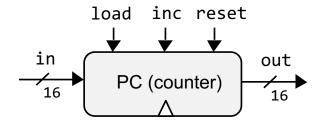
- Later in the course (chapter 5), we will see that the computer must keep track of which instruction should be fetched and executed next
- This task is regulated by a register typically called Program Counter
- We'll use the PC to store the address of the instruction that should be fetched and executed next
- The PC should support three abstractions:

Reset: fetch the first instruction PC = 0

Next: fetch the next instruction PC++

Goto: fetch instruction n PC = n

# Counter



if reset(t) out(t+1) = 0 else if load(t) out(t+1) = in(t) else if inc(t) out(t+1) = out(t) + 1 else out(t+1) = out(t)

## <u>Usage:</u>

#### To read:

probe out

#### To set:

set in to v, assert load, set the other control bits to  $\theta$ 

#### To reset:

assert reset, set the other control bits to 0

#### To count:

assert inc, set the other control bits to 0



# Chapter 3: Memory

## **Abstraction**

• Representing time



- Clock
- Registers
- RAM
- Counters

## **Implementation**

- Data Flip Flop
- Registers
- RAM
- Project 3: Chips
- Project 3: Guidelines

# Chapter 3: Memory

## Abstraction

- Representing time
- Clock
- Registers
- RAM
- Counters

## **Implementation**



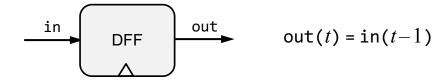
Data Flip Flop

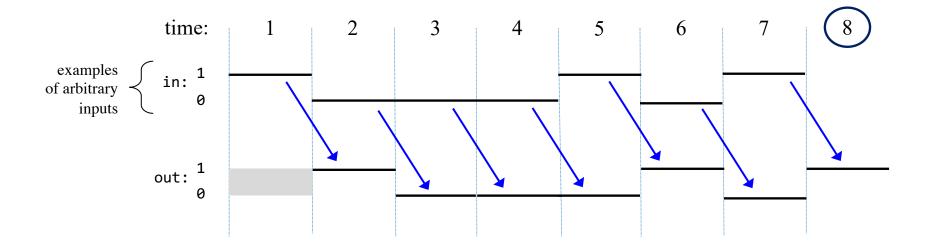
- Registers
- RAM
- Project 3: Chips
- Project 3: Guidelines

# **DFF**

## Data Flip Flop (aka latch)

The most elementary sequential gate: Outputs the input in the previous time-step

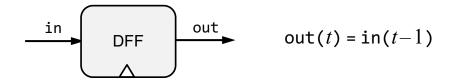


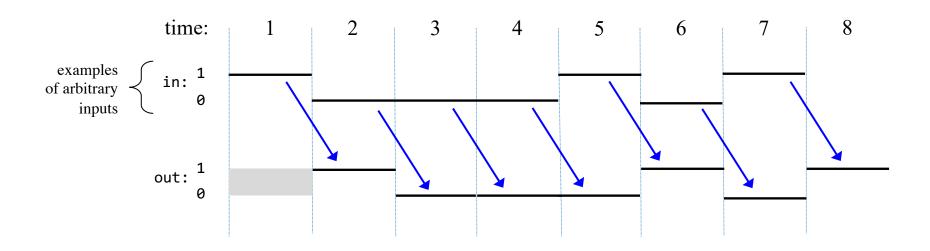


# From DFF to a 1-bit register

#### Data Flip Flop (aka *latch*)

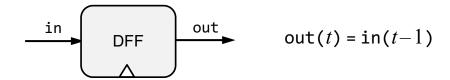
The most elementary sequential gate: Outputs the input in the previous time-step





How can we "load" and then "maintain" a value (0 or 1) over time, without having to feed the value in every cycle?

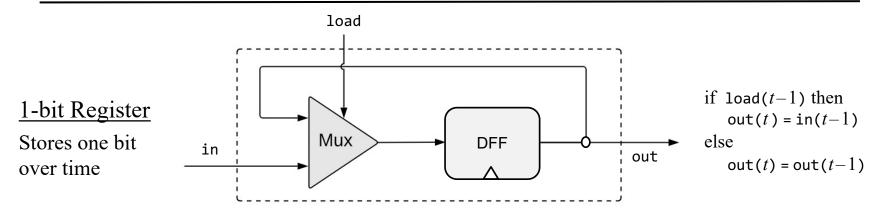
# From DFF to a 1-bit register



We have to realize a "loading" behavior and a "storing" behavior, and be able to select between these two states

How can we "load" and then "maintain" a value (0 or 1) over time, without having to feed the value in every cycle?

# From DFF to a 1-bit register

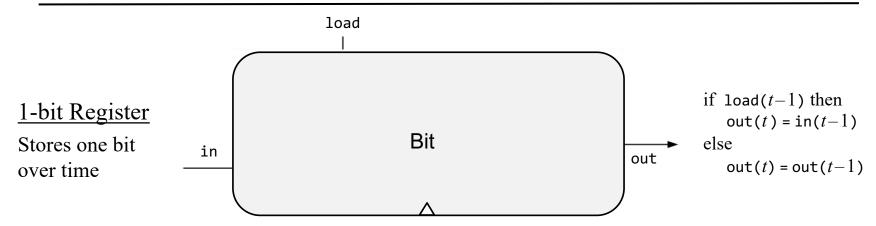


We have to realize a "loading" behavior and a "storing" behavior, and be able to select between these two states

## **Behavior**

if load == 1 the register's value becomes in else the register maintains its current value

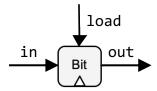
# Register



# Register

## 1-bit Register

Stores one bit over time



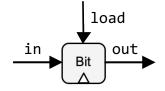
zoom out...

if 
$$load(t-1)$$
 then  
 $out(t) = in(t-1)$   
else  
 $out(t) = out(t-1)$ 

# Register

## 1-bit Register

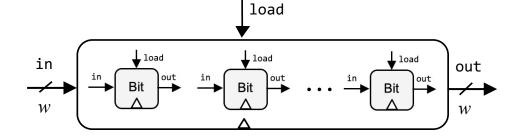
Stores one bit over time



if load(t-1) then out(t) = in(t-1)else out(t) = out(t-1)

## w-bit Register:

Stores *w* bits over time



Partial diagram, showing some of the chip-parts, without connections

# Chapter 3: Memory

## **Abstraction**

- Representing time
- Clock
- Registers
- RAM
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## **Implementation**

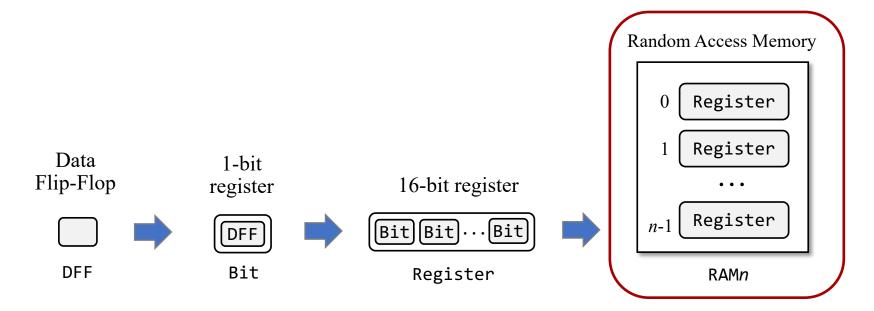




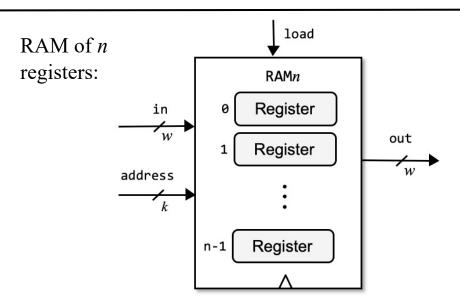


- Project 3: Chips
- Project 3: Guidelines

# Memory hierarchy



# RAM: Abstraction



## <u>Usage:</u> To read register i:

set address = i, probe out (out always emits the state of RAM[i])

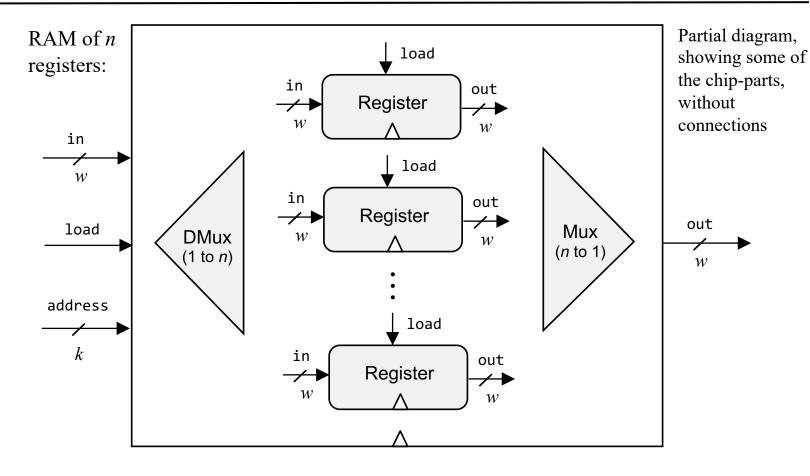
## To write v in register i:

```
set address = i,

set in = v, Result: RAM[i] \leftarrow v

set load = 1 From the next time-step onward, out emits v
```

# **RAM: Implementation**

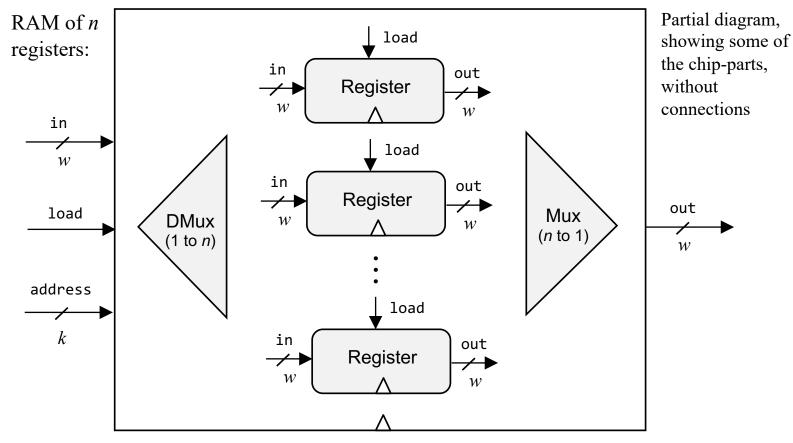


Reading: Can be realized using a Mux

Writing: Can be realized using a DMux

Connections?
You figure it out

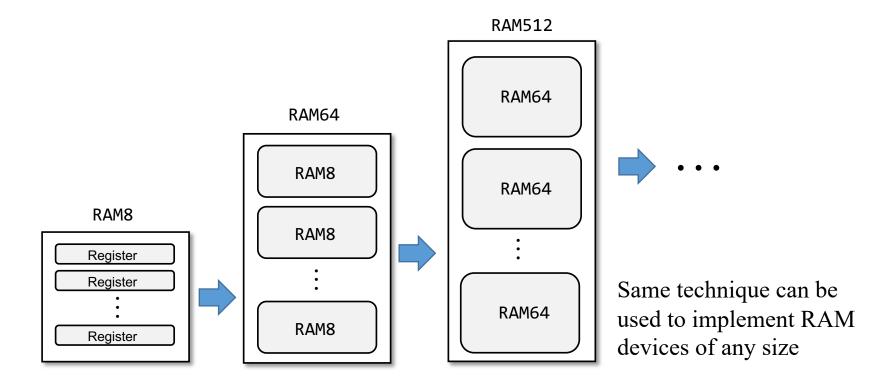
# RAM: Implementation



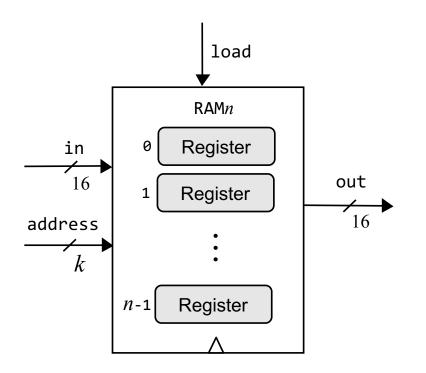
## **Observations**

- The addressing/selection/reading logic is *combinational*
- The writing logic is (i) sequential (clocked)
  - (ii) embedded in the Register logic.

# RAM: Implementation



# Hack RAM



A family of 16-bit RAM chips:

chip name	n	k
RAM8	8	3
RAM64	64	6
RAM512	512	9
RAM4K	4096	12
RAM16K	16384	14

Why these particular RAM chips?

Because that's what we need for building the Hack computer.

# Chapter 3: Memory

## Abstraction

- Representing time
- Clock
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## **Implementation**









• Project 3: Guidelines

# Project 3

## Given:

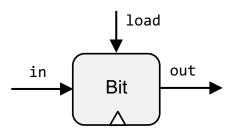
- All the chips built in projects 1 and 2
- Data Flip-Flop (built-in DFF gate)

## **Build:**

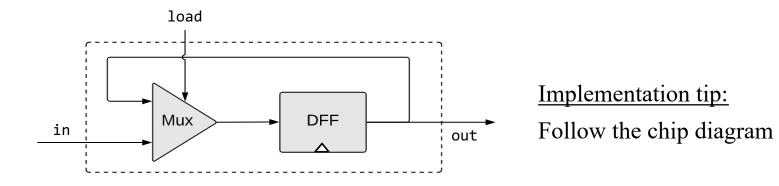


- Register
- PC
- RAM8
- RAM64
- RAM512
- RAM4K
- RAM16K

# 1-bit Register



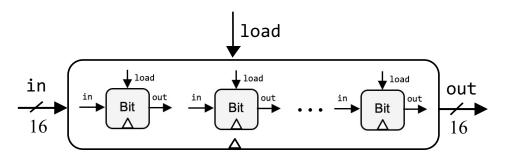
#### Bit.hdl



# 16-bit Register

# in Register 16

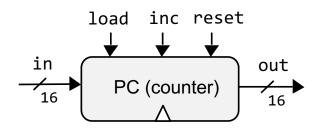
#### Register.hdl



Partial diagram, showing some of the chip-parts, without connections Implementation tip:

Follow the chip diagram

# 16-bit Counter



```
/**
  A 16-bit counter with control bits.
         reset(t-1) out(t) = 0
                                           // resetting
  else if load(t-1) out(t) = in(t-1)
                                           // setting
  else if inc(t-1) out(t) = out(t-1) + 1 // incrementing
                     out(t) = out(t-1)
  else
                                           // maintaining
*/
CHIP PC {
   IN in[16], load, inc, reset;
   OUT out[16];
   PARTS:
   // Put your code here:
```

Implementation tip: Can be built from a Register, an Incrementer, and Mux's

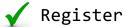
# Project 3

## Given

- All the chips built in projects 1 and 2
- Data Flip-Flop (built-in DFF gate)

## Build the following chips





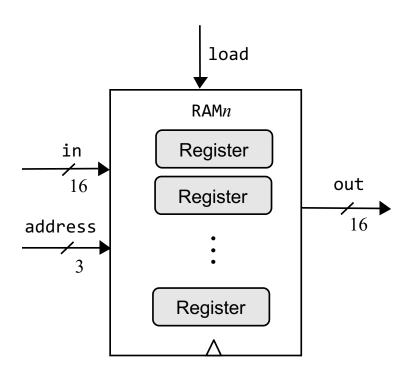




RAM8

- RAM64
- RAM512
- RAM4K
- RAM16K

# 8-Register RAM: Abstraction

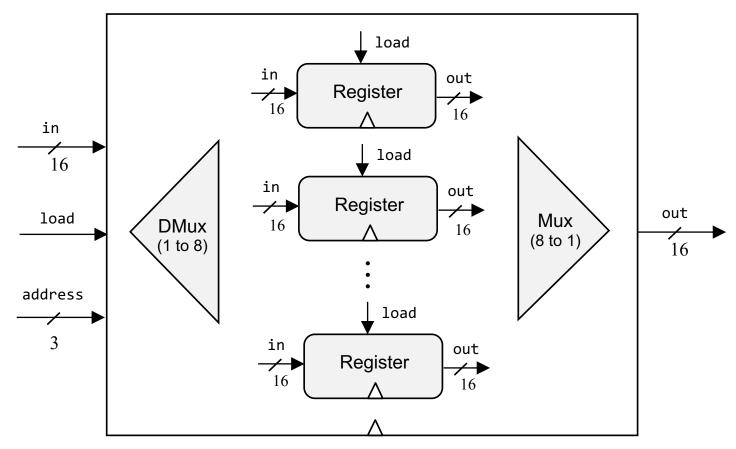


#### RAM8.hdl

```
Let M stand for the state of the register
selected by address.
if load(t - 1) then {M = in(t), out(t) = M}
else out(t) = M

*/
CHIP RAM8 {
    IN in[16], load, address[3];
    OUT out[16];
    PARTS:
    // Put your code here:
}
```

# 8-Register RAM: Implementation



Partial diagram, showing some of the chip-parts, without connections

## <u>Implementation tip:</u>

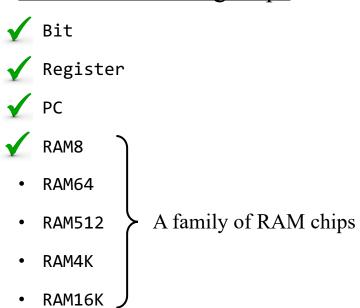
Follow the chip diagram

# Project 3

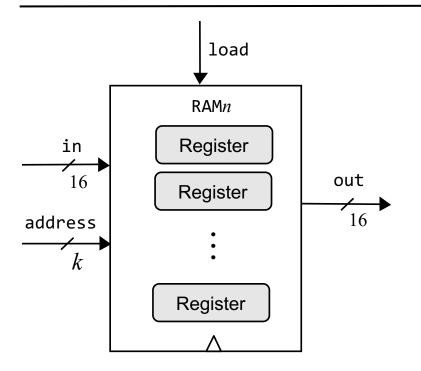
## Given

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- Data Flip-Flop (built-in DFF gate)

## Build the following chips

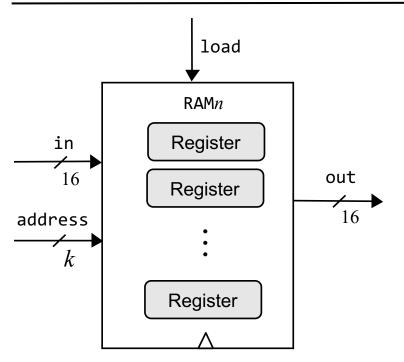


# *n*-Register RAM



#### $RAM_n.hdl$

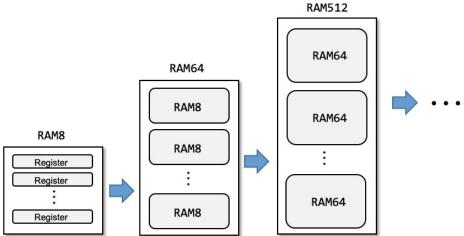
# *n*-Register RAM



chip name	n	k
RAM8	8	3
RAM64	64	6
RAM512	512	9
RAM4K	4096	12
RAM16K	16384	14

## <u>Implementation tips</u>

- Think about the RAM's address input as consisting of two fields:
  - One field selects a RAM-part;
  - The other field selects a register within that RAM-part
- Use logic gates to effect this addressing scheme.



# Chapter 3: Memory

## Abstraction

- Representing time
- Clock
- Registers
- RAM
- Counters

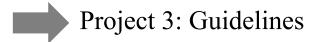
## **Implementation**











# Project 3



Home Prerequisites Syllabus

#### Course

Book Software

Terms

Papers

Talks

Cool Stuff

About Team

Q&A

## **Project 3: Sequential Chips**

#### Background

The computer's main memory, also called  $Random\ Access\ Memory$ , or RAM, is an addressable sequence of n-bit registers, each designed to hold an n-bit value. In this project you will gradually build a RAM unit. This involves two main issues: (i) how to use gate logic to store bits persistently, over time, and (ii) how to use gate logic to locate ("address") the memory register on which we wish to operate.

#### Objective

Build all the chips described in Chapter 3 (see list below), leading up to a *Random Access Memory* (RAM) unit. The only building blocks that you can use are primitive DFF gates, chips that you will build on top of them, and chips described in previous chapters.

#### Chips

Chip (HDL)	Description	Test script	Compare file
DFF	Data Flip-Flop (primitive)		
Bit	1-bit register	Bit.tst	Bit.cmp
Register	16-bit register	Register.tst	Register.cmp
RAM8	16-bit / 8-register memory	RAM8.tst	RAM8.cmp
RAM64	16-bit / 64-register memory	RAM64.tst	RAM64.cmp
RAM512	16-bit / 512-register memory	RAM512.tst	RAM512.cmp
RAM4K	16-bit / 4096-register memory	RAM4K.tst	RAM4K.cmp
RAM16K	16-bit / 16384-register memory	RAM16K.tst	RAM16K.cmp
PC	16-bit program counter	PC.tst	PC.cmp

All the necessary project 3 files are available in: nand2tetris / projects / 03

# Resources

Project 3 folder (.hdl, .tst, .cmp files): nand2tetris/projects/03

#### <u>Tools</u>

- Text editor (for completing the given .hdl stub-files)
- Hardware simulator: nand2tetris/tools

### <u>Guides</u>

- Hardware Simulator Tutorial
- HDL Guide
- Hack Chip Set API

# Best practice advice

- Implement the chips in the order in which they appear in the project guidelines
- If you don't implement some chips, you can still use their built-in implementations
- No need for "helper chips": Implement / use only the chips we specified
- In each chip definition, strive to use as few chip-parts as possible
- You will have to use chips implemented in previous projects;

  For efficiency and consistency's sake, use their built-in versions, rather than your own HDL implementations.

For technical reasons, the chips of project 3 are organized in two sub-folders named projects/03/a and projects/03/b

When writing and simulating the .hdl files, leave this folder structure as is.

That's It!

Go Do Project 3!

# Chapter 3: Memory

## **Abstraction**

• Representing time



Clock

- Registers
- RAM
- Counters

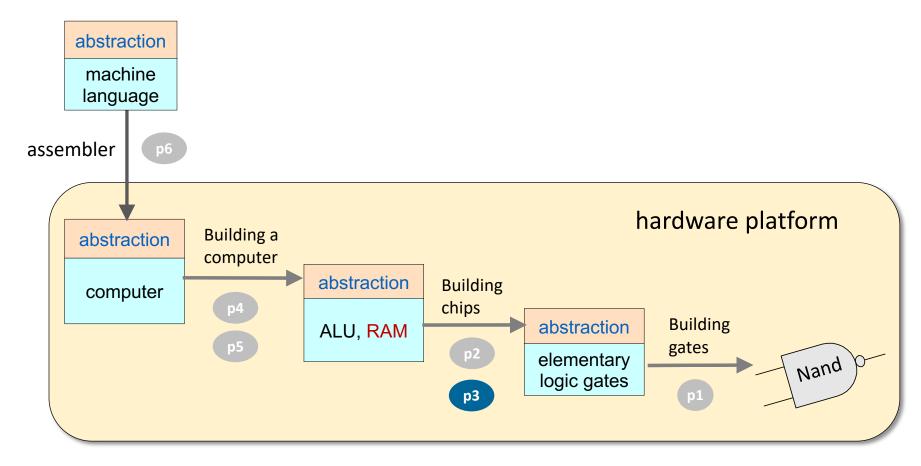
# **Implementation**

- Data Flip Flop
- Registers



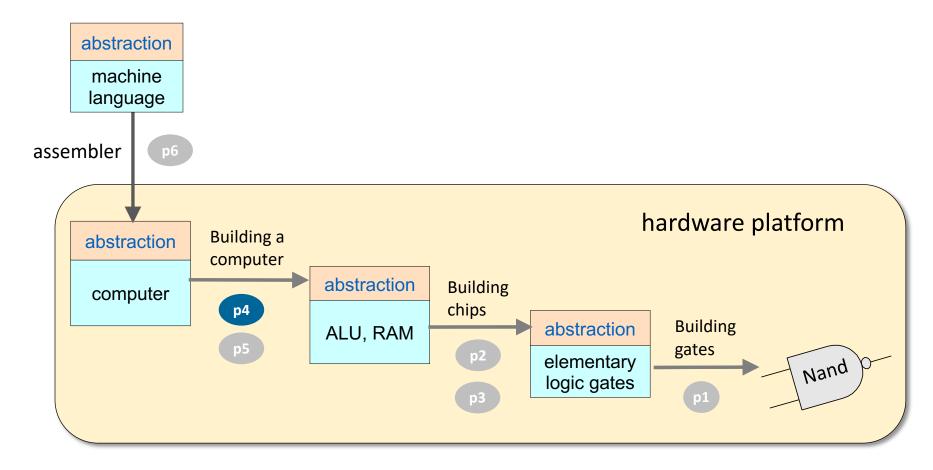
- Project 3: Chips
- Project 3: Guidelines

# What's next?



This lecture / chapter / project:
Build the computer's RAM

## What's next?



# Next lecture / chapter / project:

- Get acquainted with the computer architecture
- Write machine language programs