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01/04/23 ML LAB II MANUAL WORK

(1) ENTROPY:

* We calculate Entropy of entire dataset:

(1) $S = [10+, 10-]$

$\therefore$ Entropy$(S) = -\frac{10}{14}\log_2\frac{10}{14} = \frac{10}{14}\log_2\frac{10}{14}$

$= 0.693$

Considering features - Gender, Car Type and Shirt Size:

(2) Gender:

$S_{Gender='M'} \leftarrow [4+, 6-] \Rightarrow$ Entropy $= -\frac{4}{10}\log_2\frac{4}{10} - \frac{6}{10}\log_2\frac{6}{10}$

$= 0.97$

$S_{Gender='F'} \leftarrow [6+, 4-] \Rightarrow$ Entropy $= -\frac{6}{10}\log_2\frac{6}{10} - \frac{4}{10}\log_2\frac{4}{10}$

$= 0.97$

$\Rightarrow$ Gain$(S, Gender)$ = Entropy$(S) - \sum_{v \in (Male, Female)} \frac{|S_v|}{|S|}$ Entropy(S_v)

$= 0.693 - \frac{10}{14}(0.97) - \frac{10}{14}(0.97)$

$= -0.693$

Similarly:

(3) Car Type:

$S_{Family} \leftarrow [3+, 1-] \Rightarrow$ Entropy $= 0.811$

$S_{Sports} \leftarrow [0+, 8-] \Rightarrow$ Entropy $= 0$

$S_{Luxury} \leftarrow [7+, 1-] \Rightarrow$ Entropy $= 0.543$

$\Rightarrow$ Gain$(S, Car\ Type)$ = Entropy$(S) - \sum_{v \in (Sports, Family, Luxury)} \frac{|S_v|}{|S|}$ Entropy(S_v)

$= 0.693 - \frac{4}{14}(0.811) - 0 - \frac{8}{14}(0.543) = 0.151$

Similarly,

④ Shirt size:

$S_{small} \leftarrow [2+, 3-] \Rightarrow Entropy = -\frac{2}{5}\log_2\left(\frac{2}{5}\right) - \frac{3}{5}\log_2\frac{3}{5}$

$= 0.971$

$S_{medium} \leftarrow [4+, 3-] \Rightarrow Entropy = 0.985$

$S_{Large} \leftarrow [1+, 2-] \Rightarrow Entropy = 0.918$

$S_{Extralarge} \leftarrow [2+, 2-] \Rightarrow Entropy = 1$

$\Rightarrow Gain(S, Shirt\ size) = 0.693 - \frac{5}{14}(0.971) - \frac{7}{14}(0.985)$

$- \frac{3}{14}(0.918) - \frac{4}{14}(1) = -0.629$

From ② ③ and ④

Gain (S, Gender) $= -0.693$

Gain (S, Car Type) $= 0.151$

Gain (S, Shirt size) $= -0.629$

Hence Car Type is root node (Max value).

⑪ GINI:

* We calculate GINI of entire dataset:

① $G = [10+; 10-]$

$\Rightarrow GINI(S) = 1 - \left[\left(\frac{10}{20}\right)^2 + \left(\frac{10}{20}\right)^2\right]$

$= 1 - \frac{1}{2} = \frac{1}{2}$

② GINI index for Gender:

$$\text{Gini (Gender = 0)} = 1 - \left[\left(\frac{4}{10}\right)^2 + \left(\frac{6}{10}\right)^2\right]$$

$$= 0.48$$

$$\text{Gini (Gender = 1)} = 1 - \left[\left(\frac{5}{10}\right)^2 + \left(\frac{4}{10}\right)^2\right]$$

$$= 0.48$$

$$\text{Weighted average} = 0.48\left(\frac{10}{20}\right) + 0.48\left(\frac{10}{20}\right)$$

$$= 0.48$$

③ GINI Index Car Type:

$$\text{Gini (Car Type 0)} = 1 - \left[\left(\frac{1}{4}\right)^2 + \left(\frac{3}{4}\right)^2\right]$$

$$= 0.375$$

$$\text{Gini (Car Type 1)} = 1 - \left[\left(\frac{1}{8}\right)^2 + \left(\frac{7}{8}\right)^2\right]$$

$$= 0.21875$$

$$\text{Gini (Car Type 2)} = 1 - \left(\left(\frac{8}{8}\right)^2\right)$$

$$= 0$$

$$\text{Weighted} = 0.375\left(\frac{4}{20}\right) + 0.21875\left(\frac{8}{20}\right) + 0$$

$$= 0.1625$$

④ GINI Index Shirt size:

$$\text{For shirt size 0} : = \left(1 - \left(\frac{2}{4}\right)^2 + \left(\frac{2}{4}\right)^2\right)$$

$$= 0.5$$

GINI (Shirt size 1):

$$= 1 - \left[\left(\frac{2}{4}\right)^2 + \left(\frac{2}{4}\right)^2 \right]$$

$$= 0.5$$

GINI (Shirt size = 2):

$$= 1 - \left[\left(\frac{3}{4}\right)^2 + \left(\frac{1}{4}\right)^2 \right]$$

$$= 0.489$$

GINI (Shirt size = 3)

$$= 1 - \left[\left(\frac{3}{5}\right)^2 + \left(\frac{2}{5}\right)^2 \right]$$

$$= 0.48$$

Weighted $= 0.5\left(\frac{4}{20}\right) + 0.5\left(\frac{1}{20}\right)$

$+ 0.489\left(\frac{7}{20}\right) + 0.49\left(\frac{5}{20}\right)$

$= 0.4913$

From (2), (3), (4):

GINI: 0.48, 0.1625, 0.4913

Least = 0.1625 = Car Type.

Hence root node.