



Joint Programme Examinations 2019/20

BBC4102 Introduction to Electronic Systems

Paper A

Time allowed 2 hours

Questions 1~ 6 are for All Students. Questions 7~ 8 are for only Classes 1~16. Questions 9~10 are for only Classes 17~22.

Complete the information below about yourself very carefully.

QM student number

**BUPT student number** 

Class number

•					
	261				

NOT allowed: electronic dictionaries.

### INSTRUCTIONS

- You must not take answer books, used or unused, from the examination room.
- 2. Write only in black or blue pen and in English.
- Do all rough work in the answer book do not tear out any pages.
- 4. If you use Supplementary Answer Books, tie them to the end of this book.
- 5. Write clearly and legibly.
- Read the instructions on the inside cover.

# **Examiners**

Hongxiang Wang, Minglun Zhang, Dong Liang, Yong Zuo, Jinnan Zhang, Hongtao Zhang, Daquan

Copyright © Beijing University of Posts and Telecommunications & © Queen Mary, University of London 2012

# BBC4102 2019/2020

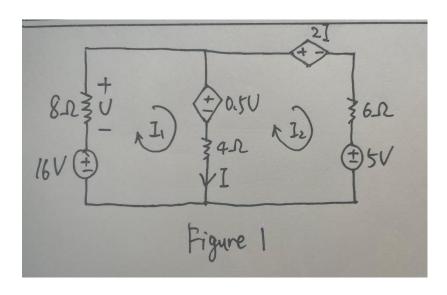
# Introduction to Electronic Systems Paper A

Solutions & Analysis

By Puyuan Zheng, BUPTIS.

(写在前面的话:解答题给分点均根据解析者本人对题目的理解认为的采分点。与实际若有不同,请以实际判分为准,本解析写出的采分点仅供参考。本解析若有问题错误,欢迎批评指正。)

Question 1 (12 Marks): Use the mesh-current method to find the power dissipated by the  $\,4\Omega\,$  resistor shown in the circuit in Figure 1.



### 【考点 Point】

网孔电流法 Mesh-current method

电阻功率计算 Find the power of a resistor

Answer: 25W.

#### 【解析 Analysis】

先用网孔电流法解出通过 4 欧姆电阻的电流 I,然后根据电阻功率的公式计算即可。

# Solution:

By mesh-current method, we have the equations

$$\begin{cases} 16 + U - 0.5U - 4I = 0 \\ 4I + 0.5U - 2I - 6I_2 - 5 = 0 \end{cases}$$

Since  $I=I_1-I_2$  and  $U=-8I_1$  ,we have

$$\begin{cases} 16 - 4I_1 - 4(I_1 - I_2) = 0 \\ 2(I_1 - I_2) - 4I_1 - 6I_2 - 5 = 0 \end{cases}$$

That is,

$$\begin{cases} 16 - 8I_1 + 4I_2 = 0 \\ -2I_1 - 8I_2 - 5 = 0 \end{cases}$$

By solving the equations, we have

$$\begin{cases} I_1 = \frac{3}{2}A \\ I_2 = -1A \end{cases}$$

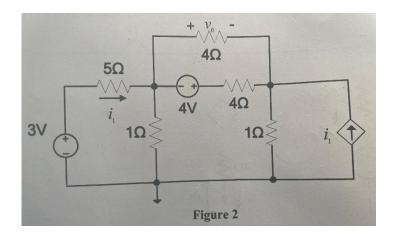
Then 
$$I = I_1 - I_2 = \frac{5}{2}A$$

The power dissipated by the  $4\Omega$  resistor is:

$$P = I^2 \cdot 4\Omega = \left(\frac{5}{2}A\right)^2 \cdot 4\Omega = 25W$$

Finish.

Question 2 (12 Marks): Use the node-voltage method to find the value of  $v_0$  in Figure 2.



# 【考点 Point】

### 节点电流法 Node-voltage method

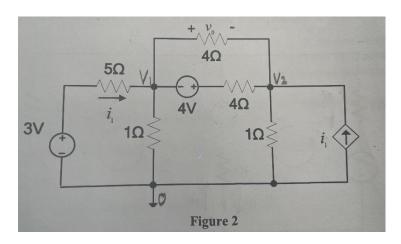
Answer: -1V.

# 【解析 Analysis】

直接节点电压法求解就可以了, 注意参考点的选择。

# Solution:

We set the reference point and the node point as the picture below.



By node-voltage method, we have the equations

$$\begin{cases} -i_1 + \frac{v_1}{1} + \frac{v_0}{4} + \frac{v_1 + 4 - v_2}{4} = 0\\ -i_1 + \frac{v_2}{1} + \frac{-v_0}{4} + \frac{v_2 - v_1 - 4}{4} = 0 \end{cases}$$

Since 
$$i_1=\frac{3-v_1}{5}$$
 and  $v_0=v_1-v_2$  ,we have 
$$\begin{cases} \frac{v_1-3}{5}+\frac{v_1}{1}+\frac{v_1-v_2}{4}+\frac{v_1+4-v_2}{4}=0\\ \frac{v_1-3}{5}+\frac{v_2}{1}+\frac{v_2-v_1}{4}+\frac{v_2-v_1-4}{4}=0 \end{cases}$$

That is,

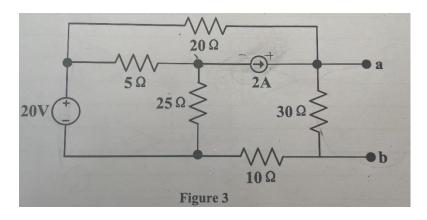
$$\begin{cases} \frac{17}{10}v_1 - \frac{1}{2}v_2 + \frac{2}{5} = 0\\ -\frac{3}{10}v_1 + \frac{3}{2}v_2 - \frac{8}{5} = 0 \end{cases}$$

By solving the equations, we have

$$\begin{cases} v_1 = \frac{1}{12}V \\ v_2 = \frac{13}{12}V \end{cases}$$

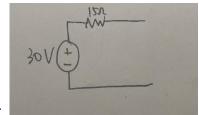
Then  $v_0 = v_1 - v_2 = -1V$  Finish.

Question 3 (13 Marks): Find the Thevenin equivalent circuit with respect to the terminals a and b in the circuit shown in Figure 3.



# 【考点 Point】

求解戴维南等效电路 Find the Thevenin Equivalent circuit



Answer:

### 【解析 Analysis】

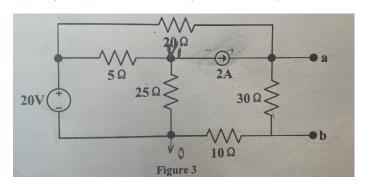
本题为求解戴维南等效电路,要解的是两个量,戴维南电压和戴维南电阻 $R_{Th}$ 。 戴维南电压即开路电压,直接用平常解电压的方法求解即可。(节点/网孔) 对于戴维南电阻,本题无受控源只有独立源,可以使用开路电压短路电流的方法, 也可以使用除源法(电压表短路,电流表断路)。

#### Solution:

# Part 1: 求解戴维南电压 $V_{Th}$

#### Method 1: 节点电压法

We set the reference point and the node point as the picture below.



By node-voltage method, we have the equations

$$\begin{cases} \frac{v_1}{25} + \frac{v_1 - 20}{5} + 2 = 0\\ \frac{v_a - v_b}{30} - 2 + \frac{v_a - 20}{20} = 0\\ \frac{v_b}{10} + \frac{v_b - v_a}{30} = 0 \end{cases}$$

That is,

$$\begin{cases} \frac{6}{25}v_1 - 2 = 0\\ \frac{1}{12}v_a - \frac{1}{30}v_b - 3 = 0\\ -\frac{1}{30}v_a + \frac{2}{15}v_b = 0 \end{cases}$$

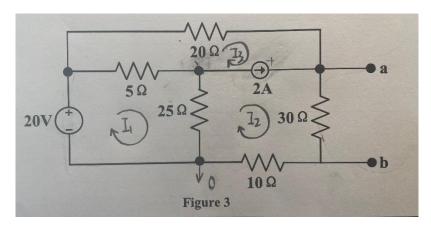
By solving the equations, we have

$$\begin{cases} v_1 = \frac{25}{3}V \\ v_a = 40V \\ v_b = 10V \end{cases}$$

Then 
$$v_{TH} = v_a - v_b = 40V - 10V = 30V$$

### Method 2: 网孔电流法

We set the meshes as the picture below.



By mesh-current method, we have the equations

$$\begin{cases}
20 - 5(I_1 - I_3) - 25(I_1 - I_2) = 0 \\
-25(I_2 - I_1) - 5(I_3 - I_1) - 20I_3 - 30I_2 - 10I_2 = 0
\end{cases}$$

Since  $2A=I_2-I_3$  ,that is  $I_3=(I_2-2)A$  ,we have

$$\begin{cases} 20 - 5(I_1 - I_2 + 2) - 25(I_1 - I_2) = 0 \\ -25(I_2 - I_1) - 5(I_2 - 2 - I_1) - 20(I_2 - 2) - 30I_2 - 10I_2 = 0 \end{cases}$$

That is,

$$\begin{cases}
-30I_1 + 30I_2 + 10 = 0 \\
30I_1 - 90I_2 + 50 = 0
\end{cases}$$

By solving the equations, we have

$$\begin{cases} I_1 = \frac{4}{3}A \\ I_2 = 1A \end{cases}$$

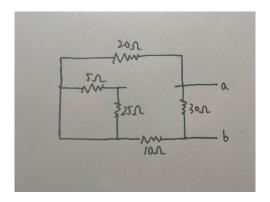
Then 
$$V_{TH} = I_2 \cdot 30\Omega = 1A \cdot 30\Omega = 30V$$

Next, we find the Thevenin equivalent resistor.

# Part 2: 求解戴维南电阻 $R_{Th}$

### Method 1: 除源法

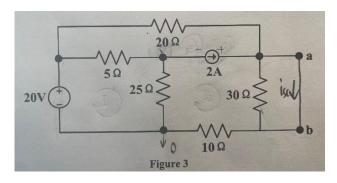
By the method of deactivating sources, we have the circuit:



Then 
$$R_{Th} = (20 + 10)||30 = 15\Omega$$

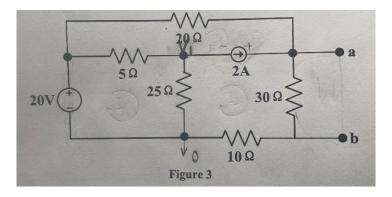
# Method 2: 短路电流法

By the method of short-circuit current, we have the circuit:



(这里只给了节点电压法, 网孔电流就不再赘述了~)

By node-voltage method, we set the reference point and the node point as the picture below:



We have the equations:

$$\begin{cases} \frac{v_1}{25} + \frac{v_1 - 20}{5} + 2 = 0\\ -2 + \frac{v_a - 20}{20} + i_{sc} = 0\\ \frac{v_b}{10} - i_{sc} = 0 \end{cases}$$

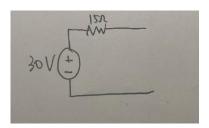
That is,

$$\begin{cases} \frac{6}{25}v_1 - 2 = 0\\ \frac{1}{20}v_a + i_{sc} - 3 = 0\\ \frac{1}{10}v_b - i_{sc} = 0 \end{cases}$$

Since  $v_b=v_a$  By solving the equations, we have

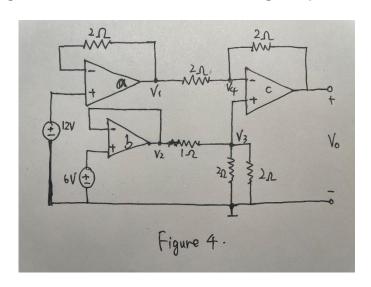
$$\begin{cases} v_1 = \frac{25}{3}V \\ v_a = 20V \\ i_{sc} = 2A \end{cases}$$

Then 
$$R_{TH} = \frac{V_{th}}{Isc} = \frac{30V}{2A} = 15\Omega$$



Finally, we find the Thevenin equivalent circuit.

Question 4 (12 Marks): The operational amplifiers in the circuit shown in Figure 4 are ideal. Find the voltage  $V_0$ .



# 【考点 Point】

# 运算放大器 Op amp

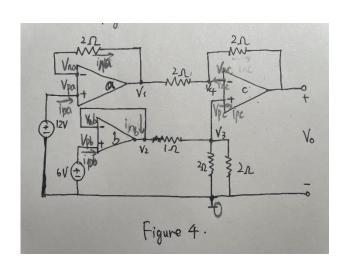
Answer: -6V.

# 【解析 Analysis】

本题考察运算放大器。核心在于"虚短路,虚开路。"

别看是级联, 电路很复杂, 其实处处藏关系。靠上述六个字就能够化简绝大多数的部分。不要恐惧哦~

# Solution:



$$v_{pa} = v_{na} = 12V$$
,  $v_{pb} = v_{nb} = 6V$ ,  $v_{pc} = v_{nc}$   $i_{na} = i_{na} = i_{nb} = i_{nb} = i_{nc} = i_{nc} = 0$ 

(记住! 碰到运算放大器看着电路就不想做的, 别怕, 先把上面所有的虚短路虚

### 开路写上,有分的!!!!)

Also, 
$$v_1 = v_{na} = 12V$$
,  $v_2 = v_{nb} = 6V$ ,  $v_3 = v_4$ 

下面用节点电压法解需要的电压 $V_0$ .

By node-voltage method, we have the equations

$$\begin{cases} \frac{v_3 - v_2}{1} + \frac{v_3}{2} + \frac{v_3}{2} = 0\\ \frac{v_4 - v_0}{2} + \frac{v_4 - v_1}{2} = 0 \end{cases}$$

That is,

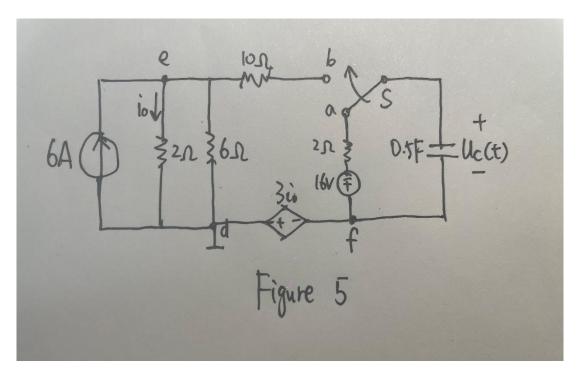
$$\begin{cases} 2v_3 - v_2 = 0 \\ v_4 - \frac{1}{2}v_0 - \frac{1}{2}v_1 = 0 \end{cases} \longrightarrow \begin{cases} 2v_3 - 6 = 0 \\ v_3 - \frac{1}{2}v_0 - 6 = 0 \end{cases}$$

By solving the equations, we have

$$\begin{cases} v_3 = 3V \\ v_0 = -6V \end{cases}$$

Finish.

Question 5 (12 Marks): The switch in the circuit in Figure 5 has been in position a for a long time. At t=0 the seitch is moved to position b. Find  $u_c(t)$  for  $t \ge 0$ .



# 【考点 Point】

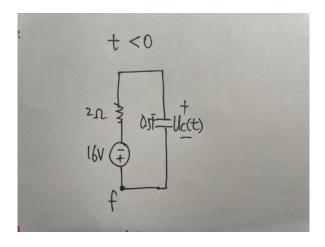
自然响应 Natural Responses in an RC circuit.

Answer: 
$$u_c(t)=-16e^{-rac{8}{55}t}(t\geq 0)$$
 .

# 【解析 Analysis】

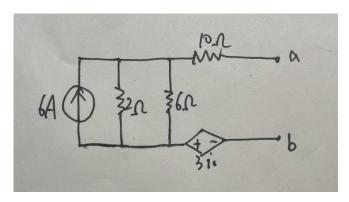
本题考察电容自然响应的电路分析。分别对t < 0和 $t \ge 0$ 的电路进行求解,还是老三步:初态、时间常数以及写表达式。初态可以直接根据 t < 0 的电路写出,时间常数是求解戴维南电阻+电容,表达式就是带个自然常数。在这个思路下,可以求得我们需要的电容的电压随时间变化的函数。

# Solution:



$$u_c(0) = -16V$$

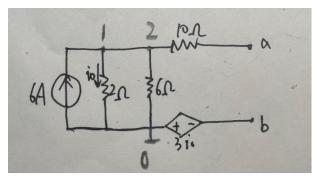
Then we find the Thevenin equivalent circuit at t>0.



Part 1: 求解戴维南电压 $V_{Th}$ 

# 这里只提供节点电压法,网孔电流不赘述了~

We set the reference point and the node point as the picture below.



By node-voltage method, we have the equations  $i_0 + \frac{i_0}{3} - 6 = 0$ 

By solving the equations, we have

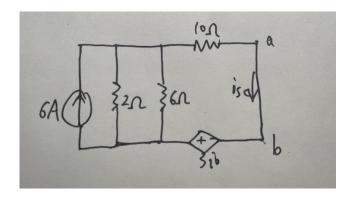
$$i_0 = \frac{9}{2}A$$

Then 
$$v_{TH} = v_a - v_b = 2i_0 - (-3i_0) = 5i_0 = 22.5V$$

Part 2: 求解戴维南电阻 $R_{Th}$ 

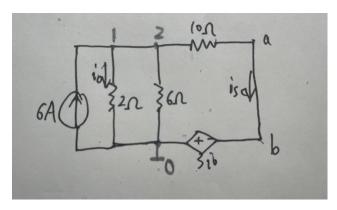
使用短路电流法求解。

By the method of short-circuit current, we have the circuit:



(这里只给了节点电压法, 网孔电流就不再赘述了~)

By node-voltage method, we set the reference point and the node point as the picture below:



We have the equations:

$$\begin{cases} i_0 + \frac{i_0}{3} - 6 + i_{sc} = 0 \\ i_{sc} = \frac{v_2 - v_a}{10} \end{cases}$$

Since 
$$v_b=v_a=-3i_0$$
 ,  $v_1=v_2=2i_0$ 

By solving the equations, we have

$$\begin{cases} i_0 + \frac{i_0}{3} - 6 + i_{sc} = 0 \\ i_{sc} = \frac{1}{2} i_0 \end{cases}$$

That is:

$$\begin{cases} \frac{11}{6}i_0 - 6 = 0\\ i_{sc} = \frac{1}{2}i_0 \end{cases}$$

By solving the equations, we have:

$$\begin{cases} i_0 = \frac{36}{11}A\\ i_{sc} = \frac{18}{11}A \end{cases}$$

Then 
$$R_{TH} = \frac{V_{th}}{Isc} = \frac{22.5V}{\frac{18}{11}A} = 13.75\Omega$$

Then, the time constant of the capacitance is:

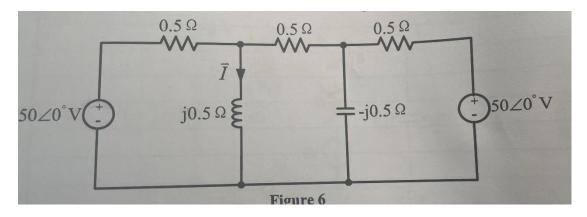
$$\tau = R_{TH}C = 6.875s$$

Then, the expression of  $u_c(t)$  is:

$$u_c(t) = -16e^{-\frac{8}{55}t}(t \ge 0)$$

Finish.

Question 6 (13 Marks): Use node voltage method to find the current I in the circuit in Figure 6.



### 【考点 Point】

### 正弦稳态分析 The analysis of steady sinusoidal circuit

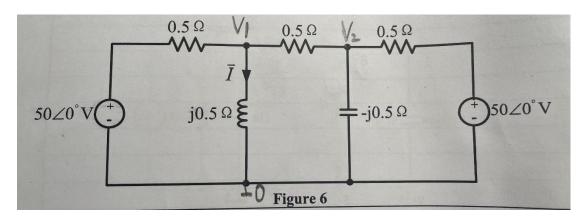
Answer: 
$$(25 - 75j)A$$
 /  $25\sqrt{10} \angle - 71.57^{\circ}A$  /  $25\sqrt{10}\cos(\omega t - 71.57^{\circ})(A)$ .

# 【解析 Analysis】

正弦稳态电路分析。和正常电路没啥区别,就多个复数计算。然后按题目要求节点电压法解就 ok 了。

### Solution:

We set the reference point and the node point as the picture below.



By node-voltage method, we have the equations

$$\begin{cases} \frac{v_1 - 50 \angle 0^{\circ}}{0.5} + \frac{v_1}{j0.5} + \frac{v_1 - v_2}{0.5} = 0\\ \frac{v_2 - 50 \angle 0^{\circ}}{0.5} + \frac{v_2}{-j0.5} + \frac{v_2 - v_1}{0.5} = 0 \end{cases}$$

That is,

$$\begin{cases} (4-2j)v_1-2v_2-100\angle 0^\circ=0\\ -2v_1+(4+2j)v_2-100\angle 0^\circ=0 \end{cases}$$
 
$$(4-2j)v_1-2v_2=-2v_1+(4+2j)v_2$$
 
$$(6-2j)v_1=(6+2j)v_2$$
 Then, 
$$v_2=\frac{6-2j}{6+2j}v_1=\left(\frac{4}{5}-\frac{3}{5}j\right)v_1$$

By solving the equations, we have

$$\left(\frac{12}{5} - \frac{4}{5}j\right)v_1 = 100$$

$$v_1 = \left(\frac{75}{2} + \frac{25}{2}j\right)V$$
Then  $I = \frac{v_1}{j0.5} = (25 - 75j)A$ 

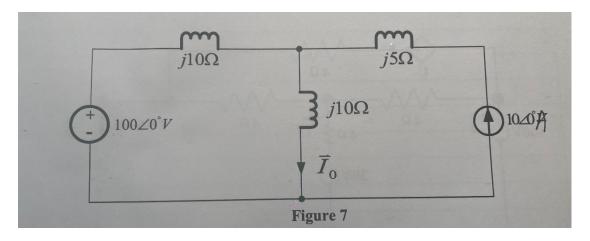
$$= 25\sqrt{10}\angle - 71.57^\circ A$$

$$= 25\sqrt{10}\cos\left(\omega t - 71.57^\circ\right)(A)$$

Finish.

Question 7 (13 Marks)——For Classes 1-16 Only:

Determine the current  $I_0$  in Figure 7 with superposition method.



# 【考点 Point】

# 叠加法 Superposition Method

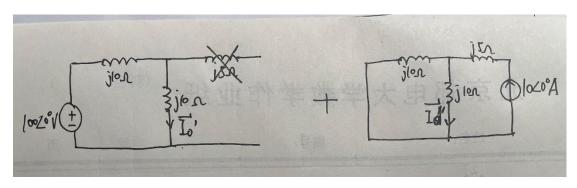
Answer:  $5 - 5jA / 5\sqrt{2} \angle - 45^{\circ}A / 5\sqrt{2}cos(\omega t - 45^{\circ})(A)$ .

### 【解析 Analysis】

叠加法来个简单复习:每次拆掉一个独立源(电压表短路、电流表断路)。 然后分别对每个电路的 $I_0$ 进行求解,再把所有的分 $I_0$ 加起来,得到答案。

# Solution:

By superposition method, since there are two independent sources, so we have two circuits to find the  $I_{\mathbf{0}}.$ 



$$I_0' = \frac{100 \angle 0^{\circ}}{j20} A = j - 5A$$
$$2I_0'' - 10 \angle 0^{\circ} = 0$$
$$I_0'' = 5 \angle 0^{\circ} A$$

Then,

$$I_0 = I'_0 + I''_0 = 5 - 5jA$$

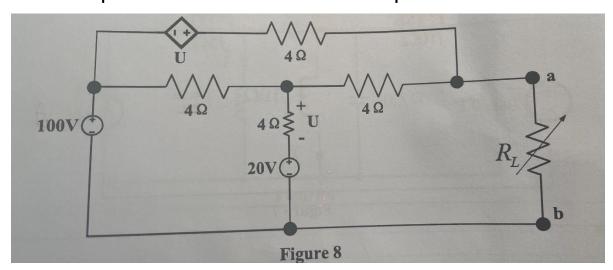
$$I_0 = 5\sqrt{2}\angle - 45^{\circ}A$$

$$I_0 = 5\sqrt{2}cos(\omega t - 45^{\circ})(A)$$

Finish.

Question 8 (13 Marks)——For Classes 1-16 Only:

In the circuit in Figure 8, what resistor  $R_L$  will absorb the maximum power? And what is the maximum power?



【考点 Point】

最大功率传输 Maximum Power transformation

戴维南等效电路求解 Find the Thevenin Equivalent Circuit

Answer:  $3\Omega$ , 1200W.

#### 【解析 Analysis】

电路达到最大功率是当外阻等于内阻的时候。我们需要先求出戴维南等效电路, 之后当 RL=戴维南电阻可以得到功率最大值(理论解释部分请看教材或各任课教 师 ppt)。在本道题的戴维南电路求解,仍然给出节点/网孔双解法(求解戴维南电压),因本题存在受控源,不能使用除源法,且因为独立源存在,我们只能用开路电压短路电流的方法来求解戴维南电阻。

### 所以说白,解对戴维南等效电路,是解对本题的关键!

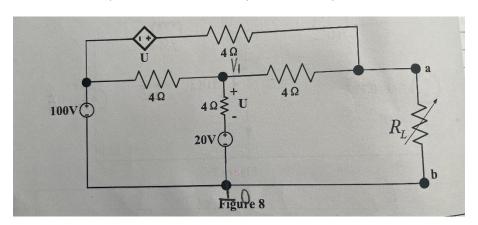
### Solution:

First, we find the Thevenin Equivalent circuit.

# Part 1: 求解戴维南电压 $V_{Th}$

### Method 1: 节点电压法

We set the reference point and the node point as the picture below.



By node-voltage method, we have the equations

$$\begin{cases} \frac{v_1 - 20}{4} + \frac{v_1 - 100}{4} + \frac{v_1 - v_a}{4} = 0\\ \frac{v_a - v_1}{4} + \frac{v_a - 100 - U}{4} = 0 \end{cases}$$

Since  $U = (v_1 - 20)V$ , we have

$$\begin{cases} \frac{v_1 - 20}{4} + \frac{v_1 - 100}{4} + \frac{v_1 - v_a}{4} = 0\\ \frac{v_a - v_1}{4} + \frac{v_a - 100 - (v_1 - 20)}{4} = 0 \end{cases}$$

That is,

$$\begin{cases} 3v_1 - 120 - v_a = 0 \\ 2v_a - 2v_1 - 80 = 0 \end{cases}$$

By solving the equations, we have

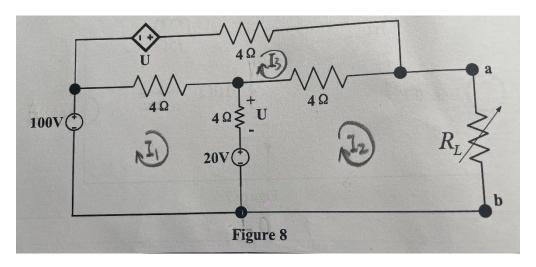
$$\begin{cases} v_1 = 80V \\ v_a = 120V \end{cases}$$

Since  $v_b=0V$ , then

$$v_{TH} = v_a - v_b = 120V - 0V = 120V$$

### Method 2: 网孔电流法

We set the meshes as the picture below.



By mesh-current method, we have the equations

$$\begin{cases} 100 - 4(I_1 - I_3) - U - 20 = 0\\ 20 + U - 4(I_2 - I_3) - v_{ab} = 0\\ U - 4I_3 - 4(I_3 - I_2) - 4(I_3 - I_1) = 0 \end{cases}$$

Since  $U=4(I_1-I_2)V$  , we have

$$\begin{cases} 100 - 4(I_1 - I_3) - 4(I_1 - I_2) - 20 = 0\\ 20 + 4(I_1 - I_2) - 4(I_2 - I_3) - v_{ab} = 0\\ 4(I_1 - I_2) - 4I_3 - 4(I_3 - I_2) - 4(I_3 - I_1) = 0 \end{cases}$$

That is,

$$\begin{cases} -8I_1 + 4I_2 + 4I_3 + 80 = 0 \\ 4I_1 - 8I_2 + 4I_3 + 20 - v_{ab} = 0 \\ 8I_1 - 12I_3 = 0 \end{cases}$$

Then,  $I_1 = 1.5I_3$ .

Since the voltage at the terminal a and b is open-circuit, then  $\,I_2=0\,$  Then,

$$\begin{cases} -8I_3 + 80 = 0 \\ 10I_3 + 20 - v_{ab} = 0 \end{cases}$$

By solving the equations, we have

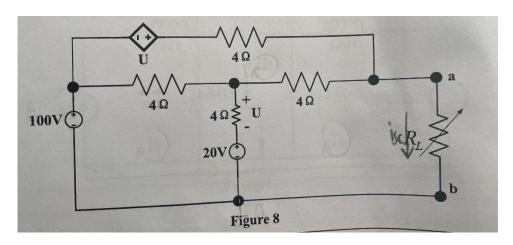
$$\begin{cases} I_1 = 15A \\ I_2 = 0A \\ I_3 = 10A \\ v_{ab} = 120V \end{cases}$$

Next, we find the Thevenin equivalent resistor.

# Part 2: 求解戴维南电阻 $R_{Th}$

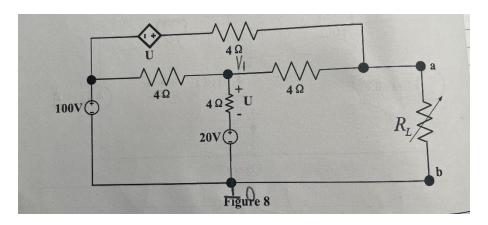
使用短路电流法求解。

By the method of short-circuit current, we have the circuit:



(这里只给了节点电压法, 网孔电流就不再赘述了~)

By node-voltage method, we set the reference point and the node point as the picture below:



And we have the equations:

$$\begin{cases} \frac{v_1 - 20}{4} + \frac{v_1 - 100}{4} + \frac{v_1 - v_a}{4} = 0\\ \frac{v_a - v_1}{4} + \frac{v_a - 100 - U}{4} + i_{sc} = 0 \end{cases}$$

Since  $U=(v_1-20)V$ , we have

$$\begin{cases} \frac{v_1 - 20}{4} + \frac{v_1 - 100}{4} + \frac{v_1 - v_a}{4} = 0\\ \frac{v_a - v_1}{4} + \frac{v_a - 100 - (v_1 - 20)}{4} + i_{sc} = 0 \end{cases}$$

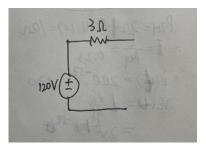
That is,

$$\begin{cases} 3v_1 - 120 - v_a = 0 \\ 2v_a - 2v_1 - 80 + 4i_{sc} = 0 \end{cases}$$

Since  $\,v_b=v_a=0\,$  By solving the equations, we have

$$\begin{cases} v_1 = 40V \\ i_{sc} = 40A \end{cases}$$

Then 
$$R_{TH} = \frac{V_{th}}{I_{SC}} = \frac{120V}{40A} = 3\Omega$$



We find the Thevenin equivalent circuit.

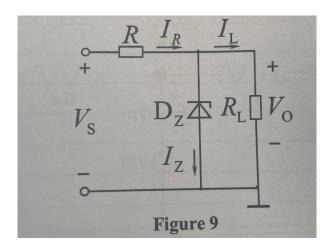
When  $R_L=R_{TH}=3\Omega$ , the resistor will absorb the maximum power, and the

power is 
$$P_{max} = \frac{(V_{Th})^2}{4R_L} = 1200W$$
 Finish.

# EEF 部分

Question 9 (10 Marks)—For Classes 17-22 Only:

In the circuit shown in Figure 9,  $V_s=12V$ ,  $R_L=500\Omega$ . For the Zener diode D, the regulation voltage  $V_Z=10V$ , the maximum regulation current  $I_{Zmax}=50mA$ , and the minimum regulation current  $I_{Zmin}=30mA$ . Determine the maximum and minimum values of the resistor R.



#### 【考点 Point】

二极管求限制电阻的范围 Find the range of a restrict resistor in a circuit with Semiconductor.

Answer: Max:  $40\Omega$ , Min:  $28.57\Omega$ .

#### 【解析 Analysis】

模电二极管稳压电路考点。先求负载电阻上的电流,然后求限流电阻上的电压,根据限流电阻上最大和最小电流的取值,分别求得电阻的最小值和最大值。

#### **Solution:**

$$V_0=V_Z=10V$$
 The current on the load resistor  $R_L$  is:  $I_L=rac{V_0}{R_L}=rac{10V}{500\Omega}=20mA$ 

The voltage of the resistor R is  $V_R = V_S - V_0 = 2V$ .

The maximum of the current passing the resistor R is:

$$I_{Rmax} = I_L + I_{Zmax} = 20mA + 50mA = 70mA$$

The minimum of the current passing the resistor R is:

$$I_{Rmin} = I_L + I_{Zmin} = 20mA + 30mA = 50mA$$

The maximum of the resistor R is:

$$R_{max} = \frac{V_R}{I_{Rmin}} = \frac{2V}{50mA} = 40\Omega$$

The minimum of the resistor R is:

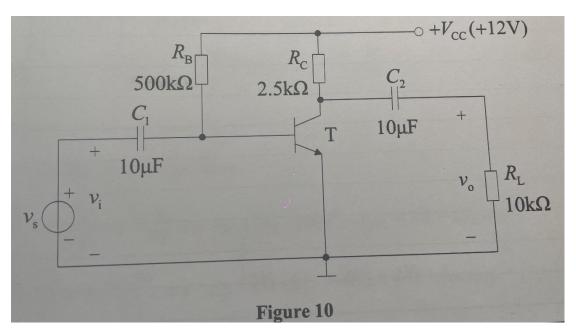
$$R_{min} = \frac{V_R}{I_{Rmax}} = \frac{2V}{70mA} = 28.57\Omega$$

Finish.

Question 10 (16 Marks)——For Classes 17-22 Only:

The common-emitter BJT circuit is shown in Figure 10.

- (1)Asusume  $m{\beta}=100$  and  $V_{BEQ}=0.6V$ , analyze the Q-point, including  $I_{BQ},\ V_{CEQ},\ I_{CQ};$
- (2)Assume  $r_{bb'}=0$  and  $r_{ce}=\infty$ , draw its small-signal hybrid- $\pi$  equivalent circuit and calculate the BJT equivalent resistance  $r_{b'e}$  and voltage gain  $A_v$ .



# 【考点 Point】

三极管(双极型晶体管)电路 BJT circuit

静态工作点分析 Analysis of quiet point Q

混合派模型电路 hybrid-П model circuit

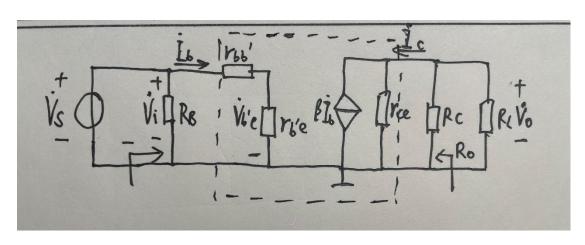
交流动态分析 Dynamic analysis

Answer:

(1) 
$$I_{BQ} = 22.8 \mu A$$
,  $I_{CQ} = 2.28 mA$ ,  $V_{CEQ} = 6.3 V$ 

(2) 
$$r_{b'e} \approx 1.14(k\Omega)$$
 ,  $A_V \approx -175.4$ 

Small-signal hybrid- $\pi$  equivalent circuit:



### 【解析 Analysis】

模电三极管混合派模型考点。第一问考察静态工作点得情况,根据已知条件和相关公式即可求解这三个量。第二问为交流电路小信号的动态分析。并画出混合派模型的电路图。根据公式可求相关交流分析量。混合派模型电路图只需根据记忆画出即可。

### **Solution:**

(1)

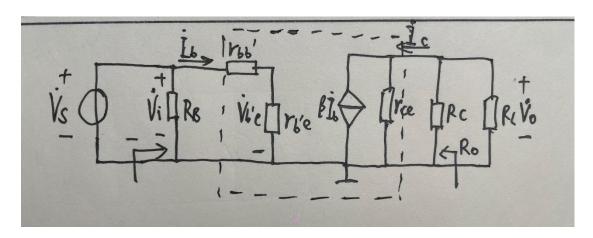
$$I_{BQ} = \frac{V_{CC} - V_{BEQ}}{R_B} = \frac{12V - 0.6V}{500k\Omega} = 22.8\mu A$$

$$I_{CQ} = \beta I_{BQ} = 2.28mA$$

$$V_{CEQ} = V_{CC} - I_{CQ}R_C = 12V - 2.28mA \times 2.5k\Omega = 6.3V$$

(2)

The small-signal hybrid- $\pi$  equivalent circuit is:



Then, the BJT equivalent resistance  $r_{b'e}$  is:

$$r_{b'e} = \frac{V_T}{I_{BO}} = \frac{26mV}{22.8 \times 10^{-3} mA} \approx 1.14 (k\Omega)$$

Next, we find the voltage gain.

$$r_{be} = r_{b'e} + r_{bb'} = r_{bb'} + \frac{V_T}{I_{BQ}} = 0 + \frac{V_T}{I_{BQ}} \approx 1.14(k\Omega)$$

Total resistor load is:

$$R_L' = r_{ce} ||R_c|| R_L = 2(k\Omega)$$

The voltage gain  $A_{v}$  is:

$$A_V = \frac{V_0}{V_i} = -\frac{\beta R_L'}{r_{be}} \approx -175.4$$

Finish.

# 考点分析

# 具体考点:

- 1、 网孔电流法
- 2、 节点电压法
- 3、 戴维南等效电路
- 4、 运算放大器
- 5、 自然响应
- 6、 正弦稳态电路
- 7、 叠加法+正弦稳态
- 8、 最大功率传输
- 9、 二极管 稳压电路 求限流电阻范围
- 10、 三极管 静态工作点分析+动态交流小信号相关物理量计算