



Introduction to Electronic Systems

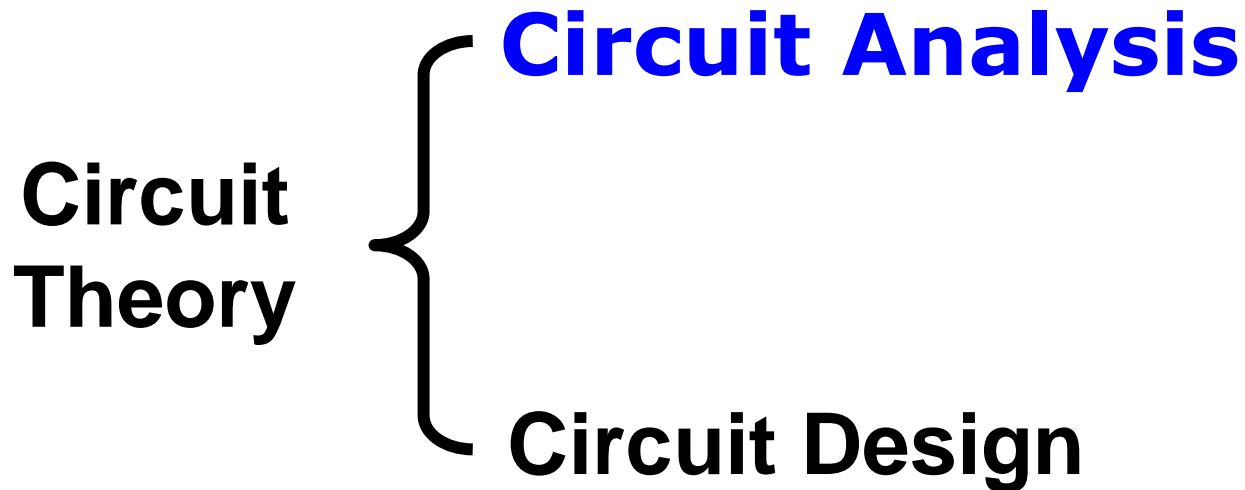


Overview of Circuit Analysis

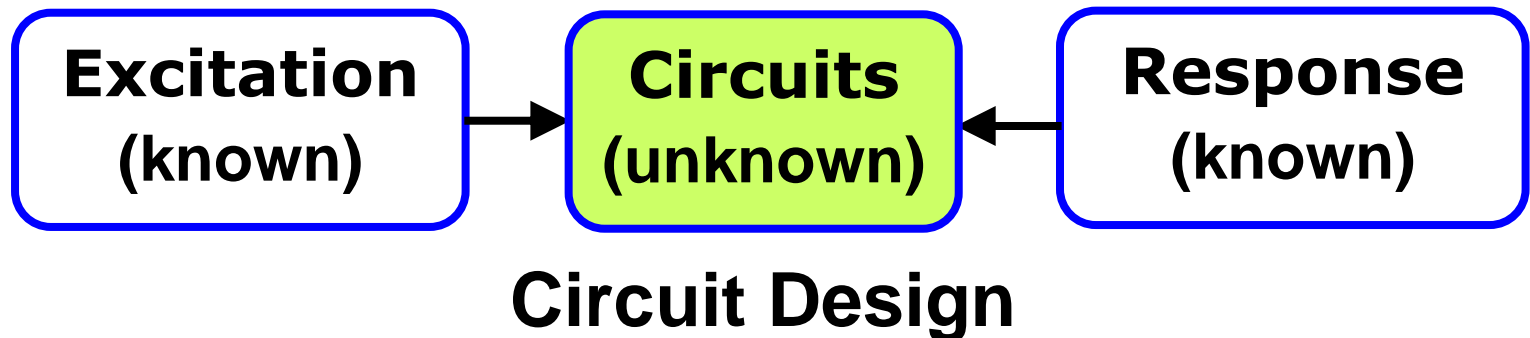
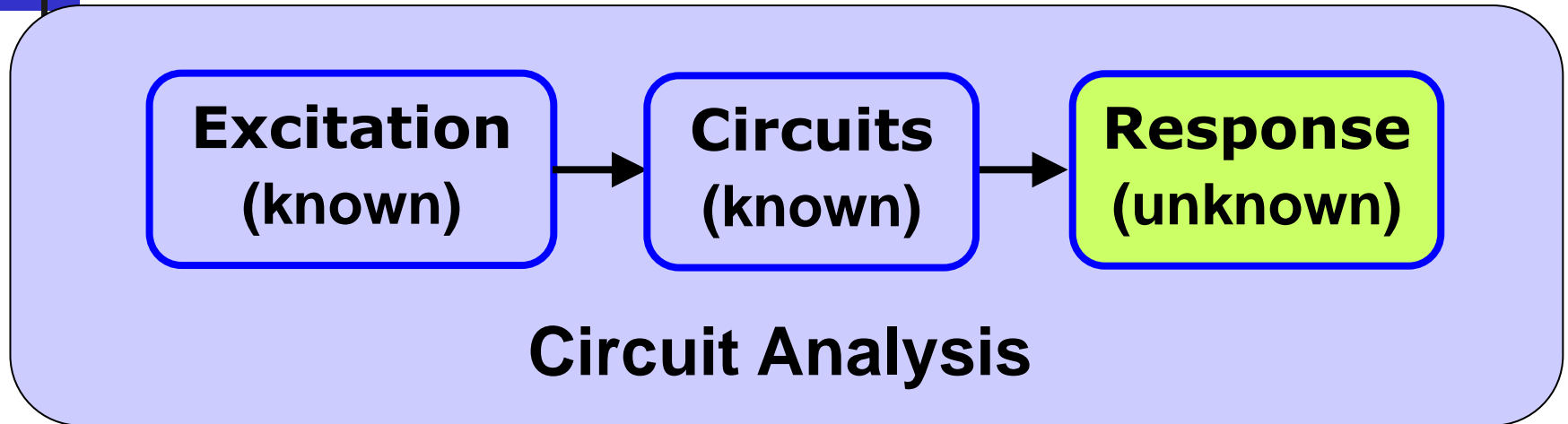
- **What is Circuit Analysis?**
- **Why do we implement Circuit Analysis?**
- **How do we implement Circuit Analysis?**



What is Circuit Analysis?



What is Circuit Analysis?

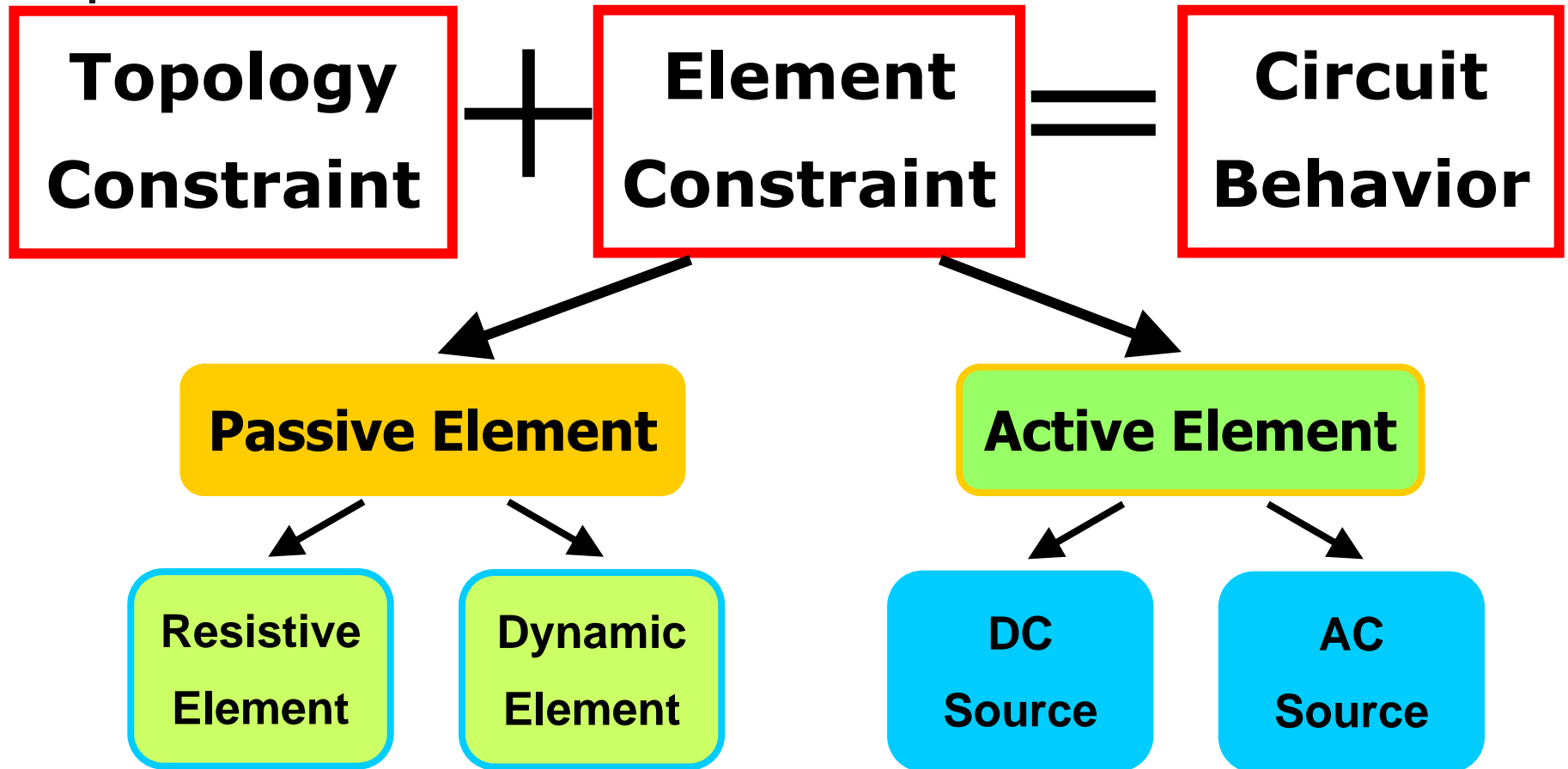




Why do we implement Circuit Analysis?

- Quantitatively predict or determine the behavior of a circuit:
 - *determine all voltages and currents*
- Lead to circuit improvements and refinements
- Circuit Analysis is **vital** for circuit design.

How is circuit behavior determined?





Three Parts of the Lecture

1. Resistive Circuit Analysis

DC + Resistive Element + Topology

2. Dynamic Circuit Analysis

DC + Dynamic/Resistive Element + Topology

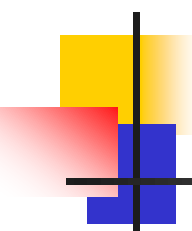
3. Sinusoidal Steady-State Analysis

AC + Dynamic/Resistive Element + Topology

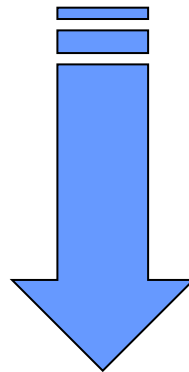


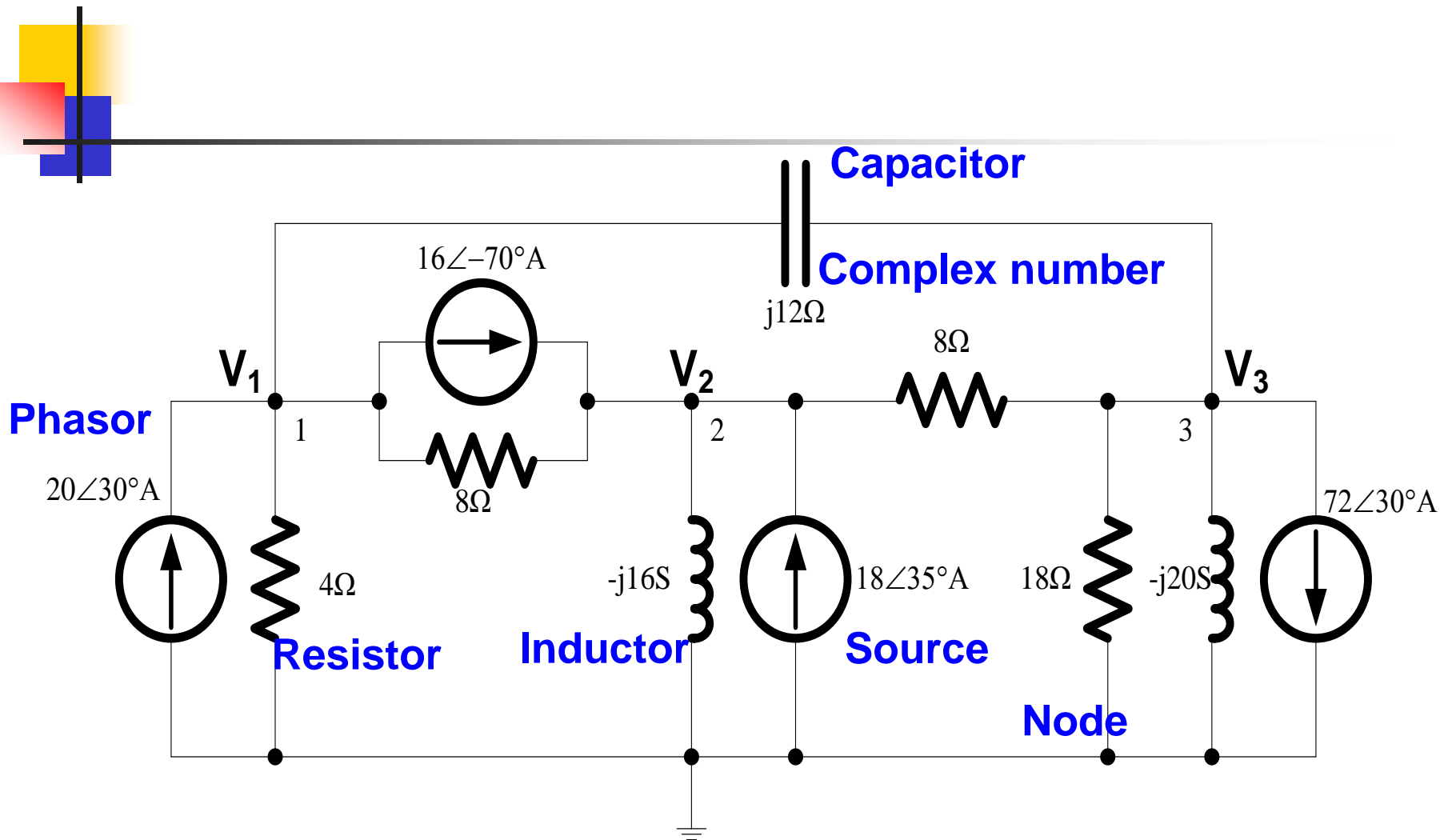
How do we implement Circuit Analysis?

- **Build equations** for a given circuit by using basic laws, theorems, and circuit analysis techniques;
- **Solve equations** to predict or determine circuit behavior (required currents and voltages).



**A Typical Problem you
should be able to solve
after this course:**





Find the voltage V_1 , V_2 and V_3 .



Part 1

Resistive Circuit Analysis (DC + Resistive Element + Topology)



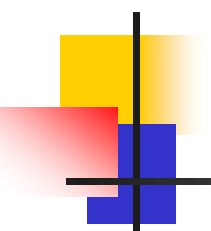
Part 1: Resistive Circuit Analysis

1. Circuit Variables and Circuit Elements

2. Simple Resistive Circuit Analysis

3. Techniques of Circuit Analysis

4. Operational Amplifier



Chapter 1: Circuit Variables and Circuit Elements

- **Circuit Variables**
- **Circuit Elements**
- **Power and Energy**
- **Voltage and Current Sources**



1-1 Circuit Variables

- Electric Charge
- Current
- Voltage
- **Power**
- **Energy**



Electric Charge (1)

- **Bipolar: Positive (proton) and Negative (electron) charge;**
- **The fundamental unit of charge is Coulomb (C);**
- **A single electron has a charge of -1.602×10^{-19} C, and a single proton has a charge of $+1.602 \times 10^{-19}$ C;**



Electric Charge (2)

- Charge in motion ---- Current;
- Separation of charge ---- voltage;
- Charge conservation law:

Electrons (or protons) are neither created nor destroyed.



Current (1)

- Motion of charge creates electric fluid (current);
- The fundamental unit of current is Ampere (A);
- The rate of charge flow is defined as current, and expressed as:

$$i(t) = \frac{dq(t)}{dt}$$

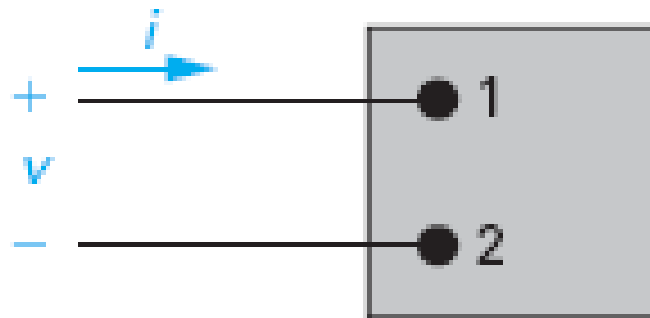
- i : current in A;
- q : charge in C;
- t : time in s.

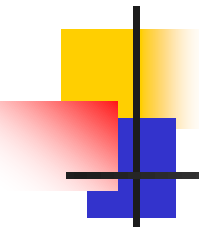
1.1 The current at the terminals of the element in Fig. 1.2 is

$$i = 0, \quad t < 0;$$

$$i = 20e^{-5000t} \text{ A}, \quad t \geq 0.$$

Calculate the total charge (in microcoulombs) entering the element at its upper terminal.





Solution:

$$\begin{aligned} Q &= \int_{-\infty}^{+\infty} i(t) dt = \int_0^{+\infty} 20e^{-5000t} dt \\ &= \frac{20}{-5000} e^{-5000t} \Big|_0^{+\infty} \\ &= \frac{20}{-5000} (0 - 1) = 4 \times 10^{-3} C \\ &= 4000 \mu C \end{aligned}$$



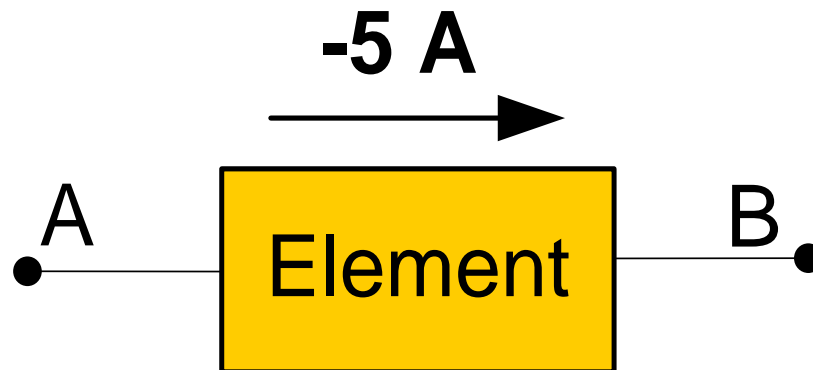
Current (2)

■ Current direction

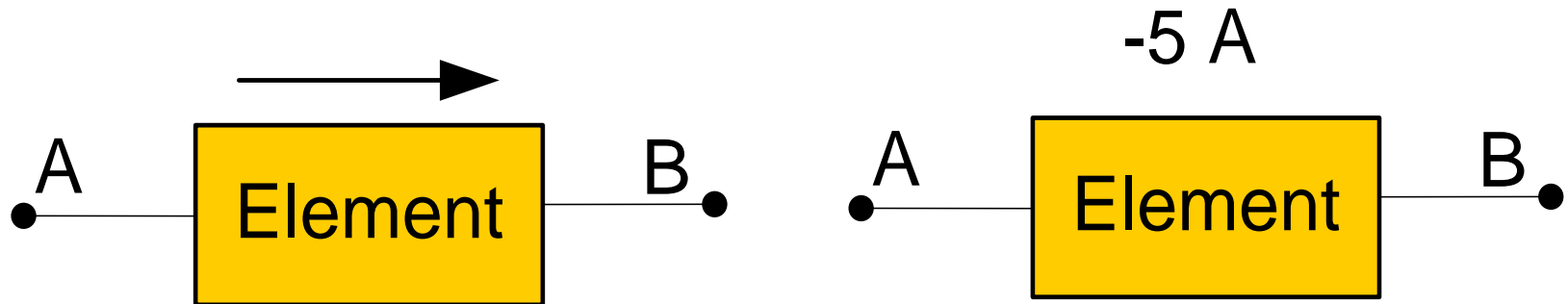
- Real direction: Moving direction of positive charges (proton)
- **Reference direction**: Arbitrary assigned direction by an arrow

Current (3)

- A current is completely specified by both its **magnitude** and **reference direction**.
- **Reference direction** is a fundamental part of a current!

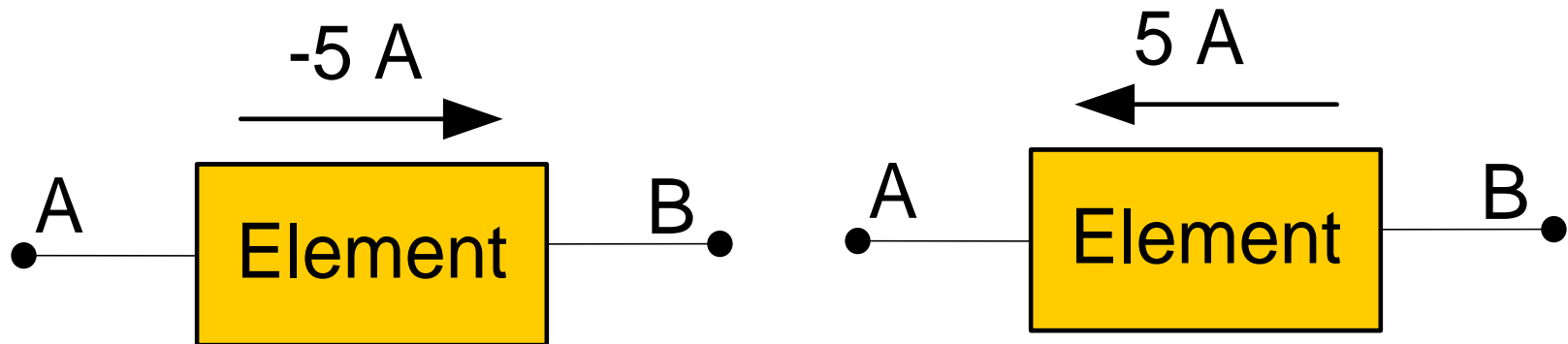


Current (4)



Incorrect definitions of a current

Current (5)



**Two correct equivalent representations
for the exact same current**



Voltage (1)

- Charge separation creates electric force (voltage);
- The fundamental unit of voltage is Volt (V);
- The energy per unit charge created by the separation is defined as voltage:

$$u = \frac{dw}{dq}$$

- u : voltage in V;
- w : energy in J;
- q : charge in C.



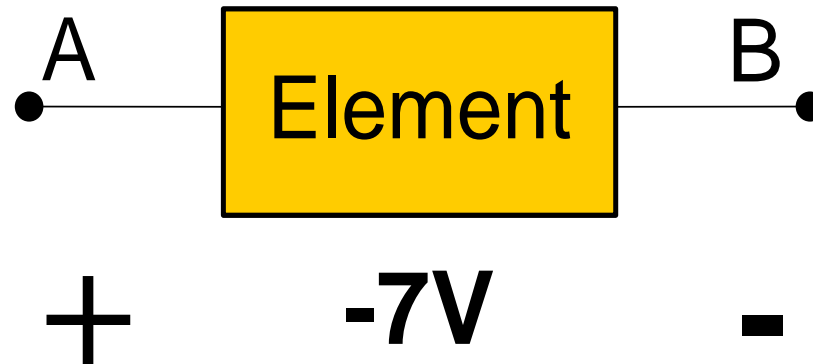
Voltage (2)

■ Voltage polarity

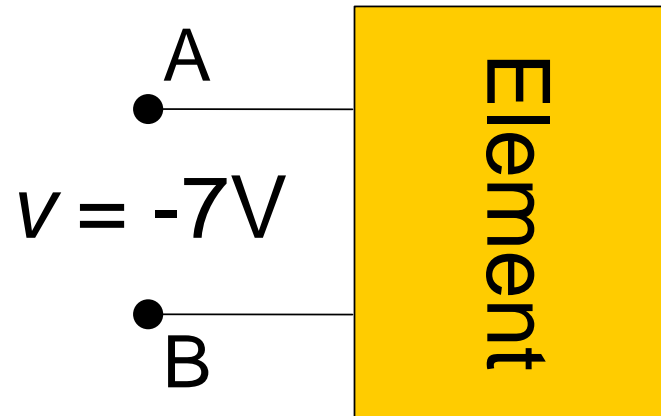
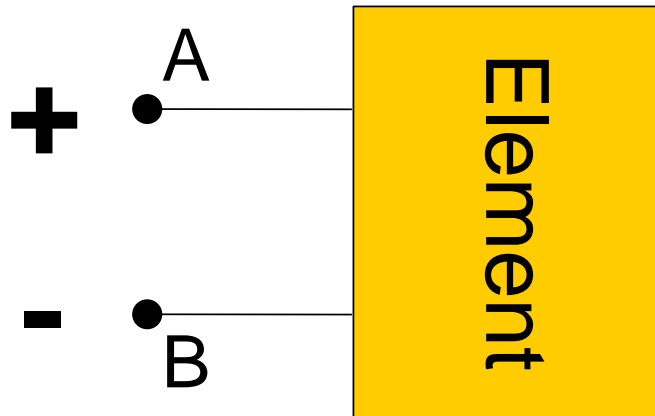
- **Real polarity:** From positive terminal to negative terminal
- **Reference polarity:** Arbitrary assigned polarity by a plus-minus sign pair

Voltage (3)

- A voltage is completely specified by both its **magnitude** and **reference polarity**.
- The definition of any voltage must include **a plus-minus sign pair!**

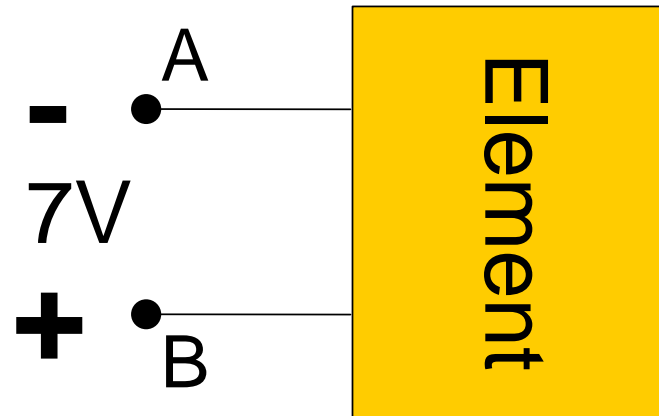
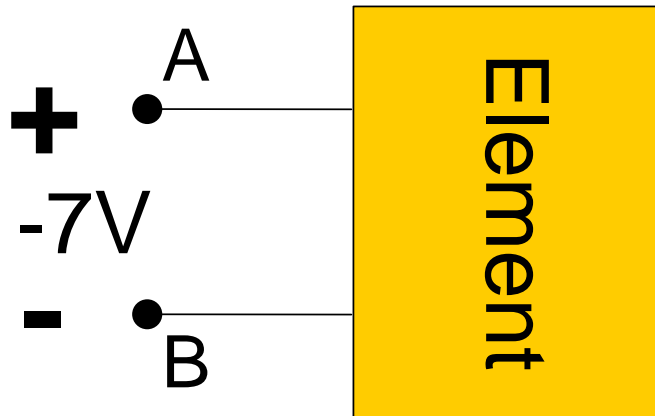


Voltage (4)



Incorrect definitions of a voltage

Voltage (5)



**Two correct equivalent representations
for the exact same voltage**



1-2 Circuit Elements

- **Ideal Basic Circuit Element**
- **Resistor (Ohm's Law)**
- **Passive Sign Convention**
- **Voltage and Current Source**
- **op amp, Capacitor, Inductor**
- **Diode, Transistor, Transformer**



Ideal Basic Circuit Element

- **Only has two terminals**
- **Described mathematically in terms of voltage and/or current**
- **Can not be further reduced or subdivided into other elements**
- **Resistor, Voltage/Current source, Capacitor, Inductor**



Ideal Basic Circuit Element

- **Ideal:**

- Can not be realizable physically**

- **Basic:**

- Can not be further reduced or subdivided into other elements**

- **Ideal Basic Circuit Element:**

- Resistor, Voltage/Current source,
Capacitor, Inductor**

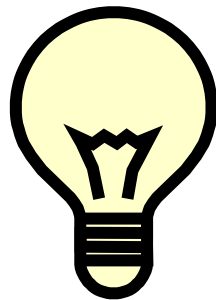
Ideal Circuit Element

- The dimension of element is 1/10th (or smaller) of the operation wavelength.

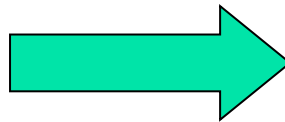
$$\lambda = \frac{C}{f}$$

$C=3 \times 10^8 \text{m/s}$

f(Hz)	50	25k	500M	30G
$\lambda(\text{m})$	6×10^6	12k	0.6	0.01



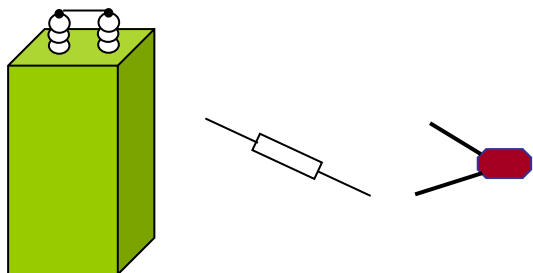
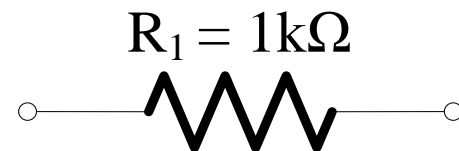
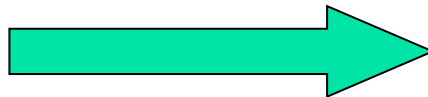
model



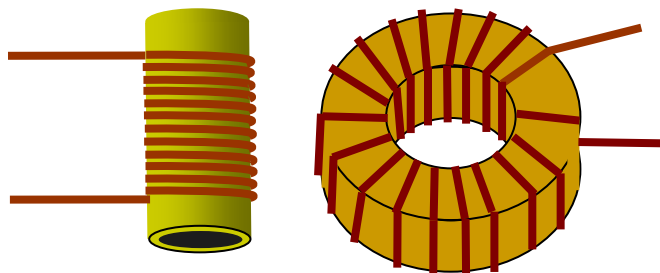
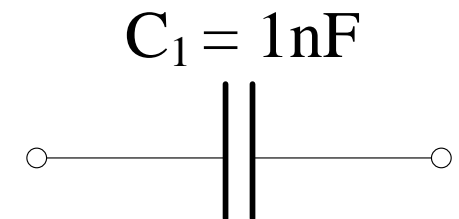
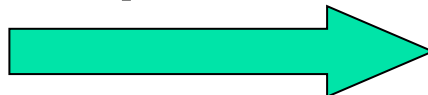
Ideal Basic Circuit Elements



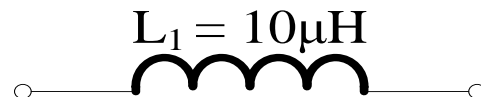
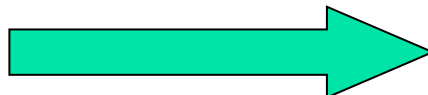
Resistor



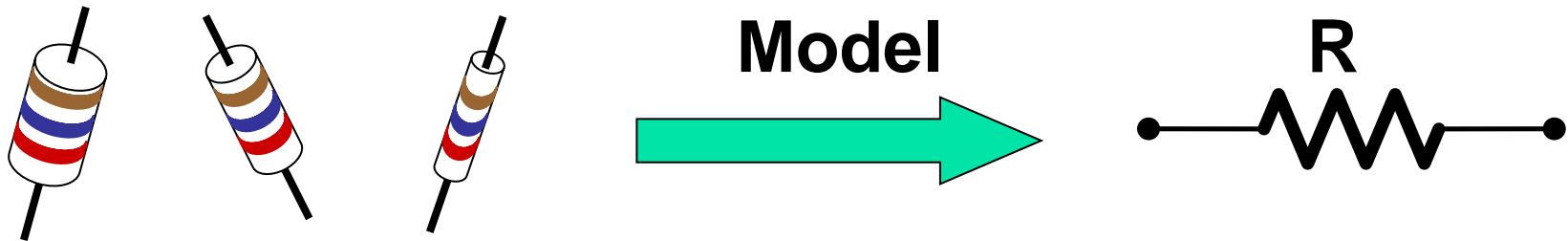
Capacitor



Inductor



Resistor



■ Resistor is an ideal basic circuit element.



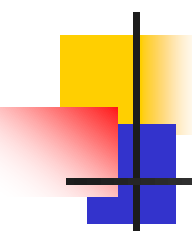
Passive Sign Convention

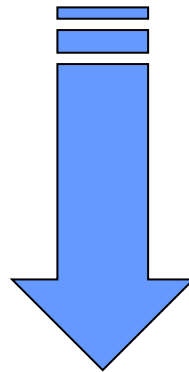
- Theoretically, the assignments of the reference direction for voltage and current are entirely arbitrary.
- But we must write all subsequent equations to agree with the chosen references.

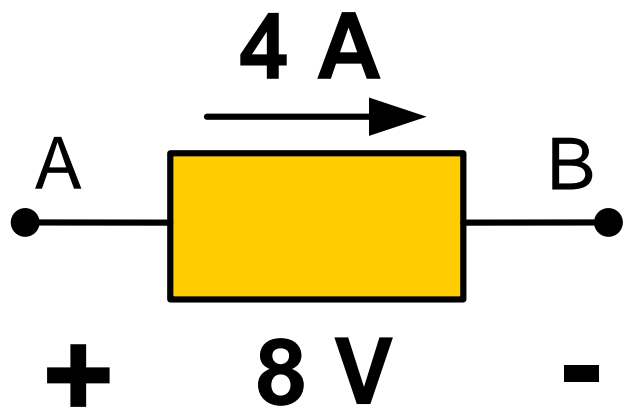
Example:



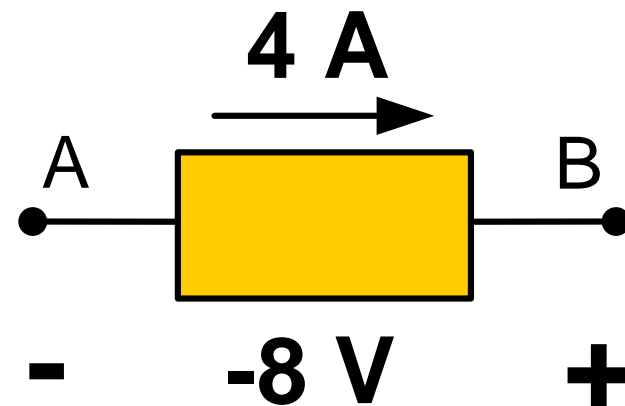
- The **REAL** direction for the current is:
4A flowing from terminal A to B
- The **REAL** polarity for the voltage is:
Terminal A is 8V positive with respect to B

- 
- By using **Reference** polarity for voltage and **Reference** direction for current, we have **FOUR** choices to represent this case :



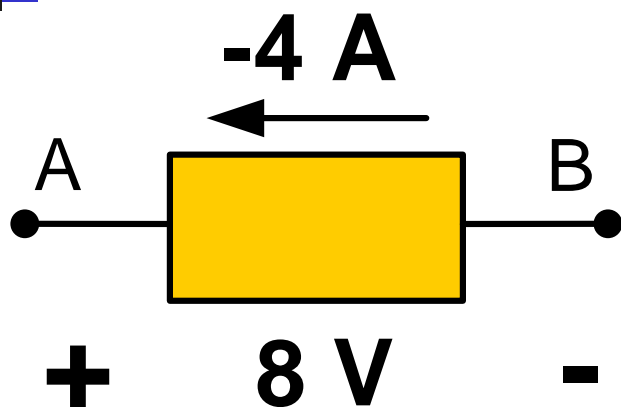


Choice 1

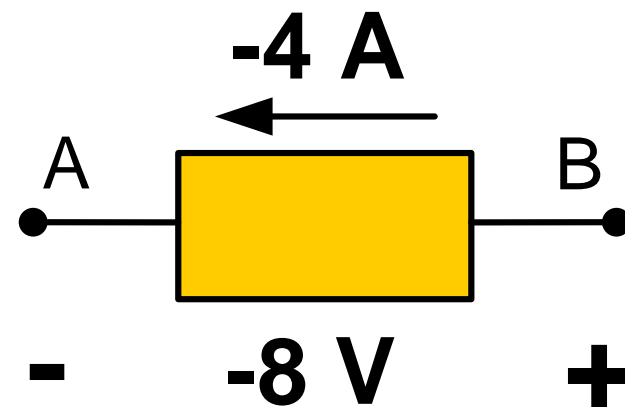


Choice 2

- If the element is a resistor, how to find the value of the resistance for each case?



Choice 3



Choice 4

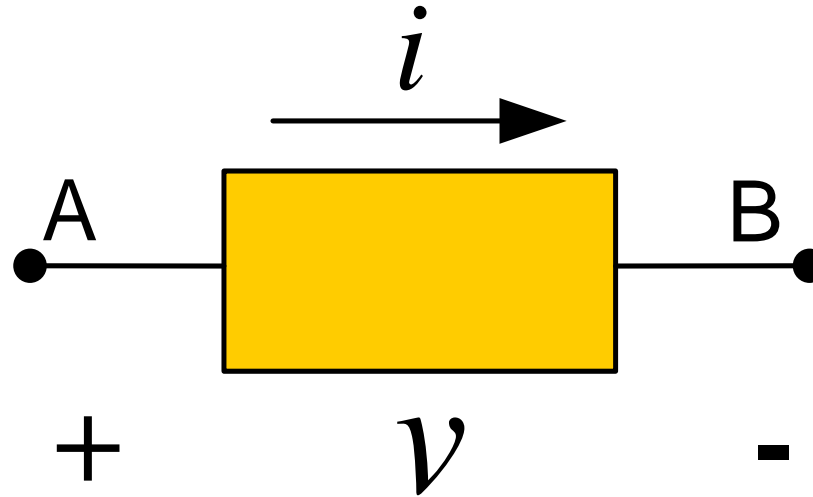
- If the element is a resistor, how to find the value of the resistance for each case?



Passive Sign Convention (PSC)

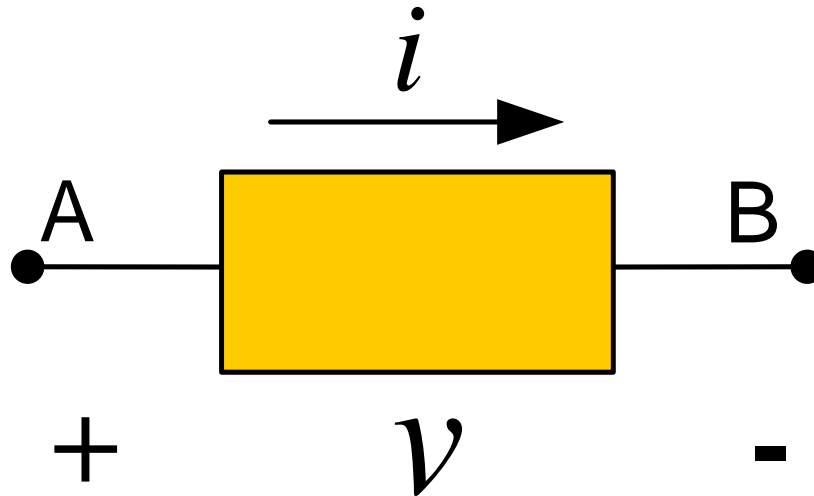
- Whenever the reference direction for the current in an element is in the direction of the reference voltage drop across the element, **use a positive sign** in any expression that relates the voltage and the current. Otherwise use **a negative sign**.

Passive Sign Convention



- The reference direction for the current is assigned in the direction of the reference voltage drop across the element.

Passive Sign Convention



- Current enters the positive terminal;
- Current leaves the negative terminal.



Passive Sign Convention

- **Passive sign convention is used only for the convenience of circuit analysis.**
- **We apply the passive sign convention in all the lectures that follow.**



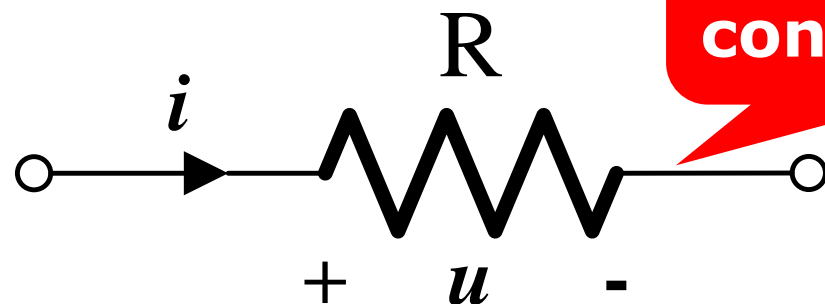
Ohm's Law

Ohm's Law with PSC

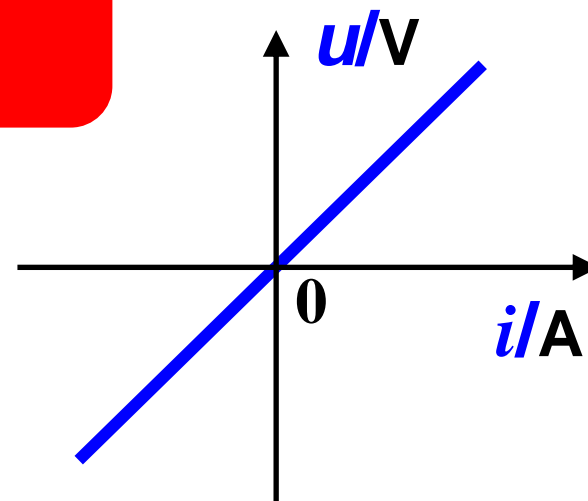
Ohm's Law w/o PSC

Power and Energy of Resistors

Ohm's Law with PSC



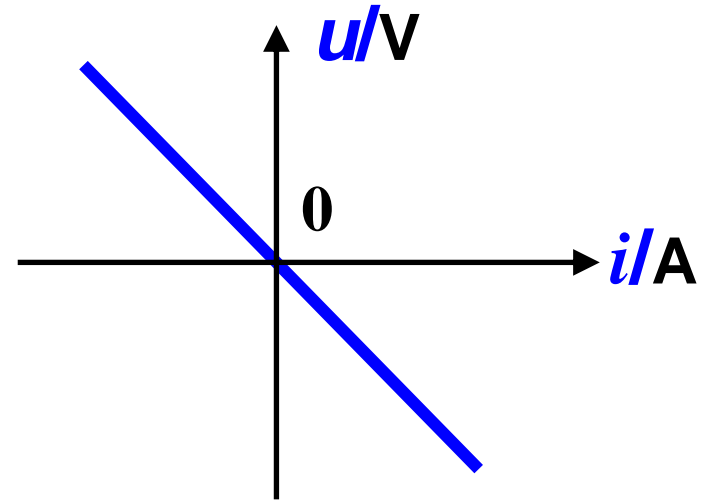
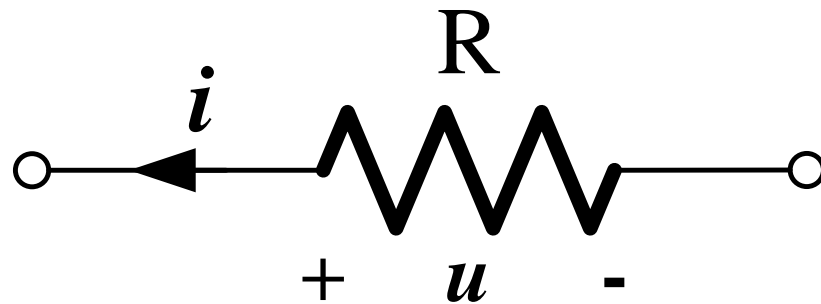
Passive sign convention



VCR of Resistor (Ohm's law):

$$u = Ri$$

Ohm's Law w/o PSC



Ohm's law (w/o PSC):

$$u = -Ri$$



1-3 Power and Energy

- **Power**
- **Energy**
- **Passive and Active Element**



Resistance and Conductance

In Ohm's law, R is measured in ohm (Ω) :

$$u = Ri$$

$$R = u/i$$

R can also be characterized by conductance;

Conductance is measured in Siemens (S);

$$i = Gu$$

$$G = \frac{1}{R}$$



Power

- Power is defined as the time rate of expending or absorbing energy, and expressed as:

$$p = \frac{dw}{dt}$$

$$= \left(\frac{dw}{dq} \right) \left(\frac{dq}{dt} \right) = vi$$

Passive sign convention

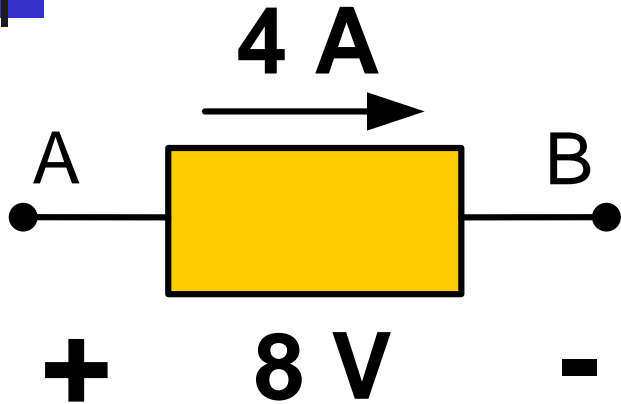


Power

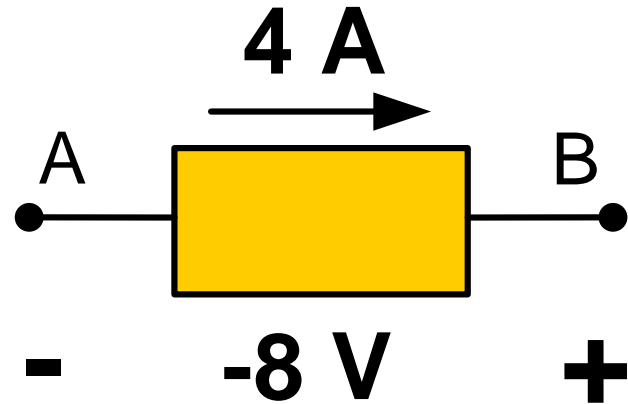
- If the passive sign convention is not applied, the power is expressed as:

$$p = -vi$$

Example:



$$\begin{aligned} p &= vi \\ &= 8 \times 4 \\ &= 32 \text{ W} \end{aligned}$$



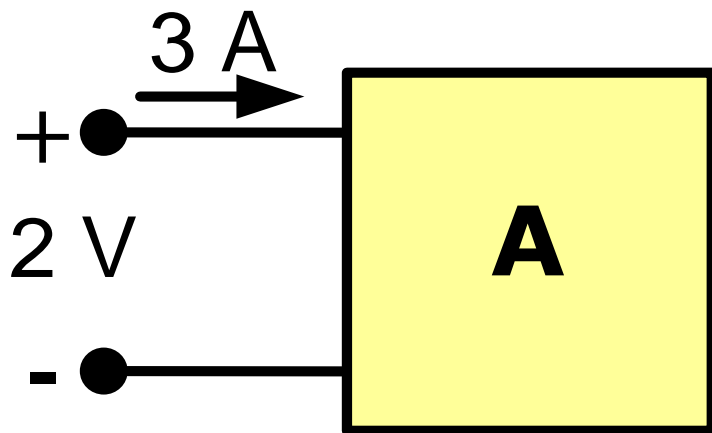
$$\begin{aligned} p &= -vi \\ &= -(-8) \times 4 \\ &= 32 \text{ W} \end{aligned}$$



Power

- If p is **positive**, power is absorbed by the element; or, power is being delivered to the element;
- If p is **negative**, the element supplies power; or, power is being extracted from the element.

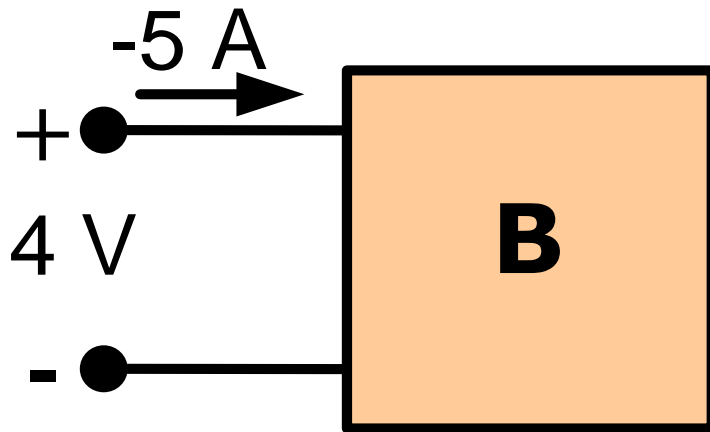
Examples:



$$p = (2V)(3A) \\ = 6W$$

- Power of 6W is **absorbed** by A;
- Or, power of 6W is **being delivered** to A.

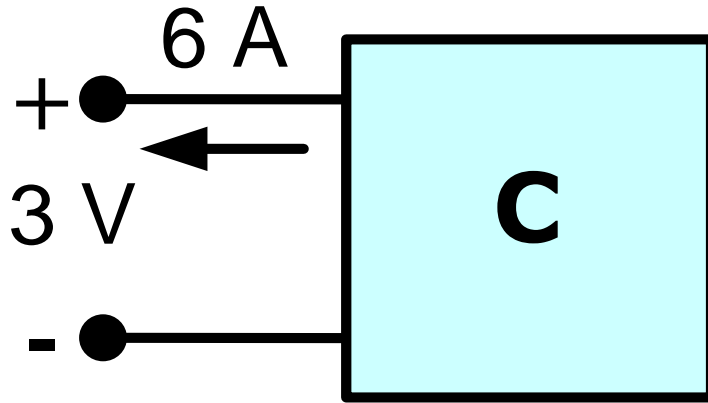
Examples :



$$\begin{aligned} p &= (4\text{V})(-5\text{A}) \\ &= -20\text{W} \end{aligned}$$

- Power of 20W is **supplied** by B;
- Or, power of 20W is **being extracted** from B.

Examples:



$$p = -(3\text{V})(6\text{A}) \\ = -18\text{W}$$

- Power of 18W is supplied by C;
- Or, power of 18W is being extracted from C.



Energy

- Inversely, energy can be calculated as:

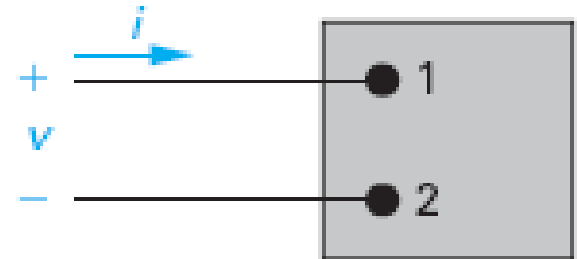
$$w = \int_{-\infty}^t p(\tau) d\tau$$



- 1.8. The voltage and current at the terminals of the circuit element in Fig. 1.2 are zero for $t < 0$. For $t \geq 0$ they are

$$v = e^{-500t} - e^{-1500t} \text{ V},$$

$$i = 30 - 40e^{-500t} + 10e^{-1500t} \text{ mA}.$$



- (a) Find the power at $t = 1 \text{ ms}$.
- (b) How much energy is delivered to the circuit element between 0 and 1 ms?
- (c) Find the total energy delivered to the element.



Solution:

P 1.8 [a] $p = vi = 30e^{-500t} - 30e^{-1500t} - 40e^{-1000t} + 50e^{-2000t} - 10e^{-3000t}$
 $p(1 \text{ ms}) = 3.1 \text{ mW}$

[b]
$$w(t) = \int_0^t (30e^{-500x} - 30e^{-1500x} - 40e^{-1000x} + 50e^{-2000x} - 10e^{-3000x}) dx$$
$$= 21.67 - 60e^{-500t} + 20e^{-1500t} + 40e^{-1000t} - 25e^{-2000t} + 3.33e^{-3000t} \mu\text{J}$$

$$w(1 \text{ ms}) = 1.24 \mu\text{J}$$

[c] $w_{\text{total}} = 21.67 \mu\text{J}$

Solution:

(c) $p=vi$

总能量就是对 p 从0到 $+\infty$ 做积分

$$\begin{aligned} E &= \int_0^{+\infty} p \, dt = \int_0^{+\infty} 1000(e^{-500t} - e^{-1500t})(30 - 40e^{-500t} + 10e^{-1500t}) \, dt \\ &= 1000 \int_0^{+\infty} (30e^{-500t} - 40e^{-1000t} + 10e^{-2000t} - 30e^{-1500t} + 40e^{-2000t} - 10e^{-3000t}) \, dt \\ &= 1000 \times \left(-\frac{30}{500}e^{-500t} + \frac{40}{1000}e^{-1000t} + \frac{30}{1500}e^{-1500t} - \frac{50}{2000}e^{-2000t} + \frac{10}{3000}e^{-3000t} \right) \Big|_0^{+\infty} \\ &= 1000 \times \left(\frac{3}{50} - \frac{1}{25} - \frac{1}{50} + \frac{1}{40} - \frac{1}{300} \right) \\ &= 1000 \times \frac{13}{600} \\ &\approx 21.67 \end{aligned}$$



Passive and Active Element

■ Energy:

$$w = \int_{-\infty}^t p(\tau) d\tau = \int_{-\infty}^t u(\tau) i(\tau) d\tau$$

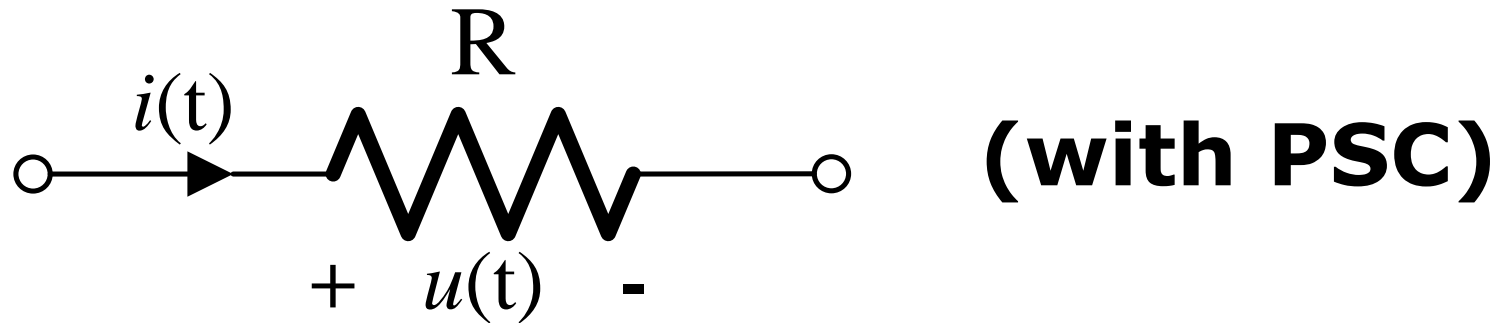
■ Passive:

$$w \geq 0$$

■ Active:

$$w < 0$$

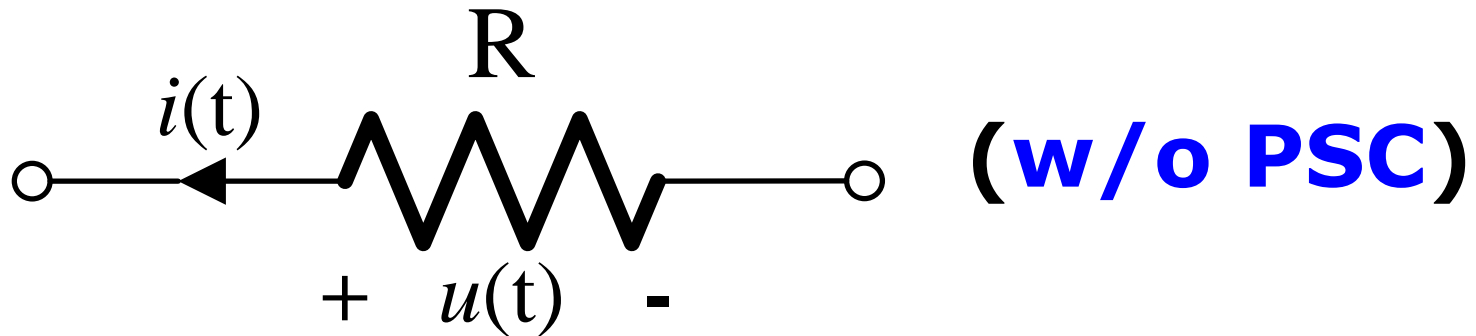
Power of a Resistor



$$p = vi = (iR)i = i^2 R$$

$$= vi = v \left(\frac{v}{R} \right) = \frac{v^2}{R}$$

Power of a Resistor



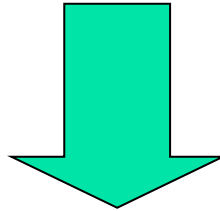
$$p = -vi = -(-iR)i = i^2 R$$

$$= -vi = -v\left(-\frac{v}{R}\right) = \frac{v^2}{R}$$



Power of a Resistor

$$p = i^2 R = \frac{v^2}{R} \geq 0$$

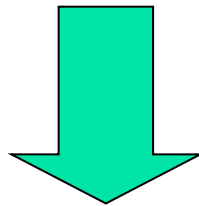


A resistor always absorbs power from the circuit.

Energy of a Resistor

$$w(t) = \int_{-\infty}^t p(\tau) d\tau$$

$$= \int_{-\infty}^t i^2 R d\tau = \int_{-\infty}^t \frac{v^2}{R} d\tau \geq 0$$



Resistor is a passive element.



1-4 Voltage and Current Source

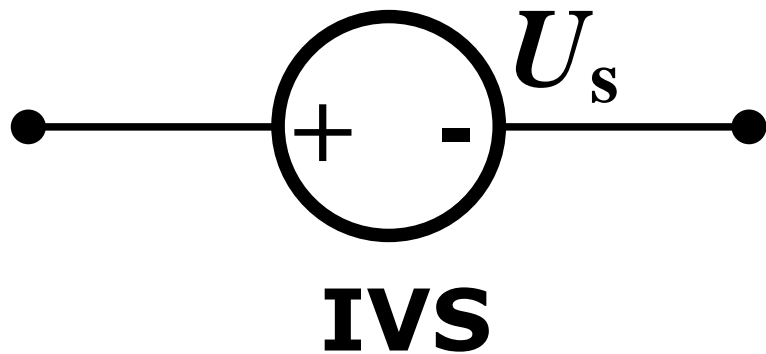
- **Independent source**
 - **IVS**
 - **ICS**
- **Dependent source (Controlled source)**
 - **CCCS**
 - **VCCS**
 - **CCVS**
 - **VCVS**



Independent Voltage Source

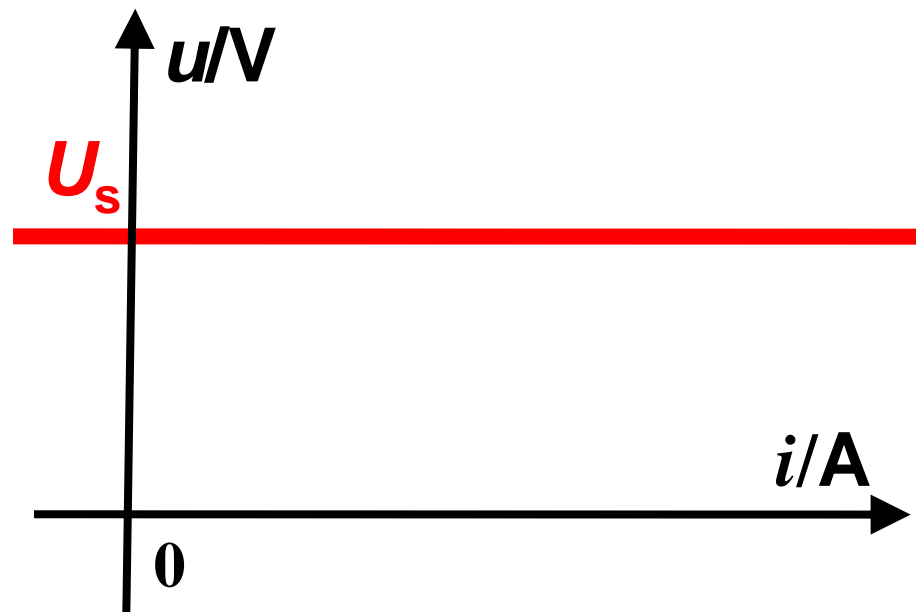
- An ideal Independent Voltage Source (IVS) is a circuit element that maintains a prescribed voltage across its terminals **regardless of** the current flowing in those terminals.

Independent Voltage Source



■ Symbol

- Reference polarity
- Magnitude

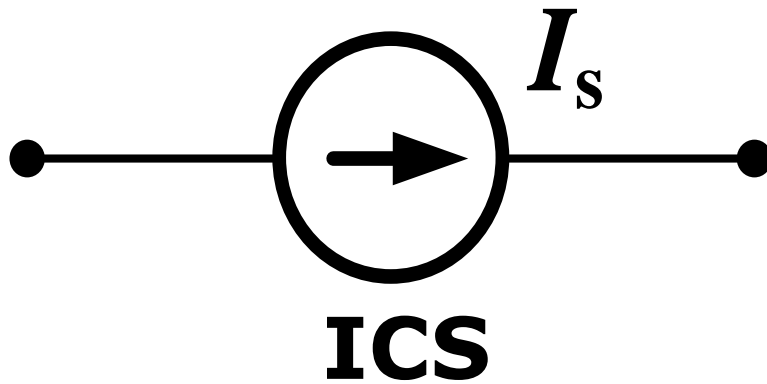




Independent Current Source

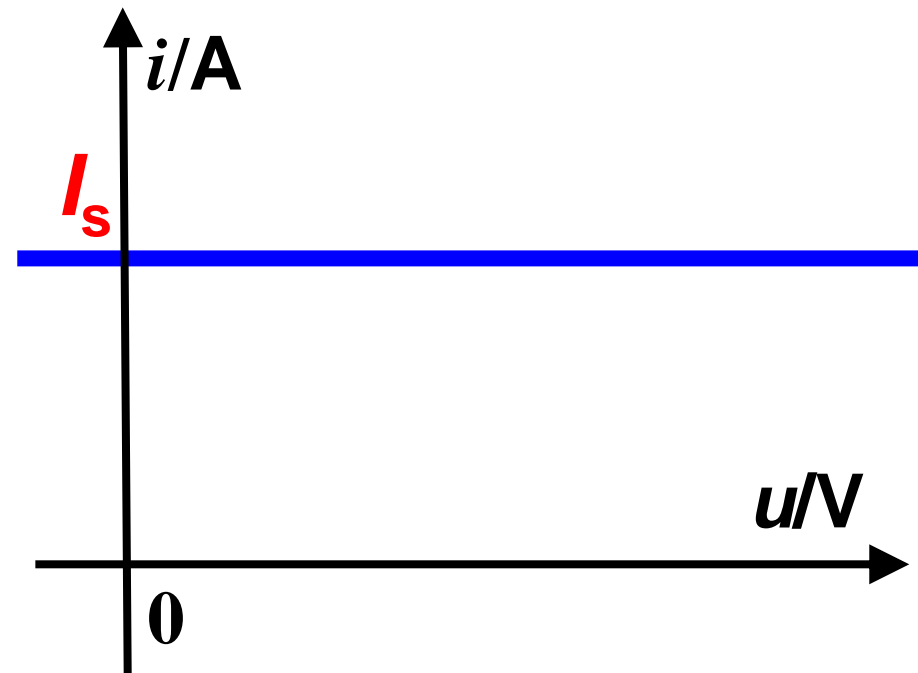
- An ideal Independent Current Source (ICS) is a circuit element that maintains a prescribed current through its terminals **regardless of** the voltage across those terminals.

Independent Current Source



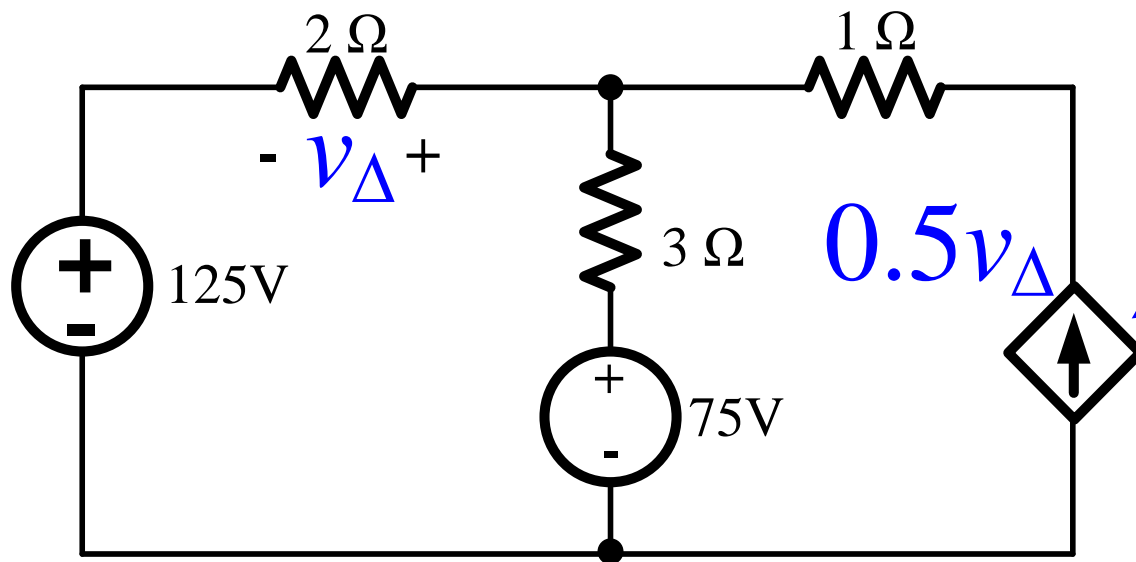
■ Symbol

- Reference direction
- Magnitude



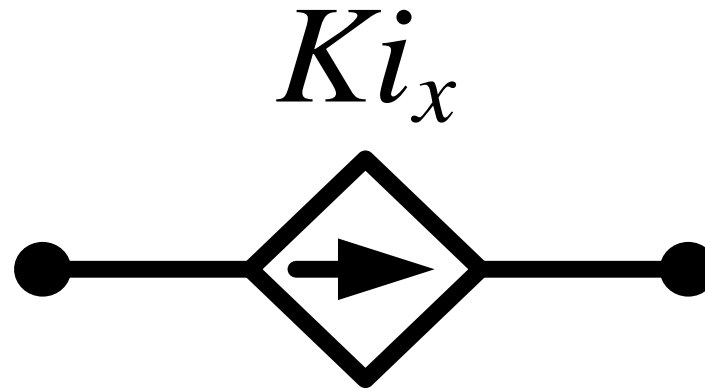
Dependent (Controlled) Sources

- Dependent source is determined by a voltage (or current) existing at some other location in the circuit.



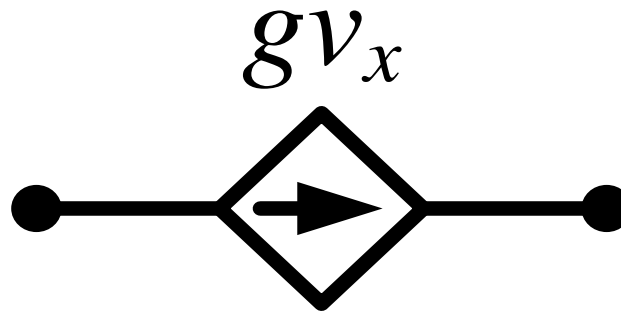
**Voltage
Controlled
Current
Source**

CCCS



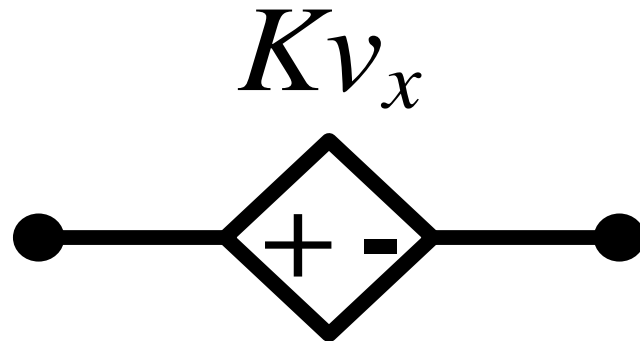
- **Current-Controlled Current Source (CCCS)**
- **K is a constant factor**

VCCS



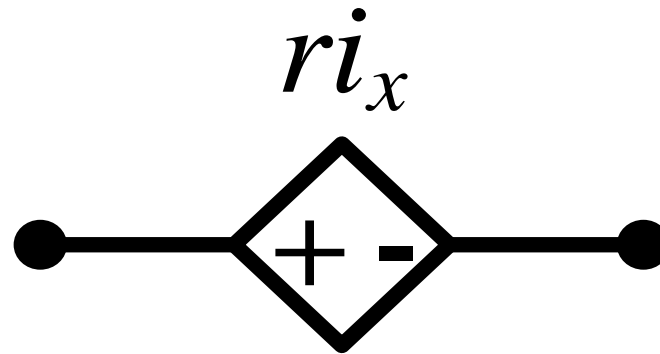
- Voltage-Controlled Current Source (VCCS)
- g is a constant factor

VCVS



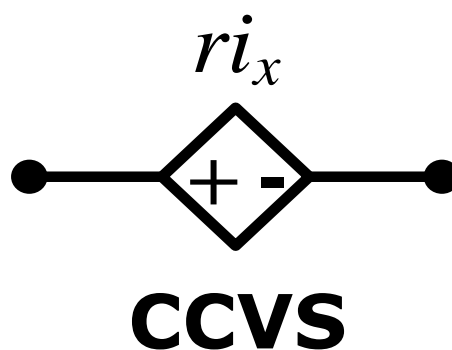
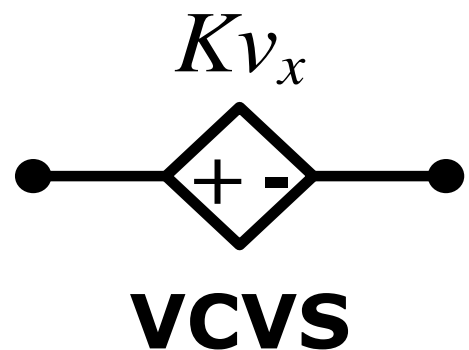
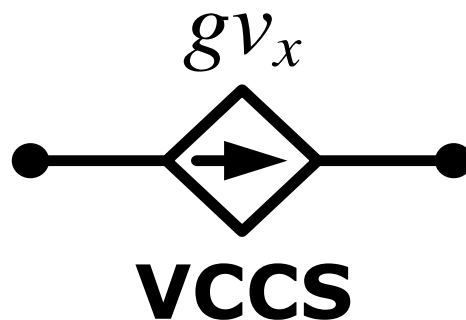
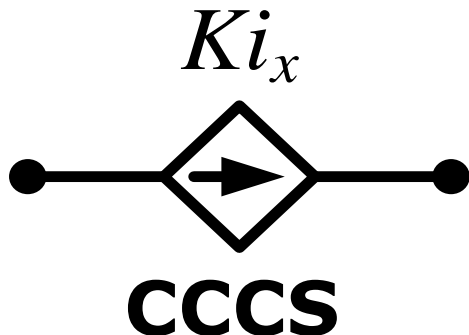
- Voltage-Controlled Voltage Source (VCVS)
- K is a constant factor

CCVS



- Current-Controlled Voltage Source (CCVS)
- r is a constant factor

Dependent (Controlled) Sources



■ K, g, r are
all const.
factors.



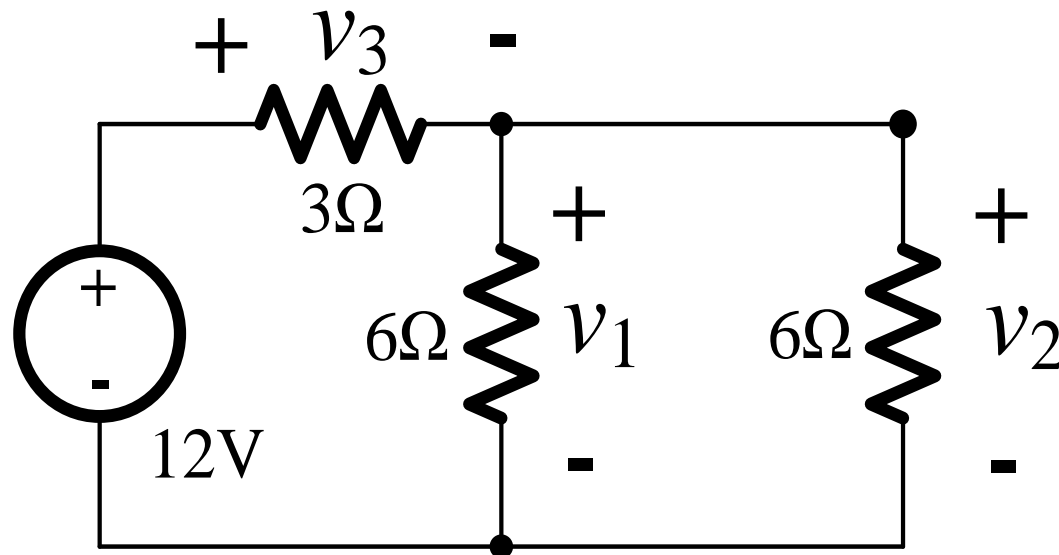
Question 1:

What are the units of the factors of K , g , and r of those controlled sources in last page?

- K is a dimensionless scaling factor;
- g is a factor with unit of A/V ;
- r is a factor with unit of V/A .

Question 2:

How to calculate the power of a voltage or current source?





Solution

- 电阻R1与电阻R2并联,根据电阻并联计算公式:

$$R' = \frac{R1 \cdot R2}{R1 + R2} = \frac{6 \times 6}{6 + 6} = 3\Omega$$

则电压源发出功率为:

$$P=UI=\frac{U^2}{R3+R'}=\frac{144}{6}=24W。$$



Summary of Chapter 1

- Basic conceptions of charge, current, voltage, power, and energy
- **Reference polarity** for voltage and **reference direction** for current
- Ideal basic circuit element
- **Passive sign convention (PSC)**
- Power and energy calculation
- IVS, ICS, CCCS, VCCS, CCVS, VCVS