9.8 (*The* **Fan** *class*) Design a class named **Fan** to represent a fan. The class contains:

- Three constants named **SLOW**, **MEDIUM**, and **FAST** with the values **1**, **2**, and **3** to denote the fan speed.
- A private **int** data field named **speed** that specifies the speed of the fan (the default is **SLOW**).
- A private **boolean** data field named **on** that specifies whether the fan is on (the default is **false**).
- A private **double** data field named **radius** that specifies the radius of the fan (the default is **5**).
- A string data field named **color** that specifies the color of the fan (the default is **blue**).
- The accessor and mutator methods for all four data fields.
- A no-arg constructor that creates a default fan.
- A method named **toString()** that returns a string description for the fan. If the fan is on, the method returns the fan speed, color, and radius in one combined string. If the fan is not on, the method returns the fan color and radius along with the string "fan is off" in one combined string.

Draw the UML diagram for the class and then implement the class. Write a test program that creates two **Fan** objects. Assign maximum speed, radius **10**, color **yellow**, and turn it on to the first object. Assign medium speed, radius **5**, color **blue**, and turn it off to the second object. Display the objects by invoking their **toString** method.

****9.9** (*Geometry: n-sided regular polygon*) In an n-sided regular polygon, all sides have the same length and all angles have the same degree (i.e., the polygon is both equilateral and equiangular). Design a class named **RegularPolygon** that contains:

- A private **int** data field named **n** that defines the number of sides in the polygon with default value **3**.
- A private **double** data field named **side** that stores the length of the side with default value **1**.
- A private **double** data field named **x** that defines the x-coordinate of the polygon's center with default value **0**.
- A private **double** data field named **y** that defines the y-coordinate of the polygon's center with default value **0**.
- A no-arg constructor that creates a regular polygon with default values.
- A constructor that creates a regular polygon with the specified number of sides and length of side, centered at (**0**, **0**).
- A constructor that creates a regular polygon with the specified number of sides, length of side, and x- and y-coordinates.
- The accessor and mutator methods for all data fields.
- The method **getPerimeter()** that returns the perimeter of the polygon.
- The method **getArea()** that returns the area of the polygon. The formula for computing the area of a regular polygon is $Area = \dfrac{n \times s^2}{4 \times \tan\left(\dfrac{\pi}{n}\right)}$.

Draw the UML diagram for the class and then implement the class. Write a test program that creates three **RegularPolygon** objects, created using the no-arg constructor, using **RegularPolygon(6, 4)**, and using **RegularPolygon(10, 4, 5.6, 7.8)**. For each object, display its perimeter and area.

***9.10** (*Algebra: quadratic equations*) Design a class named `QuadraticEquation` for a quadratic equation $ax^2 + bx + x = 0$. The class contains:

- Private data fields `a`, `b`, and `c` that represent three coefficients.
- A constructor for the arguments for `a`, `b`, and `c`.
- Three getter methods for `a`, `b`, and `c`.
- A method named `getDiscriminant()` that returns the discriminant, which is $b^2 - 4ac$.
- The methods named `getRoot1()` and `getRoot2()` for returning two roots of the equation

$$r_1 = \frac{-b + \sqrt{b^2 - 4ac}}{2a} \quad \text{and} \quad r_2 = \frac{-b - \sqrt{b^2 - 4ac}}{2a}$$

These methods are useful only if the discriminant is nonnegative. Let these methods return `0` if the discriminant is negative.

Draw the UML diagram for the class and then implement the class. Write a test program that prompts the user to enter values for a, b, and c and displays the result based on the discriminant. If the discriminant is positive, display the two roots. If the discriminant is 0, display the one root. Otherwise, display "The equation has no roots." See Programming Exercise 3.1 for sample runs.

***9.11** (*Algebra:* 2×2 *linear equations*) Design a class named `LinearEquation` for a 2×2 system of linear equations:

$$\begin{aligned} ax + by &= e \\ cx + dy &= f \end{aligned} \quad x = \frac{ed - bf}{ad - bc} \quad y = \frac{af - ec}{ad - bc}$$

The class contains:

- Private data fields `a`, `b`, `c`, `d`, `e`, and `f`.
- A constructor with the arguments for `a`, `b`, `c`, `d`, `e`, and `f`.
- Six getter methods for `a`, `b`, `c`, `d`, `e`, and `f`.
- A method named `isSolvable()` that returns true if $ad - bc$ is not 0.
- Methods `getX()` and `getY()` that return the solution for the equation.

Draw the UML diagram for the class and then implement the class. Write a test program that prompts the user to enter `a`, `b`, `c`, `d`, `e`, and `f` and displays the result. If $ad - bc$ is 0, report that "The equation has no solution." See Programming Exercise 3.3 for sample runs.

****9.12** (*Geometry: intersecting point*) Suppose two line segments intersect. The two endpoints for the first line segment are (`x1`, `y1`) and (`x2`, `y2`) and for the second line segment are (`x3`, `y3`) and (`x4`, `y4`). Write a program that prompts the user to enter these four endpoints and displays the intersecting point. As discussed in Programming Exercise 3.25, the intersecting point can be found by solving a linear equation. Use the `LinearEquation` class in Programming Exercise 9.11 to solve this equation. See Programming Exercise 3.25 for sample runs.