

Documentation for Algorithms Project

Team 7

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Code of the Following Algorithms & Its Analysis

a. Allocation Strategies (Heuristics)

i. Worst-fit

- Using Linear Search :

```
#Overall complexity for the function is  $O(N*M) + O(M) = O(N*M)$ 
def WorstFit_LinearSearch(files, folder_size):
    folders=[]
    outputlist=[]
    #Overall complexity for the outer loop is  $N*M$  so it is  $O(N*M)$ 
    for fileName, fileDuration in files.items():
        if len(folders)==0:
            folders.append([folder_size-fileDuration, [(fileName, fileDuration)]])
        else:
            worst_fit_index=-1
            largest_remaining_size=-1
            #Overall complexity for the inner loop is  $M*1$  so it is  $O(M)$ 
            for i in range(len(folders)):
                folder = folders[i]
                if folder[0] >= fileDuration and folder[0] > largest_remaining_size:
                    worst_fit_index = i
                    largest_remaining_size = folder[0]
            if worst_fit_index==-1:
                folders.append([folder_size-fileDuration, [(fileName, fileDuration)]])
            else:
                folders[worst_fit_index][0]-=fileDuration
                folders[worst_fit_index][1].append((fileName, fileDuration))
        for folder in folders:
            outputlist.append(folder[1])
    return outputlist
```

- Using Priority Queue:

```
#Overall complexity of the function =  $O(N \log M) + O(M \log M) = O(N \log M)$  -->Because  $N \log M$  is much larger relative to  $M$ 
def WorstFit_PriorityQueue(files, folder_size):
    folders=[]
    outputlist=[]
    #Overall complexity for this loop =  $N * 3 \log M = O(N \log M)$ 
    for fileName, fileDuration in files.items():
        if len(folders)==0:
            heapq.heappush(folders, [-folder_size + fileDuration, [(fileName, fileDuration)]])
        else:
            folder=folders[0]
            largest_remaining_size=-folder[0]
            if largest_remaining_size >= fileDuration:
                heapq.heappop(folders)
                folder[1].append((fileName, fileDuration))
                heapq.heappush(folders, [-largest_remaining_size + fileDuration, folder[1]])
```

```

        else:
            heapq.heappush(folders, [-folder_size + fileDuration, [(fileName, fileDuration)]] # O(log M): Add new folder
#Overall complexity for this loop = M * log M = O(M*log M)
    while folders:
        folder=heapq.heappop(folders) # O(M): Loop through all folders
        outputlist.append(folder[1]) # O(log M): Remove folder with the largest space
        # O(1): Add folder content to output list

    return outputlist # O(1): Return the final output list

```

ii. Worst-fit decreasing

- Using Linear Search:

```

#Overall complexity for this function = O(max(NlogN , N*M)) + O(M) which we can ignore because it is very small = O(max(NlogN , N*M))
def WorstFit_LinearSearch_Decreasing(files, folder_size): # O(1): Function definition
    folders=[] # O(1): Initialize an empty list for folders
    outputlist=[] # O(1): Initialize an empty list for output
    sorted_files=filehandler.sortduration(files) # O(N log N): Sort files in descending order by duration where N = number of audio files
#Overall complexity for this outer loop = N * M = O(N*M)
    for fileName, fileDuration in sorted_files.items(): # O(N): Loop through sorted files
        if len(folders)==0: # O(1): Check if folders list is empty
            folders.append([folder_size-fileDuration, [(fileName, fileDuration)]] # O(1): Add new folder
        else:
            worst_fit_index=-1 # O(1): Initialize worst fit index
            largest_remaining_size=-1 # O(1): Track largest remaining space
            #Overall complexity for this inner loop = O(M)
            for i in range(len(folders)): # O(M): Iterate through all folders
                folder = folders[i] # O(1): Access folder
                if folder[0] >= fileDuration and folder[0] > largest_remaining_size: # O(1): Check space conditions
                    worst_fit_index= i # O(1): Update worst fit index
                    largest_remaining_size = folder[0] # O(1): Update largest remaining space

            if worst_fit_index==-1: # O(1): If no folder fits the file
                folders.append([folder_size-fileDuration, [(fileName, fileDuration)]] # O(1): Add new folder
            else:
                folders[worst_fit_index][0]-=fileDuration # O(1): Reduce folder space
                folders[worst_fit_index][1].append((fileName, fileDuration)) # O(1): Add file to folder
#Overall complexity for this loop = O(M)
    for folder in folders: # O(M): Loop through all folders
        outputlist.append(folder[1]) # O(1): Append folder content to output

    return outputlist # O(1): Return the final output list

```

- Using Priority queue:

```

#Overall complexity of this function = O(N log M) + O(M log M) + O(N log N) = O(N log N) because it is much greater relatively
def WorstFit_PriorityQueue_Decreasing(files, folder_size): # O(1): Function definition
    folders=[] # O(1): Initialize an empty priority queue
    outputlist=[] # O(1): Initialize an empty list for output
    sorted_files=sortduration(files) # O(N log N): Sort files by duration where N = number of audio files
#Overall complexity of this loop = N * 4 log M = O(N log M)
    for fileName, fileDuration in sorted_files.items(): # O(N): Iterate through sorted files
        if len(folders)==0: # O(1): Check if priority queue is empty
            heapq.heappush(folders, [-folder_size + fileDuration, [(fileName, fileDuration)]] # O(log M): Add folder
        else:
            folder=folders[0] # O(1): Access folder with largest space
            largest_remaining_size=-folder[0] # O(1): Convert negative size back to positive
            if largest_remaining_size >= fileDuration: # O(1): Check folder capacity
                heapq.heappop(folders) # O(log M): Remove folder
                folder[1].append((fileName, fileDuration)) # O(1): Add file
                heapq.heappush(folders, [-largest_remaining_size + fileDuration, folder[1]]) # O(log M): Update folder
            else:
                heapq.heappush(folders, [-folder_size + fileDuration, [(fileName, fileDuration)]] # O(log M): Add new folder
#Overall complexity = O(M log M)
    while folders: # O(M) loop all folders
        folder=heapq.heappop(folders) # O(log M): Remove folder
        outputlist.append(folder[1]) # O(1): Add folder content

    return outputlist # O(1): Return final output

```

iii. Sort Function & First-Fit decreasing

- Sort-Function:

```
def sortduration(audio):
    # Sorting the items of the dictionary by their values in descending order using Timsort
    sorted_items = sorted(audio.items(), key=lambda item: item[1], reverse=True)
    # O(N log N), where N is the number of items in the `audio` dictionary.
    # - `audio.items()` creates a view of the dictionary items → O(N).
    # - `sorted()` sorts the items using Timsort → O(N log N).
    # - The lambda function extracts the value (`item[1]`) for sorting → O(1) per call, called N times.

    # Converting the sorted list of tuples back into a dictionary
    sorted_Aura = dict(sorted_items)
    # O(N), where N is the number of items in the list `sorted_items`.
    # - `dict()` iterates over the list and constructs a new dictionary.

    return sorted_Aura # O(1), returning the sorted dictionary.
```

- **First-Fit decreasing :**

```
def FirstFit(tracks, DDPF):
    # Sorting the tracks by duration in descending order using Timsort
    sortedtracks = filehandler.sortduration(tracks) # O(N log N), Timsort complexity for sor

    Folders = [] # O(1),
    FoldersSize = [] # O(1),

    for key, value in sortedtracks.items(): # O(N), iterating over a
        if len(Folders) == 0: # O(1),
            Folders.append([(key, value)]) # O(1),
            FoldersSize.append(value) # O(1),
        else:
            Found = False # O(1),
            for i in range(len(Folders)): # O(M), iterating over t
                if value <= (DDPF - FoldersSize[i]): # O(1),
                    Folders[i].append((key, value)) # O(1),
                    FoldersSize[i] += value # O(1),
                    Found = True # O(1),
                    break # O(1),
            if not Found: # O(1),
                Folders.append([(key, value)]) # O(1),
                FoldersSize.append(value) # O(1),

    return Folders # O(1),
# Overall Time Complexity: O(N log N + N × M)
# - Sorting: O(N log N)
# - Outer loop over tracks: O(N)
# - Inner loop over folders: O(M)
# - Combined looping complexity: O(N × M)
```

iv. Best-Fit

- **Best-Fit Greedy:**

```
#_Code Analysis_____
import heapq # O(1)
def best_fit(file_sizes, folder_capacity): # O(1)
    # Sort files by size in descending order
    sorted_files = sorted(file_sizes.items(), key=lambda item: item[1], reverse=True)# item()-> O(1) ,sorted()->O(nlogn)"t
    # total complexity->O(nlogn)

    folders = [] # O(1)

    for file_name, size in sorted_files: # for loop indexing ->O(n) , the tot
al complexity -> O(n * (m + k)) ,Simplification: O(n * m) .
        # Skip if file is larger than folder capacity
        if size > folder_capacity: #O(1)
            raise ValueError(f"File '{file_name}' with size {size} exceeds folder capacity {folder_capacity}.") # raise Va
lueError() ->O(1)
        # Find the best folder for the current file
        best_fit_index = -1 #O(1)
        min_remaining_space = float('inf') #O(1)

        # Check for the folder with the smallest remaining space that can fit the file
        for i in range(len(folders)): # O(m) "where m is the number of folde
rs"
            remaining_capacity, files = folders[i] #O(1)
            if remaining_capacity >= size and (remaining_capacity - size) < min_remaining_space:#O(1)
                best_fit_index = i #O(1)
```

```

        min_remaining_space = remaining_capacity - size #O(1)

        # If no suitable folder was found, create a new one
        if best_fit_index == -1: #O(1) ,total if complexity -> O(k)
            # Create a new folder with the current file
            heapq.heappush(folders, (folder_capacity - size, [(file_name, size)])) # O(log k) "where k is the number of f
olders in heap (having remaining capacity)".
        else:
            # Update the folder with the new file
            remaining_capacity, files = folders[best_fit_index] #O(1)
            files.append((file_name, size)) #append() -> O(1)
            folders[best_fit_index] = (remaining_capacity - size, files) #O(1)
            heapq.heapify(folders) #O(k) "where k is the number of folders
in the heap (having remaining capacity)"
            #Rebuilding the heap to restore the heap property after modifying the folder list.

    return [folders for _, folders in folders] #o(m)

#_time complexity _____
#total code complexity is O(n*m+nlogn)
#worst case O(n^2) as m is equal to n
#best case o(nlogn) where m is equal 1

#_space complexity_____
# - The sorted_files list requires O(n) space where n is the number of files.
# - The folders list holds tuples of (remaining_capacity, files) for each folder.
# - In the worst case, this list can hold n folders, so the space complexity is O(n).
# - The heap used for managing the folders requires O(n) space because there could be up to n folders in the worst case.
# - Therefore, the total space complexity is O(n), where n is the number of files.

```

• Best-Fit Dynamic Programming :

```

def best_fit_dp(file_sizes, folder_capacity): # Total time complexity: O(n * C + n ^2)

    file_names = list(file_sizes.keys()) # O(n) - Extracting file names
    file_sizes_list = list(file_sizes.values()) # O(n) - Extracting file sizes
    n = len(file_sizes_list) # O(1) - Calculating number of files

    dp = [[False] * (folder_capacity + 1) for _ in range(n + 1)]
    # O(n * C) - Initializing the DP table (2D list of size n+1 by C+1)

    dp[0][0] = True # O(1) - Base case assignment
    # Build the DP table
    for i in range(1, n + 1): # O(n) - Looping through files
        for cap in range(folder_capacity + 1): # O(C) - Looping through capacities
            dp[i][cap] = dp[i - 1][cap] # O(1) - Excluding the current file
            if cap >= file_sizes_list[i - 1]: # O(1) - Checking if the file can fit
                if dp[i - 1][cap - file_sizes_list[i - 1]]: # O(1) - Checking previous DP value
                    dp[i][cap] = True # O(1) - Marking this capacity as achievable

    # Backtracking
    folders = [] # O(1) - Initialize list for storing folders
    remaining_files = set(range(n)) # O(1) - Initialize set of all files

    while remaining_files: # O(n) - Looping until all files are allocated
        cap = folder_capacity # O(1) - Reset folder capacity
        folder = [] # O(1) - List to store current folder's files
        current_file_indices = set() # O(1) - Set to track current folder's files

        for i in range(n, 0, -1): # O(n) - Looping over files in reverse order
            if (i - 1) in remaining_files and dp[i][cap] and dp[i - 1][cap - file_sizes_list[i - 1]] and cap >= file_sizes_l
                # O(1) - Check if file fits and is available for allocation
                folder.append((file_names[i - 1], file_sizes_list[i - 1])) # O(1) - Add file to folder
                cap -= file_sizes_list[i - 1] # O(1) - Update folder capacity
                current_file_indices.add(i - 1) # O(1) - Mark file as allocated

        # Ensure progress is made
        if not folder: # O(1) - Check if folder is empty (no files were allocated)
            print("Warning: No more files can be allocated to a folder. Exiting.")
            break # O(1) - Exit if no files can be allocated

        folders.append(folder) # O(1) - Add folder to result

    # Remove the allocated files from the remaining files set

```

```

        remaining_files -= current_file_indices # O(n) - Removing allocated files

    return folders # O(1) - Return the list of allocated folders

# Time complexity:
# Backtracking : O(n ^2)
# DP complexity: O(n * C)

# Space complexity:
# - DP table: O(n * C)
# - Folders and file sets: O(n)
# Total space complexity: O(n * C)

```

- **Best-Fit Linear Search:**

```

import FileHandling
import os

def look_ahead(folders, sound, folder_capacity): #complexity: O(k)
    bestFolder = None #complexity:O(1)
    min_remaining_space=folder_capacity #complexity:O(1)

    for i, (capacity, _) in enumerate(folders): #complexity:O(k) , where k is the number of folders
        remaining_space=folder_capacity-capacity #complexity:O(1)

        if remaining_space>=sound[1] and remaining_space<min_remaining_space: #complexity:O(1)
            bestFolder= i #complexity:O(1)
            min_remaining_space=remaining_space #complexity:O(1)

    return bestFolder #complexity:O(1)

def pack(sounds: dict[str, int], folder_capacity: int) -> list[list[tuple[str, int]]]:
    folders = [] # Complexity: O(1)
    sorted_items = sorted(sounds.items(), key=lambda item: item[1], reverse=True) # Complexity: O(nlogn)

    for sound in sorted_items: # Complexity: O(n*k) where n is the total number of sounds
        placed = False #comlexity:O(1)
        bestFolder=look_ahead(folders,sound,folder_capacity) #complexity:O(k)

        if bestFolder is not None: #complexity:O(1)
            capacity, content = folders[bestFolder] #complexity:O(1)
            folders[bestFolder] = (capacity + sound[1], content + [sound]) #complexity:O(1)
            placed = True #complexity:O(1)

        if not placed: #complexity:O(1)
            folders.append((sound[1], [sound])) #complexity:O(1)

    # Convert to list of lists of tuples format
    return [folder[1] for folder in folders]#complexity: O(k)

#total complexity: O(nlogn) + O(n*k) + O(k) = O(nlogn)+ O(n*k)

# Test case execution logic
if __name__ == "__main__":
    folder_capacity = 100
    packed_folders = None

    # Determine which test case to execute
    if FileHandling.workingOn_testcase == 1:
        source = r"./Sample Tests/Sample 1/INPUT/Audios"
        tracks_dict = FileHandling.t1 # Audio metadata
    elif FileHandling.workingOn_testcase == 2:
        source = r"./Sample Tests/Sample 2/INPUT/Audios"
        tracks_dict = FileHandling.t2
    elif FileHandling.workingOn_testcase == 3:
        source = r"./Sample Tests/Sample 3/INPUT/Audios"
        tracks_dict = FileHandling.t3
    else:
        source = r"./Complete Tests/Complete1/Audios"
        tracks_dict=FileHandling.t4

    try:
        audio_files = os.listdir(source)

```

```

except FileNotFoundError:
    print(f"Directory not found: {source}")
    exit(1)

# Process the audio metadata
if tracks_dict:
    packed_folders = pack(tracks_dict, folder_capacity)

```

v. Next-Fit:

- Next-Fit Divide and conquer:

```

import heapq

def next_fit_D_C(file_sizes, folder_capacity): # Main function to allocate files into folders.
    # Convert file_sizes dictionary into a list of tuples (filename, size)
    file_list = list(file_sizes.items()) # Converts file_sizes into a list of tuples for easier processing. O(n)

    def allocate_files(file_list): # Recursive function to allocate files using divide-and-conquer.
        # Base case: if there's only one file, allocate it in its own folder.
        if len(file_list) == 1:
            return [[file_list[0]]] # Single folder containing the file. O(1)

        # Divide: Split the file list into two halves.
        mid = len(file_list) // 2
        left_files = file_list[:mid] # Left half of the file list. O(n)
        right_files = file_list[mid:] # Right half of the file list. O(n)

        # Conquer: Recursively allocate files in the left and right halves.
        left_folders = allocate_files(left_files) # Recursive call for left half. O(log n)
        right_folders = allocate_files(right_files) # Recursive call for right half. O(log n)
        # T(N)=2T(N/2)+O(mlogm)

        # Combine: Merge the allocated folders from both halves.
        return merge_folders(left_folders, right_folders, folder_capacity) # Combine results. O(m log m)

    def merge_folders(left_folders, right_folders, folder_capacity): # Function to merge folders efficiently.
        folders = left_folders # Start with the folders from the left half. O(1)

        # Create a min-heap for folder remaining capacities.
        folders_heap = [(folder_capacity - sum(size for _, size in folder), i) for i, folder in enumerate(folders)]
        # Heap stores (remaining capacity, folder index) for each folder. O(n)

        heapq.heapify(folders_heap) # Convert list to a min-heap. O(n)

        # Iterate through the folders in the right half.
        for folder in right_folders: # O(m), where m is the total number of files in right_folders.
            for file_name, size in folder: # Iterate through files in the current folder. O(k), where k is the number of files
                placed = False # Track whether the file is placed in an existing folder.

                while folders_heap: # Check existing folders for available capacity. O(log n) per operation.
                    remaining_capacity, folder_index = heapq.heappop(folders_heap) # Pop folder with the most available space
                    if size <= remaining_capacity: # Check if the file fits in the folder. O(1)
                        folders[folder_index].append((file_name, size)) # Add file to folder. O(1)
                        remaining_capacity -= size # Update remaining capacity. O(1)
                        heapq.heappush(folders_heap, (remaining_capacity, folder_index)) # Push updated folder back into the heap
                        placed = True # Mark the file as placed. O(1)
                        break # Exit the loop once the file is placed. O(1)

                if not placed: # If the file couldn't be placed in any existing folder.
                    new_folder = [(file_name, size)] # Create a new folder for the file. O(1)
                    folders.append(new_folder) # Add the new folder to the list of folders. O(1)
                    heapq.heappush(folders_heap, (folder_capacity - size, len(folders) - 1)) # Push new folder into the heap

        return folders # Return the merged list of folders. O(1)

    allocated_folders = allocate_files(file_list) # Start the recursive allocation. O(n log n)
    #Output(source, "..\Karim\k", allocated_folders, "nextfit D&C")
    return allocated_folders # Return the final allocation of folders. O(1)

# _____ Time Complexity _____ #
# 1. The `allocate_files` function has a time complexity of O(n log n) because it recursively divides the file list and merges the results.
# 2. The `merge_folders` function involves iterating through the right folder list (O(m)) and inserting/removing items from the heap (O(log m)).
# 3. Thus, the total time complexity of the algorithm is O(n log n + m log m), where n is the number of files and m is the number of folders.

```

```
# _____Worst-Case Complexity_____#
# - The worst-case time complexity occurs when:
#   1. Every file requires its own folder because it doesn't fit into any existing folder.
#   2. The merging step involves checking all existing folders for each file, resulting in the maximum number of heap operations.
# - In this case, both the recursive allocation and the merging process each take  $O(n \log n)$  time, leading to a worst-case time complexity of  $O(n \log n)$ .

# _____Space Complexity_____#
# - Space used by the `file_list`:  $O(n)$  (for storing the file sizes).
# - Space used by the recursive call stack:  $O(\log n)$  (due to the divide-and-conquer recursion).
# - Space used by the `folders` list:  $O(n)$  (for storing the allocated folders).
# - Space used by the min-heap `folders_heap`:  $O(n)$  (for managing the folder capacities).
# Total space complexity:  $O(n)$ 
```

- **Next-Fit Greedy:**

```
def next_fit_greedy(file_sizes, folder_capacity):
    # Sort files in descending order to place larger files first
    sorted_files = sorted(file_sizes.items(), key=lambda x: x[1], reverse=True) #  $O(n \log n)$ 
    # Explanation: Sorting the file sizes, where n is the number of files.

    # List to store the folders (represented as a list of tuples (file_name, size))
    folders = [] #  $O(1)$ 

    # Min-heap to track the remaining capacity of folders
    heap = [] #  $O(1)$ 

    heapq.heapify(heap)

    for file_name, size in sorted_files: #  $O(n)$ 

        if heap: #  $O(1)$ 

            # Pop the folder with the largest remaining capacity
            remaining_capacity, folder_index = heapq.heappop(heap) #  $O(\log k)$ 

            # If the file fits in the folder
            if remaining_capacity >= size: #  $O(1)$ 

                # Add file to the folder
                folders[folder_index].append((file_name, size)) #  $O(1)$ 

                remaining_capacity -= size #  $O(1)$ 
                # Update the remaining capacity

                # Push the updated folder back into the heap
                heapq.heappush(heap, (remaining_capacity, folder_index)) #  $O(\log k)$ 

            else:
                # File does not fit in any existing folder, create a new folder
                new_folder_index = len(folders) #  $O(1)$ 

                folders.append([(file_name, size)]) #  $O(1)$ 

                # Push the new folder's remaining capacity into the heap
                heapq.heappush(heap, (folder_capacity - size, new_folder_index)) #  $O(\log k)$ 

        else: #  $O(1)$ 
            # No folders yet, create the first folder
            new_folder_index = len(folders) #  $O(1)$ 

            folders.append([(file_name, size)]) #  $O(1)$ 

            # Push the new folder's remaining capacity into the heap
            heapq.heappush(heap, (folder_capacity - size, new_folder_index)) #  $O(\log k)$ 

    return folders #  $O(1)$ 
```

```

# _____ Time Complexity _____ #
# 1. Sorting files:  $O(n \log n)$ 
# 2. For each file (n iterations):
#   - Popping and pushing from the heap:  $O(\log k)$ 
# Total:  $O(n \log n + n \log k)$ , simplified as  $O(n \log n + n \log k)$ .

# _____ Worst-Case Complexity _____ #
# The worst-case time complexity happens when:
# 1. Each file is placed in its own folder because no file fits into any existing folder.
# 2. This leads to the following operations:
#   - Sorting the files:  $O(n \log n)$ 
#   - For each file (n iterations), we are performing heap operations (popping and pushing):
#     - Popping and pushing from the heap:  $O(\log n)$  since the maximum number of folders will be n.
# Total worst-case time complexity:  $O(n \log n + n \log n) = O(n \log n)$ .

# _____ Space Complexity _____ #
# 1. Storing folders:  $O(m)$ , where m is the total number of folders.
# 2. Storing files:  $O(n)$ , where n is the number of files.
# 3. Heap storage:  $O(k)$ , where k is the maximum number of folders in the heap at any time.
# Total:  $O(n + m + k)$ .

```

vi. Harmonic Partitioning:

```

import FileHandling
import os

def look_ahead(folders, sound, folder_capacity): #complexity:  $O(k)$ 
    bestFolder = None #complexity: $O(1)$ 
    min_remaining_space=folder_capacity #complexity: $O(1)$ 

    for i, (capacity, _) in enumerate(folders): #complexity: $O(k)$  , where k is the number of folders
        remaining_space=folder_capacity-capacity #complexity: $O(1)$ 

        if remaining_space>=sound[1] and remaining_space<min_remaining_space: #complexity: $O(1)$ 
            bestFolder= i #complexity: $O(1)$ 
            min_remaining_space=remaining_space #complexity: $O(1)$ 

    return bestFolder #complexity: $O(1)$ 

def pack(sounds: dict[str, int], folder_capacity: int) -> list[list[tuple[str, int]]]:
    folders = [] # Complexity:  $O(1)$ 
    sorted_items = sorted(sounds.items(), key=lambda item: item[1], reverse=True) # Complexity:  $O(n \log n)$ 

    for sound in sorted_items: # Complexity:  $O(n*k)$  where n is the total number of sounds
        placed = False #complexity: $O(1)$ 
        bestFolder=look_ahead(folders,sound,folder_capacity) #complexity: $O(k)$ 

        if bestFolder is not None: #complexity: $O(1)$ 
            capacity, content = folders[bestFolder] #complexity: $O(1)$ 
            folders[bestFolder] = (capacity + sound[1], content + [sound]) #complexity: $O(1)$ 
            placed = True #complexity: $O(1)$ 

        if not placed: #complexity: $O(1)$ 
            folders.append((sound[1], [sound])) #complexity: $O(1)$ 

    # Convert to list of lists of tuples format
    return [folder[1] for folder in folders]#complexity:  $O(k)$ 

#total complexity:  $O(n \log n) + O(n*k) + O(k) = O(n \log n) + O(n*k)$ 

# Test case execution logic
if __name__ == "__main__":
    folder_capacity = 100
    packed_folders = None

    # Determine which test case to execute
    if FileHandling.workingOn_testcase == 1:
        source = r"./Sample Tests/Sample 1/INPUT/Audios"
        tracks_dict = FileHandling.t1 # Audio metadata
    elif FileHandling.workingOn_testcase == 2:
        source = r"./Sample Tests/Sample 2/INPUT/Audios"
        tracks_dict = FileHandling.t2

```



```

elif FileHandling.workingOn_testcase == 3:
    source = r"./Sample Tests/Sample 3/INPUT/Audios"
    tracks_dict = FileHandling.t3
else:
    source = r"./Complete Tests/Complete1/Audios"
    tracks_dict=FileHandling.t4

try:
    audio_files = os.listdir(source)
except FileNotFoundError:
    print(f"Directory not found: {source}")
    exit(1)

# Process the audio metadata
if tracks_dict:
    packed_folders = pack(tracks_dict, folder_capacity)

```

vii. Fractional Packing:

```

import os
import concurrent.futures
from FileHandling import *

filehandler = FileHandlingClass()

def process_sound(name, duration_to_process): #complexity: O(1)
    """Mock process a sound file and print what would be done."""

def fractional_packing(tracks, total_duration_available): #complexity: O(nlogn) + O(n) + O(k*n)

    sortedtracks = sorted(tracks.items(), key=lambda item: item[1], reverse=True) #complexity: O(nlogn)
    # List to store packed folders
    folders = [] #complexity: O(1)
    # Tracks in the current folder
    current_folder_tracks = [] #complexity:O(1)
    current_folder_duration = 0 #complexity:O(1)

    for sound_name, duration in sortedtracks: #complexity: O(n)
        if current_folder_duration + duration <= total_duration_available: #complexity: O(1)
            current_folder_tracks.append((sound_name, duration)) #complexity: O(1)
            current_folder_duration += duration #complexity: O(1)
        else:
            # calculates the fraction of the track that can fit into the remaining folder capacity.
            fraction_to_fit = (total_duration_available - current_folder_duration) / duration #complexity: O(1)
            fraction_duration = duration * fraction_to_fit #complexity: O(1)
            current_folder_tracks.append((sound_name, fraction_duration)) #complexity: O(1)

            # Store the remaining part in a new folder
            remaining_duration = duration - fraction_duration #complexity: O(1)
            folders.append(current_folder_tracks) #complexity: O(1)
            current_folder_tracks = [(sound_name, remaining_duration)] #complexity: O(1) # Start new folder
            current_folder_duration = remaining_duration #complexity: O(1) # Reset folder duration

    # Add the last folder if it has any tracks
    if current_folder_tracks: #complexity: O(1)
        folders.append(current_folder_tracks) #complexity: O(1)

    # Calculate fractions for each folder
    split_fractions = [] #complexity: O(n)
    for folder_tracks in folders: #complexity: O(k*n) , k is the number of iterations
        for track in folder_tracks: #complexity: O(n)
            fraction = track[1] / total_duration_available #complexity: O(1)
            split_fractions.append((track[0], fraction)) #complexity: O(1)

    # Initialize ThreadPoolExecutor with the number of CPU cores, with: ensures proper cleanup of resources after block is e
    with concurrent.futures.ThreadPoolExecutor(max_workers=os.cpu_count()) as executor: #complexity: O(n)
        #list of objects representing the execution of async tasks
        futures = [
            executor.submit(
                process_sound,
                entry[0],
                #duration to process
                entry[1] * total_duration_available,
            )
            #submit the task for each entry
            for entry in split_fractions
        ] #complexity: O(n)

```

```

        for future in concurrent.futures.as_completed(futures): #complexity:  $O(n)$ 
            future.result() #complexity:  $O(1)$ 

    return folders #complexity:  $O(1)$ 

#total complexity:  $o(n \log n) + o(k*n) + o(n) = o(n \log n) + o(k*n)$ 
#worst case: number of files= number of folders, complexity=  $o(n \log n) + o(n^2) = o(n^2)$ 

```

b. Folder Filling Algorithm

```

def folder_filling(files, folder_capacity):
    # dp function returns two things:
    # 1) Maximum value obtained by including or not including the current file
    # 2) List of files used to achieve this maximum value

    def dp(names, index, remaining_duration, memo):
        # Base case
        if index == len(names) or remaining_duration == 0:
            (1) ->  $O(1)$ 
            return 0, []
        ->  $O(1)$ 

        # Check if result is already computed and stored in memo
        if (index, remaining_duration) in memo:
            ->  $O(1)$ 
            return memo[(index, remaining_duration)]
        ->  $O(1)$ 

        file_name = names[index]
        ->  $O(1)$ 
        file_duration = files[file_name]
        ->  $O(1)$ 

        # leave_value is the maximum value obtained by not including this file
        # leave_files is the list of files used to achieve leave_value
        leave_value, leave_files = dp(names, index + 1, remaining_duration, memo)
        take_value, taken_files = 0, []

        if file_duration <= remaining_duration:
            # take_value is the maximum value obtained by including this file
            # take_files is the list of files used to achieve take_value
            take_value, taken_files = dp(names, index + 1, remaining_duration - file_duration, memo)
            take_value += file_duration
            taken_files = [(file_name, file_duration)] + taken_files

        # Choose the better option: including or not including the current file
        if leave_value > take_value:
            memo[(index, remaining_duration)] = (leave_value, leave_files)
        else:
            memo[(index, remaining_duration)] = (take_value, taken_files)
            #names.remove(file_name)
        return memo[(index, remaining_duration)]

    # Main logic of folder filling function
    folders = []
    files_names = list(files.keys())

    while files_names:
        memo = {}
        # Get the best subset of files for the current folder capacity
        _, files_in_a_folder = dp(files_names, 0, folder_capacity, memo)
        if not files_in_a_folder:
            break
        folders.append(files_in_a_folder)

        # Remove the files that have been added to the current folder
        for file_name, _ in files_in_a_folder:
            files_names.remove(file_name)

    lexity ->  $O(n*k)$ 
    return folders

    #Assume that  $k = 1$ , this is the worst case scenario that at each iteration we only remove 1 file so the  $n$  is reduced slowly
    #if  $k > 1$  this means that  $n$  is reduced faster. So, when  $k = 1$  the time complexity is upper bounded by  $O(n)$ 

    # Total Time complexity of while loop :  $(O(n*D) + O(n))*O(n) = O(n^2 * D) + O(n^2) = O(n^2 * D)$ 

```

```
# Time complexity of dp function without memoization:  $T(n) = 2T(n-1) + O(1) \rightarrow O(2^n)$ 
# Time complexity of dp function with memoization:  $O(n \cdot D)$ 
```

c. File Handling

```
import os
import shutil
#from traceback import print_tb

class FileHandlingClass:
    _instance = None

    def __new__(cls, *args, **kwargs):
        if not cls._instance:
            cls._instance = super(FileHandlingClass, cls).__new__(cls, *args, **kwargs)
        return cls._instance

    def __init__(self):
        if not hasattr(self, "initialized"):
            self.initialized = True

    @staticmethod
    def hms_to_seconds(time_str):
        hours, minutes, seconds = time_str.split(':')
        return int(hours) * 3600 + int(minutes) * 60 + int(seconds)

    @staticmethod
    def seconds_to_hms(seconds):
        hours = seconds // 3600
        minutes = (seconds % 3600) // 60
        secs = seconds % 60
        return f"{hours:02}:{minutes:02}:{secs:02}"

    @staticmethod
    def readfile(folderdir):
        file_data = {}
        target_path = os.path.abspath(folderdir)
        with open(target_path, 'r') as file:
            num_entries = int(file.readline().strip())

            for i in range(num_entries):
                line = file.readline().strip()

                filename, time_str = line.split()

                key = filename

                value = FileHandlingClass.hms_to_seconds(time_str)

                file_data[key] = value

            return file_data

    @staticmethod
    def sortduration(audio):
        # Sorting the items of the dictionary by their values in descending order using Timsort
        sorted_items = sorted(audio.items(), key=lambda item: item[1], reverse=True)
        #  $O(N \log N)$ , where  $N$  is the number of items in the `audio` dictionary.
        # - `audio.items()` creates a view of the dictionary items  $\rightarrow O(N)$ .
        # - `sorted()` sorts the items using Timsort  $\rightarrow O(N \log N)$ .
        # - The lambda function extracts the value (`item[1]`) for sorting  $\rightarrow O(1)$  per call, called  $N$  times.

        # Converting the sorted list of tuples back into a dictionary
        sorted_Aura = dict(sorted_items)
        #  $O(N)$ , where  $N$  is the number of items in the list `sorted_items`.
        # - `dict()` iterates over the list and constructs a new dictionary.

        return sorted_Aura #  $O(1)$ , returning the sorted dictionary.

    @staticmethod
    def Output(src, dest, folder, funcname, sample):
        # path
        outputdir = os.path.join(os.path.abspath(dest), rf"OUTPUT\{sample}", funcname)
        os.makedirs(outputdir, exist_ok=True)
```

```

# //////////////////////////////////////
it = 1
# Display
print("Folders Content:")
for i in folder:
    # path
    currentfolder = os.path.join(outputdir, f"F{it}")
    os.makedirs(currentfolder, exist_ok=True)
    # //////////////////////////////////////
    # text file
    with open(os.path.join(outputdir, f"F{it}_METADATA.txt"), "w") as file:
        file.write(f"F{it}\n")
    # //////////////////////////////////////
    timesum = 0
    for j in i:
        sourcefile = os.path.join(os.path.abspath(src), j[0])
        destfile = os.path.join(currentfolder, j[0])
        # txt file
        # convert sec to time format
        time = FileHandlingClass.seconds_to_hms(j[1])
        # Open the file in write mode ('w')
        with open(os.path.join(outputdir, f"F{it}_METADATA.txt"), "a") as file:
            file.write(f"{j[0]} {time}\n")
        timesum += j[1]

    try:
        shutil.copyfile(sourcefile, destfile)
        # print("File copied successfully.")

    # If source and destination are same
    except shutil.SameFileError:
        print("Source and destination represents the same file.")

    # If destination is a directory.
    except IsADirectoryError:
        print("Destination is a directory.")

    # If there is any permission issue
    except PermissionError:
        print("Permission denied.")

    # For other errors
    except:
        print("Error occurred while copying file.")
    # write to text file
    with open(os.path.join(outputdir, f"F{it}_METADATA.txt"), "a") as file:
        file.write(f"{FileHandlingClass.seconds_to_hms(timesum)}\n")
    # //////////////////////////////////////
    with open(os.path.join(outputdir, f"F{it}_METADATA.txt"), "r") as file:
        # Read the file's content
        content = file.read()
        # Print the file's content
        print(content)
    it += 1
print(f"Number of folders: {it-1}")

```

Time Complexity Summary for All Algorithms

Complete Test Case 1 on PC1 :

Algorithm Type	Algorithm Details	Time Complexity	Number Of Folders	Time Of Execution
Worst-fit Linear Search	Scans folders to find the worst fit (largest remaining space) or adds a new one.	$O(N * M)$	102	0.9 seconds
Worst-fit Priority Queue	Uses a priority queue to quickly find the folder with the largest remaining space.	$O(N \log M)$	102	0.96 seconds
Worst-fit Decreasing Linear Search	Sorts files by size, then applies the linear search method.	$O(\max(N \log N, N * M))$	100	1.1 seconds
Worst-fit Decreasing Priority Queue	Sorts files by size, then uses a priority queue for efficient allocation.	$O(N \log N)$	100	1.9 seconds
Harmonic Partitioning	Uses categories based on size thresholds	$O(N \log N + N * M)$	100	1.75 seconds
First-fit Linear Search Decreasing	Files sorted then search for First-Fit folder	$O(N \log N + N \times M)$	100	2.02 seconds
Best-fit With Dynamic Programming	guarantees that you will find an optimal solution	$O(n * C + n^2)$	105	1.49 seconds

Algorithm Type	Algorithm Details	Time Complexity	Number Of Folders	Time Of Execution
Best-fit With Priority Queue	Prioritizes best space utilization	$O(n \log n) + O(n * m)$	100	1.7 seconds
Fractional Packing	Handles partial file fitting	$O(n \log n) + O(n * m)$	100	2.09 seconds
Next-fit Divide and Conquer approach	Allocates the files using D&C	$O(n \log n + m \log m)$	104	1.7 seconds
Next-fit Greedy approach	Aims for a globally optimal solution	$O(n * \log n + n * \log k)$	107	1.76 seconds
Look-ahead Packing	Evaluates ahead to optimize packing	$O(n \log n) + O(n * m)$	100	1.47 seconds
Folder Filling Dynamic Programming	Uses memorization to maximize the used space	$O(n^2 \times D)$	100	10.7 seconds

Complete Test case 2 on PC2 :

Algorithm Type	Algorithm Details	Time Complexity	Number Of Folders	Time Of Execution
Worst-fit Linear Search	Scans folders to find the worst fit (largest remaining space) or adds a new one.	$O(N * M)$	1046	8.9 seconds
Worst-fit Priority Queue	Uses a priority queue to quickly find the folder with the largest remaining space.	$O(N \log M)$	997	8.3 seconds
Worst-fit Decreasing Linear Search	Sorts files by size, then applies the linear search method.	$O(\max(N \log N, N * M))$	1046	8.1 seconds
Worst-fit Decreasing Priority Queue	Sorts files by size, then uses a priority queue for efficient allocation.	$O(N \log N)$	997	7.95 seconds
Harmonic Partitioning	Uses categories based on size thresholds	$O(N \log N + N * M)$	997	8.15 seconds
First-fit Linear Search Decreasing	Files sorted then search for First-Fit folder	$O(N \log N + N \times M)$	997	7.2 seconds
Best-fit With Dynamic Programming	guarantees that you will find an optimal solution	$O(n * C + n^2)$	999	9.57 seconds
Best-fit With Priority Queue	Prioritizes best space utilization	$O(n \log n) + O(n * m)$	997	8.6 seconds
Fractional Packing	Handles partial file fitting	$O(n \log n) + O(n * m)$	997	8 seconds
Next-fit Divide and Conquer approach	Allocates the files using D&C	$O(n \log n + m \log m)$	1059	7.95 seconds
Next-fit Greedy approach	Aims for a globally optimal solution	$O(n * \log n + n * \log k)$	1078	8 seconds
Look-ahead Packing	Evaluates ahead to optimize packing	$O(n \log n) + O(n * m)$	997	7.9 seconds
Folder Filling Dynamic Programming	Uses memorization to maximize the used space	$O(n^2 \times D)$	999	2114.6 seconds ≈ 35.2433 minutes

Complete Test case 3 on PC3:

Algorithm Type	Algorithm Details	Time Complexity	Number Of Folders	Time Of Execution
Worst-fit Linear Search	Scans folders to find the worst fit (largest remaining space) or adds a new one.	$O(N * M)$	10348	125.445 seconds
Worst-fit Priority Queue	Uses a priority queue to quickly find the folder with the largest remaining space.	$O(N \log M)$	10348	42.611 seconds
Worst-fit Decreasing Linear Search	Sorts files by size, then applies the linear search method.	$O(\max(N \log N, N * M))$	10012	133.279 seconds
Worst-fit Decreasing Priority Queue	Sorts files by size, then uses a priority queue for efficient allocation.	$O(N \log N)$	10012	42.042 seconds
Harmonic Partitioning	Uses categories based on size thresholds	$O(N \log N + N * M)$	10154	100.934 seconds
First-fit Linear Search Decreasing	Files sorted then search for First-Fit folder	$O(N \log N + N \times M)$	10012	138.452 seconds
Best-fit With Dynamic Programming	guarantees that you will find an optimal solution	$O(n * C + n^2)$	10089	274.944 seconds
Best-fit With Priority Queue	Prioritizes best space utilization	$O(n \log n) + O(n * m)$	10008	514.689 seconds
Fractional Packing	Handles partial file fitting	$O(n \log n) + O(n * m)$	9986	54.905 seconds
Next-fit Divide and Conquer approach	Allocates the files using D&C	$O(n \log n + m \log m)$	10694	60.630 seconds
Next-fit Greedy approach	Aims for a globally optimal solution	$O(n * \log n + n * \log k)$	10799	48.952 seconds
Look-ahead Packing	Evaluates ahead to optimize packing	$O(n \log n) + O(n * m)$	10008	179.278 seconds
Folder Filling Dynamic Programming	Uses memorization to maximize the used space	$O(n^2 \times D)$	—	>2 hours

Explanation of Parameters:

- **N, n**: Number of files.
- **M, m**: Number of folders (different contexts use M or m).
- **k**: Number of folders in heap (with remaining capacity)
- **D**: Total capacity in some unit, relevant in dynamic programming contexts.
- **C**: Folder capacity