

# DSA ASSIGNMENT 5

BT22CSH011

Devashish Athawale

## Problem Statement:

Q1) Build a min heap from array and make sure that heap order property is maintained after every input. The input is checked if it is greater than its parent, if it's not, it is swapped. You can take the sample array as:  $arr = [1, 5, 6, 8, 9, 7, 3]$

Write a generalized program so that user can input any set of values. Your insertion function should take  $O(n)$  time as compared to  $O(n \log n)$  time.

Q2) Write a `delete_max` function to delete the element with the maximum key in a min-max heap. It should take  $O(\log n)$ .

Q3) Write a program to implement Heap sort by building a heap for the given set of elements and then deleting one element at a time. Show the complexity of your code.

# Q1)

```
#include <iostream>
#include <vector>

void adjustHeap(std::vector<int>& data, int size, int index) {
    int smallest = index;
    int left = 2 * index + 1;
    int right = 2 * index + 2;
    if (left < size && data[left] < data[smallest])
    {
        smallest = left;
    }
    if (right < size && data[right] < data[smallest])
    {
        smallest = right;
    }
    if (smallest != index)
    {
        std::swap(data[index], data[smallest]);
        adjustHeap(data, size, smallest);
    }
}

void buildHeap(std::vector<int>& data)
{
    int size = data.size();
    for (int i = size / 2 - 1; i >= 0; i--)
    {
        adjustHeap(data, size, i);
    }
}

void insertValue(std::vector<int>& arr, int data)
{
    arr.push_back(data);
    int i = arr.size() - 1;
    while (i > 0 && arr[i] < arr[(i - 1) / 2])
    {
        std::swap(arr[i], arr[(i - 1) / 2]);
        i = (i - 1) / 2;
    }
}

int main() {
    std::vector<int> data = { 1, 5, 6, 8, 9, 7, 3 };
    buildHeap(data);
    std::cout << "Min Heap: \n";
    std::cout << "Original: ";
    for (int i = 0; i < data.size(); i++)
    {
        std::cout << data[i] << " ";
    }
    std::cout << std::endl;
    int n = 4;
    insertValue(data, n);
    std::cout << "After inserting " << n << ": ";
    for (int i = 0; i < data.size(); i++)
    {
        std::cout << data[i] << " ";
    }
    std::cout << std::endl;
    return 0;
}
```

Output:

```
Microsoft Visual Studio Debu x + v - □ x  
Min Heap:  
Original: 1 5 3 8 9 7 6  
After inserting 4: 1 4 3 5 9 7 6 8
```

## Q2)

```
#include <iostream>
#include <vector>

void heapify(std::vector<int>& arr, int size, int index, bool isMinLevel) {
    int largeOrSmall = index;
    int left = 2 * index + 1;
    int right = 2 * index + 2;
    if (isMinLevel) {
        if (left < size && arr[left] < arr[largeOrSmall]) {
            largeOrSmall = left;
        }
        if (right < size && arr[right] < arr[largeOrSmall]) {
            largeOrSmall = right;
        }
    }
    else {
        if (left < size && arr[left] > arr[largeOrSmall]) {
            largeOrSmall = left;
        }
        if (right < size && arr[right] > arr[largeOrSmall]) {
            largeOrSmall = right;
        }
    }
    if (largeOrSmall != index) {
        std::swap(arr[index], arr[largeOrSmall]);
        heapify(arr, size, largeOrSmall, !isMinLevel);
    }
}

int deleteMaxElement(std::vector<int>& arr)
{
    if (arr.empty())
    {
        std::cout << "Heap is empty!" << std::endl;
        return -1; // Return a sentinel value to indicate an empty heap.
    }
    int maxElement = arr[0];
    int lastIndex = arr.size() - 1;
    std::swap(arr[0], arr[lastIndex]);
    arr.pop_back();
    bool isMinLevel = true;
    heapify(arr, arr.size(), 0, isMinLevel);
    return maxElement;
}

void main()
{
    std::vector<int> arr = { 9, 8, 6, 7, 5, 1, 3 };
    std::cout << "Original Min-Max Heap: ";
    for (int i = 0; i < arr.size(); i++)
    {
        std::cout << arr[i] << " ";
    }
    std::cout << "\n";
    std::cout << "Element Deleted: " << deleteMaxElement(arr) << std::endl;
    std::cout << "Remaining Min-Max Heap: ";
    for (int i = 0; i < arr.size(); i++)
    {
        std::cout << arr[i] << " ";
    }
}
```

Output:

```
Microsoft Visual Studio Debu x + v - □ ×  
Original Min-Max Heap: 9 8 6 7 5 1 3  
Element Deleted: 9  
Remaining Min-Max Heap: 3 8 6 7 5 1
```

# Q3)

```
#include <iostream>
#include <vector>


void heapify(std::vector<int>& arr, int size, int i)
{
    int largest = i;
    int left = 2 * i + 1;
    int right = 2 * i + 2;
    if (left < size && arr[left] > arr[largest])
    {
        largest = left;
    }
    if (right < size && arr[right] > arr[largest])
    {
        largest = right;
    }
    if (largest != i)
    {
        std::swap(arr[i], arr[largest]);
        heapify(arr, size, largest);
    }
}

void buildMaxHeap(std::vector<int>& arr)
{
    for (int i = arr.size() / 2 - 1; i >= 0; i--)
    {
        heapify(arr, arr.size(), i);
    }
}

void heapSort(std::vector<int>& arr)
{
    buildMaxHeap(arr);
    for (int i = arr.size() - 1; i > 0; i--)
    {
        std::swap(arr[0], arr[i]);
        heapify(arr, i, 0);
    }
}

void main()
{
    std::vector<int> arr = { 12, 11, 13, 5, 6, 7 };
    std::cout << "Original array: ";
    for (int i = 0; i < arr.size(); i++)
    {
        std::cout << arr[i] << " ";
    }
    std::cout << std::endl;
    heapSort(arr);
    std::cout << "Sorted array: ";
    for (int i = 0; i < arr.size(); i++)
    {
        std::cout << arr[i] << " ";
    }
    std::cout << std::endl;
}
```

Output:

A screenshot of a Microsoft Visual Studio Debug Console window. The window has a dark theme and a title bar with the text "Microsoft Visual Studio Debug Console". The console displays two lines of text: "Original array: 12 11 13 5 6 7" and "Sorted array: 5 6 7 11 12 13".

```
Microsoft Visual Studio Debug Console  
Original array: 12 11 13 5 6 7  
Sorted array: 5 6 7 11 12 13
```

Time Complexity:  $n \log n$