

**LAPORAN TUGAS KECIL 3**

**IF2211 STRATEGI ALGORITMA**

# **Implementasi 15 Puzzle Solver Menggunakan Algoritma Branch & Bound**



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## 1. Penjelasan Algoritma *Branch and Bound*

Algoritma yang saya lakukan adalah pertama mencari dulu fungsi Kurang(i), apabila fungsi Kurang(i) + posisi ubin kosong = ganjil, maka puzzle *unsolvable*, sedangkan bila genap maka puzzle *solvable*. Bila solvable. Maka akan dibuat sebuah *queue*, dan menginisiasi nilai kedalaman pohon. Lalu memasukkan simpul akar kedalam queue. Melakukan iterasi dari semua kemungkinan gerakan (atas, bawah, kiri, kanan) dari simpul dan hasil gerakannya akan dimasukkan kedalam queue bila pergerakan yang sekarang berbeda dengan pergerakan sebelumnya. Lalu mengambil simpul *queue* yang memiliki cost paling kecil, dan bila simpul tersebut merupakan jawaban akhir maka akan stop, jika tidak, iterasikan lagi semua kemungkinan pergerakan.

## 2. Screen-shot Input-output Program

```
pilih jenis input puzzle:
1. input dari file
2. input random
pilih: 1
Masukkan nama file:
file.txt
Posisi Awal:


|    |    |    |    |
|----|----|----|----|
| 1  | 2  | 3  | 4  |
| 5  | 6  |    | 8  |
| 9  | 10 | 7  | 11 |
| 13 | 14 | 15 | 12 |


Fungsi kurang ( 1 ) = 0
Fungsi kurang ( 2 ) = 0
Fungsi kurang ( 3 ) = 0
Fungsi kurang ( 4 ) = 0
Fungsi kurang ( 5 ) = 0
Fungsi kurang ( 6 ) = 0
Fungsi kurang ( 16 ) = 9
Fungsi kurang ( 8 ) = 1
Fungsi kurang ( 9 ) = 1
Fungsi kurang ( 10 ) = 1
Fungsi kurang ( 7 ) = 0

Langkah 1 :


|    |    |    |    |
|----|----|----|----|
| 1  | 2  | 3  | 4  |
| 5  | 6  | 7  | 8  |
| 9  | 10 |    | 11 |
| 13 | 14 | 15 | 12 |



Langkah 2 :


|    |    |    |    |
|----|----|----|----|
| 1  | 2  | 3  | 4  |
| 5  | 6  | 7  | 8  |
| 9  | 10 | 11 |    |
| 13 | 14 | 15 | 12 |



Langkah 3 :


|    |    |    |    |
|----|----|----|----|
| 1  | 2  | 3  | 4  |
| 5  | 6  | 7  | 8  |
| 9  | 10 | 11 | 12 |
| 13 | 14 | 15 |    |


```

```
pilih jenis input puzzle:
1. input dari file
2. input random
pilih: 1
Masukkan nama file:
file2.txt
Posisi Awal:


|    |    |    |    |
|----|----|----|----|
| 1  | 6  | 2  | 3  |
| 5  | 7  | 4  |    |
| 9  | 10 | 11 | 8  |
| 13 | 14 | 15 | 12 |


Fungsi kurang ( 1 ) = 0
Fungsi kurang ( 6 ) = 4
Fungsi kurang ( 2 ) = 0
Fungsi kurang ( 3 ) = 0
Fungsi kurang ( 5 ) = 1
Fungsi kurang ( 7 ) = 1
Fungsi kurang ( 4 ) = 0
Fungsi kurang ( 16 ) = 8
Fungsi kurang ( 9 ) = 1
Fungsi kurang ( 10 ) = 1
Fungsi kurang ( 11 ) = 1
Fungsi kurang ( 8 ) = 0
Fungsi kurang ( 13 ) = 1
Fungsi kurang ( 14 ) = 1
Fungsi kurang ( 15 ) = 1
Fungsi kurang ( 12 ) = 0
Total Fungsi Kurangi + posisi ubin = 20
Solvahle Puzzle
```

1	2	3	
5	6	7	4
9	10	11	8
13	14	15	12

Langkah 6 :

1	2	3	4
5	6	7	
9	10	11	8
13	14	15	12

Langkah 7 :

1	2	3	4
5	6	7	8
9	10	11	
13	14	15	12

Langkah 8 :

1	2	3	4
5	6	7	8
9	10	11	12
13	14	15	

Waktu yang diperlukan = 0.0010001659393310547 detik
Jumlah simpul yang dihasilkan = 23

```
pilih jenis input puzzle:
1. input dari file
2. input random
pilih: 2


|    |    |    |    |
|----|----|----|----|
| 12 | 9  | 8  | 10 |
| 7  | 14 |    | 15 |
| 3  | 5  | 13 | 6  |
| 11 | 4  | 1  | 2  |


Fungsi kurang ( 12 ) = 11
Fungsi kurang ( 9 ) = 8
Fungsi kurang ( 8 ) = 7
Fungsi kurang ( 10 ) = 7
Fungsi kurang ( 7 ) = 6
Fungsi kurang ( 14 ) = 8
Fungsi kurang ( 16 ) = 9
Fungsi kurang ( 15 ) = 8
Fungsi kurang ( 3 ) = 2
Fungsi kurang ( 5 ) = 3
Fungsi kurang ( 13 ) = 5
Fungsi kurang ( 6 ) = 3
Fungsi kurang ( 11 ) = 3
Fungsi kurang ( 4 ) = 2
Fungsi kurang ( 1 ) = 0
Fungsi kurang ( 2 ) = 0
Total Fungsi Kurangi + posisi ubin = 83
Unsolvable Puzzle
```

```
pilih jenis input puzzle:
1. input dari file
2. input random
pilih: 1
Masukkan nama file:
file2.txt
Posisi Awal:


|   |    |    |    |
|---|----|----|----|
| 1 | 2  | 3  | 4  |
| 6 | 10 | 7  | 8  |
| 5 | 13 | 15 | 11 |
| 9 |    | 14 | 12 |


Fungsi kurang ( 1 ) = 0
Fungsi kurang ( 2 ) = 0
Fungsi kurang ( 3 ) = 0
Fungsi kurang ( 4 ) = 0
Fungsi kurang ( 6 ) = 1
Fungsi kurang ( 10 ) = 4
Fungsi kurang ( 7 ) = 1
Fungsi kurang ( 8 ) = 1
Fungsi kurang ( 5 ) = 0
Fungsi kurang ( 13 ) = 3
Fungsi kurang ( 15 ) = 4
Fungsi kurang ( 11 ) = 1
Fungsi kurang ( 9 ) = 0
Fungsi kurang ( 16 ) = 2
Fungsi kurang ( 14 ) = 1
Fungsi kurang ( 12 ) = 0
Total Fungsi Kurangi + posisi ubin = 18
Solvable Puzzle
```

1 2 3 4

Langkah 8 :

1	2	3	4
5	6	7	8
9	10		11
13	14	15	12

Langkah 9 :

1	2	3	4
5	6	7	8
9	10	11	
13	14	15	12

Langkah 10 :

1	2	3	4
5	6	7	8
9	10	11	12
13	14	15	

Waktu yang diperlukan = 0.0019986629486083984 detik
Jumlah simpul yang dihasilkan = 45
PS D:\KULIAH\SEMESTER 4\Strategi Algoritma\Tugas\Tugas Kecil\Tucil 3>

### 3. Kode Program (Python)

```
def generatePuzzle():
    listRandom = random.sample(range(1, 17), 16)
    puzzle = listToMatrix(listRandom)
    return listRandom, puzzle

def readFile(fileName):
    array = []
    with open(fileName, 'r') as file:
        for line in file:
            line.split(" ")
            strings = parseString(line.split())
            array += strings
    return array

def parseString(strings):
    for i in range(len(strings)):
        strings[i] = int(strings[i])
    return strings

def listToMatrix(array):
    puzzle = [[0 for a in range(4)] for b in range(4)]
    for i in range(4):
        for j in range(4):
            puzzle[i][j] = array[i*4+j]
    return puzzle

# mencari nilai kurang(i) dari satu elemen
def totalKurang(list, a, i, j):
    sum = 0
    for b in range((i*4+j), len(list)):
        if(a > list[b] and list[b] != 0):
            sum += 1
        else:
            sum += 0
    return sum
```

```
import utility

print("pilih jenis input puzzle:")
print("1. input dari file")
print("2. input random")
pilihan = int(input("pilih: "))

if pilihan == 1:
    print("Masukkan nama file: ")
    array = utility.readFile(input())
    puzzle = utility.listToMatrix(array)
    print("Posisi Awal:")
    utility.printPuzzle(puzzle)
    utility.branchBound(puzzle, array)
else:
    array, puzzle = utility.generatePuzzle()
    utility.print_matrix(puzzle)
    utility.branchBound(puzzle, array)
```

```
You, 5 minutes ago | 1 author (You)
import random
import time
target = [[1, 2, 3, 4], [5, 6, 7, 8], [9, 10, 11, 12], [13, 14, 15, 16]]
moveset = ("right", "down", "left", "up")
```

```
You, 2 days ago | 1 author (You)
class PriorityQueue(object):
    def __init__(self):
        self.queue = []

    def __str__(self):
        return '\n'.join([str(i) for i in self.queue])

    def enqueue(self, data):
        self.queue.append(data)

    def dequeue(self):
        index = 0
        for i in range(len(self.queue)):
            if(self.queue[i][0] < self.queue[index][0]):
                index = i
            item = self.queue[index]
            del self.queue[index]
            return item
```

```
You, 2 days ago | 1 author (You)
class Node:
    def __init__(self, data=None):
        self.matrix = data
        self.parent = None
        self.depth = 0
```

```

# mencari posisi ubin kosong pada puzzle
def posisiKosong(puzzle):
    for i in range(4):
        for j in range(4):
            if(puzzle[i][j] == 16):
                if((i+j) % 2 == 0):
                    return 0, i, j
                else:
                    return 1, i, j

# nilai formula kurang(i) + posisi ubin kosong
def kurang(puzzle, array):
    sum = 0
    for i in range(4):
        for j in range(4):
            sum += totalKurang(array, puzzle[i][j], i, j)
    posisikosong, _, _ = posisiKosong(puzzle)
    return (sum + posisikosong)

# mencari nilai cost dari bentuk puzzle terkini
def cost(depth, matrix):
    sum = 0
    for i in range(4):
        for j in range(4):
            if((matrix[i][j] != target[i][j]) and matrix[i][j] != 16):
                sum += 1
    return (depth+sum)

```

```

def moveFiles(puzzle, movement):
    matrixCopy = copyMatrix(puzzle)
    _, x, y = posisiKosong(matrixCopy)
    if(movement == "left" and y != 0):
        y -= 1
    elif(movement == "right" and y != 3):
        y += 1
    elif(movement == "up" and x != 0):
        x -= 1
    elif(movement == "down" and x != 3):
        x += 1
    matrixCopy = swap(matrixCopy, x, y)
    return matrixCopy

```

```

def swap(matrix, row, column):
    _, x, y = posisiKosong(matrix)
    matrix[x][y] = matrix[row][column]
    matrix[row][column] = 16
    return matrix

```

```

def lawanMove(prevMove):
    if(prevMove == "up"):
        return "down"
    elif(prevMove == "down"):
        return "up"
    elif(prevMove == "left"):
        return "right"
    elif(prevMove == "right"):
        return "left"

```

```

def solved(matrix):
    for i in range(4):
        for j in range(4):
            if(matrix[i][j] != target[i][j]):
                return False
    return True

def printPuzzle(matrix):
    print("
|_|_|_|_|
")
    for i in range(4):
        for j in range(4):
            print("| ", end="")
            print(matrix[i][j], end="")
            if(matrix[i][j] < 10):
                print(" ", end="")
            print("
", end="")
        print("
")
    if(i != 3):
        print("
|_|_|_|_|
")
    print("
|_|_|_|_|
")

def solved(matrix, target):
    for i in range(4):
        for j in range(4):
            if(matrix[i][j] != target[i][j]):
                return False
    return True

def copyMatrix(matrix):
    newMatrix = [[0 for a in range(4)] for b in range(4)]
    for i in range(4):
        for j in range(4):
            newMatrix[i][j] = matrix[i][j]
    return newMatrix

```

```

def printStep(node):
    if(node.parent == None):
        return
    printStep(node.parent)
    print("\n")
    print("Langkah "+str(node.depth)+" : ")
    printPuzzle(node.matrix)

def printKurangi(puzzle, array):
    for i in range(4):
        for j in range(4):
            print("Fungsi kurang (", puzzle[i][j], ") = ", totalKurang(array, puzzle[i][j], i, j))
    print("Total Fungsi Kurangi = ", kurangi(puzzle, array))

```

```

def branchBound(puzzle, array):
    if(kurangi(puzzle, array) % 2 == 0):
        timeStart = time.time()
        printKurangi(puzzle, array)
        print("Solvable Puzzle\n")
        Queue = PriorityQueue()
        generatedNode = 0

        simul = Node(puzzle)
        Queue.enqueue((cost(0, simul.matrix), simul, "", 0))

        tempQueue = Queue.dequeue()
        simul = tempQueue[1]
        matrixMove = simul.matrix
        prevMove = ""
        depth = tempQueue[3] + 1
        generatedNode += 1

        while(not solved(matrixMove, target)):
            for mov in moveset:
                if(mov != prevMove):
                    after_move = moveTiles(matrixMove, mov)
                    if(not solved(after_move, matrixMove)):
                        newNode = Node(after_move)
                        newNode.parent = simul
                        newNode.depth = simul.depth + 1
                        generatedNode += 1
                        Queue.enqueue(
                            (cost(depth, newNode.matrix), newNode, mov, depth))

            tempQueue = Queue.dequeue()
            simul = tempQueue[1]
            matrixMove = simul.matrix
            moveNew = tempQueue[2]
            prevMove = lawanMove(moveNew)
            depth = tempQueue[3] + 1
            timeEnd = time.time()
            timeEstimated = timeEnd - timeStart
            printStep(simul)
            print("Waktu yang diperlukan = ", timeEstimated, "detik")
            print("Jumlah simul yang dihasilkan = ", generatedNode)

        else:
            printKurangi(puzzle, array)
            print("Unsolvble Puzzle\n")

```

#### 4. Contoh Instansiasi 5 Buah Persoalan

Solvable:

```
1 2 3 4
5 6 16 8
9 10 7 11
13 14 15 12
```

```
1 · 2 · 3 · 4
6 · 10 · 7 · 8
5 · 13 · 15 · 11
9 · 16 · 14 · 12
```

```
1 6 2 3
5 7 4 16
9 10 11 8
13 14 15 12
```

Unsolvable

```
8 14 16 9
13 6 4 1
11 10 3 15
12 5 2 7
```

```
12 9 8 10
7 14 16 15
3 5 13 6
11 4 1 2
```

Poin	Ya	Tidak
1. Program berhasil dikompilasi	✓	
2. Program berhasil <i>running</i>	✓	
3. Program dapat menerima input dan menuliskan output	✓	
4. Luaran sudah benar untuk semua data uji	✓	
5. Bonus dibuat	✓	

Link Github: <https://github.com/Hambinn/Tucil-3-Stima>