

# Artificial neural networks for forecasting the 24 hours ahead of global solar irradiance

Mathematical Modeling with Applications (M2A19)

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#### **Talk Outlines**



- I. Introduction:
- II. Forecast Methodology:
  - 1. Pre-processing
  - 2. Time series methods
  - 3. A machine learning framework
- III. Results and discussions
- IV. Conclusion

#### I. Introduction: what is global solar irradiance?



Direct Normal Irradiance (DNI)

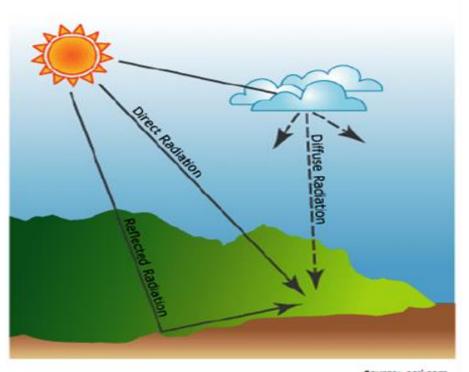


Diffuse Horizontal Irradiance (DHI)



Global Horizontal Irradiance (GHI)





Source: esri.com

Forecasting global horizontal irradiance (GHI) is the first and most essential step in most PV power prediction systems.

#### **I. Introduction**: why forecasting global solar irradiance?



- The contribution of photovoltaic systems power production to the electric power supply is constantly increasing.
- Transmission system operators have to deal with the fluctuating input from PV system energy sources.
- This is a new challenge compared with power production from conventional power plants that can be adjusted to the expected load profiles.
- An efficient use of the fluctuating energy output of PV systems requires reliable forecast information.
- These **predictions** are used by utility companies, transmission system operators, energy service providers, energy traders, and independent power producers in their scheduling, dispatching and regulation of power.
- An efficient forecasting method will help the grid operators to better manage the electrical balance between demand and power generation.

#### I. Introduction: Forecast Methods

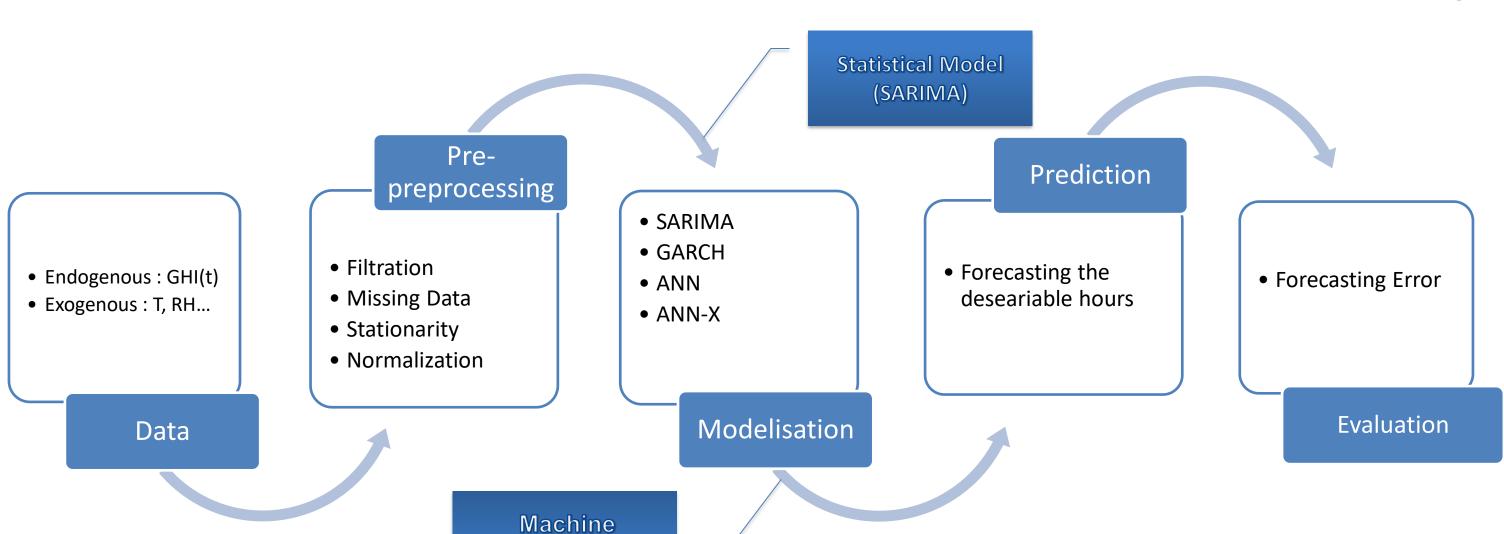


Forecasting methods based on historical data of solar irradiance are two categories:

- statistical methods: Seasonality analysis, Box-Jenkins or Auto Regressive Integrated Moving Average (ARIMA), Multiple Regressions and Exponential Smoothing are examples of statistical models.
- Machine learning: Al algorithms include fuzzy inference systems, genetic algorithm, Neural Networks, Bayesian Networks, etc.

#### II. Forecast Methodology





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learning (ANN)

#### II. Forecast Methodology



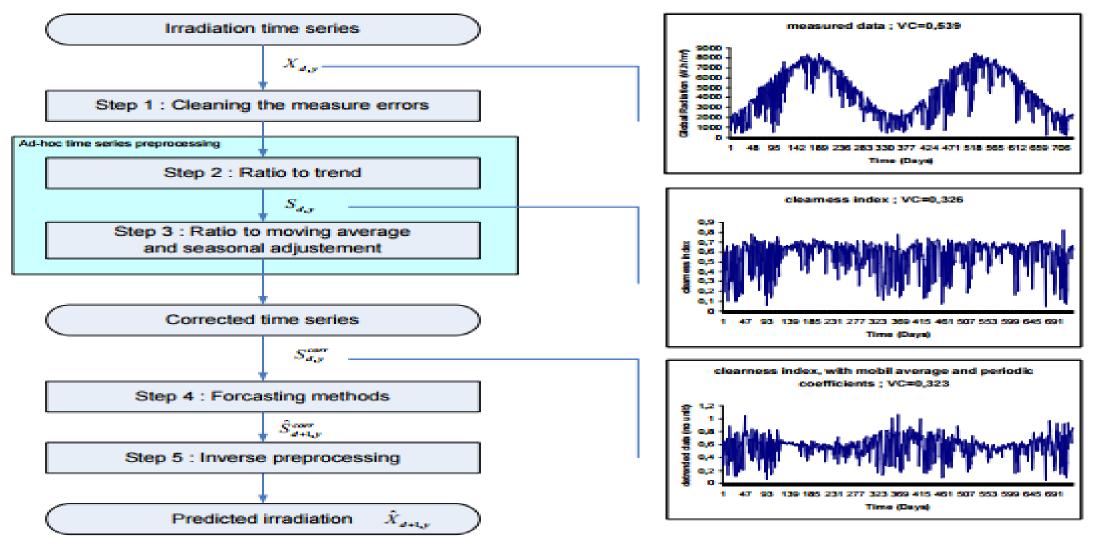


Fig. 5. Summarize of the protocol followed to obtain the predicted irradiation.

# II. Forecast Methodology SARIMA model



#### Definition 1

For a time series  $K_t$ , a SARIMA $(p, d, q)(P, D, Q)^s$  model is defined as the following :

$$\Phi_P(B^s)\phi_P(B)(1-B)^d(1-B^s)^D K_t = \theta_q(B)\Theta_Q(B^s)\epsilon_t, \qquad (1$$

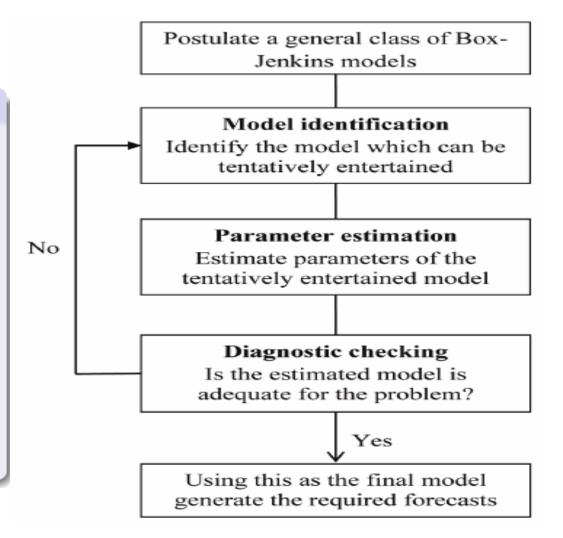
where,

$$\phi_{p}(B) = (1 - \phi_{1}B - \phi_{2}B^{2} - \dots - \phi_{p}B^{p}),$$

$$\theta_{q}(B) = (1 + \theta_{1}B + \theta_{2}B^{2} + \dots + \theta_{q}B^{q}),$$

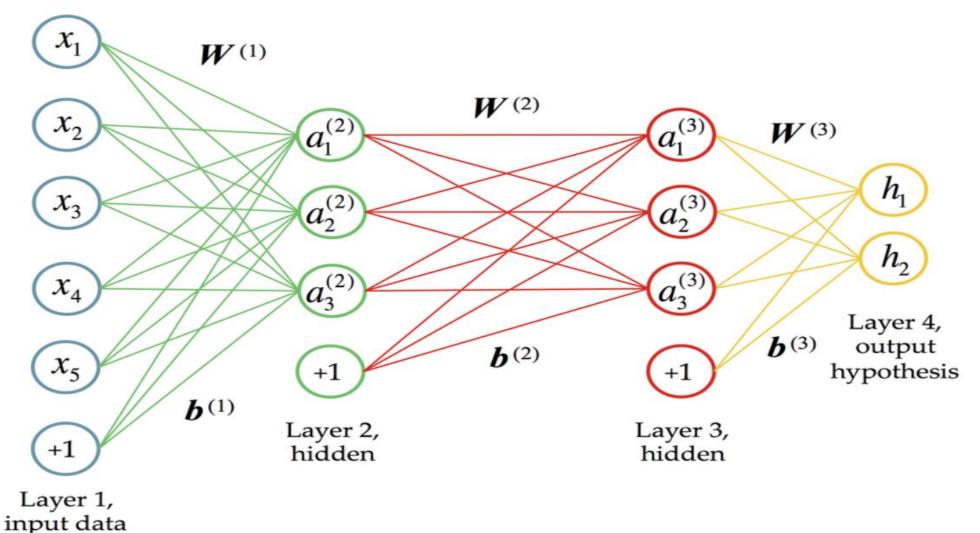
$$\Phi_{p}(B^{s}) = (1 + \Phi_{1}B^{s} + \dots + \Phi_{p}B^{s+P}),$$

$$\Theta_{Q}(B^{s}) = (1 + \Theta_{1}B^{s} + \dots + \Theta_{Q}B^{s+Q}).$$



### II. Forecast Methodology Artificial neural networks (ANN)





#### II. Forecast Methodology MultiLayer Perceprton (MLP)



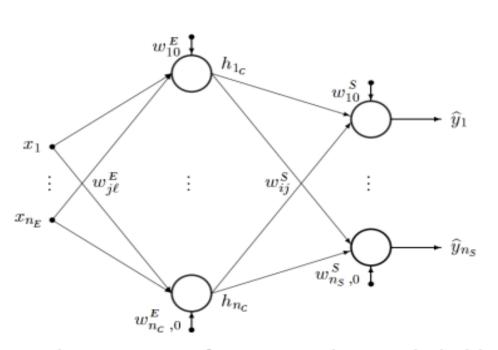


Figure 1 – The structure of a MLP with a single hidden layer.

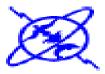
$$h_j(x) = f\left(\sum_{l=1}^{n_E} \omega_{jl}^E x_l + \omega_{j0}^E\right)$$
$$\hat{y}_i(x) = g\left(\sum_{l=1}^{n_C} \omega_{ij}^S h_j(x) + \omega_{i0}^S\right)$$

The forecast of our time series at the forecast horizon h is given by the equation (4):

$$\hat{y}_{t+h} = \sum_{j=1}^{n_C} \hat{\omega}_j^S f\left(\sum_{l=1}^{n_E} \hat{\omega}_{jl}^E \hat{y}_{t-l+h} + \hat{\omega}_{j0}^E\right) + \hat{\omega}_0^S, \tag{4}$$

where  $\hat{\omega}_{j}^{S}$ ,  $\hat{\omega}_{jl}^{E}$ ,  $\hat{\omega}_{j0}$  and  $\hat{\omega}_{0}^{S}$  are the network weights after training, and f is the activation function.

#### II. Forecast Methodology MultiLayer Perceprton (MLP)



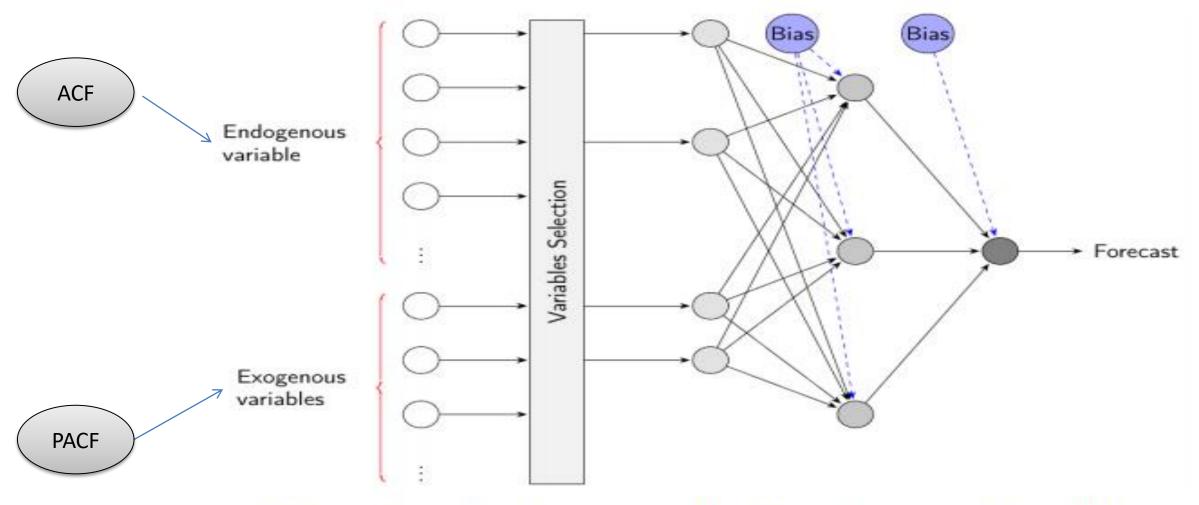


Figure 2 – The forecast methodology based on the MLP.





Mean Absolute Percentage Error (MPAE) :

$$\mathsf{MAPE} = \frac{1}{n} \sum_{t=1}^{n} |\frac{e_t}{y_t}| \times 100$$

Root Mean Squared Error (RMSE):

$$\mathsf{RMSE} = \sqrt{\frac{1}{n} \sum_{t=1}^{n} e_t^2}$$

normalized Root Mean Squared Error (nRMSE)

$$\mathsf{nRMSE} = \frac{RMSE}{\bar{y}}$$

# III. Results and discussions The region Rabat



- The dataset of hourly GHI for the region **Rabat** used in this study was provided by The Copernicus Atmosphere Monitoring Service.
- Hourly meteorological dataset was provided by MERRA-2\* hosted by NASA.
- The model ARIMA was used to forecast the missing data.

<sup>\*</sup>Modern-Era Retrospective analysis for Research and Applications, version 2.





Variable	Base	Unity	Period		
GHI	Hourly	KWh/m²	from 2012-01-01 to 2015-12-31		
GHI <sub>clear-sky</sub>	Hourly	$KWh/m^2$	from 2012-01-01 to 2015-12-31		
Temperature (T)	Hourly	C°	from 2012-01-01 to 2015-12-31		
Relative Humidity(RH)	Hourly	%	from 2012-01-01 to 2015-12-31		
Pressure (P)	Hourly	hPa	from 2012-01-01 to 2015-12-31		
Wind speed (WS)	Hourly	m/s	from 2012-01-01 to 2015-12-31		
Wind direction (WD)	Hourly	deg	from 2012-01-01 to 2015-12-31		
Rainfall (R)	Hourly	$kg/m^2$	from 2012-01-01 to 2015-12-31		

Tableau 1 – Characteristics of the datasets used in this study.

## III. Results and discussions Time series pre-processing



- Dataset filtration.
- Using the McClear model to product a new time series : the so-called clear-sky index  $k_t$ ;

$$k_t = \frac{GHI(t)}{GHI_{clear-sky}(t)},\tag{2}$$

- Training: from 01-01-2012 to 29-12-2015.
  - Testing: the last two days.

## III. Results and discussions Time series pre-processing



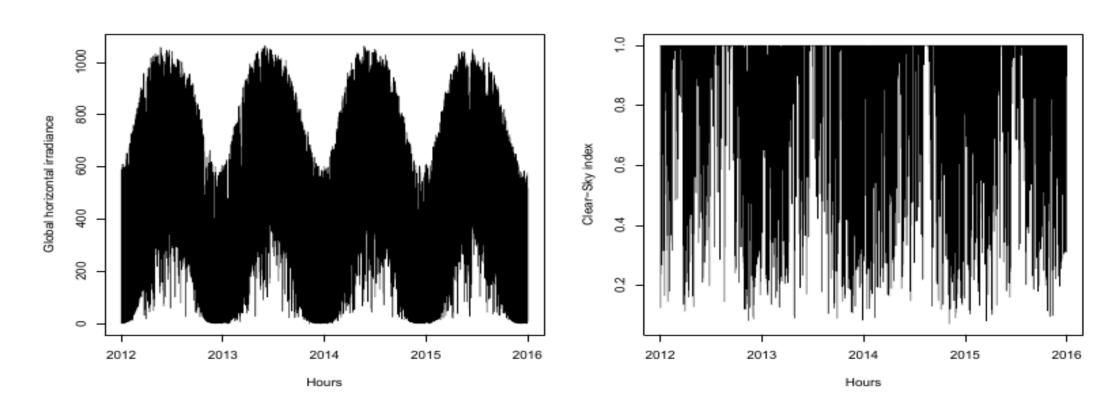


Figure 3 – Hourly global horizontal irradiance before (left) and after the transformation into the clear-sky index (right).

#### III. Results and discussions



#### MLP modelization: univariate case

The Partial autoregressive correlation function (PACF) determines the correlation between  $K_t$  and  $K_{t+k}$  after their linear dependency on the intervening variables  $K_{t+1}, K_{t+2}, ..., K_{t+k-1}$  has been removed.

Determination of the number of time lags for the endegenous variable

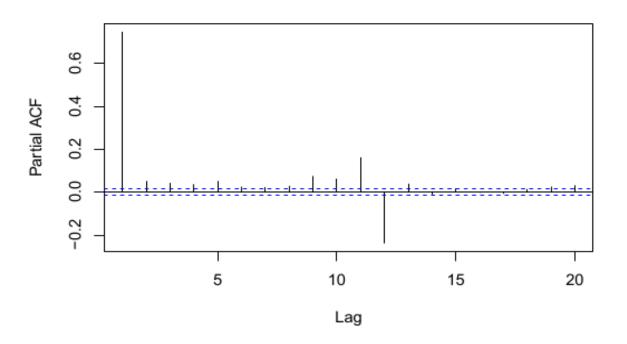


Figure 4 – Sample PACF of the clear-sky index  $k_t$ .

### III. Results and discussions MLP modelization: univariate case



Determination of the number of hidden neurons.

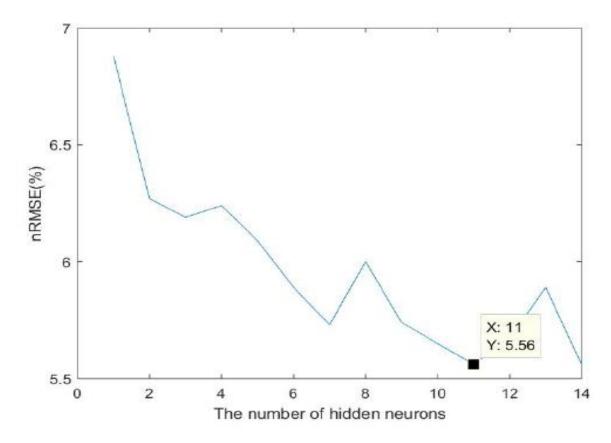


Figure 5 – forecasting error nRMSE of the global horizontal irradiance in function of the number of hidden neurons.

### III. Results and discussions MLP modelization: univariate case



Hence, the choice of the architecture of MLP were fixed on :

- inputs = 13, hidden neurons = 3 and outputs = 1.
- Activation function in the hidden layer : logistic function  $\left(f(x) = \frac{1}{1+e^{-2x}}\right).$
- Activation function in the output layer : linear function (g(x) = x).
- Learning algorithm : Levenberg-Marquardt.

### III. Results and discussions MLP modelization: multivariate case



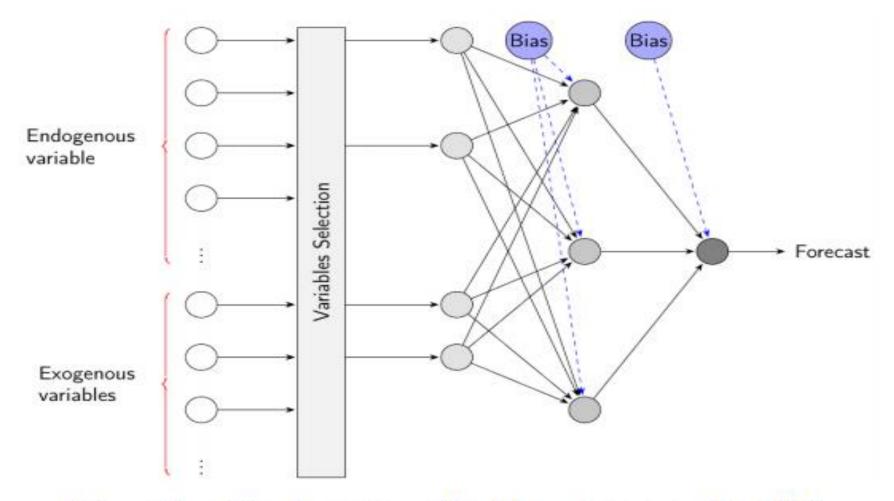


Figure 2 – The forecast methodology based on the MLP.

### III. Results and discussions MLP modelization: multivariate case



Determination of the number of time lags for the endegenous variable.

Determination of the number of time lags for each exogenous variable.

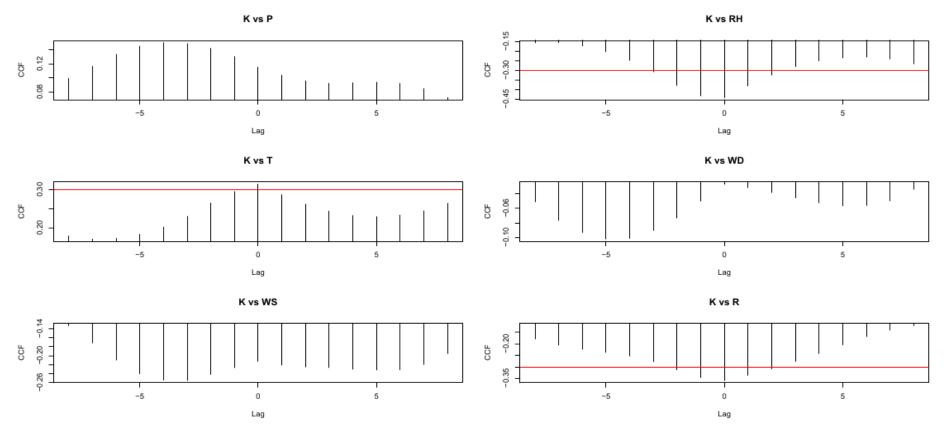
- The number of endogenous time lags has already identified in the previous section by using the PACF
- The exogenous variables were normalized by the minmax<sup>3</sup> normalization, then they were stationarized in case of no stationary time series.

Cross-correlation study.

### III. Results and discussions



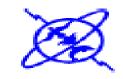
MLP modelization: multivariate case



Cross-correlation study

Figure 7 – Sample CCF between the clear-sky index  $k_t$  and the meteorological variables (Pressure (P), Temperature (T), Relative Humidity (RH), Wind Speed (WS), Wind direction (WD), Rainfall (R)), the red line represents the chosen confidence band.

### III. Results and discussions MLP modelization: multivariate case



RH time lag	R time lag	T time lag	n <sub>C</sub>	nRMSE(%)
2	2	0	11	5.90
2	_	_	11	5.25
_	2	_	11	6.53
_	_	0	11	5.72
_	_	_	11	5.56

Tableau 2 – forecast errors of the global irradiance by testing each variable alone from the correlated variables with the clear-sky index

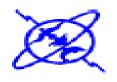
### III. Results and discussions MLP modelization: multivariate case



Hence, the choice of the architecture of ANN-X were fixed on :

- endogenous inputs = 13, exogenous inputs = 2, hidden neurons = 13, outputs = 1.
- Activation function in the hidden layer : logistic function  $\left(f(x) = \frac{1}{1 + e^{-2x}}\right).$
- Activation function in the output layer : linear function (g(x) = x).
- Learning algorithm : Levenberg-Marquardt.

## III. Results and discussions Forecasting errors for the region Rabat



Methodology	SARIMA	ANN	ANN-X
MAPE (%)	10.15	8.95	9.79
nRMSE(%)	8.97	5.56	5.19
RMSE ( $KWh/m^2$ )	27.72	17.17	16.03
Mean of errors	21.66	-4.41	-5.89
Variance of errors	0.0051	0.0060	0.0050

Tableau 3 – Performance metrics of forecasting the global horizontal irradiance.

# III. Results and discussions The region Hokkaido (Japan)



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No.	Туре	Contents		
1	Total solar power output	Period: 2016/1/1~2017/12/31		
	(each area)	Total solar power output measured in each area (S1, S2)		
2	Temperature and global	erature and global Period: 2016/1/1~2017/12/31		
_	solar radiation values	Temperature and global solar radiation values of 4 measurement locations.		

## III. Results and discussions The region Hokkaido (Japan)



Methodology	SARIMA-GARCH	ANN	ANN-X
MAPE (%)	12.87	11.90	11.5
nRMSE(%)	10.64	8.55	8.3
RMSE (MW)	43.70	35.03	34.5

Tableau 4 – Performance metrics of forecasting the total output of solar power.

#### IV. Conclusion



- The Machine Learning (ANN) approach is more efficient than the conventional forecasting approaches.
- The performance of ANN improves when exogenous variables are added.
- The difficulty of using ANN is to find the optimal structure.

#### **Future work:**

- All these results encourage us to study in the future how to adapt at different sites.
- Making the methodology more automatizing.

#### Let's work together:

New family of deep neural network; Deep Neural Ordinary Differential Equations

#### Refferences



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### Thank you for your attention