

Data Structure And Algorithms

Bubble Sort Algorithm

- Bubble sort is a simple sorting algorithm.
- This sorting algorithm is comparison-based algorithm in which each pair of adjacent elements is compared and the elements are swapped if they are not in order.
- This algorithm is not suitable for large data sets as its average and worst case complexity are of $O(n^2)$ where n is the number of items.

How Bubble Sort Works?

- We take an unsorted array for our example. Bubble sort takes $O(n^2)$ time so we're keeping it short and precise.



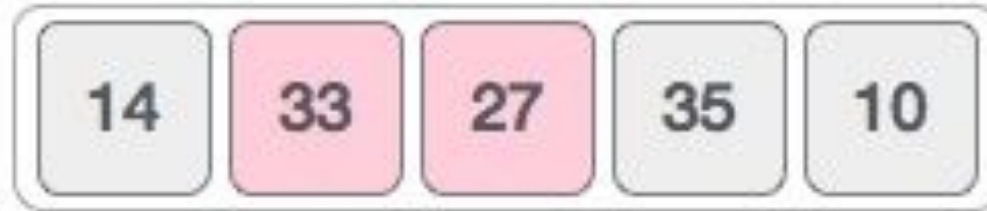
Bubble sort starts with very first two elements, comparing them to check which one is greater.



- In this case, value 33 is greater than 14, so it is already in sorted locations. Next, we compare 33 with 27.



- We find that 27 is smaller than 33 and these two values must be swapped.



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The new array should look like this –



- Next we compare 33 and 35. We find that both are in already sorted positions.

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- Then we move to the next two values, 35 and 10.



- We know then that 10 is smaller 35. Hence they are not sorted.



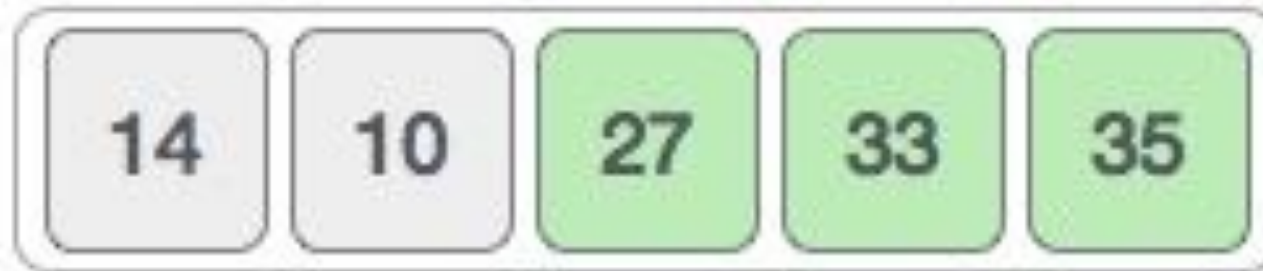
- We swap these values. we find that we have reached the end of the array. After one iteration, the array should look like this –



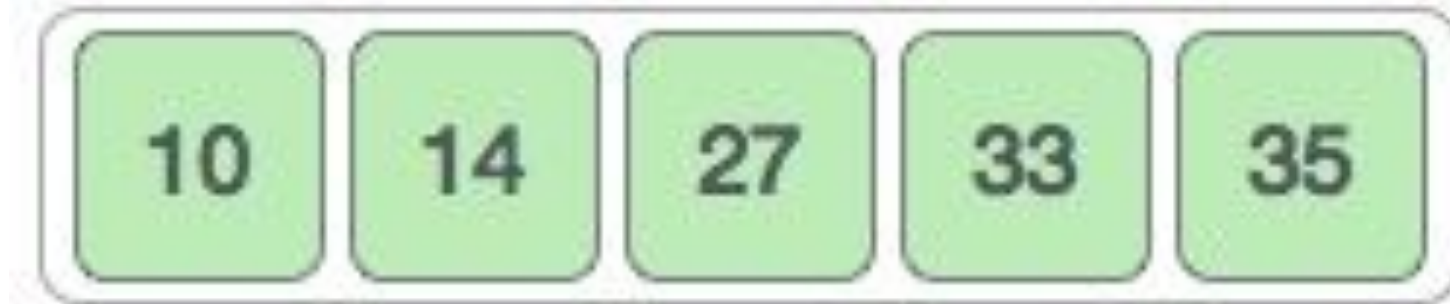
- To be precise, we are now showing how an array should look like after each iteration. After the second iteration, it should look like this —



- Notice that after each iteration, at least one value moves at the end.



- And when there's no swap required, bubble sort learns that an array is completely sorted.
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Algorithm

- begin BubbleSort(list)
- for all elements of list
- if $\text{list}[i] > \text{list}[i+1]$
- swap(list[i], list[i+1])
- end if
- end for
-
- return list
-
- end BubbleSort

```
public static void bubbleSort(int arr[],int n){
    n=arr.length;
    if (n==0||n==1){
        return;
    }

    int temp=0;
    for(int i=0;i<n-1;i++){
        for(int j=0;j<n-i-1;j++){
            if(arr[j]>arr[j+1]){
                temp=arr[j];
                arr[j]=arr[j+1];
                arr[j+1]=temp;
            }
        }
    }

    for(int k:arr){
        System.out.print(k+" ");
    }
}
```

Worst Case Analysis for Bubble Sort:

- **At pass 1 :** *Number of comparisons = $(n-1)$
Number of swaps = $(n-1)$*
- **At pass 2 :** *Number of comparisons = $(n-2)$
Number of swaps = $(n-2)$*
- **At pass 3 :** *Number of comparisons = $(n-3)$
Number of swaps = $(n-3)$*
- \vdots
- **At pass $n-1$:** *Number of comparisons = 1
Number of swaps = 1*
- *Now , calculating total number of comparison required to sort the array*
$$= (n-1) + (n-2) + (n-3) + \dots + 2 + 1$$
$$= (n-1) * (n-1+1) / 2 \quad \{ \text{by using sum of N natural Number formula} \}$$
$$= n(n-1)/2$$

- ***Total number of swaps = Total number of comparison***
Total number of comparison (Worst case) = $n(n-1)/2$
Total number of swaps (Worst case) = $n(n-1)/2$