

(1)

① Solution:-

ASSIGNMENT-2

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 $P(A) = \text{I}^{\text{st}} \text{ Card is spade}$

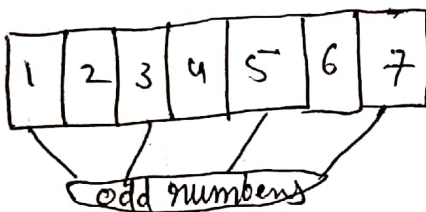
$$P(A) = \frac{{}^{13}C_1}{{}^{52}C_1} = \frac{13}{52}$$

 $P(B) = \text{II}^{\text{nd}} \text{ Card is spade (without replacing)}$

$$= \frac{{}^{12}C_1}{{}^{51}C_1} = \frac{12}{51} = \frac{4}{17}$$

Ans:- Probability of Second Card drawn is spade = $\frac{4}{17}$

② Sol:-

 $A \rightarrow$ (having three balls with odd numbers.) ~~$P(A) = \frac{3}{7}$~~ $A \rightarrow \text{I}^{\text{st}} \text{ ball odd.}$

$$P(A) = \frac{{}^4C_1}{{}^7C_1}$$

$$P(B) = P\left(\frac{B}{A}\right) = \frac{{}^3C_1}{{}^6C_1} = \frac{3}{6}$$

$$P(C) = \text{III}^{\text{rd}} \text{ odd ball} = \frac{{}^2C_1}{{}^5C_1} = \frac{2}{5}$$

$$P(\text{having three odd balls}) = P(A) \cdot P\left(\frac{B}{A}\right) \cdot P\left(\frac{C}{A \cap B}\right)$$

$$= \frac{4}{7} \times \frac{3}{6} \times \frac{2}{5} = \frac{4}{35}$$

I win	II win
2 (W) 1 (B)	1 (W) 5 (B)

Suppose shifted ball is white.
 $P(\text{Drawn ball white}) = \frac{2}{3} \times \frac{2}{7}$

$$= \frac{4}{21}$$

4)

B ₁	B ₂
3 S.S. 3 C.S.	5 C.S. 3 S.S.

$$P(A) = P(\text{Selecting } B_1 \text{ Box}) = \frac{2}{3}$$

$$P(B) = P(\text{" - } B_2) = \frac{1}{3}$$

solution

$$P(A) = P(B_1) + P(B_2)$$

$$= \frac{2}{3} + \frac{1}{3}$$

$$P(A) = P(A) \cdot P\left(\frac{B}{A}\right) + P(B) \cdot P\left(\frac{A}{B}\right)$$

$$= \frac{2}{3} \times \frac{2}{6} + \frac{1}{3} \times \frac{3}{8}$$

$$= \frac{1}{3} + \frac{1}{8} = \frac{8+3}{24} = \frac{11}{24}$$

Ans = 11/24

Ans 5) → B → $\frac{6}{13}$

A	B
Diagnosed Correctly 60%	wrong diagnosed
Death = D.	

$$P(A) = \text{D. Correctly} = \frac{60}{100}$$

$$P(B) = \text{W. Diagnosed} = \frac{40}{100}$$

$$P(A \cap D) = P(\text{Death by D.C.})$$

$$= P(A) \cdot P\left(\frac{D}{A}\right)$$

=

$$P(B \cap D) = P(\text{Death by D. wrongly})$$

$$= P(B \cap D)$$

$$= P(B) \cdot P\left(\frac{D}{B}\right)$$

$$P(A \cap D)$$

$$P\left(\frac{A}{D}\right) = \frac{P(A) \cdot P\left(\frac{D}{A}\right)}{P(A) \cdot P\left(\frac{D}{A}\right) + P(B) \cdot P\left(\frac{D}{B}\right)}$$

$$= \frac{60}{100} \times \frac{40}{100}$$

$$= \frac{\frac{60}{100} \times \frac{40}{100} + \frac{40}{100} \times \frac{70}{100}}{\frac{60}{100} \times \frac{40}{100} + \frac{40}{100} \times \frac{70}{100}}$$

$$= \frac{\frac{24}{100} + \frac{28}{100}}{\frac{24}{100} + \frac{28}{100}} = \frac{6/25}{52/100}$$

$$= \frac{6}{25} \times \frac{100}{52} = \frac{24}{52} = \frac{6}{13}$$

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$X=x$	-2	-1	0	1	2
$P(x)$	$1/9$	$2/9$	$3/9$	$2/9$	$1/9$

$$P(|X| > 1) = P(-2 > 1) + P(1 > 1)$$

$$= P(2 > 1)$$

$$= \frac{1}{9}$$

$$= \frac{2 \times}{9} \times P(x) = \frac{2}{9}$$

8 $\Sigma P(x) = 1$

$$11K^2 + 10K = 1$$

$$K \in (11K^2 + 10K - 1) = 0$$

$$K=0, K=-1, K=-1/11$$

$$\Sigma P(x) = 1$$

$$11K^2 + 10K - 1 = 0$$

$$11K^2 + (11-1)K - 1 = 0$$

$$11K(K+1) - 1(K+1) = 0$$

$$(K+1)(11K-1) = 0 \Rightarrow K = -1, -1/11$$

$$P(X < 3) = P(X=0) + P(X=1) + P(X=2)$$

$$= 0 + 2K + 3K$$

$$= 5K = 5 \times \frac{1}{11}$$

$$= \frac{5}{11} = 0.4545$$

Ans ⑧ = $0.4545 \approx 0.455$

9 $n \rightarrow$ Mutually independent events are given

$$P_1, P_2, \dots, P_n$$

$P_i \rightarrow$ is the prob. of happ. of event

$(1-P_i) \rightarrow$ is the prob. of non happ. of event

So $(1-P_1)(1-P_2) \dots (1-P_n)$ is the prob. of non happening of events

So $= \{1 - \{(1-P_1)(1-P_2) \dots (1-P_n)\}\}$ is the prob. of Happening of at least of one event happens

Ans = (B)

(9)

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(6) $\rightarrow 0.6561$

$$(1-p_1)(1-p_2)(1-p_3)(1-p_4) \\ = (0.9)(0.9)(0.9)(0.9)$$

(7)

A	B
Dry 91% chargers fail 2.5%	wet 9% 5.6%

Total probability theorem.

$$P(\text{Fails}) = P(A) \cdot P\left(\frac{E}{A}\right) + P(B) \cdot P\left(\frac{E}{B}\right)$$

$$= \frac{2.5}{100} \times \frac{91}{100} + \frac{5.6}{100} \times \frac{9}{100}$$

$$= 0.025 \times 0.91 + 0.056 \times 0.09$$

$$= 0.0277$$

$$\approx 0.28$$

Ans 7(D)