A coherently stimulated Brillouin spectrometer

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We present a novel coherently stimulated Brillouin spectrometer utilizing a detuned pump-probe design that exploits a relaxation of phase-matching requirements at small lengths, enabling room-temperature traveling-wave phonon spectroscopy at the micrometer scale with sub-10 femtowatt sensitivity. This approach overcomes the limitations of traditional stimulated Brillouin techniques, particularly regarding phase-matching constraints and spatial resolution. Our instrument's sensitivity was validated using 1 cm of UHNA3 fiber and 100 micrometers of bulk carbon disulfide liquid, demonstrating its capability to measure Brillouin scattering in materials with low Brillouin gain or, with particular advantage, small effective lengths. This advancement opens new possibilities for nanometer-scale Brillouin spectroscopy and the development of nano-acousto-optic devices.

I. INTRODUCTION

Brillouin scattering, the inelastic interaction between light and acoustic phonons, is a fundamental phenomenon used to probe the mechanical and structural properties of materials at microscopic scales. In spontaneous Brillouin scattering, thermally excited acoustic phonons scatter incident light, resulting in frequency shifts that reveal information about the material's elastic properties and acoustic modes [1]. However, the weak signal inherent to spontaneous Brillouin scattering often necessitates long acquisition times and limits spatial resolution, posing challenges for high-resolution material characterization.

Stimulated Brillouin scattering (SBS) enhances this interaction by using intense optical fields to amplify the acoustic wave through a nonlinear optical process. In SBS, a strong pump laser interacts with the counterpropagating Stokes wave generated within the medium, leading to the generation of acoustic phonons via electrostriction. This increased phonon population leads to greater generation of the Stokes wave, which interferes with the Pump wave to electrostrictively reinforce the acoustic wave. This positive feedback process creates exponential amplification that allows for more efficient excitation and detection of acoustic phonons and enables applications in optical signal processing, sensing, and high-resolution spectroscopy [2–5].

However, conventional SBS techniques face notable limitations when probing small volumes or samples with low Brillouin gain [6, 7]. The strict phase-matching conditions required for efficient SBS typically demand interaction lengths on the order of centimeters to meters, restricting spatial resolution and making it challenging to

study micro- and nanoscale systems. Additionally, separating the pump and scattered signals often requires complex optical filtering due to their close spectral proximity, complicating the experimental setup.

To overcome these challenges, various approaches have been explored [8–10]. Techniques utilizing optical cavities enhance the interaction by increasing the effective interaction length, but they require precise alignment and are sensitive to environmental fluctuations [11]. Forward Brillouin scattering methods, such as those demonstrated by Kittlaus et al., are advantageous in applications requiring relaxed phase-matching conditions, but come at the cost of increased modal complexity [12]. Coherent probe beam amplification schemes have been proposed to improve sensitivity, yet they can introduce additional noise and complexity, as phase noise in laser sources can lead to significant gain fluctuations and performance penalties [13].

In this work, we present a coherently stimulated Brillouin spectrometer that employs a detuned pump-probe scheme to relax the phase-matching requirements at small interaction lengths. By introducing a separate probe laser detuned from the pump, we achieve coherent amplification of the acoustic wave without the need for strict phase-matching over long distances. This design allows for the separation of the probe and pump frequencies, simplifying signal detection and filtering.

Our approach enables room-temperature traveling-wave phonon spectroscopy at the micrometer scale with sub-10 femtowatt sensitivity, surpassing the limitations of traditional SBS techniques. We demonstrate the capabilities of our instrument by measuring Brillouin scattering in 1 centimeter of ultrahigh numerical aperture (UHNA3) fiber and 100 micrometers of bulk carbon disulfide liquid. These measurements highlight the instrument's ability to characterize materials with low Brillouin gain or small effective lengths.

The development of this coherently stimulated Brillouin spectrometer opens new avenues for nanometer-

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scale Brillouin spectroscopy and facilitates the characterization and development of nano-acousto-optic devices. It holds promise for advancing research in material science, photonics, and sensing technologies, where high spatial resolution and sensitivity are paramount, marking a significant step toward practical, room-temperature Brillouin-based spectroscopy and sensing solutions.

II. THEORETICAL FRAMEWORK

Coherently stimulated four-wave Brillouin scattering

Stimulated Brillouin scattering (SBS), illustrated by the schematic in Fig. 1(a) for the Stokes process, is a three-wave mixing process in which incident pump laser light of frequency ω_{Pump} inelastically scatters from a traveling-wave phonon of frequency Ω to produce light that is frequency-shifted by the phonon frequency. In the Stokes process the phonon is retreating from the incident laser light and the scattered light is shifted down in frequency ($\omega_{Stokes} = \omega_{Pump} - \Omega$). Spatial overlap of the backscattered light with the incident laser light allows for interference of the two optical fields to produce a frequency at the difference of the two $(\omega_{Pump} - \omega_{Stokes})$. Since this difference frequency is exactly equal to the frequency of the acoustic field Ω , the beating of the incident pump light with the backscattered Stokes light produces an electrostrictive reinforcement of the acoustic wave. This driving of the acoustic wave in turn increases the scattering rate of the incident pump light, producing a positive feedback process and an exponential increase of the amplitude of the backscattered Stokes wave.

Fig. 1(b) shows the schematic of coherently stimulated four-wave Brillouin scattering for the Stokes process. We introduce a strong, controlled external Stokes wave of frequency ω_{Stokes} that drives electrostrictive reinforcement of the acoustic field in the medium. The backscattered Stokes light, normally collected in an SBS process, is then drowned out by the external Stokes laser. To resolve this, we inject light of a distinct frequency ω_{Probe} from an additional external laser which copropagates with the Pump and backscatters in the medium from the strongly driven acoustic field. This produces backscattered Signal light to be collected ($\omega_{Signal} = \omega_{Probe} - \Omega$) which is spectrally distinct from the high-powered Stokes laser light.

To describe this interaction and characterize the performance of the instrument, we derive the coupled-wave equations for the four-wave mixing process in Appendix A. These equations describe the relationship between the optical fields and the acoustic field in the material and result in the following expression for the scattered power of the backscattered signal,

$$P_{Sig} = \frac{1}{4} (G_B L)^2 P_P P_S P_{Pr} sinc^2 \left(\frac{\Delta k L}{2}\right), \qquad (1)$$

where P_P , P_S , and P_{Pr} are the powers of the pump,

Stokes, and probe lasers, respectively, and G_B is the effective Brillouin gain,

$$G_B = \frac{g_0}{A_{eff}} \frac{\left(\frac{\Gamma_B}{2}\right)^2}{(\Omega - \Omega_B)^2 + \left(\frac{\Gamma_B}{2}\right)^2},\tag{2}$$

with the on-resonance gain factor of the material given by

$$g_0 = \frac{\gamma_e^2 \omega^2}{nvc^3 \rho_0 \Gamma_B}. (3)$$

Here, γ_e is the electrostrictive constant, ω is the pump frequency, n is the refractive index of the material, v is the sound speed of the material, c is the speed of light, ρ_0 is the mean density of the material, and Γ_B is the Brillouin linewidth, or phonon dissipation rate, of the material. In Eq. 2, Ω_B is the resonant Brillouin frequency of the material, A_{eff} is the effective area of the material, Δk is the wavevector mismatch between the optical fields, to be discussed next, and L is the effective length of the material.

Phase matching relaxation

In all nonlinear optical processes, efficiency is maximized when phase matching conditions are satisfied. A frequency mismatch (energy unconservation) or a wavevector mismatch (momentum unconservation) each result in drastically reduced efficiency of a given process.[14] This can be seen by Eq. 1, where the wavevector mismatch, Δk , is contained within a $sinc^2$ function. This $sinc^2$ term thereby defines the phase matching bandwidth of the system, notably scaling with effective interaction length L.

We apply this wavevector mismatch allowance to the pump and probe waves ($\Delta k = k_{Pump} - k_{Probe}$) so that the backscattered signal is different than the applied Stokes wave. This choice allows for selection of the signal and rejection of the Stokes with a bandpass filter, as will be discussed later. Expressed in terms of wavelengths, this gives

$$\Delta k = \frac{4\pi n \Delta \lambda}{\lambda_{Pump} \lambda_{Probe}} \approx \frac{4\pi n \Delta \lambda}{\lambda_{Pump}^2}.$$
 (4)

We can apply this to the phasematching bandwidth term to find the fraction of maximum scattered power, Φ , that can be expected for a given interaction length, L, and phase mismatch $\Delta\lambda$ between the pump and probe,

$$\Phi \equiv sinc^2 \left(\frac{2\pi n \Delta \lambda L}{\lambda_{Pump}^2} \right). \tag{5}$$



FIG. 1: Illustration of 4-Wave Brillouin Scattering.

Using this expression for Φ , we see that for an effective length of one meter, a wavelength mismatch of only 0.6 pm from a typical wavelength of 1.55 μ m pump light in UHNA3 fiber drops the scattered power to one half of maximum. However, for shorter effective lengths the wavevector mismatch becomes more forgiving; a 36 pm mismatch preserves 82.5% of the maximum signal for a length of 1 cm under identical conditions. This separation, translating to about 4.5 GHz, is meaningful, as it represents sufficient spectral separation for the backscattered signal to be isolated from the applied Stokes light.

Furthermore, for decreasing lengths, Eq. 5 predicts an increase in the fraction of maximum signal produced, given equivalent pump-probe detuning, as the $sinc^2$ function is sampled closer to its peak center. Alternatively, as length decreases, the probe may be further detuned from the pump and still achieve the same fraction of the maximum signal as for longer lengths, perhaps offering a slight advantage in noise reduction. It should be noted that the scattered power, as given by Eq. 1, scales with the square of the effective length. Thus, while smaller lengths allow for the ability to capture a larger fraction of this maximum scattered power, the actual amount of scattered power decreases dramatically as length decreases.

III. METHODS

Instrument design

The design of the instrument is shown in the schematic in Fig. 2. A pump and Stokes wave is synthesized from a single tunable laser source for coherent stimulation of a sample. The pump wave (ω_{Pump}) is amplified by an erbium-doped fiber amplifier (EDFA) and passed through a variable optical attenuator (VOA) for power control. The output is then polarization-controlled to reflect at a polarizing beam splitter (PBS) for injection into the sample. For Stokes synthesis, an AC signal (Ω) is supplied to an intensity modulator (IM) with carrier frequency nulled and a tunable filter is used to select the lower-frequency Stokes side band $(\omega_{Pump} - \Omega)$. This Stokes light is then amplified by an EDFA, passed through a

VOA, and polarization-controlled to reflect at a second PBS for couter-propagation to the pump through the sample.

A separate tunable laser is used to supply a probe wave $(\omega_{Probe} = \omega_{Pump} + \Delta k)$ and local oscillator (LO). Probe light is amplified by an EDFA and passed through a VOA and a polarization controller aligns the polarization for transmission through the first PBS whereby it copropagates with the pump through the sample. Backscattered light exits the sample and transmits back through the first PBS, whereas the orthogonally polarized Stokes light reflects at this same point to be diverted to a tap for power monitoring. The backscattered signal (ω_{Signal} = $\omega_{Probe} - \Omega$) then routes through two subsequent circulators for spectral filtering by a 5 GHz bandpass tunable filter. This filter allows the desired backscattered signal to pass while rejecting any reflected probe light as well as any reflected, transmitted, or backscattered light from the pump or Stokes waves that was not already diverted by the PBS.

The filtered signal then heterodynes via a 99-1 splitter with the LO which is frequency-upshifted by an acoustooptic modulator (AOM) ($\omega_{LO} = \omega_{Probe} + \omega_{AOM}$) and controlled to be copolarized with the signal. Of the resulting frequencies from the heterodyne process, only the difference frequency term is considered, as all others are beyond the range of detection. This heterodyned signal $(\omega_{signal} = \Omega + \omega_{AOM})$ is then captured by a photodiode detector and heterodyned again by a radio frequency (RF) mixer with a second AC signal $(\Omega + \omega_{AOM} - \omega_{Lock})$, where ω_{Lock} is a fixed-frequency to be detected by a lock-in amplifier set to this frequency after being passed through a low-pass filter and amplified by an RF amplifier. Synchronous sweeping of both AC signals, each involving Ω , allows for ω_{Lock} to remain fixed throughout measurement over a frequency range.

Experimental Techniques

Here we detail some of the experimental techniques, design choices, and specific device settings which optimize the signal-to-noise (SNR) of our measurements with the instrument. Our experimental setup generates the pump, Stokes, and Probe optical fields required for co-



FIG. 2: Design schematic of a coherently stimulated phonon spectrometer. A tunable CW laser at approximately 1.55 μ m emits light that passes through an isolator (Iso) and a splitter, diverting 10% to a 27 dBm EDFA followed by a variable optical attenuator (VOA). This pump light (ω_P) is polarization-controlled to reflect off a polarizing beam splitter (PBS) and is recoupled to fiber via a fiber port (FP), then directed to the sample either by direct fiber coupling or through a pair of FPs and lenses (L) for free-space samples. After passing through the sample, the pump light traverses a corrective polarization controller that mitigates fiber twists and bends before reflecting off a second PBS, where it is routed to port (c) for power monitoring. To synthesize the Stokes wave, a 90% split from the original pump is processed through an intensity modulator (IM) and a fiber Bragg grating (FBG), generating a Stokes sideband downshifted from the pump by Ω . This frequency shift is swept via a signal generator to capture Ω_B . A 99/1 splitter provides a tap at port (a) to optimize Stokes synthesis. The Stokes wave (ω_S), amplified by a 1 W EDFA and VOA-controlled, counter-propagates along the pump path and is monitored at port (b). A second tunable CW laser, detuned from the pump, generates the Probe wave (ω_{Pr}) , which is amplified by a 1 W EDFA, attenuated variably, and polarization-controlled to pass through the initial PBS where it is incident on the sample. Backscattered Signal light (ω_{sig}) transmits back through the PBS, while unscattered Probe light transmits to a power meter at port (d). A circulator parts the Signal from the Probe path, with an FBG filtering out any unwanted noise or Stokes light. Finally, the Signal is heterodyned with an EDFA-amplified, AOM-shifted local oscillator (LO) derived from the Probe laser and directed to a photodiode for detection. The resulting RF signal is mixed with an AC LO supplied by the signal generator which sweeps synchronously with the Stokes synthesis frequency, and collected by a lock-in amplifier for data processing.

herently stimulated Brillouin scattering. The pump laser emits approximately 45 mW of power, of which 10% is split and amplified to approximately 0.5 W to become the pump optical field. The other 90% of power emitted from the pump laser is shifted to become the Stokes optical field and is amplified to approximately 1 W. Similarly, the Probe laser emits approximately 45 mW of power, of which 10% is split and amplified to approximately 1 W to become the Probe optical field and the remaining 90% is used as the LO. A 99/1 splitter was specifically chosen over a more common 50/50 splitter to heterodyne the signal and LO in order to minimize loss of the backscattered signal before being collected by the detector, as this preserves 99% of the signal power at no cost if the LO is amplified by 50x. Thus, in our setup the LO is amplified to approximately 230 mW prior to combining with the signal, resulting in the maximum allowable input power for our detector of <2.4 mW to be incident at the detector. Post-detector, the electronic signal is mixed with a 17 dbm AC signal and amplified by a 23 dbm RF amplifier before it is collected by a lock-in amplifier. For all measurements, it was found that setting both pump and Probe lasers to emit in whisper mode (as opposed to dither) dramatically improves the spectral density and SNR of the measurement.

Proper matching of the demodulator settings of our Zurich Instruments HF2LI 50 MHz lock-in amplifier to the signal input is critical for maximizing the SNR of the measurement. Clock timing is synced between the signal generater and the lock-in amplifier with a 10 MHz reference signal output from the signal generator and fed into the lock-in amplifier set to accept this reference clock signal. The input signal range, which defines the gain of the analog input amplifier, should exceed the incoming signal by roughly a factor two including a potential DC offset. This is best chosen by selecting the auto feature within the lock-in software interface, which automatically adjusts the range according to a rolling 100 ms window of the maximum measured input signal amplitude. The coupling mode is set to AC, which inserts a high-pass filter that rejects DC components of the input signal, and the input impedance is set to $1M\Omega$. We set the low-pass filter order to the 8th order, which sets the filter to roll off at the maximum 48 dB/oct, and the data sampling rate of the input signal is set to the maximum 1.84 million Sa/s.

The SNR of a measurement is further optimized when the low-pass filter bandwidth for the lock-in amplifier input signal is minimized to match the frequency linewidth and thermally-driven variability or random drift of the incoming signal, ω_{Lock} . While the linewidth of the signal is sub-hertz, the range within which it drifts is dependent on the stability of instrument components and is typically on the order of tens of hertz. We find this frequency drift of the input signal to be less than 100 Hz after all components of the system reach equilibrium temperature (approximately 30 minutes) and thus set the low-pass filter bandwidth to 100 Hz for long measurements of a few

hours. For shorter measurements of less than 15 minutes this bandwidth can typically be reduced to as little as 40 Hz without risking the signal drifting out of range.

In addition to the signal linewidth being defined by this slight signal variability just discussed, the input signal frequency is also affected by the thermally-driven variations in precision of the electronic components. The mean frequency of the incoming signal, ω_{Lock} , must precisely match the frequency that the lock-in amplifier expects to recieve, as specified in its control parameters. Achieving maximum precision requires that the frequency difference between the two output signals of the signal generator, $\omega_{Ch1} = \Omega$ and $\omega_{Ch2} =$ $\Omega - \omega_{Lock} + \omega_{AOM}$, precisely match the lock-in frequency specified for the lock-in amplifier. This presents a challenge because, while Ω is directly controlled to subhertz precision by the signal generator, ω_{AOM} varies according to the precision of our AOM device with nominal temperature fluctuations. Despite efforts to thermally ground the device for stability, our AOM has been found to initially shift its input signal by its specified value of 40 MHz, before gradually increasing its applied shift over approximately 30 minutes as the internal components of the device warm to equilibrium operating temperature. Once at thermal equilibrium, however, the device maintains a stable shift of the signal by $40,000,820~\mathrm{Hz}\pm50$ Hz, allowing for a stable mean lock-in frequency and a relatively narrow filter bandwidth of 100 Hz to capture the variability contribution of the AOM.

IV. RESULTS

Instrument sensitivity

We begin by testing the sensitivity of the instrument as a way of defining a performance metric for the instrument which can be used to indicate what material, power, and length combinations might be possible to measure. From Eq. 1, the sensitivity of the instrument is the minimum scattered power, P_{Signal} , to produce a statistically significant measurement. To determine this, we target a specific length, L, of a sample of known effective Brillouin gain, G_B . We keep the pump-probe detuning, $\Delta \lambda$, constant across measurements and record the pump, Stokes, and probe optical powers to calculate the scattered power. Starting with sufficient optical powers to produce a clearly distinguishable measurement, we gradually reduce the optical powers until the sensitivity floor is reached.

To serve as our sensitivity testbed, we prepared 1 cm of Nufern's UHNA3 fiber, a well-studied fiber with known effective Brillouin gain[15]. Additionally, UHNA3 fiber offers several properties that make it ideal for this task of unambiguous detection of the Brillouin signal as it diminishes with each subsequent reduction in optical powers. First, it offers a Brillouin shift that is spectrally far from that of the single-mode fiber (SMF28) which constitutes

1 cm UHNA3 CABS



FIG. 3: 5 fW sensitivity measurement

much of the instrument. This ensures that the Brillouin response of the sample is not conflated with the Brillouin response of the instrument itself. Additionally, the core of UHNA3 fiber features a high concentration of germanium which improves the optical and acoustic guidance in the fiber as a result of the large refractive index difference between core and cladding. Finally, UHNA3 fiber offers a high optomechanical nonlinear response, with an effective Brillouin gain of $0.6~W^{-1}m^{-1}$ measured at room temperature [15]. This gain factor is larger than that of SMF28 by an order of magnitude [16].

The Brillouin signal corresponding to a sensitivity of $P_{Signal} = 5 \,\mathrm{fW}$ is shown in Fig. 3. The data represent an average of five consecutive measurements, from which an average of five consecutive background measurements has been subtracted. Error bars indicate the 1σ standard deviation of the mean, also known as the standard error. The measurement appears to offer an SNR greater than 5, estimated by visually comparing the peak spectral density at the center frequency to the spectral density off resonance. Assuming a normal noise distrubution profile, an SNR of 5 is equivalent to a 5σ confidence interval, or 99.7% confidence in the statistical significance of this measurement. This characterization of the sensitivity of our instrument provides the essential information needed to assess the feasibility of more challenging measurements going forward, such as those involving materials with low Brillouin gain or samples with small effective lengths. Relevant parameters used for this measurement and calculation of on-resonance scattered power are listed in Table I.

G_B	L	P_P		P_{Pr}	
$(W^{-1}m^{-1})$	(m)	(μW)	(μW)	(mW)	(pm)
0.6	0.01	506	504	2.01	20

TABLE I: Measurement parameters for sensitivity measurement and calculation.

1 cm UHNA3 CABS



FIG. 4: 1cm UHNA3

Measurements

We demonstrate the capabilities of the instrument on the two most common classes of samples: fiber and bulk material. For a fiber sample we again choose UHNA3 for its higher nonlinear response and excellent optical and acoustic guidance. In contrast to the sensitivity measurements, we now seek to demonstrate the full measuring capabilities of the instrument and so apply all available optical power (about 1.5 W) to maximize the backscattered signal from the sample. We target the same 1 cm segment of UHNA3 fiber as was used for determining sensitivity.

Fig. 4 shows the spectral profile captured for 1 cm of UHNA3 fiber, revealing the expected lorentzian profile consistent with Eq. 2. The peak amplitude of the spectra occurs at 9.1704 GHz, indicating the Brillouin resonance frequency of the longitudinal traveling-wave mode in the fiber. The FWHM of the measurement is 80 MHz and provides a measure of the phonon dissipation rate. Both values match what is seen in the literature for SBS measurements of UHNA3 fiber.[15] The data shown are a background-subtracted average of five successive measurements taken over 10 minutes with error bars corresponding to 1σ of the standard deviation of the mean, or standard error.

To achieve this measurement of UHNA3 fiber, the in-

100 μm CS2 CABS

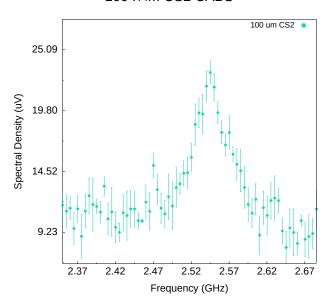


FIG. 5: $100\mu m$ CS2

strument design was altered to include only fiber-coupled segments connecting the fiber ports between the two PBSs. The pump laser wavelength was set to 1549.000 nm and the probe laser wavelength was set to 1549.020 nm. giving a frequency mismatch of approximately 2.5 GHz. The pump-probe mismatch is chosen to be only as large as needed to allow the edge of the pass-band of the probe filter to split the backscattered pump and probe light, thus rejecting any backscattered light from the pump laser and accepting only the backscattered signal from the probe laser. The Stokes filter was placed at 1549.073 nm, an offet of approximately 9.18 GHz from the pump laser to capture the Stokes sideband from the intensity modulator. This corresponds to the center of the measured frequency range and was chosen to allow the Stokes sideband output from the intensity modulator to remain within the pass band of the Stokes filter as the RF signal fed to the intensity modulator is swept through the full measurement range. The probe filter was set to 1549.109 nm, an offset of approximately 11.18 GHz from the probe laser, to capture the Stokes-shifted backscattered signal from the probe. The center frequency of the backscattered signal is of course shifted 9.18 GHz from the probe laser, however an extra offset of 2 GHz is chosen for improved rejection of any pump light as the pass band of our filter extends approximately 2.5 GHz on either side of center.

For a free-space bulk example we target carbon disulfide liquid for its exceptionally high Brillouin gain factor of 1.5 m/GW.[1] Figure 5 reveals the Brillouin signal of carbon disulfide liquid contained in a 100 μ m path length cell. To our knowledge, measurement of Brillouin scattering at this scale has not been reported in the literature. A scattered power comparison would reveal that achiev-

ing such a measurement using traditional SBS techniques would require excessively high optical powers or cooling the material to cryogenic temperatures, which, of course, would be prohibitive for carbon disulfide in the liquid state.

For this measurement of carbon disulfide, the pump and probe laser wavelengths were set to 1548.808 nm and 1548.898 nm, respectively. The short path length of the sample significantly broadens Φ , the $sinc^2$ term defining the phasematching bandwidth, allowing for further separation of the pump and probe wavelengths for improved signal isolation without significant reduction in scattered power of the signal produced in the carbon disulfide. Specifically, the additional pump-probe wavelength separation of 70 pm employed for this measurement compared to the UHNA3 measurement results in a negligible 0.045% reduction in scattered power. This additional separation contributes meaningfully, however, to improved rejection of pump light by the probe filter and thus higher SNR of the signal.

Placement of the Stokes filter is critical for measurements of materials that give small Brillouin shifts, such as with carbon disulfide's 2.55 GHz shift. We offset our 5GHz bandwidth Stokes filter an additional 2 GHz to ensure the nearby carrier signal and anti-Stokes sideband from the intensity modulator are rejected and only the Stokes sideband is allowed to pass. For the measurement shown in Fig. 5, this corresponds to a Stokes and probe filter placement of 1548.844 nm and 1548.934 nm, respectively.

Phase Matching Bandwidth

We performed an additional experiment to characterize the phase matching tolerance of the instrument for a given length of sample. In this experiment, we performed a series of measurements of 1 cm of UHNA3 at constant optical powers while increasing the detuning of pump and probe lasers. From Eq. 1, this experiment holds G_B , L, P_P , P_S , and P_{Pr} constant while letting Δk vary. We expect the amplitudes of these measurements to trace out a $sinc^2$ function as given by Eq. 5. Fig. 6 shows the result of this experiment which includes 75 measurements performed between 5 GHz and 42 GHz pump-probe frequency separation, at 0.5 GHz intervals, with the peak amplitude of each measurement represented by a point. The theoretical $sinc^2$ function for the parameters used in the experiment is shown on the plot with a solid red line.

Fano-Resonant Asymmetries at Small Signals

Under certain conditions where the resonant Brillouin amplitude approaches the background continuum level, we observe an asymmetric, Fano-type lineshape[17–20]. These Fano distortions can shift the apparent peak frequency, complicate simple Lorentzian fitting, and affect

1 cm UHNA3 Phase-Matching Bandwidth

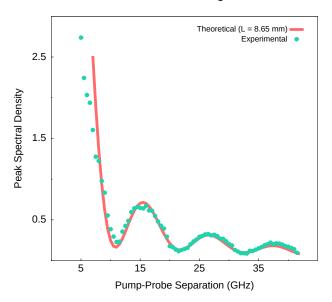


FIG. 6: Phase-matching $sinc^2$ func

the extracted linewidth in small-signal measurements.[?] Fano resonances arise when a discrete resonance (in our case, the Brillouin mode) interferes with a continuum background (e.g., noise floor or broad, non-resonant scattering). When the resonance amplitude is no longer much larger than the continuum, the interference leads to an asymmetric lineshape described by the Fano formula[17],

$$I(\omega) \propto \frac{(q+\epsilon)^2}{1+\epsilon^2},$$
 (6)

where $\epsilon \equiv (\Omega - \Omega_B)/(\Gamma_B/2)$ is the dimensionless detuning from the Brillouin peak (measured in half the spectral linewidth) and q is the Fano asymmetry parameter.

We first noticed this behavior in our small-length CS_2 data, where a small shift in probe wavelength revealed an asymmetric lineshape. For the measurements of 100 μm CS_2 (Fig. 5) and 1 cm UHNA3 at low power (Fig. 3), the amplitude of the resonant Brillouin peak is only 1x to 2x that of the non-resonant continuum, giving a strong chance for Fano interference. Whenever $\frac{I_{\rm res}}{I_{\rm bkg}} \approx 1$, the parameter q can become finite (rather than $\pm \infty$ in the limit that the background is negligible), and Fano interference arises. Indeed, for 100 μm of CS_2 , even a small shift in the probe laser's wavelength produced noticeable asymmetry in the line shape. To explore this further, we performed a similar phase-matching experiment as was done for 1 cm UHNA3 (see Phase Matching Bandwidth subsection), this time with 1 mm of CS_2 . Results from this are presented in Appendix C and offer a striking example of line shapes with pronounced asymmetry and featuring clear characteristic morphologies associated with various values and signs of q. These pronounced distortions in spectral line shape for small signal measurements

underscore the role of Fano interference in small resonant amplitudes relative to the background.

As our instrument is well suited to measuring samples of length < 10 m and low Brillouin gain, typical signal amplitudes are often small and may sometimes approach the order of the background continuum amplitude. For this reason, Fano effects may more often be present with this technique and must be handled appropriately, such as fitting data with a Fano profile as opposed to a Lorentzian to ensure accurate capture of relevant parameters such as linewidth and peak amplitude. Beyond fitting, it is important to be aware of these effects and when they are likely to occur so that difficult measurements pushing the limits of equipment capability may be more easily recognized or confirmed, as the data is likely to present a spectrum that deviates from the standard Lorentian. In some cases, Fano interference may even boost the measured peak above its nominal amplitude—i.e., 'amplify' it—when q < 0. This peak-boosting effect occurs when the scattered Brillouin signal lags the background continuum in phase, resulting in a negative q.

In principle, the Fano lineshape can exhibit a higher peak amplitude than a pure Lorentzian if the discrete Brillouin response interferes constructively with the background near resonance. However, this does not represent net energy gain, since it is an interference effect rather than a true amplification mechanism. Depending on the phase relationship and the background noise level, the observed peak may be taller (enhancing local amplitude), but the net SNR may or may not improve globally, since the background continuum also contributes noise. However, by just tuning the wavelength of the probe, an operator can fine-tune the measurement for optimal Fano behavior for a given system and measurement. Remarkably, this can be done even without giving up independent control of the phase matching bandwidth. This can be achieved through simultaneous adjustment of the pump laser wavelength in step with the probe such that the desired pump-probe detuning is preserved.

In the phase-matching bandwidth experiment performed on 1 cm UHNA3 (Fig. 6 and described in Phase Matching Bandwidth subsection), several factors contribute to a slight deviation from the simple theory of a pure $sinc^2$ function, including noise floor, alignment drifts, fiber dispersion, among possible others. We largely see the $sinc^2$ dependence, however near the troughs of the $sinc^2$ function and for greater pump-probe detunings, the measured peaks become quite weak, and a slight spectral asymmetry emerges (see Appendix C). This is consistent with a Fano-type distortion, wherein the signal amplitude is comparable to the underlying continuum, leading to an interference phenomenon that slightly skews the measured peak. Because of the Fano line shape, the raw peak amplitude from the spectral trace is not exactly at the Lorentzian center. A naive Lorentzian fit would thus not accurately capture the peak amplitude of these greater pump-probe detunings. We corrected for this by fitting a standard Fano profile, which accurately captures the peak amplitudes. Comparing a pure Lorentzian vs. a Fano fit in the limiting data sets indicates that ignoring the Fano effect overestimates the peak amplitude by 5–10%. However, even with a good fit, the Fano-resonant effects serve to amplify or diminish the underlying Brillouin response depending on the sign of the Fano asymmetry parameter q for any given set (e.g. whether the Brillouin response slightly lags (q < 0) or leads (q > 0) the broad background continuum in phase, respectively).

V. CONCLUSION

In conclusion, we have introduced a coherently stimulated Brillouin spectrometer utilizing a detuned pumpprobe design to achieve high sensitivity and roomtemperature operation in micrometer-scale samples. This approach successfully overcomes the spatial resolution limitations imposed by conventional SBS methods, demonstrating sub-10 femtowatt sensitivity in UHNA3 fiber and enabling Brillouin measurements in bulk liquid carbon disulfide with unprecedented efficiency. By relaxing phase-matching constraints, this instrument opens new possibilities for characterizing nanoscale material properties and developing nano-acousto-optic devices in standard laboratory settings without the need for cryogenic environments. Moving forward, our methodology could facilitate advancements in high-resolution phonon spectroscopy and inspire further innovations in the study of material mechanics at the microscale, reinforcing the broader applicability of Brillouin-based techniques across materials science, photonics, and sensing technologies.

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Appendix:

A Coherently Stimulated Brillouin Spectrometer

Appendix A: Coupled-Wave Equations

Here we derive the coupled wave equations that describe coherent stimulated Brillouin scattering involving a pump, Stokes, probe, and backscattered optical field given respectively by

$$\tilde{E}_P(z,t) = A_P e^{i(k_P z - \omega_P t)} + c.c., \tag{A1}$$

$$\tilde{E}_S(z,t) = A_S e^{i(k_S z - \omega_S t)} + c.c., \tag{A2}$$

$$\tilde{E}_{Pr}(z,t) = A_{Pr}e^{i(k_{Pr}z - \omega_{Pr}t)} + c.c., \tag{A3}$$

$$\tilde{E}_{Sig}(z,t) = A_{Sig}e^{i(k_{Sig}z - \omega_{Sig}t)} + c.c., \tag{A4}$$

and a common acoustic field given by

$$\tilde{\rho}(z,t) = \rho_0 + \rho(z,t)e^{i(qz-\Omega t)} + c.c., \tag{A5}$$

where $\Omega = \omega_P - \omega_S$ and $q = k_P - k_S = 2k_P$.

1. Acoustic Field

As in the case of SBS [1], we start by assuming that the material obeys the acoustic wave equation,

$$\frac{\partial^2 \tilde{\rho}}{\partial t^2} - \Gamma' \nabla^2 \frac{\partial \tilde{\rho}}{\partial t} - v_s^2 \nabla^2 \tilde{\rho} = \nabla \cdot \vec{f}, \tag{A6}$$

where v_s is the sound speed in the material and Γ' is a damping parameter given by

$$\Gamma' = \frac{1}{\rho} \left[\frac{4}{3} \eta_s + \eta_b + \frac{\kappa}{C_p} (\gamma - 1) \right], \tag{A7}$$

where η_s and η_b are the shear and bulk viscosity coefficients of the material, respectively. The source term on the right side of Eq. (A6) is the divergence of the electrostrictive force:

$$\vec{f} = \nabla p_{st} = \nabla \cdot \left[-\frac{1}{2} \epsilon_0 \gamma_e \left(\langle \tilde{E}_P \cdot \tilde{E}_S \rangle + \langle \tilde{E}_{Pr} \cdot \tilde{E}_{Sig} \rangle \right) \right], \tag{A8}$$

which yields, after applying the slowly varying amplitude approximation,

$$\nabla \cdot \vec{f} = \epsilon_0 \gamma_e q^2 (A_P A_S^* + A_{Pr} A_{Sig}^*) e^{i\Delta kz}, \tag{A9}$$

Where $\Delta k = (k_{Pr} - k_{Sig}) - (k_P - k_S)$ is the phase mismatch between the four optical fields. Only two electrostrictive

terms survive after accounting for the orthogonal polarization of the pump and Stokes fields with respect to that of the probe and backscattered signal. Inserting this electrostrictive force term and the acoustic field (Eq. (A5)) into Eq. (A6), and assuming a slowly varying acoustic amplitude, we find

$$-2i\Omega\frac{\partial\rho}{\partial t} - \Gamma'2iq^2\Omega\rho - 2iqv_s^2\frac{\partial\rho}{\partial z} = \epsilon_0\gamma_e q^2(A_P A_S^* + A_{Pr} A_{Sig}^*)e^{i\Delta kz},\tag{A10}$$

which can be restated in terms of the Brillouin linewidth, $\Gamma_B=q^2\Gamma'$, as

$$-2i\Omega\frac{\partial\rho}{\partial t} - 2i\Omega\Gamma_B\rho - 2iqv_s^2\frac{\partial\rho}{\partial z} = \epsilon_0\gamma_e q^2(A_P A_S^* + A_{Pr} A_{Sig}^*)e^{i\Delta kz}.$$
 (A11)

Given the phonon dispersion relations $\Omega_B = |q_B|v_s$ and $\Omega^2 = q^2(v^2 - i\Omega\Gamma')$, Eq. (A11) can be rewritten as

$$-2i\Omega\frac{\partial\rho}{\partial t} + \left(\Omega^2 - \Omega^2 - i\Omega\Gamma_B\right)\rho - 2iqv_s^2\frac{\partial\rho}{\partial z} = \epsilon_0\gamma_e q^2(A_P A_S^* + A_{Pr} A_{Sig}^*)e^{i\Delta kz}.$$
(A12)

We take the common assumption that the phonon propagation distance is small compared to the distance over which the source term varies significantly, which allows the spatial derivative term in Eq. (A12) to be dropped. We further assume steady-state conditions such that the time derivative term also vanishes, leaving

$$(\Omega_B^2 - \Omega^2 - i\Omega\Gamma_B)_\rho = \epsilon_0 \gamma_e q^2 (A_P A_S^* + A_{Pr} A_{Siq}^*) e^{i\Delta kz}. \tag{A13}$$

We thus find the acoustic field amplitude to be

$$\rho(z,t) = \epsilon_0 \gamma_e q^2 \frac{(A_P A_S^* + A_{Pr} A_{Sig}^*) e^{i\Delta kz}}{\Omega_B^2 - \Omega^2 - i\Omega \Gamma_B}.$$
(A14)

2. Optical Fields

We now turn to the spatial evolution of the optical fields, described by the wave equation,

$$\frac{\partial^2 \tilde{E}_i}{\partial z^2} - \frac{n^2}{c^2} \frac{\partial^2 \tilde{E}_i}{\partial t^2} = \frac{1}{\epsilon_0 c^2} \frac{\partial^2 \tilde{P}_i}{\partial t^2},\tag{A15}$$

where i denotes the four optical fields, namely: pump, Stokes, probe, and the backscattered signal. The total nonlinear polarization that gives rise to the source term in the wave equation is given by

$$\tilde{P} = \epsilon_0 \Delta \chi \tilde{E} = \epsilon_0 \Delta \epsilon \tilde{E} = \epsilon_0 \rho^{-1} \gamma_e \tilde{\rho} \tilde{E}. \tag{A16}$$

The parts of \tilde{P} that can act as phase-matched source terms for the optical fields are

$$\tilde{P}_{P} = p_{P}e^{i(k_{P}z - \omega_{P}t)} + c.c. = \frac{1}{2}\epsilon_{0}\rho_{0}^{-1}\gamma_{e}\rho A_{S}e^{i(k_{P}z - \omega_{P}t)}, \tag{A17}$$

$$\tilde{P}_S = p_S e^{i(-k_S z - \omega_S t)} + c.c. = \frac{1}{2} \epsilon_0 \rho_0^{-1} \gamma_e \rho^* A_P e^{i(-k_S z - \omega_S t)}, \tag{A18}$$

$$\tilde{P}_{Pr} = p_{Pr}e^{i(k_{Pr}z - \omega_{Pr}t)} + c.c. = \frac{1}{2}\epsilon_0\rho_0^{-1}\gamma_e\rho A_{Sig}e^{i(k_{Pr}z - \omega_{Pr}t)}e^{i\Delta kz}, \tag{A19}$$

$$\tilde{P}_{Sig} = p_{Sig}e^{i(-k_{Sig}z - \omega_{Sig}t)} + c.c. = \frac{1}{2}\epsilon_0\rho_0^{-1}\gamma_e\rho^*A_{Pr}e^{i(-k_{Sig}z - \omega_{Sig}t)}e^{-i\Delta kz}.$$
(A20)

Inserting the optical fields (Eqs. A1-A4) and phase-matched source terms (Eqs. A17-A20) into Eq. (A15), we obtain

$$\frac{\partial A_P}{\partial z} + \frac{n}{c} \frac{\partial A_P}{\partial t} = \frac{i\omega_P \gamma_e}{2nc\rho_0} \rho A_2, \tag{A21}$$

$$-\frac{\partial A_S}{\partial z} + \frac{n}{c} \frac{\partial A_S}{\partial t} = \frac{i\omega_S \gamma_e}{2nc\rho_0} \rho^* A_P, \tag{A22}$$

$$\frac{\partial A_{Pr}}{\partial z} + \frac{n}{c} \frac{\partial A_{Pr}}{\partial t} = \frac{i\omega_{Pr} \gamma_e}{2nc\rho_0} \rho A_{Sig}, \tag{A23}$$

$$-\frac{\partial A_{Sig}}{\partial z} + \frac{n}{c} \frac{\partial A_{Sig}}{\partial t} = \frac{i\omega_{Sig}\gamma_e}{2nc\rho_0} \rho^* A_{Pr}, \tag{A24}$$

We again assume steady-state conditions, allowing the time derivative term to be dropped. Plugging in the acoustic field amplitude (Eq. A14), we arrive at the coupled-amplitude wave equations for the optical fields,

$$\frac{\partial A_P}{\partial z} = \frac{i\epsilon_0 \omega_P q^2 \gamma_e^2}{2nc\rho_0} \frac{(A_P |A_S|^2 + A_{Pr} A_{Sig}^* A_S) e^{i\Delta kz}}{\Omega_B^2 - \Omega^2 - i\Omega \Gamma_B},\tag{A25}$$

$$\frac{\partial A_S}{\partial z} = -\frac{i\epsilon_0 \omega_S q^2 \gamma_e^2}{2nc\rho_0} \frac{(|A_P|^2 A_S^* + A_{Pr} A_{Sig}^* A_P) e^{-i\Delta kz}}{\Omega_B^2 - \Omega^2 + i\Omega \Gamma_B},\tag{A26}$$

$$\frac{\partial A_{Pr}}{\partial z} = \frac{i\epsilon_0 \omega_{Pr} q^2 \gamma_e^2}{2nc\rho_0} \frac{(A_P A_S^* A_{Sig} + A_{Pr} |A_{Sig}|^2) e^{i\Delta kz}}{\Omega_B^2 - \Omega^2 - i\Omega\Gamma_B},\tag{A27}$$

$$\frac{\partial A_{Sig}}{\partial z} = -\frac{i\epsilon_0 \omega_{Sig} q^2 \gamma_e^2}{2nc\rho_0} \frac{(A_P A_S^* A_{Pr} + |A_{Pr}|^2 A_{Sig}^*) e^{-i\Delta kz}}{\Omega_B^2 - \Omega^2 + i\Omega \Gamma_B}.$$
(A28)

We drop the very small signal amplitude terms on the right side of Eqs. A25-A28 and integrate each along the effective length to get the amplitudes,

$$A_P = \frac{i\epsilon_0 \omega_P q^2 \gamma_e^2}{2nc\rho_0} \frac{A_P |A_S|^2}{\Omega_B^2 - \Omega^2 - i\Omega\Gamma_B} \frac{e^{i\Delta kL} - 1}{i\Delta k},\tag{A29}$$

$$A_S = -\frac{i\epsilon_0 \omega_S q^2 \gamma_e^2}{2nc\rho_0} \frac{|A_P|^2 A_S^*}{\Omega_B^2 - \Omega^2 + i\Omega\Gamma_B} \frac{e^{-i\Delta kL} - 1}{-i\Delta k},\tag{A30}$$

$$A_{Pr} = \frac{i\epsilon_0 \omega_{Pr} q^2 \gamma_e^2}{2nc\rho_0} \frac{A_P A_S^* A_{Sig}}{\Omega_B^2 - \Omega^2 - i\Omega \Gamma_B} \frac{e^{i\Delta kL} - 1}{i\Delta k},\tag{A31}$$

$$A_{Sig} = -\frac{i\epsilon_0 \omega_{Sig} q^2 \gamma_e^2}{2nc\rho_0} \frac{A_P A_S^* A_{Pr}}{\Omega_B^2 - \Omega^2 + i\Omega \Gamma_B} \frac{e^{-i\Delta kL} - 1}{-i\Delta k}.$$
 (A32)

We focus on the signal amplitude given by Eq. A32, noting that close to resonance, the denomenator of the middle term containing Ω can be approximated as,

$$\Omega_B^2 - \Omega^2 + i\Omega\Gamma_B \approx \Omega_B(\Omega - \Omega_B + i\Gamma_B), \tag{A33}$$

giving

$$A_{Sig} = -\frac{i\epsilon_0 \omega_{Sig} q^2 \gamma_e^2}{2nc\rho_0} \frac{A_P A_S^* A_{Pr}}{\Omega_B (\Omega - \Omega_B + i\Gamma_B)} \frac{e^{-i\Delta kL} - 1}{-i\Delta k},\tag{A34}$$

and in fact on resonance the expression reduces to

$$A_{Sig} = -\frac{i\epsilon_0 \omega_{Sig} q^2 \gamma_e^2}{2nc\rho_0} \frac{A_P A_S^* A_{Pr}}{\Omega_B i\Gamma_B} \frac{e^{-i\Delta kL} - 1}{-i\Delta k}.$$
 (A35)

Using $q = 2k_P = 2\omega n/c$ and $q = \Omega_B/v_s$, we can express the leading terms as

$$A_{Sig} = -\frac{\epsilon_0 \omega^2 \gamma_e^2}{c^2 v_s \rho_0 \Gamma_B} A_P A_S^* A_{Pr} \frac{e^{-i\Delta kL} - 1}{-i\Delta k}, \tag{A36}$$

where we have dropped the signal designator on ω . Defining the brillouin gain factor, g_0 , as Boyd does,

$$g_0 = \frac{\gamma_e^2 \omega^2}{nvc^3 \rho_0 \Gamma_B},\tag{A37}$$

reduces this expression to

$$A_{Sig} = -\epsilon_0 ncg_0 A_P A_S^* A_{Pr} \frac{e^{-i\Delta kL} - 1}{-i\Delta k}.$$
(A38)

The intensity of the backscattered signal is given by the magnitude of the time-averaged Poynting vector, given by

$$I_i = 2n\epsilon_0 c|A_i|^2, \qquad i = 1, 2, 3, \dots$$
 (A39)

which produces for the signal intensity

$$I_{Sig} = 2\epsilon_0 nc(\epsilon_0 ncg_0)^2 |A_P|^2 |A_S^*|^2 |A_{Pr}|^2 \left| \frac{e^{-e\Delta kL} - 1}{-i\Delta k} \right|^2 = 2\epsilon_0^3 \epsilon_0 n^3 c^3 g_0^2 \frac{I_P}{2\epsilon_0 nc} \frac{I_S}{2\epsilon_0 nc} \frac{I_{Pr}}{2\epsilon_0 nc} \left| \frac{e^{-e\Delta kL} - 1}{-i\Delta k} \right|^2.$$
 (A40)

The squared modulus term containing Δk can be reduced as

$$\left| \frac{e^{-i\Delta kL} - 1}{-i\Delta k} \right|^2 = \frac{(e^{-i\Delta kL} - 1)(e^{i\Delta kL} - 1)}{(\Delta k)^2} = \frac{L^2}{(\Delta kL)^2} \left[2 - 2\left(\frac{e^{i\Delta kL} + e^{-1\Delta kL}}{2}\right) \right]$$

$$=\frac{2L^2(1-\cos\Delta kL)}{(\Delta kL)^2} = \frac{4L^2\sin^2\left(\frac{\Delta kL}{2}\right)}{\left(\Delta kL\right)^2} = \frac{L^2\sin^2\left(\frac{\Delta kL}{2}\right)}{\left(\frac{\Delta kL}{2}\right)^2} = L^2\sin^2\left(\frac{\Delta kL}{2}\right),\tag{A41}$$

giving as a final expression for backscattered signal intensity,

$$I_{Sig} = \frac{1}{4} (g_0 L)^2 I_P I_S I_{Pr} sinc^2 \left(\frac{\Delta kL}{2}\right). \tag{A42}$$

To find the power of the backscattered signal, we would integrate this intensity over the effective area. For a uniform area A_{eff} , this gives

$$P_{Sig} = I_{Sig} A_{eff} = \frac{1}{4} (g_0 L)^2 \frac{A_{eff}}{A_{eff}} I_P \frac{A_{eff}}{A_{eff}} I_S \frac{A_{eff}}{A_{eff}} I_{Pr} sinc^2 \left(\frac{\Delta kL}{2}\right) A_{eff}, \tag{A43}$$

or,

$$P_{Sig} = \frac{1}{4} (G_B L)^2 P_P P_S P_{Pr} sinc^2 \left(\frac{\Delta k L}{2}\right), \tag{A44}$$

where,

$$G_B = \frac{g_0}{A_{eff}}. (A45)$$

We can also see that off resonance, the Ω term from Eq. A34 goes to a lorentzian form after taking the squared modulus for intensity.

Appendix B: Scattered Power Comparison to Traditional Brillouin Scattering Processes

This appendix provides a comparative analysis of the scattered power produced by our instrument to that of standard Brillouin scattering processes-that is, spontaneous and stimulated Brillouin scattering. The difference in behavior of our instrument from the traditional techniques arises due to the coherent stimulation of the acoustic mode by the pump and Stokes fields, producing a 4-wave-coupled-amplitude interaction that yields much higher scattered powers in smaller lengths. While our instrument is particularly well suited to small interaction lengths due to enhanced phase-matching relaxation, it maintains production of a significant amount of scatterd power at greater lengths as well (greater than 1 meter). This is because the reduction in scattered power from the breakdown of phase-matching relaxation at greater lengths is perfectly counter-balanced by the quadradic dependence on length in the overall scattered power, as seen in Eq. 1. At very large lengths (greater than 1 km), the instrument is ultimately limited by the coherence length of the lasers employed, as the process relies on the coherent stimulation of the phonon mode and thus the mutual coherence of the pump and Stokes fields over the interaction length. Here we offer an exploration into the respective performance of each technique across the entire meaningful length scale, from nanometers to kilometers.

Despite shared dependence on basic Brillouin scattering principles, the three techniques compared here (spontaneous-, stimulated-, and coherently stimulated Brillouin scattering) yield significantly different scattered power for identical experimental paramters. At small lengths, the high-gain threshold for optical stimulation of the material fluctuations is often not achievable without the use of extremely large optical powers. This prevents the system from entering a process of exponential growth of the scattered Stokes light indicative of stimulated Brillouin scattering.[1] In this low-gain regime, any scattered Stokes light is spontanously scattered from thermal fluctuations of the material, or from quantum-mechanical fluctuations of materials at the ground state. The low-gain regime is defined by an overall process gain factor, denoted by $G = G_P P_P L$, which is much less than unity $(G \ll 1)$. Here, G_B is the effective Brillouin gain in $W^{-1}m^{-1}$ ($G_B = \frac{g}{A_{eff}}$), P_P is the pump power, and L is the effective length. This spontaneous scattering process follows a linear growth trend described by Boyd et al in 1990[21] as

$$R = \frac{\langle |E_S|^2 \rangle}{\langle |E_P|^2 \rangle} = (\bar{n} + 1)g\hbar\omega_S \Gamma_B \frac{L}{4A_{eff}},\tag{B1}$$

where R is the reflectivity, or the ratio of scattered Stokes intensity to incident pump intensity, and $\bar{n} = (e^{\frac{\hbar\Omega_B}{k_bT}} - 1)^{-1}$ is the mean number of phonons occupying the mode due to thermal fluctuations of the material. Rearranging this equation and converting to effective Brillouin gain, G_B , and power by applying the effective area, we arrive at the scattered power of the Stokes spontaneous Brillouin scattering process,

$$P_S = \frac{1}{4} G_B P_P L \hbar \omega_S \Gamma_B(\bar{n} + 1). \tag{B2}$$

At room temperature and typical Brillouin frequencies in the GHz range, the quantity $k_b T \gg \hbar \Omega_B$, allowing

$$e^{\frac{\hbar\Omega_B}{k_bT}} \approx 1 + \frac{\hbar\Omega_B}{k_bT}$$
 (B3)

to be a good approximation. We thus find that

$$(\bar{n}+1) \approx \bar{n} \approx \frac{k_b T}{\hbar \Omega_B}.$$
 (B4)

Inserting this reduced quantity into Eq. B2, we arrive at a convenient expression for the scattered power of the Stokes spontaneous Brillouin scattering process,

$$P_{S, SponBS} = \frac{G_B P_P L \omega_S \Gamma_B k_b T}{4\Omega_B}.$$
 (B5)

It may be noted that the derived expression for the low-gain spontaneous regime here matches the form reported by Kharel et al. in 2016 [22] for the complementary forward scattering processe. While the two scenarios—our backward scattering geometry versus the forward scattering geometry discussed by Kharel et al.—differ in directionality, the

underlying physics of light coupling to thermally excited acoustic modes is the same and reflects the fundamental similarity in how thermal phonons mediate the interaction between optical fields in the low-gain (spontaneous) regime.

Next we turn to the high-gain regime leading to a stimulated Brillouin scattering process. This regime is defined by an overall process gain factor, $G = G_P P_P L$, that is much greater than unity $(G \gg 1)$. For organic liquids, this crossover threshold from spontaneous to stimulated regimes occurs in the range of 20 < G < 25,[21] whereas for typical lengths of single mode fiber it can be lower[5] owing to the small effective area compared to longer effective lengths of fiber typically used.

The reflectivity of a stimulated Brillouin scattering process in the high-gain regime is given by [21]

$$R = \frac{\langle |E_S|^2 \rangle}{\langle |E_P|^2 \rangle} = \frac{Y}{\sqrt{\pi}} \frac{e^G}{G^{\frac{3}{2}}},\tag{B6}$$

where Y is the reflectivity of the low-gain (spontaneous) regime given above and G is the overall process gain factor, $G = G_P P_P L$. Again, converting to the effective Brillouin gain, G_B , and power by applying the effective area, we solve for the scattered power of the Stokes field,

$$P_{S, StimBS} = \frac{G_B P_P L \omega_S \Gamma_B k_b T}{4\sqrt{\pi}\Omega_B} \frac{e^G}{G^{\frac{3}{2}}}$$
(B7)

This expression captures the exponential growth in scattered power as any parameter within the overall process gain factor, $G = G_B P_P L$, increases. However, this exponential growth can only continue while the pump is not significantly undepleted. Once the scattered power described by Eq. B7 grows to a significant fraction of the driving pump power, the exponential increase in scattered Stokes power asymptotically approaches the pump power. For very large G, virtually all of the pump energy is converted to scattered Stokes energy in a complete transfer process.[1] To account for pump depletion, we numerically solve the transendental equation derived in Boyd's Nonlinear Optics which describes the effects of pump depletion, given here in terms of power as

$$P_S(L) = \frac{P_S(0)x(1-x)}{e^{G_B}P_P(0)L(1-x) - x},$$
(B8)

where $x = P_S(0)/P_P(0)$, or the ratio of the unknown Stokes power at the end of its journey through the medium (z = 0) to the known pump power at the beginning (also z = 0). This solution for x, specific to system parameters such as length, offers via its definition the solution to the unknown power of the scattered Stokes light at the end of its traversal through the effective length, given as

$$P_S(0) = xP_P(0).$$
 (B9)

The solution to this numeric approach to scattered power in the high-gain (stimulated) Brillouin scattering regime with pump depletion effects at large G is plotted for varying effective lengths in Fig. 7, along with the analytical solutions derived previously for the low-gain (spontaneous) regime and our coherently stimulated Brillouin spectrometer given by Eq. 1. System parameters used to generate the plot for each of the three processes are provided in Tables II and III. Wherever possible, the parameters shared by all three Brillouin scattering processes were kept consistent, while quantities unique to each process were assigned their respective values.

Coherently Stimulated Brillouin Scattering Process Model System Parameters

G_B		-			ı		$\Delta \lambda$
$0.6 \ W^{-1} m^{-1}$	1	W	1	W	1	W	20 pm

TABLE II: Parameters relevant to the coherently stimulated backward Brillouin scattering process for the example UHNA3 fiber. G_B is the effective Brillouin gain, P_P is the pump power, P_S is the Stokes power, P_{Pr} is the probe power, and $\Delta\lambda$ is the wavelength detuning of the probe from the pump.

At lengths beyond a centimeter, the phase-matching relaxation of the coherently stimulated process begins to break down, and the specific choice in pump and probe detuning becomes critical. This corresponds to a narrowing of the $sinc^2$ function given in Eq. 5. The scattered power beyond this length rises and falls according to the oscillations of the $sinc^2$ function far from the origin. As length increases continuously beyond 1 meter, the scattered power oscillates

Spontaneous and Stimulated Scattering Process Model System Parameters

G_B	P_P	$P_{S,seed}$	n	λ_P	Γ_B	k_B	T	Ω_B
$0.6 \ W^{-1} m^{-1}$	1 W	1 pW	1.48	$1549~\mathrm{nm}$	$2\pi \cdot 80 \text{ MHz}$	$1.38 \times 10^{-23} \text{ J/K}$	295 K	$2\pi \cdot 9.18 \text{ GHz}$

TABLE III: Parameters relevant to the spontaneous and/or stimulated backward Brillouin scattering processes for the example UHNA3 fiber. G_B is the Brillouin gain coefficient, P_P is the pump power, ω is the optical angular frequency, Γ_B is the acoustic damping rate, k_B is Boltzmann's constant, T is the temperature, and Ω_B is the acoustic angular frequency.

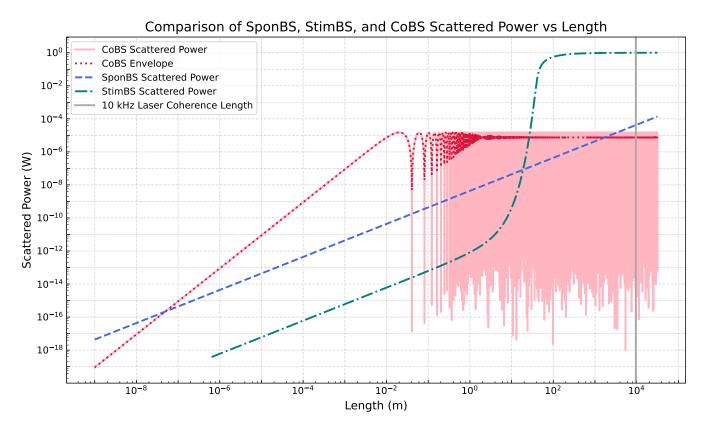


FIG. 7: Comparison of scattered power from a spontaneous Brillouin scattering process and our coherently stimulated Brillouin spectrometer.

with increasing frequency and ceases to offer practical significance. To better visualize the scattered power offered by the instrument in this region, we have computed the envelope of scattered power. In a laboratory setting, the appropriate pump and probe detuning would be selected for the specific sample length being measured such that the scattered power function lies on a local peak of the $sinc^2$ function.

Fig. 7 shows the advantage that our coherently stimulated Brillouin spectrometer offers compared to the traditional Brillouin processes for the example medium of UHNA3 fiber. For lengths up to about 50 meters and down to as low as 100 nanometers, the coherently stimulated process employed by our instrument offers superior scattered power, with the relative advantage peaking for a length just under 1 cm. At this length, the gain factor G places the traditional process within the low-gain (spontaneous) regime, and thus the scattered power generated is only on the order of 10s of picoWatts. In contrast, the scattered power for the same system offered by our instrument is on the order of 10s of microWatts, exceeding that of the spontenous process by a factor of a million. This is, of course, the most ideal case for this system, however it can be seen from Fig. 7 that the coherently stimulated process offers orders of magnitude more scattered power than either traditional process through a wide range of lengths.

Appendix C: Observance of Fano-Resonant Asymmetries at Small Signals

Appendix D: Pump, Stokes, and Probe Contribute Equally

Equation 1 gives the somewhat unintuitive result that the powers of the Pump, Stokes, and Probe waves contribute equally to the resulting scattered power of the Signal and invites verification with a miniexperiment. Initially, this experiment was motivated by a practical consideration: determination of whether the placement of a high power amplifier on any specific line of the setup (Pump, Stokes, or Probe) would offer any advantage over another.

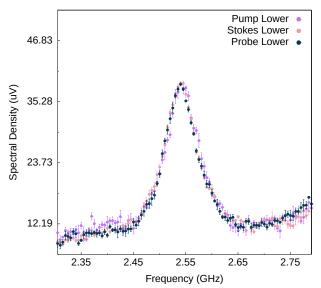
To test this, we conducted a controlled experiment with a 1 mm carbon disulfide (CS_2) sample. For each measurement, one of the three source powers (Pump, Stokes, or Probe) was systematically reduced by 75% while holding the others constant and ensuring consistent experimental conditions across trials. Table IV shows the respective powers for each source during the three measurements, along with the multiplicative total contribution of the three powers for each measurement towards the generation of scattered power of the Signal.

Measurement	Pump Power (mW)	Stokes Power (mW)	Probe Power (mW)	Total (mW ³)
Pump Lower	19.190	32.210	54.560	3.372×10^4
Stokes Lower	76.600	8.020	54.650	3.359×10^4
Probe Lower	76.600	32.530	13.480	3.359×10^4

TABLE IV: Power values for each source (Pump, Stokes, Probe) across the three measurements, with the multiplicative total power for each setup.

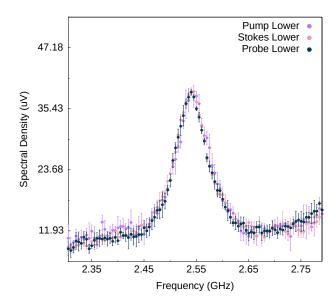
Figure 8a displays the average results from these three measurements, plotted with error bars representing one standard deviation of the mean. For increased certainty, Figure 8b presents the same data with error bars extended to two standard deviations, providing additional confidence in the reproducibility of the results. This experiment confirms that the scattered Signal power indeed depends equally on each of the three contributing wave powers, as expected from the theoretical framework. Consequently, boosting the power of any of the three sources affects the Signal power equally, allowing flexibility in pragmatic design across any of the three lines. Ultimately, this result reinforces the reliability of Equation 1 for predicting Signal power across a range of power distributions within practical settings.

1 mm CS2 CABS



(a) Signal power contributions with error bars representing one standard deviation of the mean for each measurement.

1 mm CS2 CABS



(b) Signal power contributions with error bars extended to two standard deviations of the mean for each measurement.

FIG. 8: Comparison of Signal power contributions with error bars representing one (a) and two (b) standard deviations of the mean for each measurement.

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