SMALL-SCALE COHERENTLY STIMULATED BRILLOUIN SPECTROSCOPY

By Joel N. Johnson

A Dissertation

Submitted in Partial Fulfillment
of the Requirements for the Degree of
Doctor of Philosophy
in Applied Physics and Materials Science

Northern Arizona University
!Month YYYY!

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Dedication

Preface

Introduction

Optomechanics is the study of light-matter interactions; it is the study of how the intangible (light) can affect change in the tangible (matter) and vice versa. Injecting light into a material under specific conditions allows for an exchange of energy to occur between the light and the mechanical oscillations of the material which changes the mechanical energy of the material. This interaction can be controlled to deposit or withdraw mechanical energy into/from a system and thus leave the system in a more, or less, mechanically energetic state respectively. The same interaction can also be harnessed for passive observation of material properties. Mechanical systems from bulk to atomic scales can be probed and characterized with light by retrieving the inelastically scattered light resulting from interaction with the material. This retrieved light contains embedded information about the energy exchange that occurred, which, when considered as part of a population of scattering events, reveals natural resonances of a mechanical system.

Optomechanics comprises a broad range of phenomena involving the interaction of optical and mechanical systems, from basic photothermal absorption to more complex nonlinear processes. Here I offer a brief overview of notable optomechanical phenomena then devote the remainder of this chapter to a more detailed description of the specific interactions that play a role in my research. Photothermal absorption is the process by which light is absorbed by a material, leading to an increase in temperature of the material and consequent changes in the material's dimensions (thermal expansion) or refractive index (thermo-optic effect). This effect has applications in optical switches, actuators, and sensors. Photothermal therapy in medicine is an emerging application of this effect, where light is used to target and heat specific areas, causing localized damage to diseased tissue. This technique becomes especially effective when combined with nanoparticle-enhanced absorption, allowing for dramatically increased absorption in ultra-localized zones within the body.

Light scattering, in its many forms, is also an optomechanical process as it involves the interaction of an optical field with the fluctuation, motion, or vibration of matter. Rayleigh scattering, perhaps the most well-known example, is the elastic scattering of light by particles much smaller than the wavelength of the light, leading to scattering in possibly a new direction but without a change in wavelength. It is responsible for the blue color of the sky because the efficiency of Rayleigh scattering is inversely proportional to the fourth power of the wavelength (λ) of the light ($\frac{1}{\lambda^4}$) and so shorter (blue) wavelengths are scattered much more than longer (red) wavelengths by the molecules in the atmosphere.

Raman scattering is the interaction of light with vibrational and rotational modes within a material (often molecular), resulting in scattered light with frequencies that are shifted from the incident light. This inelastically scattered light provides insights into the material's molecular structure and properties. Raman scattering is widely used in chemical and material science for identifying chemical compounds, analyzing molecular structures, and studying molecular dynamics. It finds application in the characterization of pharmaceuticals, monitoring changes in biological tissues for medical diagnostics, and investigation stress and temperature distributions in engineering materials, among others.

Brillouin scattering, around which much of my work is centered, is the scattering of light with acoustic phonons or coherent traveling density waves in a material, resulting in scattered light with a frequency that is slightly shifted from the incident light. This inelastically scattered light reveals mechanical properties of the material such as its bulk and elastic moduli. This phenomenon is used in materials science to measure elastic properties and viscoelasticity of materials, in fiber optic sensing to monitor temperature and strain over large distances, and in physics to study phase transitions and mechanical properties of crystals, liquids, and gases.

Rayleigh-wing scattering is the broad, smooth extension of the Rayleigh scattering spectrum that results from interactions with low-frequency excitations in a material, providing insights into dynamic processes like rotational and translational diffusion of molecules that make up a material. This scattering is particularly useful in studying the dynamics of complex fluids, gases, and soft materials, where it can reveal information about molecular orientation, diffusion rates, and interactions within the medium. Applications include the analysis of atmospheric phenomena, characterization of liquid crystals, and investigations into the properties of polymers and biological materials, aiding in the understanding of their behavior at the molecular level.

Figure 1.1 shows the relative domains of typical frequency shifts for Rayleigh, Rayleigh-wing, Brillouin, and Raman scattering. Rayleigh-wing scattering is broad and shares part of its domain with Brillouin scattering. This makes sense because the diffusive translational motion of molecules can be thought of as indistinguishable from traveling density waves which host brillouin scattering within the timescale that this motion occurs. In this way, Rayleigh-wing scattering represents a sporadic distribution of fleeting, localized Brillouin scattering. Of course, the difference between incoherent diffusion of molecules and coherently traveling acoustic modes within a material is an important distinction, however this thought experiment offers a perspective for bridging the gap between Rayleigh-wing and Brillouin scattering and understanding

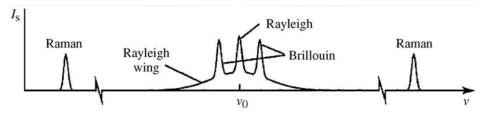


Figure 1.1: Relative domains of typical frequency shifts for Rayleigh, Rayleigh-wing, Brillouin, and Raman scattering.

their common frequency domains. Moreover, it serves as a reminder of the rich continuum of material behavior and responses that affect light scattering as opposed to the distinct categories we ascribe for convenience. This is a core concept of my work.

Returning to other optomechanical phenomena beyond scattering processes, the momentum of photons can exert forces on objects, leading to phenomena like radiation pressure, optical tweezing, and optical trapping. These effects are widely used in manipulating microscopic particles, biological cells, and atoms, enabling studies of single molecules, cold atoms, and quantum computing elements.

The final category of optomechanical interactions I will note here is that of nonlinear optical phenomena. Second harmonic generation, parametric oscillation, and four-wave mixing all feature the interaction between light and material nonlinearities that lead to the generation of new light frequencies. ¹ The Kerr effect is the change in the refractive index of a material in response to an applied electric field, which can be induced optically with sufficient intensities of light. In general, nonlinear optical responses of materials are often only accessible with the use of high intensity laser light. This is emphasized by the fact that the field of nonlinear optics can be traced back to the discovery of second-harmonic generation in 1961², just one year after the first demonstration of the laser by American physicist Theodor Maiman. ³ These nonlinear effects provide the foundation for a range of technologies, including high-speed optical communication systems, frequency converters, and lasers for materials processing.

Also included within nonlinear optical phenomena is electrostriction. Electrostriction is a reversible material deformation induced by an electric field, which can be generated by light in electro-optic materials. This effect is quadratic, scaling with the square of the applied electric field, and hence a nonlinear optical effect. At sufficiently high intensities, electrostrictive forces serve to enhance Brillouin scattering whereby the scattered light electrostrictively reinforces the acoustic wave that caused its scattering, leading to a nonlinear positive feedback loop known as stimulated Brillouin scattering Stimulated Brillouin Scattering (SBS). Photostriction is a related phenomenon that occurs when light absorption causes a change in the lattice structure of a material, leading to mechanical strain. It combines photovoltaic and piezoelectric effects and can be seen as an optically induced strain. These effects are utilized in designing optical modulators,

tunable photonic devices, and smart materials that respond to light.

In the remainder of this chapter I further describe the specific optomechanical phenomena that pertain to my research: Brillouin scattering, Raman scattering, and electrostriction as it pertains to the stimulated brillouin scattering process.

1.1 Spontaneous Brillouin Scattering

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1.2 Stimulated Brillouin Scattering

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1.3 Phase-matching

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1.4 Brillouin Gain of Materials

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1.5 Raman Scattering

1.6 Raman-like Brillouin Modes

Foundational Experimental Techniques and Instrumentation

This is an inline citation, ¹. This is a parenthetical citation ¹. This is a figure reference (Figure 1.1). This is a section reference §1.1. This is a chapter reference with chapter spelled out: chapter 3. This is an acronym definition American Geophysical Union (AGU). This is the second time I use the acronym in this section AGU. This is if I want to spell out the full acronym again American Geophysical Union (AGU). Define new acronyms in the acronyms.tex file.

2.1 Experimental Techniques

- 2.1.1 ways we can direct light in a photonic system
- 2.1.2 photonic devices and diagrams
- 2.1.3 ways we can select and isolate signals
- 2.1.4 heterodyne detection and the role of the LO
- 2.1.5 loss in a photonic system
- 2.1.6 free space optics and beam alignment
- 2.1.7 special fiber types and properties

2.2 Optical Instrumentation

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2.3 Electronic Instrumentation

2.4 Noise and Background Handling

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2.5 Custom Software

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2.5.1 Description of Python Script for CABS Data Collection

2.5.2 Description of Plotting Data in Go Program

Manuscript I: Laser cooling of traveling wave phonons in an optical fiber

- 3.1 Optomechanical Cooling and Heating
- 3.2 Cooling Platform: CS_2 -Liquid Core Optical Fiber
- 3.2.1 Optomechanical Properties
- 3.2.2 Fabrication
- 3.2.3 Fabrication Iterative Refinement
- 3.3 Intention of the Pump-Probe Experiment
- 3.4 Experimental Setup
- 3.4.1 Main Experiment
- 3.4.2 Pump-Probe Experiment
- 3.5 Results
- 3.5.1 Main Experiment Results
- 3.5.2 Pump-Probe Experiment Results
- 3.6 Discussion
- 3.6.1 Application to Ground State Cooling
- 3.6.2 Standardized Cooling Metric
- 3.6.3 Syncronous Achievement by Max Plank Group
- 3.6.3.1 Platform: Tapered chalcogenide Photonic Crystal Fiber

Manuscript II: A coherently stimulated phonon spectrometer

Joel N. Johnson^{1,2}, Nils T. Otterstrom³, Peter T. Rakich⁴, Ryan O. Behunin^{1,2}

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4.1 Abstract

4.2 Introduction

State of brillouin microscopy Applications and usefulness Challenges: selection of backscattered signal conflated with Stokes field phase-matching requires probe wavelength to be exactly that of Stokes Wouldn't it be nice if we could break free of strict phase-matching requirements, therefore perfectly isolating the signal In this work

4.2.1 Theory of CABS

description of physics with scattered power equation

4.2.2 Phase-matching at short lengths

phase-matching bandwidth description with equation

4.3 Methods

4.3.1 Theory of CABS

full CABS theory arriving at scattered power

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⁴ Department of Applied Physics, Yale University, New Haven, CT 06520, USA

4.3.2 Phase-matching bandwidth

phase-matching bandwidth theory

4.4 Results

4.4.1 Design of instrument

description of design figure: instrument apparatus design sensitivity measurements

4.4.2 From fiber-coupled to micrometer-scale free-space

figure: demonstration measurements 1mm uhna3 fiber 1mm CS2 bulk comparison to stimulated brillouin and spontaneous brillouin?

4.4.3 Relaxation of Phase-matching conditions

figure: phase-matching peak vs pump-probe separation 1cm uhna3, CS2 peak vs pump-probe separation 1mm uhna3, CS2

4.5 Discussion

4.6 Acknowledgements

4.7 Appendix

4.7.1 Equal contribution of P, S, Pr

figure: P, S, Pr equal contributors

100 μm CS2 CABS



Figure 4.1: CABS measurement of 100um of CS2.

Manuscript III: Brillouin-induced Raman modes

5.1 Abstract

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17

Table 5.1: Table caption.

	Parameter	Value	Description
	lat	-85°-85°	Latitude (35 bins in 5° increments)
Looleum	ALBEDO	0.05 – 0.225	Bolometric albedo (6 bins in 0.035 increments)
Lookup Variables	SLOPE	0°-90°	Surface slope (19 bins in 5° increments)
variables	SLOAZI	0°-360°	Surface azimuth (19 bins in 20° increments)
	DELLS	$4 \degree$	L_s step size (90 bins spanning 0°-360°)
	EMISS	0.96	Emissivity
	thick	0.05	Upper layer thickness [m]
	DENSITY	1100	Upper layer density [kg/m ³]
Thermal	DENS2	1800	Lower layer density [kg/m ³]
Parameters	lbound	18	Interior heat flow $[mW/m^2]$
	PhotoFunc	0.045/albedo	Photometric function (Keihm-style)
	SphUp0/SphLo0	602.88098583	
	SphUp1/SphLo1	235.98988249	Specific heat capacity expressed as 4th-order
	SphUp2/SphLo2	-29.59742178	polynomial $(c0 + c1 \cdot T + c2 \cdot T^2 + c3 \cdot T^3)$
	$\mathrm{SphUp3/SphLo3}$	-3.78707193	,
Temperature-dependent parameters	ConUp0 ConUp1 ConUp2 ConUp3	0.00133644 0.00073150 0.00033250 0.00005038	Upper layer conductivity expressed as 4th-order polynomial $ (c0+c1\cdot T+c2\cdot T^2+c3\cdot T^3) $
	ConLo0	0.00634807	T 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
	ConLo1	0.00347464	Lower layer conductivity expressed as
	ConLo2	0.00157938	4th-order polynomial
	ConLo3	0.00023930	$(c0 + c1 \cdot T + c2 \cdot T^2 + c3 \cdot T^3)$
	body	Moon	Target body
	k_style	Moon	Conductivity style (Moon for airless bodies)
	LKofT	${ m T}$	Temperature-dependent conductivity
Model Setup	FLAY	0.01	First layer thickness [m]
Parameters	RLAY	1.3	Layer thickness multiplier
	N1	26	Number of layers
	N24	288	Timesteps per day (5 min steps)
	DJUL	0	Start date

Manuscript IV: Nanoscale Brillouin scattering

6.1 Abstract

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luctus mauris.

6.2 Introduction

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cursus luctus mauris.

19

Table 6.1: Table caption.

	Parameter	Value	Description
	lat	-85°-85°	Latitude (35 bins in 5° increments)
Lookup	ALBEDO	0.05 – 0.225	Bolometric albedo (6 bins in 0.035 increments)
Lookup Variables	SLOPE	0°-90°	Surface slope (19 bins in 5° increments)
variables	SLOAZI	0°-360°	Surface azimuth (19 bins in 20° increments)
	DELLS	$4\degree$	L_s step size (90 bins spanning 0°-360°)
	EMISS	0.96	Emissivity
	thick	0.05	Upper layer thickness [m]
	DENSITY	1100	Upper layer density [kg/m ³]
Thermal	DENS2	1800	Lower layer density [kg/m ³]
Parameters	lbound	18	Interior heat flow [mW/m ²]
	PhotoFunc	0.045/albedo	Photometric function (Keihm-style)
	SphUp0/SphLo0	602.88098583	
	SphUp1/SphLo1	235.98988249	Specific heat capacity expressed as 4th-order
	SphUp2/SphLo2	-29.59742178	polynomial $(c0 + c1 \cdot T + c2 \cdot T^2 + c3 \cdot T^3)$
	$\mathrm{SphUp3/SphLo3}$	-3.78707193	
Temperature-dependent parameters	ConUp0 ConUp1 ConUp2 ConUp3	0.00133644 0.00073150 0.00033250 0.00005038	Upper layer conductivity expressed as 4th-order polynomial $(c0+c1\cdot T+c2\cdot T^2+c3\cdot T^3)$
	ConLo0 ConLo1 ConLo2 ConLo3	0.00634807 0.00347464 0.00157938 0.00023930	Lower layer conductivity expressed as 4th-order polynomial $(c0 + c1 \cdot T + c2 \cdot T^2 + c3 \cdot T^3)$
	body	Moon	Target body
	k_style	Moon	Conductivity style (Moon for airless bodies)
	LKofT	${ m T}$	Temperature-dependent conductivity
Model Setup	FLAY	0.01	First layer thickness [m]
Parameters	RLAY	1.3	Layer thickness multiplier
	N1	26	Number of layers
	N24	288	Timesteps per day (5 min steps)
	DJUL	0	Start date

Discussion & Conclusion

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Appendix A

Acronyms

 ${f SBS}$ Stimulated Brillouin Scattering

AGU American Geophysical Union

Appendix B

 \mathbf{Code}

B.1 Python Code for CABS Data Collection

B.2 Plotting Data In Go Program

Appendix C

Supplementary Information for Chapter 3: Manuscript I

C.1 Data

Appendix D

Supplementary Information for Chapter 4: Manuscript II

D.1 Data

References

- [1] Robert W Boyd. Nonlinear optics. Academic press, 2020.
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