

EEE105 Tutorial Questions & Review Topics W11

Fundamental Constants

Boltzman Constant, $k = 1.381 \times 10^{-23} \text{ JK}^{-1} = 8.62 \times 10^{-5} \text{ eVK}^{-1}$

Charge on Electron, $q = 1.602 \times 10^{-19} \text{ C}$

Mass of the Electron, $m_e = 9.11 \times 10^{-31} \text{ kg}$

Planck's Constant, $h = 6.626 \times 10^{-34} \text{ Js}$

Speed of Light in a Vacuum, $c = 3 \times 10^8 \text{ ms}^{-1}$

Mass of a Proton, $m_p = 1.673 \times 10^{-27} \text{ kg}$

Permittivity of Free Space, $\epsilon_0 = 8.85 \times 10^{-12} \text{ Fm}^{-1}$

Avogadro's Number, $A = 6.0221415 \times 10^{23}$

1. A certain n-p-n bipolar transistor has the following properties:

emitter resistivity	$3 \times 10^{-4} \Omega\text{m}$
base resistivity	$6 \times 10^{-3} \Omega\text{m}$
cross-sectional area	10^{-8} m^2
electron mobility	$0.13 \text{ m}^2\text{V}^{-1}\text{s}^{-1}$
hole mobility	$0.05 \text{ m}^2\text{V}^{-1}\text{s}^{-1}$
intrinsic carrier density	$1.5 \times 10^{16} \text{ m}^{-3}$

The transistor is operated at 20°C with a base-emitter applied voltage of 0.65 V and a collector voltage of 10 V .

Determine:

- (a) the majority and minority carrier concentrations in base and emitter

($n_n = 1.6 \times 10^{23} \text{ m}^{-3}$, $p_n = 1.4 \times 10^9 \text{ m}^{-3}$, $p_p = 2.1 \times 10^{22} \text{ m}^{-3}$, $n_p = 1.1 \times 10^{10} \text{ m}^{-3}$)

- (b) the built-in potential at the base-emitter junction

(0.77 V)

- (c) the base-emitter junction current, assuming a saturation current density of $1 \mu\text{A m}^{-2}$

(1.52 mA)

- (d) the approximate ratio of electron to hole currents flowing across the base-emitter junction

($20:1$)

- (e) the collector current, neglecting recombination in the base and leakage current

(1.45 mA)

n.b. In order to make the sheet more similar to the exam – a full list of constants is provided so as to not give any “clues”....

Revision Topics, Bipolar Junction Transistor....

Solutions

1.(a) For the majority carrier concentrations, use the standard equation for resistivity:

$$\rho = \frac{1}{nq\mu}$$

and apply to the emitter and the base. The resistivities and mobilities are given so you should find

$$p = 2.08 \times 10^{22} \text{ m}^{-3}$$

$$n = 1.6 \times 10^{23} \text{ m}^{-3}$$

Looking at these numbers, they are reasonable for majority carrier densities. To get the minority carrier concentrations use $p_n = n_i^2$. The intrinsic carrier concentration is given so:

$$n_p = 1.08 \times 10^{10} \text{ m}^{-3}$$

$$p_n = 1.4 \times 10^9 \text{ m}^{-3}$$

As expected, these are much smaller than the majority carrier concentrations.

(b) For this, you need to remember that the built in potential across a junction is given by

$$V_0 = \frac{kT}{q} \ln \left(\frac{n_n}{n_p} \right)$$

Putting in the values calculated in (a) gives $V_0 = 0.77 \text{ V}$

Try using the equation for the holes and prove that it gives the same result.

(c) To calculate the base emitter current, first calculate the current density. Remember that

$$J = J_0 \left(e^{\frac{qV}{kT}} - 1 \right)$$

You're told the applied voltage is 0.65 V and the saturation current density is $1 \mu\text{A m}^{-2}$. You should get an answer around $1.52 \times 10^{-3} \text{ A}$

(d) The ratio of electron and hole currents across a junction can be considered to be controlled by the ratios of conductivity. **So the electron current is 20 times the hole current.** Of course this is what we want in a bipolar transistor since we want most of the emitter current to be due to carriers injected from the emitter into the base.

(e) Note that if we neglect any recombination in the base, then all the electrons injected at the emitter will reach the collector. Written another way $I_C = I_e$

We know the emitter current (from part c) and the proportion of that due to electrons (from part d)

$$I_E = I_e + I_h = I_e \left(1 + \frac{1}{20} \right) = \frac{21}{20} I_e$$

$$\therefore I_C = \frac{20}{21} I_E = 1.45 \text{ mA}$$