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**DEPARTMENT OF ELECTRONIC AND ELECTRICAL ENGINEERING**

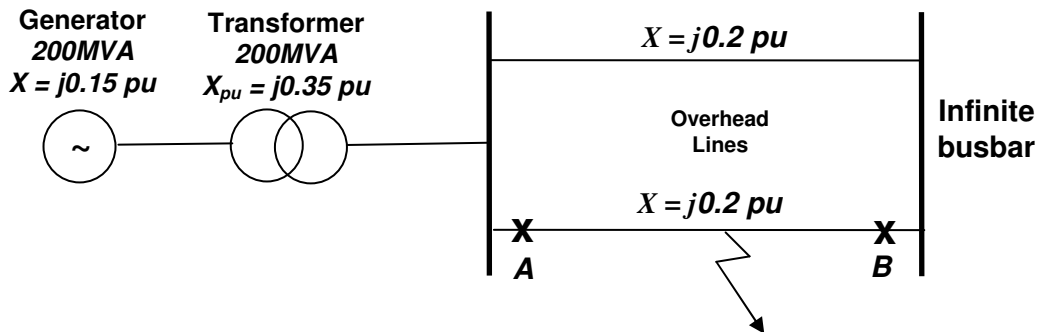
**Spring Semester 2014-15 (2.0 hours)**

**EEE301 Power Systems Engineering**

Answer **THREE** questions. **No marks will be awarded for solutions to a fourth question.** Solutions will be considered in the order that they are presented in the answer book. Trial answers will be ignored if they are clearly crossed out. **The numbers given after each section of a question indicate the relative weighting of that section.**

1.

- a. What is meant by a synchronous machine “losing synchronisation”. Explain why this is undesirable. (2)
- b. A 200MVA generator is connected to an infinite busbar via a transformer and a pair of identical overhead transmission lines, each having negligible resistance and a reactance of  $j0.2$  pu as shown in figure 1.1. The generator voltage is 1.1 pu and the voltage of the infinite busbar is 1.0 pu.



**Figure 1.1 Generator and transmission system.**

- (i) Determine the power-load angle equation for the system. If the generator is delivering 180MW, calculate its load angle. (3)
- (ii) When a 3-phase short-circuit occurs at the middle of one of the overhead transmission lines, between A and B, the effective system reactance becomes  $j1.9$ pu. Determine the power-load angle equation for the system under fault conditions. (1)
- (iii) The short-circuit is then cleared by the simultaneous opening of the circuit breakers, A and B at each end of the faulted line. Determine the new power-load angle equation for the system. (1)
- (iv) Sketch the power transfer curves for before, during, and after the fault. Mark on the sketch the accelerating area, decelerating area, and the critical load angle. (3)
- (v) By deriving an analytical expression or otherwise, determine the critical switching angle at which the fault must be cleared in order to ensure system stability. (5)
- c. If the circuit breakers clear the fault in 0.2s determine if this is sufficient to maintain system stability if the inertia constant of the generator,  $M = 2.5 \times 10^{-4}$  pu. Use a time interval,  $\Delta t = 0.05$ s in conjunction with the swing equation.

$$\left( \text{Use may be made of the equation: } \Delta\delta_n = \Delta\delta_{n-1} + \frac{(\Delta t)^2}{M} P_{a(n-1)} \right) \quad (5)$$

2.

Figure 2.1 shows the single-line diagram of a power system comprising three 132kV busbars, *Bus 1*, *Bus 2* and *Bus 3*, connected together by overhead transmission lines, *L1* and *L2*. Each busbar is supplied by a generator via a step-up transformer. Generator, *G2*, has its star point earthed through a reactor,  $X_N$ , of  $j0.3\Omega$ , all other star points in the system are solidly earthed. A single phase to earth fault occurs on one end of *L2*, as shown.

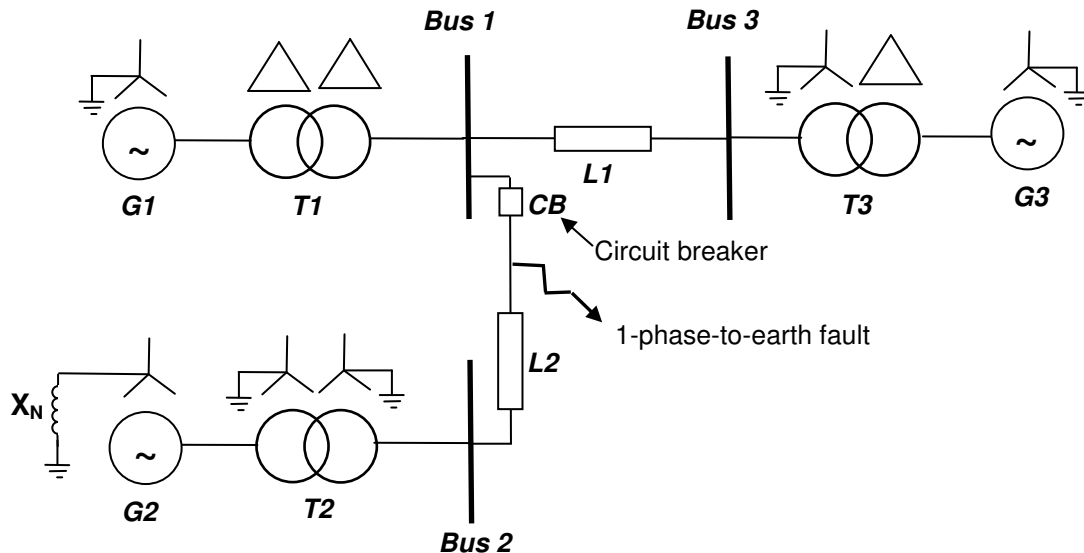


Figure 2.1 Line diagram of power system

	Rating MVA	Voltage kV	$X_+$	$X_-$	$X_0$
<i>G1</i>	100	25	$j0.1 \text{ pu}$	$j0.1 \text{ pu}$	$j0.08 \text{ pu}$
<i>G2</i>	120	25	$j0.15 \text{ pu}$	$j0.18 \text{ pu}$	$j0.14 \text{ pu}$
<i>G3</i>	80	19.5	$j0.08 \text{ pu}$	$j0.08 \text{ pu}$	$j0.06 \text{ pu}$
<i>T1, T2</i>	120	25/132	$j0.12 \text{ pu}$	$j0.12 \text{ pu}$	$j0.12 \text{ pu}$
<i>T3</i>	80	20/132	$j0.06 \text{ pu}$	$j0.06 \text{ pu}$	$j0.06 \text{ pu}$
<i>L1, L2</i>	-	132	$j8\Omega$	$j8\Omega$	$j30\Omega$

- Calculate all the per-unit reactances of the system using a reference base of 120MVA. (6)
- Draw the positive, negative and zero sequence diagrams for the system and determine  $Z_+$ ,  $Z_-$  and  $Z_0$ . (7)
- Determine the total fault current when a single phase-to-earth fault occurs at one end of line, *L2*, as shown in Figure 2.1. (3)
- If each phase of circuit breaker *CB* is set to trip on an over-current of 2500A explain whether circuit breaker *A* is adequately rated for this type of fault. (4)

**3.**

- a.** Give two examples of the sources of short circuits in power systems and explain why protection is required. (2)
- b.** (i) Sketch a diagram showing the main components of an induction relay and explain its operation. (3)
- (ii) Describe a type of protection relay which may be used to detect faults in an oil-filled transformer and explain its operation. (3)
- c.** (i) Explain what is meant by time and current grading in relation to power system protection. (5)
- (ii) Describe, with the aid of a suitable diagram, how protection may be achieved for a 2 source system using directional relays. (3)
- d.** (i) Explain why a current transformer should never be operated without a load. (2)
- (ii) A 5A current transformer is used to monitor a busbar carrying a maximum current of 15000A. If the reluctance of the core is  $3 \times 10^5 \text{ H}^{-1}$  and the frequency is 50Hz, estimate the typical emf produced if the load on the secondary winding is accidentally removed. (2)

4.

- a. Show that, if skin effect is neglected, the component of self-inductance due to the magnetic field within a solid circular conductor is independent of the radius of the conductor. (5)
- b. Show that the geometric mean radius of the 7-strand conductor shown in figure 4.1, in which the radius of each strand is 1.5mm, is approximately 3.27mm.

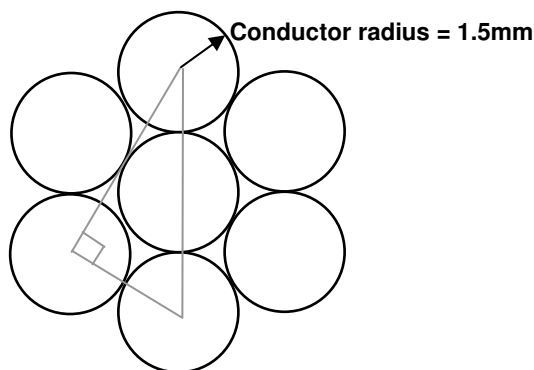


Figure 4.1: 7-strand conductor

(6)

- c. A three phase, 50Hz transmission line has its phases arranged in a flat, horizontal formation. The spacing between phases is 1.4m, and the phases are fully transposed, determine the reactance per kilometre if:
- (i) the line has one solid conductor of 4mm radius per phase (3)
- (ii) the line has a 7-strand conductor, as described in part (b), per phase (1)

(You may assume the inductance per metre for the fully transposed line is given by:

$$L = 2 \times 10^{-7} \ln \left( \frac{D_g}{R_g} \right) \text{ H/m}$$

where  $D_g$  is the geometric mean distance between conductors, and  $R_g$  is the geometric mean radius of the conductors).

- d. If the transmission line using the stranded conductors (see part c(ii) above) is 20km long and supplies a 11kV, 400kW load at 0.8 power factor lagging, calculate the line voltage at the sending end of the line. The resistance of the stranded conductor is  $0.25\Omega/\text{km}$ . (4)
- e. Suggest two mechanisms by which the voltage at the receiving end of the line could be regulated. (1)

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