



The
University
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EEE105

“Electronic Devices”

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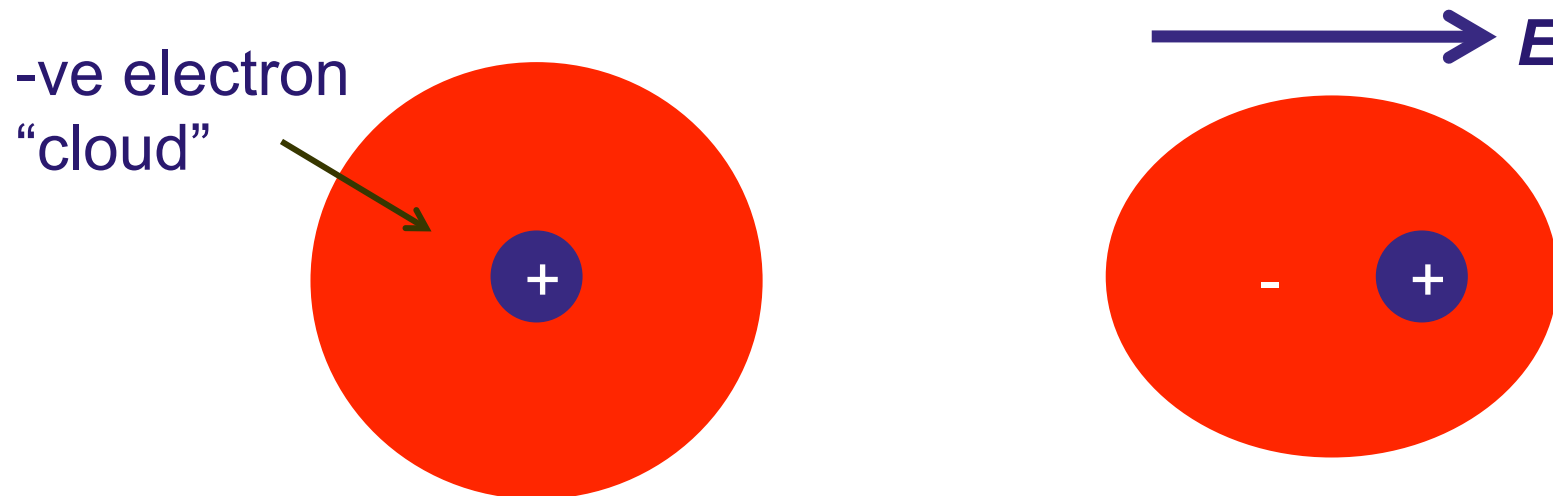
Lecture 3

- Insulator Review
- Polarization
- Capacitors
- RC time constant

Insulators

- Insulators –electrons in bands for which a large amount of energy is required to promote them to the conduction band – essentially the charge remains in the chemical bonds
- e.g. NaCl, C (diamond)
- Used as “Jam in the sandwich” in capacitors – termed a dielectric - insulation between conductors which modifies capacitor performance

Electronic Polarization -Dielectric



- When a system is subject to an electric field, \mathbf{E} , there is a tendency of the +ve and -ve charge to displace relative to one another so the system has an electric dipole moment. The dipole moment per unit volume is the polarization \mathbf{P} . See EEE101.

Permittivity

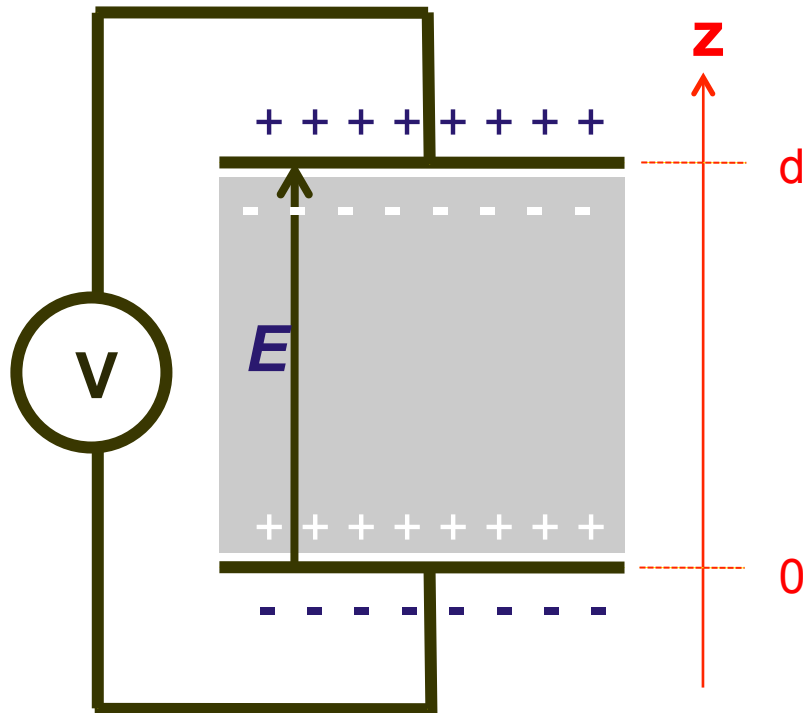
- **Permittivity**, ϵ , is a physical property of a solid (dielectric medium). Measure of the ability of the material to polarize in response to the field, and thereby reduce the total electric field inside the material. It is a measure of how easily the material “permits” the electric field to propagate.
- We usually compare the permittivity of a material to free space (i.e. vacuum) ϵ_0 ($= 8.8 \times 10^{-12}$ F/m) through the relative permittivity ϵ_r
- The permittivity of air \sim permittivity of free space so $\epsilon_r = 1$ for air

$$\epsilon = \epsilon_0 \epsilon_r \quad \text{Often we forget to mention } \epsilon_0 \text{ but it is important!}$$

Polarization Mechanisms

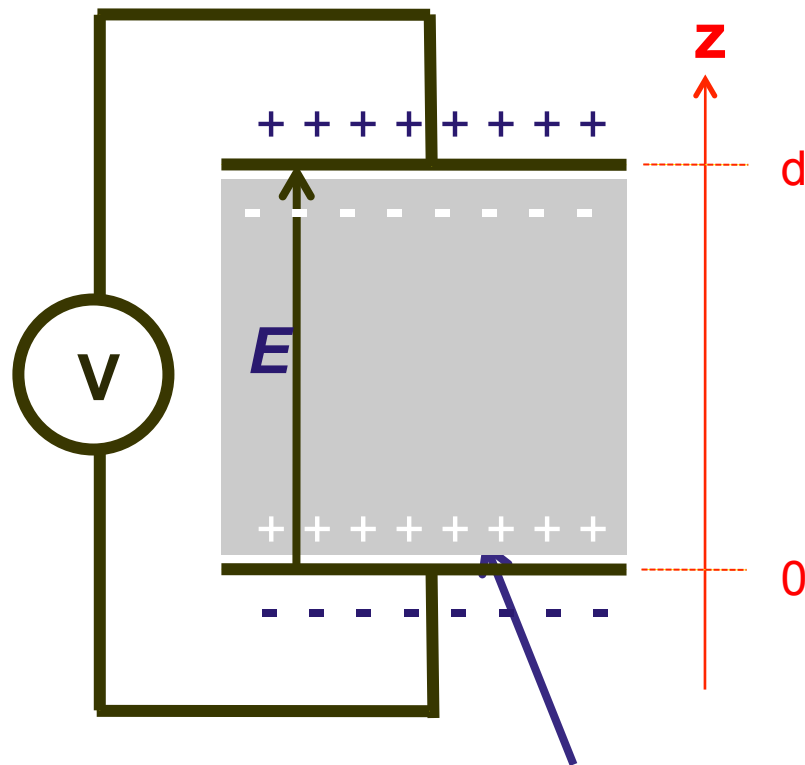
- **Electronic or Induced Polarization.** All dielectric materials – fast frequency response $\sim 10^{15} \text{ s}^{-1}$
- **Ionic Polarization** – In ionic crystals e.g. NaCl E field can shift sub lattice of Na^+ and Cl^- ions. Moderate frequency response $\sim 10^9 \text{ s}^{-1}$
- **Orientational Polarization** – can have a dipole within a molecule (polar molecule). E field aligns randomly oriented dipoles causing net polarization. Important for liquids & gases. Slow frequency response $\sim 10^4 \text{ s}^{-1}$
- Moving charge and molecules takes energy – loss appears as resistive component to impedance – energy is lost – “leaky”

Dielectric Capacitor



- In response to an E -field a dielectric produces a polarization
 - Dipoles below surface cancel out – only consider surface charge
 - Displaced surface charge opposite the capacitor plates
- Charge on plates to maintain E -field
- Capacitance, $C=Q/V$ where Q = charge and V = voltage

Dielectric Capacitor



Charge per unit area $= Q/A = \rho$

$$V = \int_0^d E \, dz = \int_0^d \frac{\rho}{\epsilon} \, dz$$

$$= \frac{\rho d}{\epsilon} = \frac{Qd}{\epsilon A}$$

inserting $C = \frac{Q}{V}$

$$C = \frac{\epsilon A}{d}$$

where $\epsilon = \epsilon_0 \epsilon_r$

ϵ_r = relative permittivity

Dielectric Breakdown

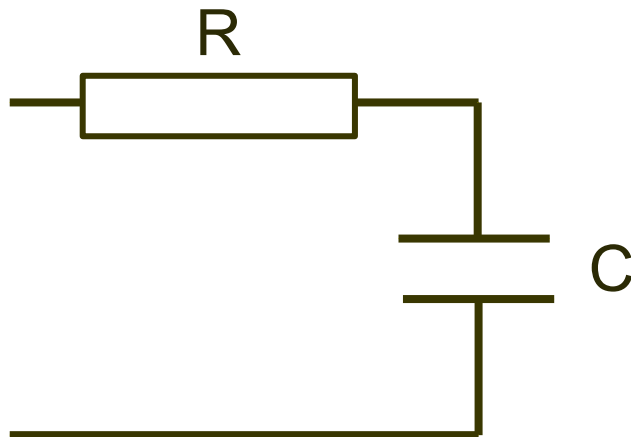
- Sudden increase in current above a critical electric field
- Limitation to dielectric – capacitor or insulator become a ~short circuit
- Can be reversible or non-reversible (i.e. catastrophic)
- Breakdown E-field can be $\sim 10^9 \text{ Vm}^{-1}$
- Ideally as high as possible

Ideal Capacitor Dielectric

- High ϵ_r
- Breakdown only at very high fields
- Low cost
- Manufacturability of thin films
- Reliability

RC Time Constant

- Vital importance to many areas of operation of devices
- Often a fundamental limit to high frequency operation



$$f_c = \frac{1}{2\pi RC}$$

For high frequency response
– small R and C

$$C = \frac{\epsilon A}{d}$$

Summary

- In an insulator charge is not free to move around the crystal
- In some materials their positions around the nuclei can be distorted if an E-field is applied - Polarization
 - This distortion leads to a surface charge which opposes the applied field – there is an increase in capacitance as ϵ increases
- Different polarization mechanisms have different frequency responses and different breakdown/failure mechanisms
- Breakdown and Ideal dielectric discussed
- RC time constant discussed as a vital factor which impacts device dimensions and dielectric choice

Capacitor Example

Q- For the same capacitor the new dielectric between the plates has a breakdown field of 50 MVm^{-1}

What is the maximum voltage which can be applied across the capacitor?

A- The maximum voltage will be that which gives breakdown field

$E = V/d$ so

$$V_{\text{max}} = E_{\text{Breakdown}} \times d_2 = 50 \times 10^6 \text{ Vm}^{-1} \times 10^{-3} \text{ m} = 50 \text{ kV}$$

Capacitor Example

Q- A parallel plate capacitor has a spacing $100\text{ }\mu\text{m}$ with air between them. If a dielectric plate of relative permittivity $\epsilon_r = 10$ is placed between the plates what should the new spacing be to leave the capacitance unchanged?

A- Capacitance needs to be constant in state “1” (before) and state “2” (after).

$$C = \frac{\epsilon_0 \epsilon_{r1} A}{d_1} = \frac{\epsilon_0 \epsilon_{r2} A}{d_2}$$

giving –

$$d_2 = \frac{\epsilon_{r2}}{\epsilon_{r1}} d_1 = \frac{10}{1} \cdot 1 \times 10^{-4}$$

$$d_2 = 1\text{mm}$$