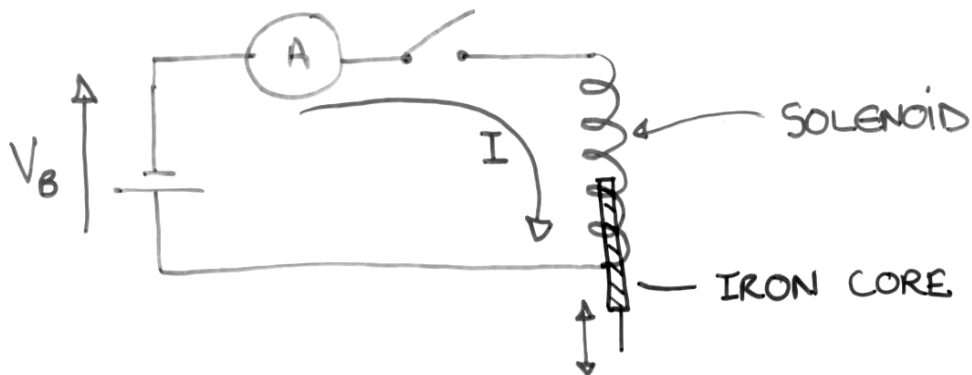
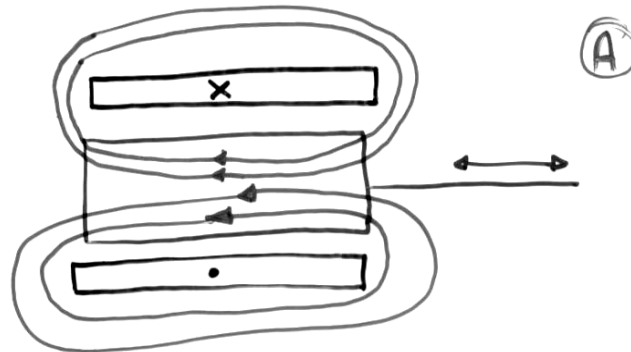


SELF EXCITED ACTUATORS



INITIALLY THE IRON CORE IS INSERTED IN SOLENOID.



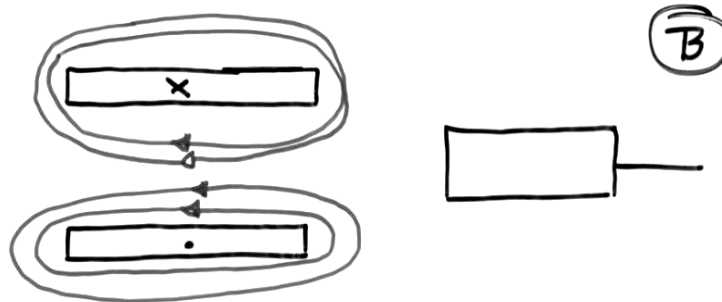
THE STRENGTH OF THE FIELD OR FLUX LINKING THE SOLENOID IS HIGH SINCE THE IRON CORE HAS A HIGH PERMEABILITY (LOW RELUCTANCE).

THE MAGNETIC STORED ENERGY IS HIGH:

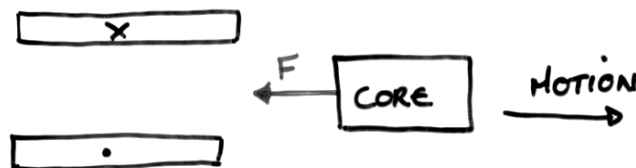
$$I = \frac{V_B}{R}$$

← SOLENOID RESISTANCE

FINALLY THE IRON CORE IS FULLY REMOVED.
THE AMPERE-TURNS OF THE SOLENOID NOW
FORM A FIELD IN AIR, HENCE THE FIELD
STRENGTH AND STORED MAGNETIC ENERGY IS
LOW.



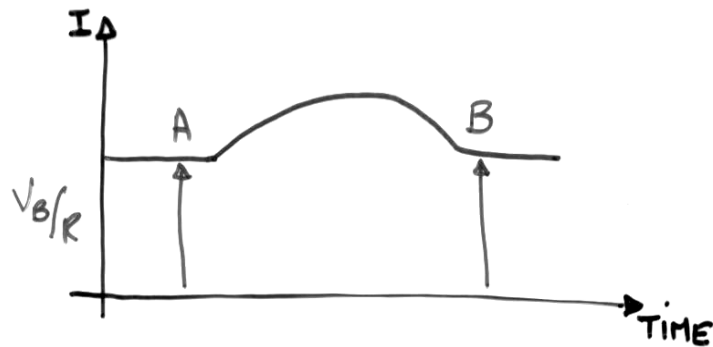
IN THE REMOVAL OF THE IRON CORE,
MECHANICAL WORK HAS TO BE PERFORMED. THE
ACTION OF THE SOLENOID IS TO 'SUCK' THE
IRON CORE INTO ITS CENTRE.



ie. IN MOVING FROM A TO B MECHANICAL WORK
IS PUT INTO THE SYSTEM.

ALSO IT IS NOTED THAT DURING THE MOTION
FROM A TO B THE CURRENT IN THE SOLENOID
INCREASES.

④



HENCE IN MOVING FROM A TO B THE BATTERY OUTPUT ENERGY INCREASES.

High STORED MAGNETIC ENERGY
 + MECHANICAL ENERGY INPUT TO THE SYSTEM
 + ADDITIONAL ELECTRICAL ENERGY FROM BATTERY

≡
 EQUATES A LOW STORED MAGNETIC ENERGY
 + ADDITIONAL LOSS IN THE SOLENOID WINDING (I^2R)
 + SMALL ENERGY ELEMENT OF IRON LOSS IN THE CORE.

CONSIDER FLUX LINKAGE OF THE SOLENOID

$$\text{FLUX LINKAGE} = \Psi$$

$$\text{FLUX } \phi = \int B \cdot dA \quad \begin{array}{l} \text{AREA} \\ \text{FLUX DENSITY} \end{array}$$

$$\text{FLUX LINKAGE } \Psi = N\phi$$

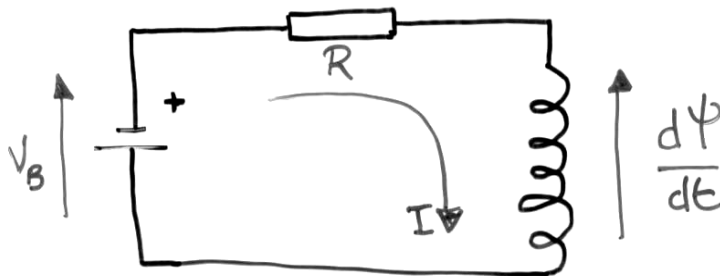
(1)

IE. FLUX LINKAGE OF A PARTICULAR COIL SYSTEM RELATES TO THE NUMBER OF TURNS AND THE EFFECTIVE FLUX WHICH COUPLES THOSE TURNS. (52)

FARADAY CHANGE IN FLUX LINKAGE LEADS TO AN INDUCED VOLTAGE WITH MAGNITUDE

$$\frac{d\psi}{dt}$$

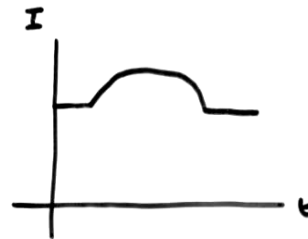
CONSIDER THE SOLENOID EXPERIMENT DURING THE MOTION



INITIALLY ψ IS A HIGH VALUE WITH THE CORE INSERTED AND AS THE CORE IS REMOVED, THE FLUX LINKAGE DECREASES.

$$\frac{d\psi}{dt} < 0$$

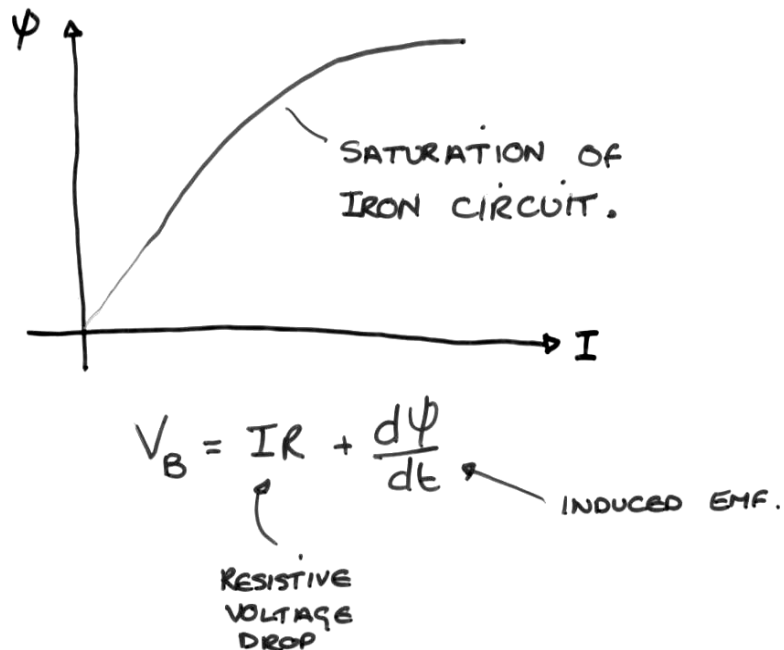
$$I = \frac{V_B - \frac{d\psi}{dt}}{R}$$



AND SINCE $\frac{d\psi}{dt} < 0$ $I > \frac{V_B}{R}$ DURING THE MOTION.

Ψ -I DIAGRAM

ie. CONSIDER A SOLENOID WITH AN IRON CORE (OR ANY OTHER MAGNETIC CIRCUIT)



$$V_B I = I^2 R + I \frac{d\Psi}{dt}$$

INPUT ELECTRICAL POWER

LOSS

$$\Rightarrow V_B I dt = I^2 R dt + I d\Psi$$

ENERGY INPUT

ENERGY LOSS

ENERGY INPUT TO MAGNETIC SYSTEM.

(63)

IN THE CASE OF NO MECHANICAL MOTION
THEN $I d\psi$ RELATES TO THE ENERGY INPUT
INTO THE MAGNETIC SYSTEM WHICH FORMS THE
STORED ENERGY.

E.G. THE TOTAL MAGNETIC ENERGY STORED
IN A MAGNETIC CIRCUIT IS GIVEN BY:

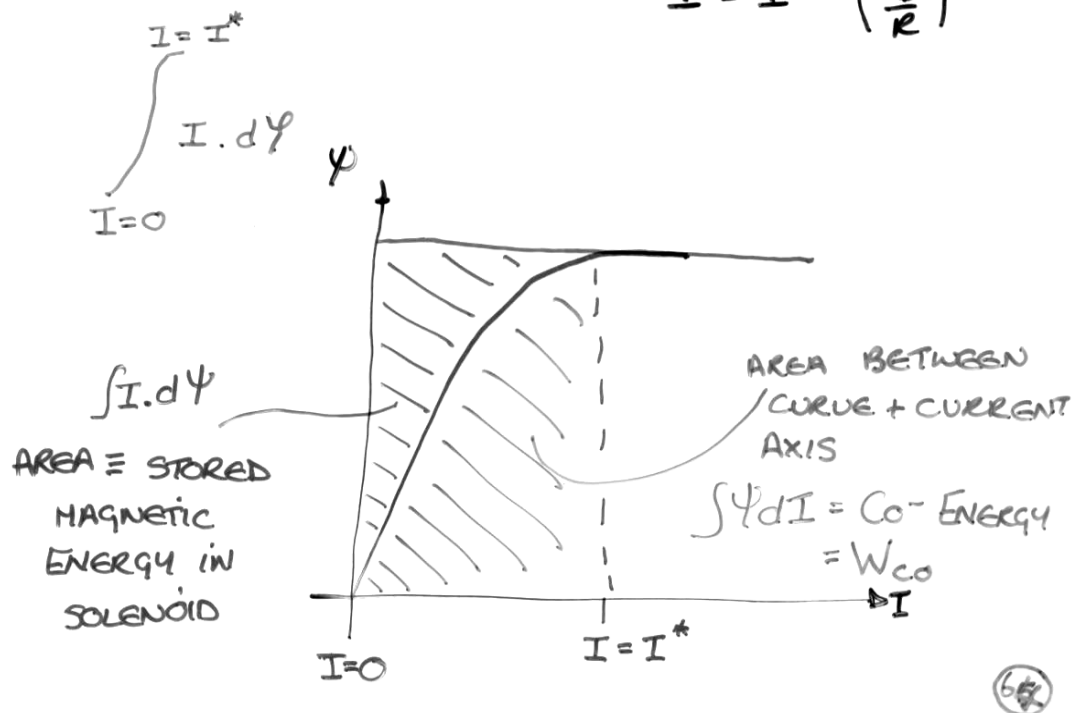
$$\int_{\text{INITIAL CONDITION}}^{\text{FINAL CONDITION}} I d\psi$$

$I = 0$ OPEN CIRCUIT
SOLENOID

ZERO STORED ENERGY

TO SOME FINAL VALUE

$$I = I^* \left(\frac{V_s}{R} \right)$$



AREA BETWEEN CURVE AND CURRENT AXIS

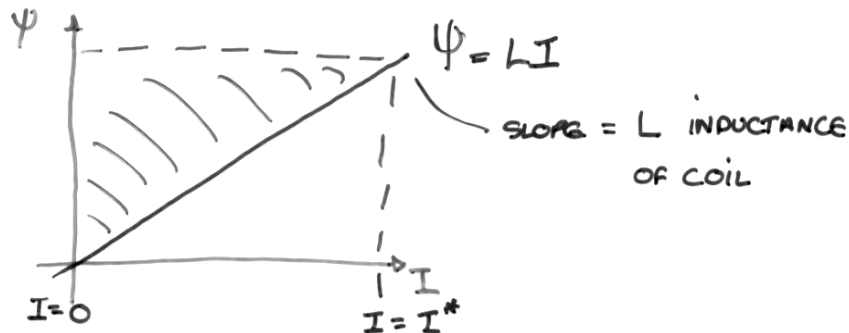
$$\int \psi \cdot dI = \text{Co-ENERGY} = W_{co}$$

NOTE IN A NON-LINEAR SYSTEM

Co-ENERGY \neq STORED MAGNETIC ENERGY

$$\int \psi \cdot dI \neq \int I \cdot d\psi$$

CONSIDER A LINEAR SYSTEM WHERE THERE IS NO SATURATION

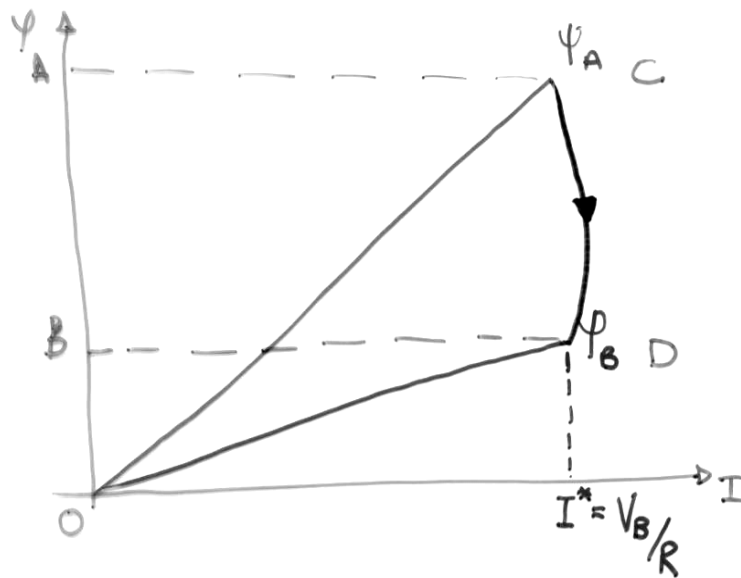


LINEAR SYSTEM IMPLIES A CONSTANT INDUCTANCE I.e. CONSTANT SLOPE.

$$\begin{aligned} \text{STORED MAGNETIC ENERGY} &= \int_0^{I^*} I \cdot d\psi \quad \text{since } \psi = LI, d\psi = L dI \\ \therefore \text{STORED ENERGY} &= \int_0^{I^*} I \cdot L \cdot dI = L \int_0^{I^*} I \cdot dI = L \left[\frac{1}{2} I^2 \right]_0^{I^*} \end{aligned}$$

$$\left(= \frac{1}{2} L I^2 \right) \text{ --- APPLIES TO A NON-SATURATED SYSTEM ONLY. } (66)$$

Ψ -I DIAGRAM WITH MECHANICAL WORK - I.E THE CASE OF REMOVING THE IRON CORE FROM THE SOLENOID



Ψ_A INITIAL FLUX LINKAGE OF THE SOLENOID WITH IRON CORE INSERTED. SLOPE $O - \Psi_A$ REPRESENTS THE INITIAL INDUCTANCE OF SOLENOID + CORE.

Ψ_B FINAL FLUX LINKAGE OF SOLENOID WITH IRON CORE REMOVED. SLOPE $O - \Psi_B$ GIVES FINAL INDUCTANCE OF SOLENOID WITHOUT CORE.

(67)

DURING THE MOTION

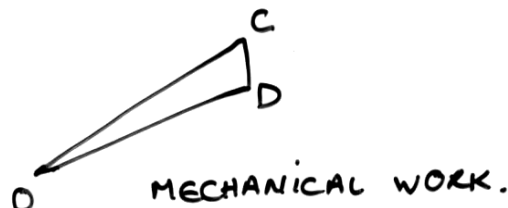
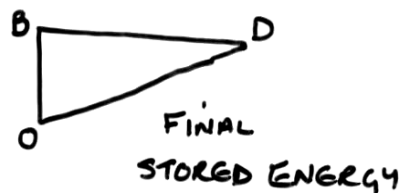
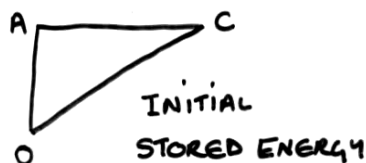
$$V_B = IR + \frac{d\psi}{dt}$$

ENERGY SUPPLIED	LOSSES	MOTION
$\int V_B I dt$	$= \int I^2 R dt$	$+ \int I d\psi$

i.e. TOTAL ENERGY PUT INTO ELECTROMECHANICAL SYSTEM $= \int I d\psi$

i.e AREA ACDB REPRESENTS THE ENERGY INPUT TO THE SYSTEM OVER THE MOTION

IT FOLLOWS THEREFORE THAT THE AREA OCD REPRESENTS THE MECHANICAL WORK PERFORMED



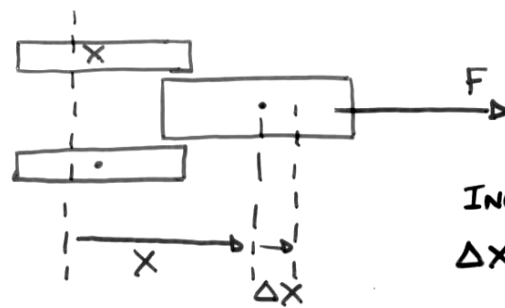
(68)

$$\text{ENERGY} = \int I \, d\psi$$

$$\text{Co-ENERGY } W_{co} = \int \psi \cdot dI$$

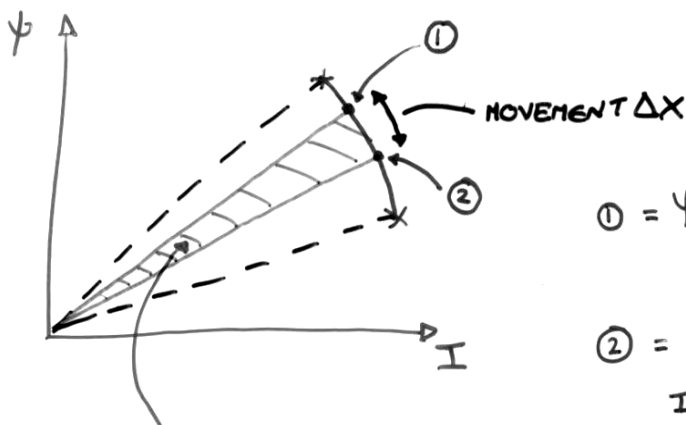
MECHANICAL WORK CAN BE CALCULATED FROM THE CHANGE IN CO-ENERGY

CONSIDER AN INSTANT IN TIME DURING THE MOTION OF THE CORE FROM ORIGINAL TO FINAL POSITION



INCREMENTAL MOVEMENT
 ΔX OVER TIME Δt

DISPLACEMENT X

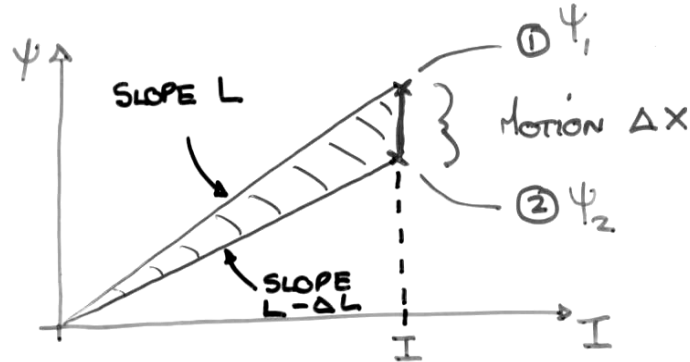


① = ψ, I POINT PRIOR TO MOTION

② = ψ, I POINT AFTER INCREMENTAL MOTION

INCREMENTAL AREA
IS MECHANICAL WORK OVER ΔX

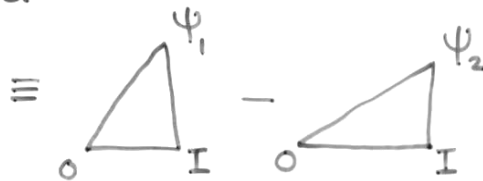
MAKING THE ASSUMPTION THAT THE CURRENT
IN THE SOLENOID IS CONSTANT DURING THE
MOTION ΔX



AT ① SOLENOID INDUCTANCE = L

AT ② SOLENOID INDUCTANCE = $L - \Delta L$ (REDUCES BY ΔL)

MECHANICAL WORK PERFORMED OVER MOTION ΔX IS
THE SHADED AREA.



$$W_{co} = \int \psi \cdot dI$$

$$W_{co} = \frac{1}{2} \psi I$$

$$\equiv W_{co1} - W_{co2}$$

$$\equiv \frac{1}{2} \psi_1 I - \frac{1}{2} \psi_2 I$$

$$= \frac{1}{2} (LI) I - \frac{1}{2} (L - \Delta L) I \cdot I$$

$$L = \frac{\psi}{I}$$

$$\psi = LI$$

$$= \frac{1}{2} I^2 \Delta L = \text{MECHANICAL WORK OVER MOTION } \Delta X.$$

(70)

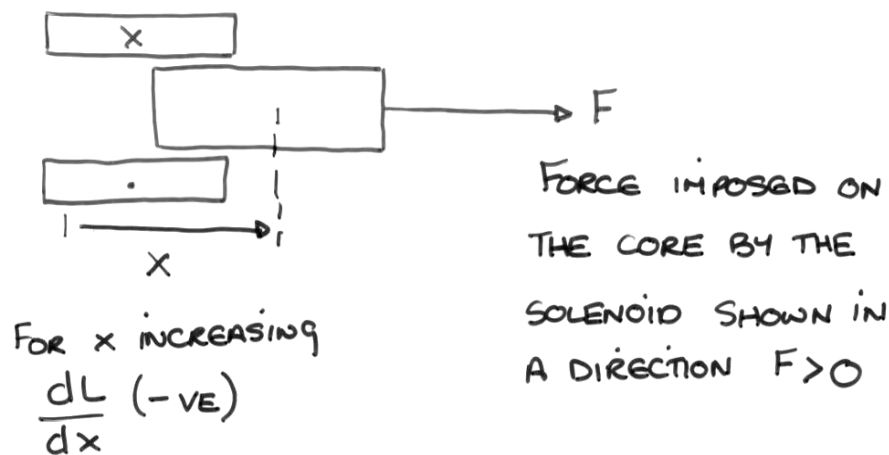
$$\text{MECHANICAL WORK PERFORMED} = \frac{1}{2} I^2 \Delta L = F \Delta X$$

$$\text{FORCE } F = \frac{1}{2} I^2 \frac{\Delta L}{\Delta X} \quad \left(\begin{array}{l} \Delta L \rightarrow 0 \\ \Delta X \rightarrow 0 \end{array} \right)$$

$$\boxed{F = \frac{1}{2} I^2 \frac{dL}{dX}} \quad \text{VALID FOR ALL SYSTEMS}$$

FORCE AT POSITION X

$$= \frac{1}{2} \cdot \left(\begin{array}{c} \text{CURRENT} \\ \text{AT } X \end{array} \right)^2 \cdot \left(\begin{array}{c} \text{RATE OF CHANGE} \\ \text{OF INDUCTANCE} \\ \text{WITH POSITION} \end{array} \right)$$

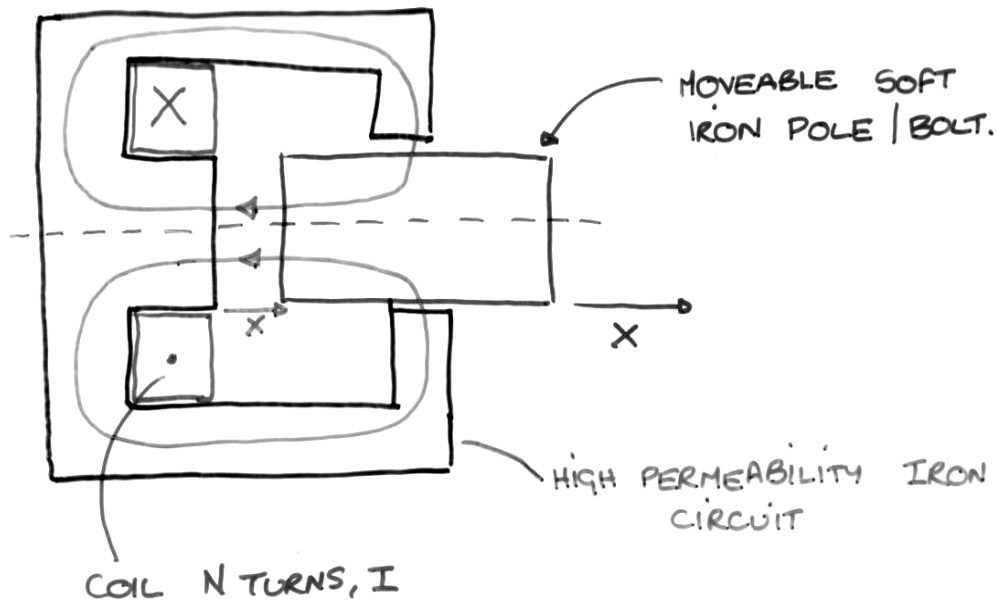


IN THIS CASE, $\frac{dL}{dx} < 0$ i.e. $F < 0$ AND THE

FORCE ACTS TO SUCK THE IRON CORE TOWARDS THE SOLENOID CENTRE.

TYPICAL CYLINDRICAL SOLENOID ACTUATOR

(7.1)



$$\text{m.m.f} = \text{RELUCTANCE} \times \text{FLUX.}$$

$$NI = \text{RELUCTANCE OF AIRGAP} \times \phi$$

$$= \frac{x}{\mu_0 A} \times \phi$$

$$\phi = \frac{NI}{\frac{x}{\mu_0 A}} = \frac{NI \mu_0 A}{x}$$

$$\text{Hence } L = \frac{\psi}{I} = \frac{N\phi}{I} = \frac{N^2 \mu_0 A}{x}$$

$$\therefore \text{FORCE ON IRON SLUG} = \frac{1}{2} I^2 \frac{dL}{dx}$$

$$= \frac{1}{2} I^2 \left(\frac{-N^2 \mu_0 A}{x^2} \right)$$

$$\Rightarrow F = -\frac{1}{2} \frac{I^2 N^2 \mu_0 A}{x^2}$$

Force is TOWARDS
CENTRE.

CONSIDER THE FLUX DENSITY IN THE AIRGAP

$$\phi = B_g A.$$

$$\phi = \frac{NI \mu_0 A}{x}$$

$$B_g = \frac{NI \mu_0}{A}$$

$$\text{i.e. } F = -\frac{1}{2} \frac{B_g^2}{\mu_0} A$$

$$|F/A| = \frac{1}{2} \frac{B_g^2}{\mu_0}$$

EXAMPLE

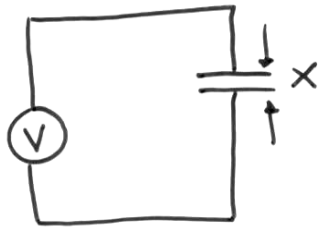
$$B_g = 1.0 \text{ T.}$$

$$\mu_0 = 4\pi \times 10^{-7}$$

$$\therefore |F/A| = 39.8 \times 10^4 \text{ N/m}^2 \text{ (Pa)}$$

$$\approx 4 \text{ Tonnes/m}^2.$$

ELECTROSTATIC SYSTEM.



$$F = \frac{1}{2} V^2 \frac{dC}{dx}$$

APPLIED VOLTS

CHANGE IN CAPACITANCE

$$\left| \frac{F}{\text{AREA}} \right| = \frac{1}{2} E^2 \epsilon_0$$

PERMITTIVITY OF FREE SPACE

$$E = 3 \times 10^6 \text{ V/m}$$

$$F/\text{AREA} = 39.8 \text{ N/m}^2$$

i.e. 10^4 LESS THAN A MAGNETIC DEVICE

TIME CONSTANT OF MAGNETIC SYSTEM

$$L/R \approx \text{ms}$$

TIME CONSTANT OF ELECTROSTATIC SYSTEM.

$$CR \approx \mu\text{s}.$$