

WEEK 2 - worked Example

	A	B	F
0	0	0	0
1	0	1	0
2	1	0	0
3	1	1	1

Express the function F as a fundamental sum-of-products and as a fundamental product-of-sums. (This is the AND function)

Solving the truth table, there is a minterm at $A=B=1$

$$\therefore F = AB = m_3 \Rightarrow F(A,B) = \sum(3)$$

If the minterm evaluates to '1' then the function evaluates to '1'. Because we know that minterms and maxterms are mutually exclusive, we can deduce that $F(A,B) = \prod(0,1,2)$

Alternatively, finding the minterms that are at locations where there is a '0' in the truth table will give an expression for NOT F .

$$\bar{F} = \bar{A}\bar{B} + \bar{A}B + A\bar{B} \quad \text{to obtain } F, \text{ invert both sides as } \bar{\bar{F}} = F$$

$$F = \overline{\bar{A}\bar{B} + \bar{A}B + A\bar{B}} \quad \text{apply De Morgan's theorem}$$

$$F = \overline{\bar{A}\bar{B}} \cdot \overline{\bar{A}B} \cdot \overline{A\bar{B}} \quad \text{apply De Morgan again}$$

$$F = (A+B) \cdot (A+\bar{B}) \cdot (\bar{A}+B) = M_0 M_1 M_2$$

$$F(A,B) = \prod(0,1,2)$$

OR read the maxterms directly from the truth table. Find the '0's in the output and take the variable if there is a '0' for the input and the complement of the variable if there is a '1' for the input.