



The  
University  
Of  
Sheffield.

## DEPARTMENT OF ELECTRONIC AND ELECTRICAL ENGINEERING

Spring Semester 2007-2008 (2 hours)

### Antennas, Radar and Navigation 6

Answer **THREE** questions. **No marks will be awarded for solutions to a fourth question.** Solutions will be considered in the order that they are presented in the answer book. Trial answers will be ignored if they are clearly crossed out. **The numbers given after each section of a question indicate the relative weighting of that section.**

1.
  - a. In the context of surveillance radar, explain how the beamwidth of the antenna affects the performance of the radar. (2)
  - b. An antenna with azimuth and elevation beamwidths of  $\Delta\phi$  and  $\Delta\theta$  is required to scan a hemisphere of sky. Determine a relationship between the gain of the antenna and the number of beam positions required to fully scan the hemisphere. If an antenna has a gain of 40dB and the hemisphere of sky needs to be fully scanned every 10s, determine the dwell time per position. (8)
  - c. A rotating pulsed radar system has the following parameters: frequency = 560MHz; pulse width =  $1.3\mu\text{s}$ ; peak power = 279kW; duty cycle =  $8.3 \times 10^{-4}$ ; antenna rotation rate = 16 RPM; vertical beamwidth =  $4^\circ$ ; number of hits on a point target per rotation = 9.9.  
Determine the following parameters:  
Wavelength; pulse repetition frequency (PRF); pulse repetition time (PRT); average power; horizontal antenna beamwidth; antenna gain; maximum unambiguous range and the range resolution. (10)
2.
  - a. Derive the bi-static radar range equation (6)
  - b. With the aid of a block diagram, describe the basic operation of a continuous wave Doppler radar system. (4)
  - c. A CW Doppler radar illuminates a rotating spherical target as shown in Figure 1. The target rotates at an angular velocity of  $\omega$  radians per second around a circular path of radius  $R$ . The radar operates at a frequency of  $f_0$  Hz and is located a distance  $d$  away from the target. Assuming that  $d \gg R$  derive an expression for

the Doppler shift detected by the radar. If  $f_0 = 10\text{GHz}$ ,  $R = 1\text{m}$  and the target rotates at 30rpm, sketch a graph of the variation in Doppler shift during one complete rotation of the target.

If the condition  $d \gg R$  does NOT apply derive a new expression for the detected Doppler shift in terms of the parameters  $\omega$ ,  $\alpha$ ,  $R$ ,  $\theta$  and  $f_0$

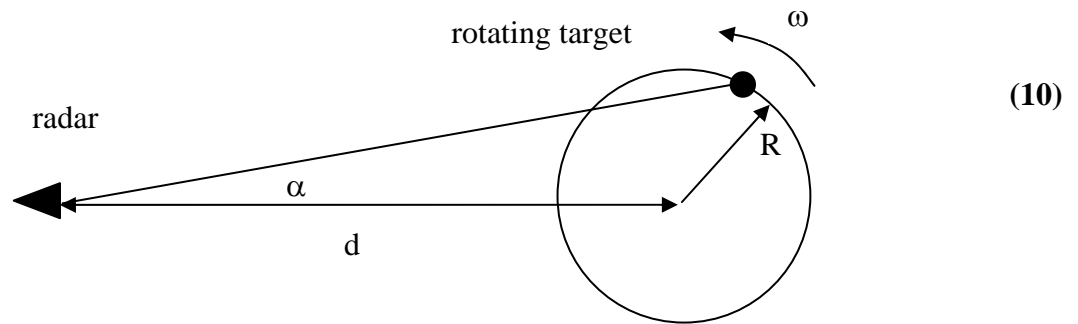


Figure 1

3. a. With the aid of a diagram explain the terms: main-beam, boresight direction, sidelobes, nulls, back-lobes and first-nulls beamwidth, as applied to an antenna's far-field radiation characteristics. (6)
- b. A 8.8GHz communications link consists of a 1.9m diameter dish transmit antenna with an aperture efficiency of 0.7, and a receive dish antenna of 1.3m diameter with an aperture efficiency of 0.65. If the distance between the link is 100km, calculate the magnitude of the transmit power required to produce a received power level of 500nW (6)
- c. Derive an expression for the normalised array factor of a simple 2-element array with element spacing  $d$  and uniform, equal phase excitation (8)  
Plot the array factor for an element spacing of  $\lambda/2$ .

4. a. Explain why and under what circumstances a wireless communication system is more power efficient than a cable based system (4)
- b. Suggest an appropriate antenna type for use in each of the following applications:
- i. Radio broadcast antenna
  - ii. Terrestrial TV reception
  - iii. Airport surveillance radar
  - iv. Airborne intercept radar
  - v. Mobile phone base station
  - vi. Simple antenna for receiving circularly polarised radiation
- (6)
- c. A resonant, lossless half-wavelength dipole antenna has a radiation pattern given by  $U = \sin^3(\theta)$ . The antenna has an input impedance of  $73\Omega$  and is connected to lossless  $50\Omega$  transmission line. If the antenna is illuminated by a plane-wave with a power density of  $5\mu\text{W}/\text{m}^2$  at a frequency of 10MHz calculate the power available at the end of the transmission line.

*You may find the following expression useful*  $\int \sin^4 ax dx = \frac{3x}{8} - \frac{\sin 2ax}{4a} + \frac{\sin 4ax}{32a}$  (10)

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