

EEE105 Tutorial Question Set 8 Solutions

1. In the notes we developed for the conductance of such a channel

$$G = G_0 \left[1 - \left(\frac{V_g}{V_p} \right)^{0.5} \right]$$

so

$$R = R_0 \left[1 - \left(\frac{V_g}{V_p} \right)^{0.5} \right]^{-1}$$

for the two cases given

$$3 \times 10^3 = R_0 \left[1 - \left(\frac{2}{V_p} \right)^{0.5} \right]^{-1}$$

$$2 \times 10^3 = R_0 \left[1 - \left(\frac{1}{V_p} \right)^{0.5} \right]^{-1}$$

dividing one by the other gives

$$1.5 = \frac{\left[1 - \left(\frac{1}{V_p} \right)^{0.5} \right]}{\left[1 - \left(\frac{2}{V_p} \right)^{0.5} \right]}$$

and manipulating this gives $V_p = 5.03 \text{ V}$.

Plugging this back into either of the two cases above gives $R_0 = 1.11 \text{ k}\Omega$, and hence the resistance for $V_g = 3 \text{ V}$ can be calculated to be $4.87 \text{ k}\Omega$.

2. Assuming a single sided “planar” JFET, V_p can be calculated from:

$$V_p = \frac{qN_A a^2}{2\epsilon}$$

No $\rho = 0.1 \text{ }\Omega\text{m}$, so using the conventional formula relating resistivity to mobility and carrier concentration we can obtain $N_A = 1.25 \times 10^{21} \text{ m}^{-3}$.

Hence $V_p = 3.8 \text{ V}$

The channel half width at $V_g = V_p/2$ and $I_d = 0$ can be obtained from:

$$b = a \left[1 - \left(\frac{V_g}{V_p} \right)^{1/2} \right]$$

where $V_g = V_p/2 = 1.9 \text{ V}$

Thus $b = 0.59 \text{ }\mu\text{m}$

(Note: as we used ‘a’ for the channel thickness with the built-in potential applied, rather than the physical thickness of the channel layer, we ignore the V_0 terms in the equations here)