

The  
University  
Of  
Sheffield.

## DEPARTMENT OF ELECTRONIC AND ELECTRICAL ENGINEERING

Spring Semester 2013-14 (2.0 hours)

### EEE305 Machine Design

Answer **THREE** questions. **No marks will be awarded for solutions to a fourth question.** Solutions will be considered in the order that they are presented in the answer book. Trial answers will be ignored if they are clearly crossed out. **The numbers given after each section of a question indicate the relative weighting of that section.**

1. a. Derive the expression of torque of a cylindrical electrical machine as a function of the electrical loading  $Q$ , the magnetic loading  $B$ , the rotor diameter  $D$  and the length  $L$ . (4)
- b. Derive the expression of torque of an axial flux machine, shown in Figure 1, as a function of the electrical loading  $Q$ , the magnetic loading  $B$ , the inner and outer diameters  $D_i$  and  $D_o$ , respectively. Describe main differences between a radial flux machine and an axial flux electrical machine.

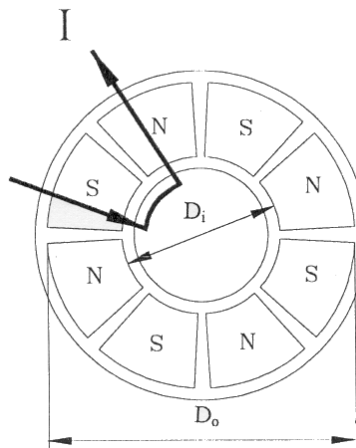


Figure 1 Rotor of axial flux machine

- c. Assuming the radial dimensions of the machine, shown in Figure 2, are increased by a factor of  $K$ , determine the relationship between the increase in electrical loading  $Q$  and the factor  $K$ . The slot number, area and current are  $N_s$ ,  $A_s$  and  $I_s$ , respectively;  $D_1$ ,  $D_2$ ,  $D_3$  are the inner diameter of stator, the diameter of slot bottom and the outer diameter of stator, respectively;  $h$  and  $w_t$  are the slot depth and the tooth width, respectively; and  $k_p$  and  $J_s$  are the slot filling factor and slot current density (constant), respectively. (5)

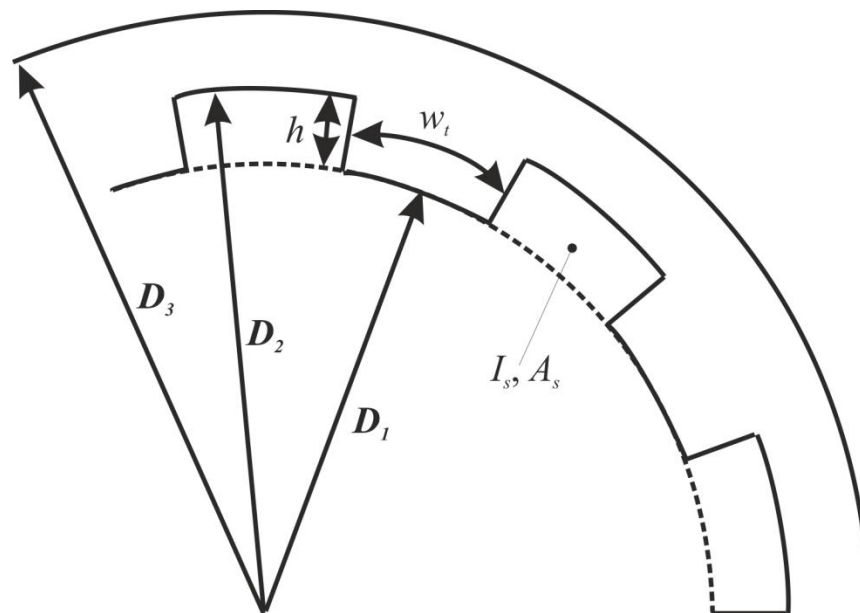


Figure 2 Stator of radial flux machine

- d. What are the major design factors that will influence the electrical loading  $Q$  and the magnetic loading  $B$ ? (4)

2. a. The magnetic circuit, shown in Figure 3, which has an airgap with a length  $l_g$  and area  $A_g$ , is excited by a permanent magnet with a length  $l_m$  and an area  $A_m$ , a remanence  $B_r$  and a relative recoil permeability  $\mu_r$ , and a coil with  $N$  turns and current  $I$ . When current  $I = 0$ , calculate the open-circuit airgap flux density. Describe the methods which help increase the airgap flux density and discuss their limitations. List all the assumptions that are made in the derivations.

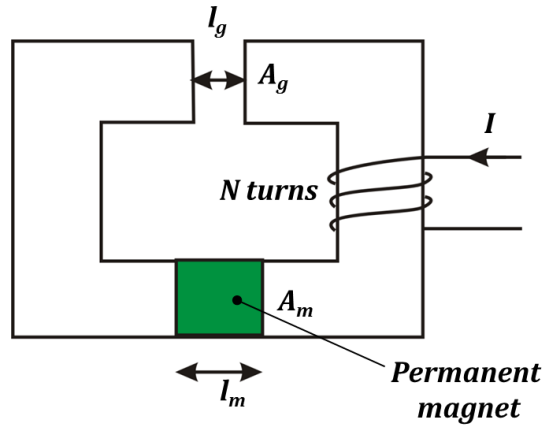


Figure 3 Magnetic circuit

- b. Derive the relationship between the magnet volume and the air-gap volume. Show graphically when the maximum energy product in magnets is achieved. (8)
- c. Now  $I \neq 0$ , draw the demagnetization curve of the magnets and calculate the minimum magnet length to avoid irreversible demagnetization. (4)
- d. Show graphically the difference between the reversible and irreversible demagnetizations. Explain the influence of temperature on the irreversible demagnetization for both Ferrite and NdFeB permanent magnets. (4)

3. a. Derive general expressions for the winding pitch factor,  $K_p$ , and the distribution factor,  $K_d$ , for both the fundamental and the  $n^{\text{th}}$  harmonic EMF components. Explain why a short-pitched winding is often preferred in practice when compared to long-pitched winding. (Both short-pitched and long-pitched windings are distributed windings). (6)
- b. Show that the winding skew factor can be derived using similar method as for the winding distribution factor. Explain the main advantages and disadvantages of using winding skew. (5)
- c. Employing coil EMF vectors, determine the coil connections for a 3-phase, 12-slot, 14-pole alternate teeth wound permanent magnet machine which has a non-overlapping winding, i.e. concentrated coils, in order to obtain a maximum winding factor. (4)
- d. Employing coil EMF vectors, determine the coil connections for a 3-phase, 9-slot, 10-pole all teeth wound permanent magnet machine which has a non-overlapping winding, i.e. concentrated coils, in order to obtain a maximum winding factor. (5)

4. a. Figure 4 shows a simple reluctance machine which consists of a stator equipped with a single coil of height  $h_2$ , a width  $b_2$ , and a number of turns  $N$ . The machine has a rotor of height  $h_1$  and width  $b_0$ , and separated from the stator by two identical airgaps of length  $h_0$ . Furthermore, the width of the air section (unwound section) of the slot is  $b_1$  and  $b_0 > h_1$ . Calculate the winding inductance per-unit length of the machine, specifying any assumptions that should be made. (full marks will not be given if the assumptions are not listed).

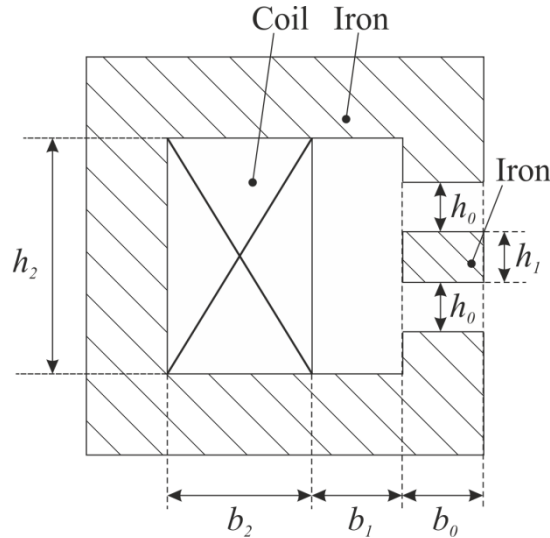


Figure 4 Simple reluctance machine

(8)

- b. The rotor shown in Figure 4 rotates to another position (90 deg. mech.), as shown in Figure 5, where the rotor surfaces are always parallel to stator teeth surfaces. Based on the assumptions given in 4.a, calculate the winding inductance per-unit length of the machine.

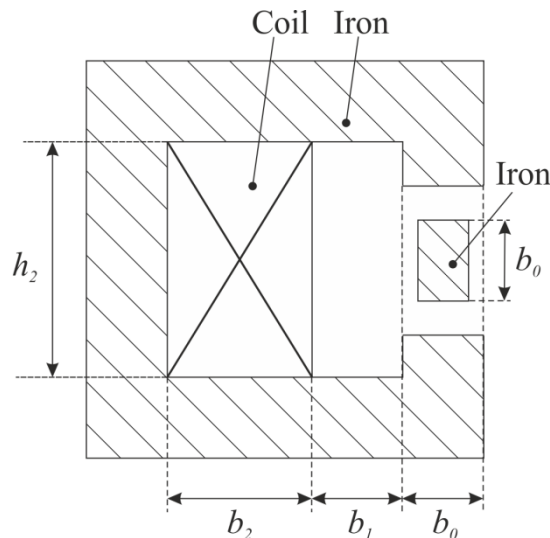


Figure 5 Simple reluctance machine

(8)

- c. Based on the results obtained from 4.a and 4.b, suggest possible ways to increase the winding inductance.

(4)

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