

# EEE 6212

## Semiconductor Materials

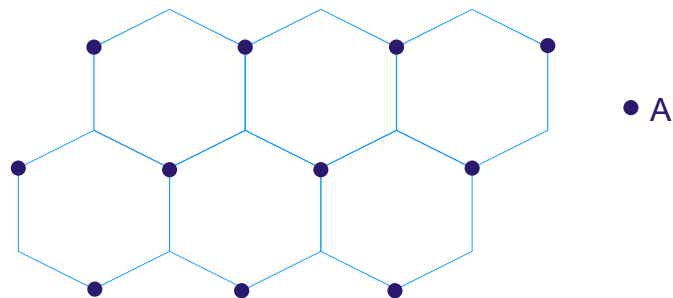
### Lecture 3: Semiconductor crystals

### Lecture 3: Semiconductor crystals

- relationship between cubic & hexagonal close-packing (partial repeat)
- coordination numbers of fcc & hcp lattices
- bond lengths and lattice spacings in fcc & hcp
- filling of interstices in close-packed arrays and atomic positions
- semiconductor crystals as examples of structures based on filling of interstices
- polymorphism and stacking faults

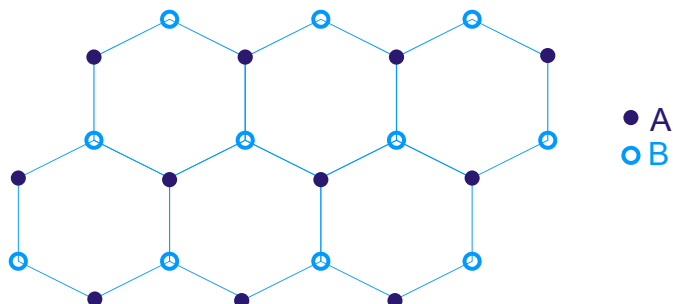
### relation between cubic & hexagonal close-packing

consider filling of successive planes in top view  
but mark only atom positions rather than spheres



### relation between cubic & hexagonal close-packing

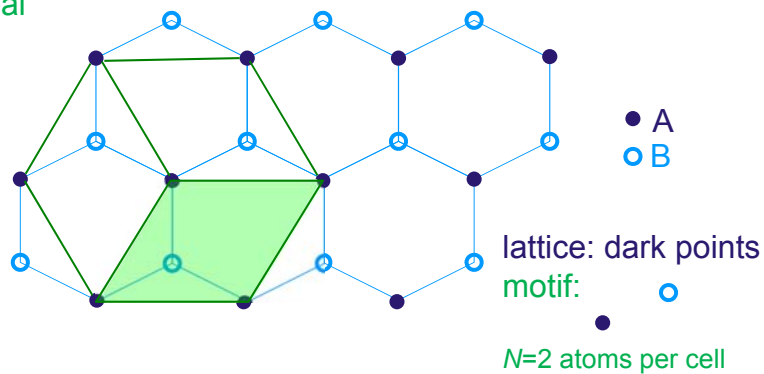
consider filling of successive planes in top view  
but mark only atom positions rather than spheres



## relation between cubic & hexagonal close-packing

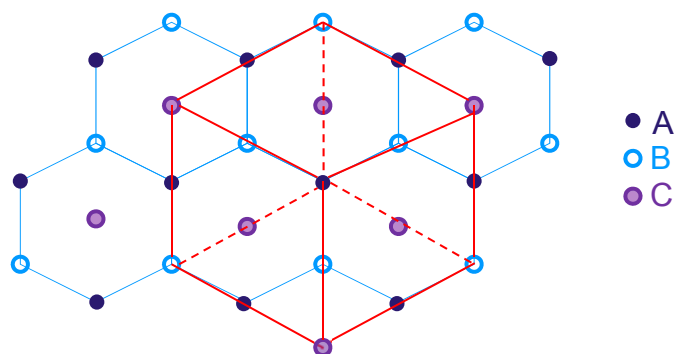
consider filling of successive planes in top view  
but mark only atom positions rather than spheres

hexagonal  
unit cell



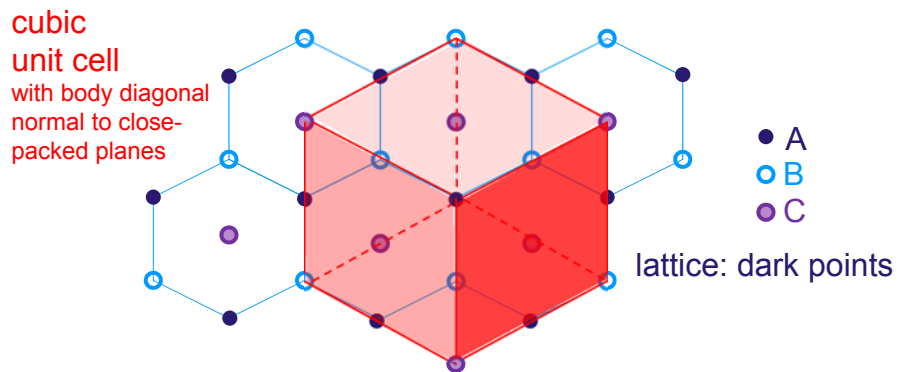
## relation between cubic & hexagonal close-packing

consider filling of successive planes in top view  
but mark only atom positions rather than spheres



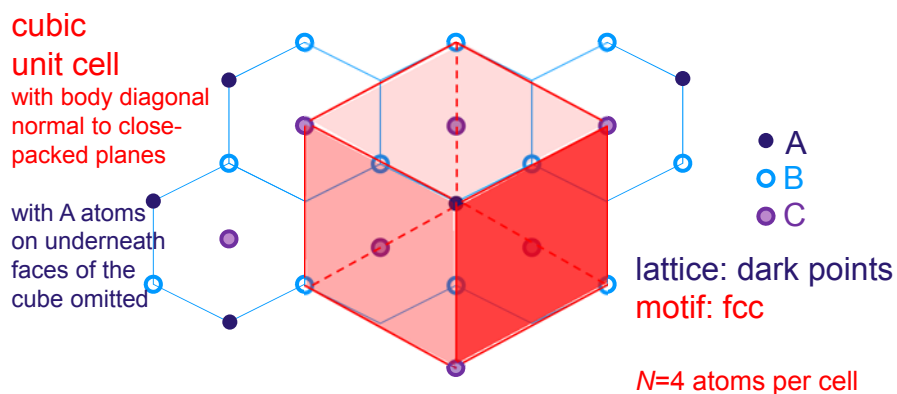
## relation between cubic & hexagonal close-packing

consider filling of successive planes in top view  
but mark only atom positions rather than spheres



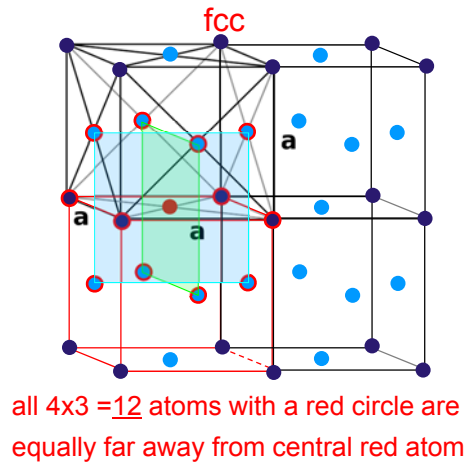
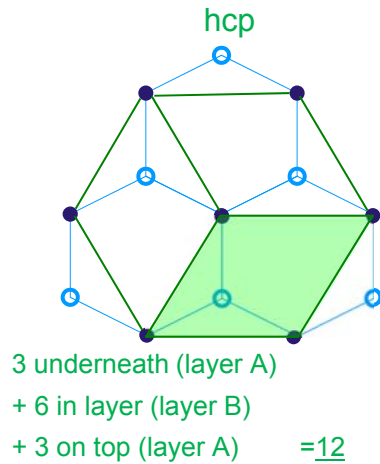
## relation between cubic & hexagonal close-packing

consider filling of successive planes in top view  
but mark only atom positions rather than spheres



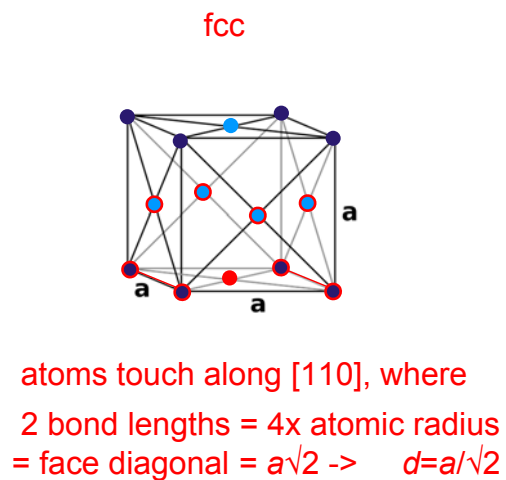
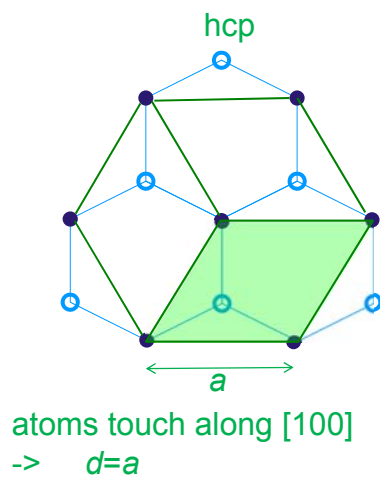
## comparison of hcp & fcc: coordination numbers

consider # of nearest-neighbour atoms in adjacent unit cells



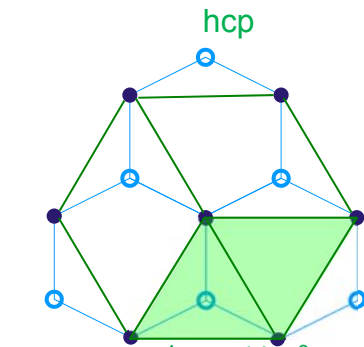
## comparison of hcp & fcc: bond lengths

consider distance between nearest-neighbour atoms



## comparison of hcp & fcc: space filling

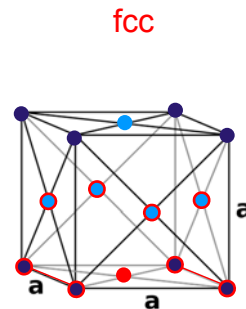
consider fractional ratio of atomic volume to unit cell volume



$$V_{\text{atoms}} = 2 \cdot \frac{4}{3} \pi \left(\frac{1}{2}a\right)^3$$

$$V_{\text{unit cell}} = 2c \cdot \frac{1}{2} a^2 \sqrt{3} \text{ with } c/a = 2\sqrt{2/3}$$

$$\text{ratio} = \pi / (3\sqrt{2}) = \underline{74\%}$$



$$V_{\text{atoms}} = 4 \cdot \frac{4}{3} \pi \left(\frac{1}{4} a\sqrt{2}\right)^3$$

$$V_{\text{unit cell}} = a^3$$

$$\text{ratio} = \frac{1}{6} \pi \sqrt{2} = \underline{74\%}$$

## relation between cubic & hexagonal close-packing

AB(ABAB): hexagonal close-packed (hcp) along c-axis

and

ABC(ABC): cubic close-packed or face-centred cubic (fcc) along  $\langle 111 \rangle$  direction















only differ in their stacking sequence!

## The 14 Bravais Lattices

The **14 Bravais lattices** come about due to combinations of point symmetry (7 lattice systems) with 4 space centerings:

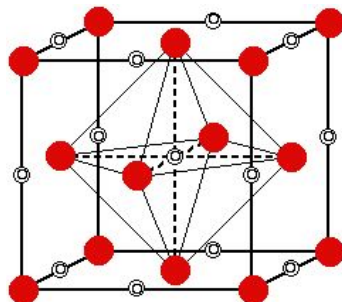
notation: lattice points at 0,0,0 and  
P: primitive -  
C: base centred  $\frac{1}{2}, \frac{1}{2}, 0$   
I: body centred  $\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$   
F: face centred  $\frac{1}{2}, \frac{1}{2}, 0; \frac{1}{2}, 0, \frac{1}{2}; 0, \frac{1}{2}, \frac{1}{2}$   
R:  $\frac{2}{3}, \frac{1}{3}, \frac{1}{3}; \frac{1}{3}, \frac{2}{3}, \frac{2}{3}$

Note: trigonal R can be hexagonal P or rhombohedral.

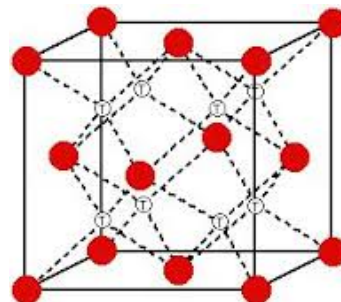
The 7 lattice systems (From least to most symmetric)	The 14 Bravais Lattices			
1. triclinic (none)	$a, b, c \neq 90^\circ$ 			
2. monoclinic (1 diad)	simple $a \neq b \neq c$ $\alpha \neq 90^\circ$ $\beta, \gamma = 90^\circ$ 	base-centered $a \neq b \neq c$ $\alpha \neq 90^\circ$ $\beta, \gamma = 90^\circ$ 		
3. orthorhombic (3 perpendicular diads)	simple $a \neq b \neq c$ $\alpha = \beta = \gamma = 90^\circ$ 	base-centered $a \neq b \neq c$ $\alpha = \beta = \gamma = 90^\circ$ 	body-centered $a \neq b \neq c$ $\alpha = \beta = \gamma = 90^\circ$ 	face-centered $a \neq b \neq c$ $\alpha = \beta = \gamma = 90^\circ$ 
4. rhombohedral (1 triad)	$a = b = c$ $\alpha = \beta = \gamma \neq 90^\circ$ 			
5. tetragonal (1 tetrad)	simple $a = b \neq c$ $\alpha = \beta = \gamma = 90^\circ$ 	body-centered $a = b \neq c$ $\alpha = \beta = \gamma = 90^\circ$ 		
6. hexagonal (1 hexad)				
7. cubic (4 triads)	simple (SC) $a = b = c$ $\alpha = \beta = \gamma = 90^\circ$ 	body-centered (bcc) $a = b = c$ $\alpha = \beta = \gamma = 90^\circ$ 	face-centered (fcc) $a = b = c$ $\alpha = \beta = \gamma = 90^\circ$ 	

## filing of interstices in close-packed arrays like fcc

4x octahedral type (O) 8x tetrahedral type (T)



at half height



at  $\frac{1}{4}$  and  $\frac{3}{4}$  heights

## semiconductor crystals: examples of structures based on filling of interstices

8x tetrahedral type (T)

diamond structure:

fill 4/8 T sites with

same atoms, i.e.

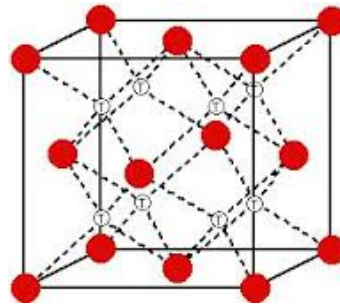
atoms also at

$(\frac{1}{4}, \frac{1}{4}, \frac{1}{4}),$

$(\frac{3}{4}, \frac{3}{4}, \frac{1}{4}),$

$(\frac{1}{4}, \frac{3}{4}, \frac{3}{4}),$

$(\frac{3}{4}, \frac{1}{4}, \frac{3}{4})$



## semiconductor crystals: examples of structures based on filling of interstices

8x tetrahedral type (T)

diamond structure:

fill 4/8 T sites with

same atoms, i.e.

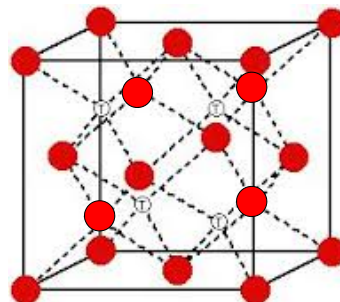
atoms also at

$(\frac{1}{4}, \frac{1}{4}, \frac{1}{4}),$

$(\frac{3}{4}, \frac{3}{4}, \frac{1}{4}),$

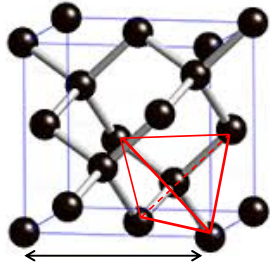
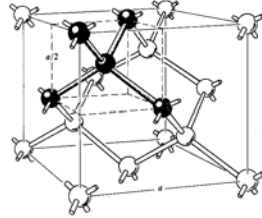
$(\frac{1}{4}, \frac{3}{4}, \frac{3}{4}),$

$(\frac{3}{4}, \frac{1}{4}, \frac{3}{4})$





## Semiconductor crystals



$a=0.381\text{nm (C)}, 0.543\text{nm (Si)}, 0.566\text{nm (Ge)}$

### 1. diamond (C, Si, Ge, $\alpha$ -Sn)

consists of two face-centred cubic crystals shifted by  $\frac{1}{4}$  of the body diagonal; **all 8 atoms are identical** and connected via 4 neighbours via **bonds forming tetrahedra**.

space group 227:  $Fd\bar{3}m$

1 atom at corners:  $8 \times \frac{1}{8}$

3 atoms at centre of faces:  $6 \times \frac{1}{2}$

4 atoms at tetrahedral sites:  $4 \times 1$

## semiconductor crystals: examples of structures based on filling of interstices

### 8x tetrahedral type (T)

sphalerite structure:

**fill 4/8 T sites with**

different atoms, i.e.

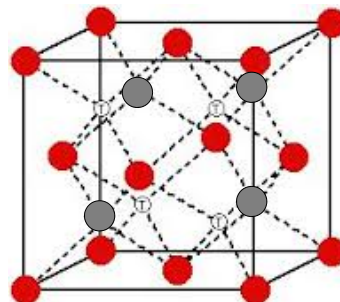
different atoms at

$(\frac{1}{4}, \frac{1}{4}, \frac{1}{4}),$

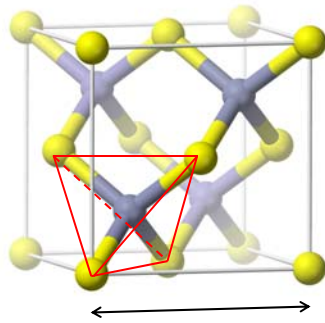
$(\frac{3}{4}, \frac{3}{4}, \frac{1}{4}),$

$(\frac{1}{4}, \frac{3}{4}, \frac{3}{4}),$

$(\frac{3}{4}, \frac{1}{4}, \frac{3}{4})$



## Semiconductor crystals



$a = 0.542\text{nm}$  (c-ZnS)  
 $0.565\text{nm}$  (GaAs),  
 $0.587\text{nm}$  (InP),  
 $0.648\text{nm}$  (InSb),  
 $0.450\text{nm}$  (c-GaN),

**2. sphalerite or zinc blende** (ZnS, GaP, InP, GaAs, AlAs, InAs, GaSb, InSb, ZnSe, HgTe,...)

consists of two face-centred cubic crystals shifted by  $\frac{1}{4}$  of the body diagonal; **both sub-lattices are occupied by different atoms** which again are tetrahedrally connected to their 4 neighbours. All tetrahedra are in the same orientation.

space group 216:  $F\bar{4}3m$

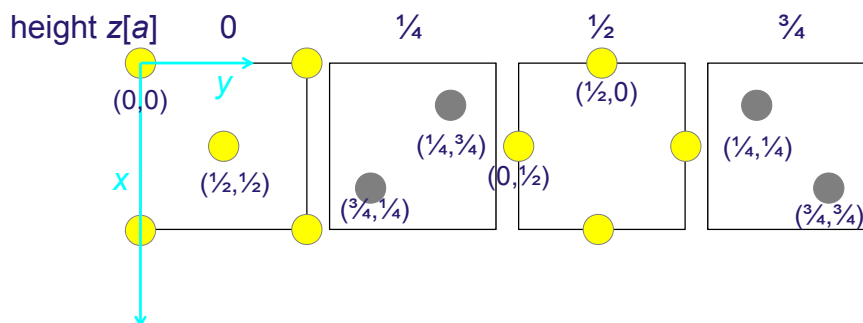
**1 atom at corners:**  $8 \times \frac{1}{8}$

**3 atoms at centre of faces:**  $6 \times \frac{1}{2}$

4 atoms at tetrahedral sites:  $4 \times 1$

## Semiconductor crystals

**2. sphalerite or zinc blende**



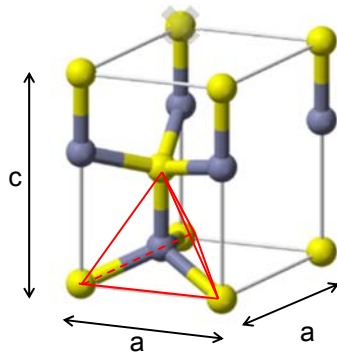
space group 216:  $F\bar{4}3m$

**1 atom at corners:**  $8 \times \frac{1}{8}$

**3 atoms at centre of faces:**  $6 \times \frac{1}{2}$

4 atoms at tetrahedral sites:  $4 \times 1$

## Semiconductor crystals



$a=0.381\text{nm}$ ,  $c=0.623\text{nm}$  (h-ZnS),  
 $a=0.319\text{nm}$ ,  $c=0.519\text{nm}$  (h-GaN),

3. **wurtzite** (ZnS, GaN, ZnO, BeO,...) consists of two hexagonal crystals (dihexagonal pyramidal) shifted by  $uc$  ( $u \approx \frac{3}{8} + \delta$ ) along  $\underline{c}$ -axis; **both sub-lattices are occupied by different atoms** which again are tetrahedrally connected to 4 neighbours.

Tetrahedra in adjacent (001) planes are rotated by  $180^\circ$  about [001].

space group 186:  $P6_3mc$

1 atom at corners  $(0, 0, 0)$

1 atom at position  $(\frac{1}{3}, \frac{2}{3}, \frac{1}{2})$

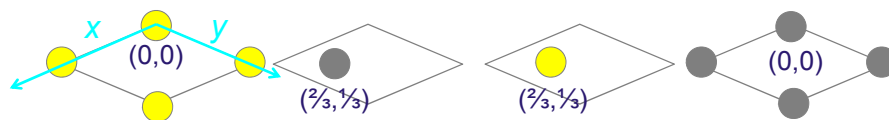
1 atom at position  $(0, 0, \frac{3}{8})$

1 atom at position  $(\frac{1}{3}, \frac{2}{3}, \frac{7}{8})$

## Semiconductor crystals

3. **wurtzite**

height  $z[c]$     0                       $u \approx \frac{1}{8}$                        $\frac{1}{2}$                        $\frac{1}{2} + u$



space group 186:  $P6_3mc$

1 atom at corners  $(0, 0, 0)$

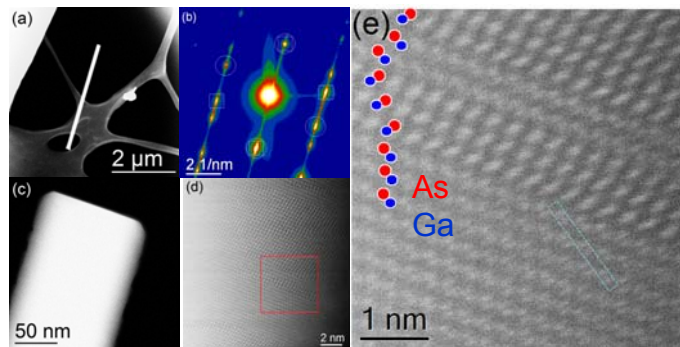
1 atom at position  $(\frac{1}{3}, \frac{2}{3}, \frac{1}{2})$

1 atom at position  $(0, 0, \frac{3}{8})$

1 atom at position  $(\frac{1}{3}, \frac{2}{3}, \frac{7}{8})$

## polymorphism and stacking faults

As hcp and fcc structures are so similar, many materials can adopt both, and their energetics are rather similar, as shown here for a GaAs nanowire imaged along  $\langle 110 \rangle$  zone axis. Changing from hcp to fcc (or back) produces stacking faults.



T. Walther &  
A.B. Krysa,  
Cryst. Res.  
Technol. (2014)  
DOI:  
10.1002/crat.  
201400166

## Summary

- hcp and fcc differ in their **stacking** sequence (ABAB... vs. ABCABC...) but have the same coordination numbers and space filling efficiency (which is why they are both called '**close-packed**').
- Semiconductor crystals exist in 3 modifications:
  - (i) The **diamond** structure is based on two identical fcc lattices shifted by  $\frac{1}{4}$  of the body diagonal, which fills  $\frac{4}{8}$  of the tetrahedral interstices.
  - (ii) The **sphalerite** structure is an ordered version of the diamond structure.
  - (iii) The **wurtzite** structure is based on two hcp lattices shifted by  $uc$  (with  $u \approx \frac{3}{8} + \delta$ ) along the  $c$ -axis.
- Changing from fcc to hcp stacking, or vice versa, produces **stacking faults**. Crystals that exist in both modifications are called **polymorphs**.