$$QI(1)$$
 $q = f_0/_{\Delta f} = \frac{1.59 \, kHz}{199 \, Hz} = \frac{8.0}{1}$

(11)
$$f_0 = \frac{1}{2\pi\sqrt{LC}} = \frac{1}{2\pi\sqrt{L.100nF}} = 1.59kHz$$

or $L = \frac{1}{10^{-7} \times (2\pi).59kHz}^2$

= $100mH$

(iii)
$$q = \frac{1}{R_T} \sqrt{\frac{L}{C}} = \frac{1}{R_T} \sqrt{\frac{100 \text{ mH}}{100 \text{ nF}}} = \frac{10^3}{R_T} = 8$$

$$R_{T} = R + R_{L} = 100 + R_{L} = 125 \text{ s.}$$

$$R_{L} = 25 \text{ s.}$$

(iv) Voltage measured at
$$V_R$$
 would be
$$\frac{V_S R}{R + R_L} = \frac{V_S}{100 + 25} = \frac{4V_S}{5} = \frac{0.8 V_S}{5}$$

(v). | Voltage across ideal bit of L | = 8Vs.

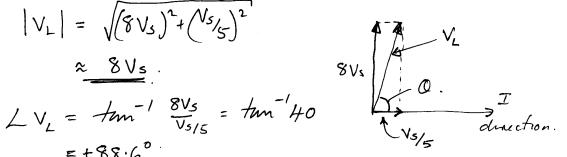
Voltage across R_L =
$$V_S \frac{R_L}{R+R_L} = \frac{V_S.1}{E}$$

$$|V_L| = \sqrt{(8V_S)^2 + (V_S/S)^2}$$

$$\approx 8V_S.$$

$$LV_{L} = tam^{-1} \frac{8V_{5}}{V_{5/5}} = tam^{-1} + 0$$

$$= +88.6^{\circ}$$



Q2
$$Z = \frac{Vs}{I} = \frac{\int WL(R + 'Uuc)}{\int WL + R + 'Jwc}$$

$$= \frac{\int WL(I + JwcR)}{I + \int WCR - W^2LC} \quad v_s = \frac{\int WL(R + 'Uuc)}{R}$$

Resonance occurs when Z is real - ie j terms

extracting j terms

$$JW \left(CR L CR W^{2} + L \left(1 - W^{2}L^{2} \right) \right) = 0$$

$$C^{2}R^{2}W^{2}L + L - W^{2}L^{2}C = 0$$

$$W^{2} \left(C^{2}R^{2}L - L^{2}C \right) = -L$$
or
$$W^{2} \left(L^{2}C - C^{2}R^{2}L \right) = L$$

$$W^{2} = \frac{L}{L^{2}C - C^{2}R^{2}L} = \frac{1}{LC - C^{2}R^{2}}$$
or
$$W = \frac{1}{\sqrt{LC - C^{2}R^{2}}} \text{ or } f = \frac{1}{2\pi} \cdot \frac{1}{\sqrt{LC - C^{2}R^{2}}}$$

Q3. The impedance of the network is

$$Z = \frac{(R_c + 'Jwc)(R_L + jwL)}{R_c + 'Jwc} + R_L + JwL$$

$$= R_c + \frac{R_L}{Jwc} + R_c JwL + \frac{L}{C}$$

$$R_c + R_L + j(wL - \frac{l}{wc})$$

Q3 conb.. =
$$\left(R_c R_L + \frac{L}{c}\right) + j\left(WLR_c - \frac{R_L}{WC}\right)$$

 $\left(R_c + R_L\right) + j\left(WL - \frac{l}{WC}\right)$

We can make the imaginary parts of the numerator + denominator the same, except for a factor, if we make $R_c = R_L = R_o$. Z then becomes

$$Z = \frac{(R^2 + \frac{L}{c}) + Rj(\omega L - \frac{1}{\omega c})}{2R + J(\omega L - \frac{1}{\omega c})}$$

(This is the argument needed by the real experts the experts Start from here)

We also need to take R out of the real part of the numerator and if we do this we get.

and the complex numerator and denominator can be made to cancel if the real parts are the same (the magnery parts are already the same), in $R + \frac{L}{ro} = 2R$

if
$$R + \overline{cR} = 2R$$

or $\overline{cR} = R$ or $R = \sqrt{\frac{L}{c}}$

This mu gmi
$$Z = R. \frac{(R + R^{2}/R) + J(WL - 1/WC)}{2R + J(WL - 1/WC)} = R$$

$$= punchy real = resonant.$$

Q4 (1) at t=0, $\underline{I}=0$ since $\frac{dv}{dt}$ must be zero.

 $t=0^+$, $I=\frac{10-V_c}{2lcn}=\frac{10-0}{2lcn}=\frac{5mA}{2lcn}$ since at $t=0^+$ There has not been any time to allow change to build up in C.

t ⇒ ∞ I = 0 since, once again, de must be zero.

(11) at $t=0^-$, $\frac{V_c=0}{V_0 | tage}$ since $V_s=0$ and there is no $V_0 | tage$ drop across R (since I=0).

t=0+, Vc=0 since there has been insufficient time for the change in C to change.

t ⇒ ∞, Vc ⇒ 10 v smce all transient effects will have settled down, dvc = 0 so Tc=0 so no vollage drop across R

Ψ5 (1) I, at t=0...= $\frac{3v}{2lin} = \frac{1.5mA}{1.5mA}$. Since at t=0...

Whe circuit is at a skeady state - ie all transcent effects have died away, Ic=0 and $v_{L}=0$ and so all v_{S} appears across $2k_{L}$.

at t=0 = I_= 1.5 mA. Since $I = \int V dt$ I must be continuous over an infinitesimally small time interval unless V can be infinitely big for an infinitely small time.

big for an infinitely small time. at $t \Rightarrow \infty$, $I_L = -\frac{6}{2} = -\frac{3}{3} = -$

(11) at t=0, I=I_L = 1.5 mA since V_L=0, all of I must flow through L

 $95 \text{ cent. at } t = 0^{+} \quad I = 1.5 \text{ mA} - \frac{9 \text{ V}}{1 \text{ k.s.}} = \frac{-7.5 \text{ mA}}{1}$

This is the trickiest one so for. On the transient the voltage across C remains unchanged - ie LHS is 3V the wir.t. RHS. But the LHS voltage changes from +3 to -6 and if the voltage across C remains unchanged the RHS must show the same change - ie from 0V to -9V. I_L at $t=0^+$ is $I \cdot S \cdot MA$ and $I = I_L + I_R = I \cdot S \cdot MA + \frac{-9}{1kn}$.

Notice that Vi can change without -9V JIR JIL changing I over small timescales.

at $t \Rightarrow \infty$ all transients with home settled and we essentially have a d.c. problem with $V_s = -6$. $I_L = I$ as $t \Rightarrow \infty = \frac{-6}{21 \text{ tr}} = \frac{-3 \text{ mA}}{21 \text{ tr}}$.

(iii) at t=0 V_L=0 V; the problem is a d.c. one.

dt t=0 t V_L=-9 v as described for the t=0 t

part of (ii).

at t⇒∞ V_L=0 v because the problem is once

again a d.c. problem - all transvents have

settled.

96 (1) at t=0 the problem is a dc problem, $V_L=0$ and I=-6, $\frac{2k|l2k}{2k+2k|l2k}$, $\frac{1}{2k}=\frac{-lmA}{2k+2k|l2k}$.

at $t=0^+$ L maintains the level of current present at $t=0^-$, in I=-1 mA.

at $t \Rightarrow \infty$ the problem is once more de $I = +12 \frac{2k||2k|}{2k + 2k||2k|} \cdot \frac{1}{2k} = +2mA$

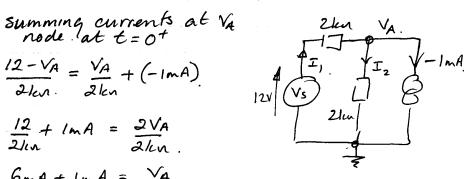
96 cont... (11)
$$V_R$$
 at $t = 0$ is $-6 \times \frac{2kn/|2kn|}{2kn + 2kn/|2kn|} = \frac{-2V}{2kn}$

at t=0 + behaves like a current source That maintains the t=0 value of I

$$\frac{12 - V_A}{2 l c n} = \frac{V_A}{2 l c n} + \left(-1 m A\right)$$

$$\frac{12}{2\ln n} + \ln A = \frac{2VA}{2\ln n}$$

$$6mA + ImA = \frac{\sqrt{A}}{Ilcn}$$



at t > 00 The problem reverts to a dc VR = 12 x 2/10 + 2/10/1/2/11

 $V_R + V_r = 0$

$$IR + L \frac{dI}{dt} = 0$$
 or $\frac{dI}{I} = -\frac{R}{dt}$.

integrating both sides gmes

$$ln I = -\frac{RE}{L} + C$$
or $I = (-\frac{RE}{L} + C) = Ae^{-\frac{RE}{L}}$

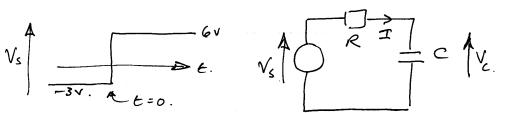
Q7 cont... When
$$t = 0$$
 $I = \frac{V_s}{R}$

$$A = \frac{V_s}{R} \quad \text{and}$$

$$I = \frac{V_s}{R} e^{-\frac{t}{(\frac{t}{R})}}$$

$$V_L = L \frac{dI}{dt} = L \frac{V_s}{R} \left(-\frac{1}{L_{IR}}\right) e^{-\frac{t}{(\frac{t}{R})}}$$

$$= -V_s e^{-\frac{t}{(\frac{t}{L_{IR}})}}$$



 $V_s = V_R + V_c = IR + \frac{1}{C} \int I dt + V_{c(0)}$ form, defferentiate both sides...

afferentiate both sides...

$$O = R \frac{dI}{dt} + \frac{I}{C} + O$$

this is the initial condition for V_c to which the integrated current adds.

integrating both sides $\ln I = -\frac{t}{Rc} + C$ I = e - tRc + C = Ae

when
$$t = 0^{\dagger}$$
, $I = \frac{6 - V_{c(0)}}{R} = \frac{6 - (-3)}{R} = \frac{9}{R} = A$.
so $I = \frac{9}{R}e^{-\frac{t}{CR}}$

Q8 cont ... The guestion actually asks you to solve the problem by developing an equation in Vc

$$V_{c}(t) + RC \frac{dV_{c}(t)}{dt} = V_{s}.$$

$$V_{c}. \qquad V_{R} = IR$$

$$C \frac{dV_{c}(t)}{dt}$$

or
$$-\frac{dt}{RC} = \frac{dV_c(t)}{(V(t) - V_s)}$$
 or $C - \frac{t}{RC} = \ln(V(t) - V_s)$
or $e^{-t/RC}$ $e^{C} = V(t) - V_s = Ae^{-t/RC}$

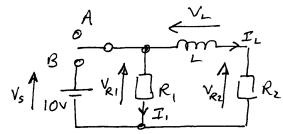
When
$$t = 0^{+}$$
 $V_{c}(0^{+}) = -3$ and $V_{s} = 6$
 $A = -9$.

$$V_{clt}$$
) - 6 = -9 e^{-t/RC}
or V_{clt}) = 6 - 9 e^{-t/RC} = 9(1-e^{-t/RC}) - 3.

Ic(t) can be derived from this result ...

$$I_{c(t)} = C \frac{d \underbrace{v_{c(t)}}}{dt} = C(-1)(-\frac{1}{Rc}) 9e^{-\frac{t}{Rc}}$$
$$= \frac{9}{R}e^{-\frac{t}{Rc}}.$$

of Ide).



and
$$V_{R_1} = V_L + V_{R2}$$

$$-I_L(E)R_1 = L \frac{dI_L(E)}{dE} + I_L(E)R_2.$$

or
$$-I_{L}(E) \left[R_{1} + R_{2} \right] = L \frac{dI_{L}(E)}{dE}$$

or $-\frac{R_{1} + R_{2}}{L} dE = \frac{dI_{L}(E)}{I_{L}(E)}$

integrating both sides gives

$$-R_{1}+R_{2} + C = \ln I_{L}(t).$$
or
$$Ae^{-R_{1}+R_{2}} = I_{L}(t).$$

$$\frac{10e^{-R_1+R_2}t}{R_2}=I_L(t).$$

$$V_{R_1} = -I_L(E) \cdot R_1 = -\frac{10 R_1}{R_2} e^{-\frac{R_1 + R_2}{L}} +$$

peak value when t = 0 because this is the biggiest value of e - Ri+Rz t

: penk
$$V_{R_1} = -10 \frac{R_1}{R_2} = -50 \text{ V}.$$

When switch goes back to position B the circuit is governed by $V_S = V_L + V_{R2}$

$$V_{S} = V_{L} + V_{R2}$$

$$= L \frac{d I_{L}(t)}{dt} + I_{L}(t) R_{2}$$

$$\frac{V_s}{R_2} = \frac{L}{R_2} \frac{dI_1(t)}{dt} + I_L(t).$$

$$-\left(I_L(t) - \frac{V_s}{R_2}\right) = \frac{L}{R_2} \frac{dI_1(t)}{dt}$$

$$-\frac{R_2}{L} dt = \frac{dI_1(t)}{I_L(t) - \frac{V_s}{R_2}}$$

$$\text{Integrating both sides}.$$

$$-\frac{R_2}{L} t + C = \ln\left(I_L(t) - \frac{V_s}{R_2}\right).$$

$$Ae^{-R_2t} = I_L(t) - \frac{V_s}{R_2}.$$

$$\text{When } t = 0 \quad I_L(t) = 0 \quad \text{so } A = -\frac{V_s}{R_2}.$$

$$I_L(t) = \frac{V_s}{R_2}\left(1 - e^{-\frac{R_2}{L}t}\right).$$

Notice that the time constant for "charging" the inductor with current, 1/R2, is longer than that for discharging, 1/(R1+R2).

The fact that current takes time to rise is important in electromechanical devices such as motors and solenoids because force tends to be proportional to current. There is thus a time delay between switching on a relay by driving a voltage across its coil and the relay switch centacts operating.