ANSWERS TO NUMERICAL QUESTIONS (2004-2005)

1d) Plane spacing
$$d_{hkl} = a_0 / \sqrt{(h^2 + k^2 + l^2)}$$

For (101)
$$d_{101} = 0.5362/\sqrt{(1+0+1)}$$
nm
$$= 0.3792$$
nm

For (111)
$$d_{111} = 0.5362/\sqrt{(1+1+1)}$$
$$= 0.3096nm$$

For (113)
$$d_{113} = 0.5362/\sqrt{(1+1+9)}$$
$$= 0.1617 \text{nm}$$

For (040)
$$d_{040} = 0.5362/\sqrt{(0+16+0)}$$
$$= 0.1341 \text{nm}$$

1e) Angle between planes
$$(h_1k_1l_1)$$
 and $(h_2k_2l_2)$ is given by
$$\cos^{-1}[(h_1h_2+k_1k_2+l_1l_2)/\sqrt{((h_1^{\ 2}+k_1^{\ 2}+l_1^{\ 2})(h_2^{\ 2}+k_2^{\ 2}+l_2^{\ 2}))}]$$

$$(100) \land (110) = \cos^{-1} [1/\sqrt{2}] = 45.0^{\circ}$$

 $(111) \land (211) = \cos^{-1} [4/\sqrt{18}] = 19.5^{\circ}$

2b) Diffusion coefficient (D) =
$$D_0 \exp -[E_A/kT]$$

At 1250°C (1523K)
$$D = 12 \text{ x exp } -[4.05/(8.61 \text{ x } 10^{-5} \text{ x } 1523)] \text{ cm}^2/\text{s}$$

= 12 x exp -[30.89] cm²/s
= 4.6 x 10⁻¹³ cm²/s

For 60min
$$2\sqrt{(Dt)} = 2\sqrt{(4.6 \times 10^{-13} \times 3600)}$$
 cm $= 8.14 \times 10^{-5}$ cm $= 0.814 \mu m$