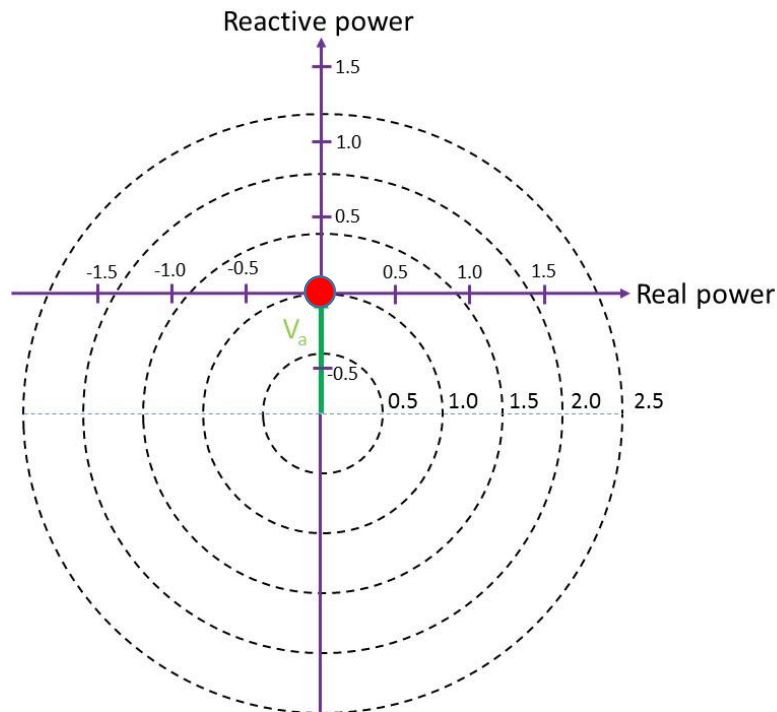


# Numerical example

Consider a 3-phase, 1.5MW, 50Hz, 8-pole, non-salient synchronous machine with a synchronous reactance of 1.25 per unit. The machine is connected to 6.6kV (rms) infinite busbars. Using the electrical diagram drawn previously for a machine with 1.25 per unit reactance.

Using a load diagram approach estimate the load angle, the real and reactive power for the following conditions:

a) On no load with 1.0 per unit excitation



On no-load, the generator does not supply or draw any net real or reactive power.

● Operating point

Load angle =  $0^\circ$

Real power = 0 per unit

Reactive power = 0 per unit

Although this can be solved in per unit, given that the question defines 1.0 per unit at 1.5MW, i.e the rated power, then we can equate per unit values with actual real and reactive powers

b) As a compensator with 2.0 per unit excitation

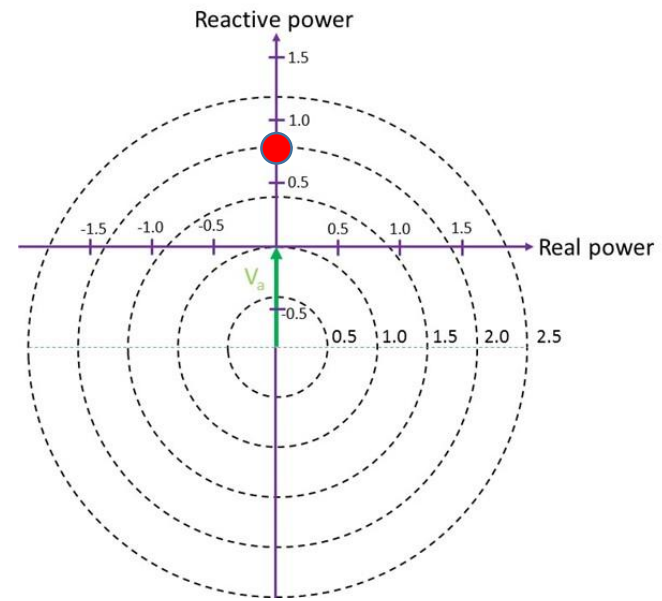
When acting as a compensator, the machine supplies +ive reactive power. Hence:

● Operating point

The load angle is  $0^\circ$

Real power = 0 per unit

Reactive power = 0.8 per unit (=1.2 MVar)



c) As a motor on full-load (1.0 per unit) operating at leading power factor of 0.87

$$\phi = \cos^{-1}(0.87) = 29.4^\circ$$

Draw a construction line at  $29.4^\circ$  for which intersects the 1.0 per unit real power contour at the operating point. We can then draw in E to establish load angle.

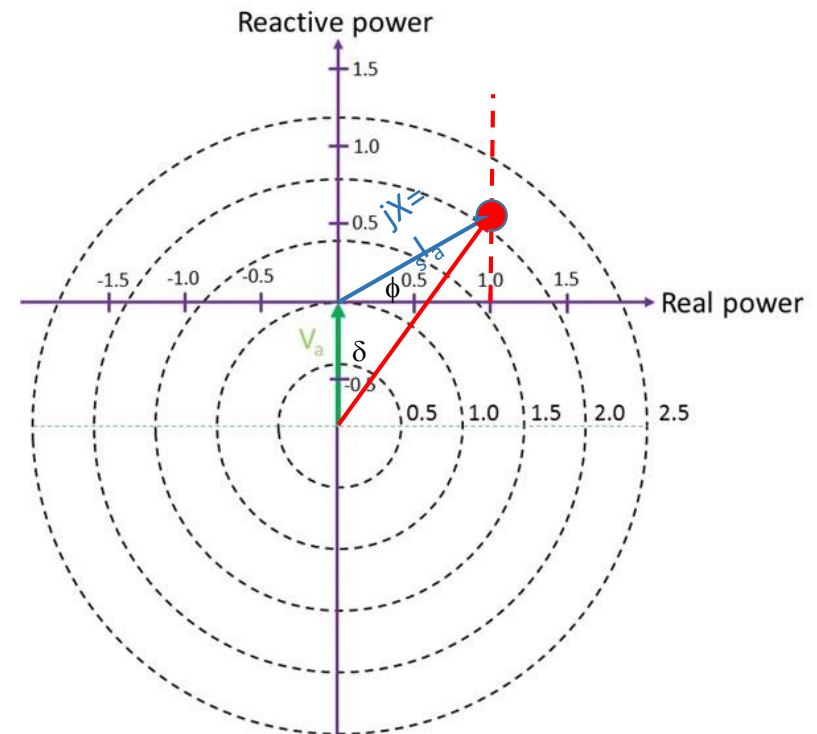
From load diagram:

$\delta = -36^\circ$  (note polarity from earlier definition)

Real power = 1.0 per unit = 1.5MW

From diagram:

Reactive power: 0.57 per unit = 0.8MVar



d) As a generator delivering a real power of 0.75 per unit at a power factor of 0.78 leading

$$\text{Apparent power (VA)} = \frac{\text{Real power}}{\text{Power factor}} = \frac{0.75}{0.78} = 0.961 \text{ per unit}$$

$$\text{Reactive power} = 0.862 \sin \phi = +0.68 \text{ per unit}$$

Draw construction lines for real and reactive power  
Intersection gives operating point. Draw E from origin gives:

$$\delta = +28^\circ \text{ (note polarity from convention)}$$

The actual real and reactive powers are:

$$P = -0.75 \times 1.5 = -1.12 \text{ MW}$$

$$Q = 0.6 \times 1.5 = +0.9 \text{ MVar}$$

