



The
University
Of
Sheffield.

EEE105

“Electronic Devices”

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Lecture 7

- Statistical mechanics and the Boltzmann function
→ Application in gases & band-gaps in semiconductors
- Formalisation of transitions between states
- Recombination and generation of carriers
- Magnitudes of n_i , σ for intrinsic semiconductors

Boltzmann Function

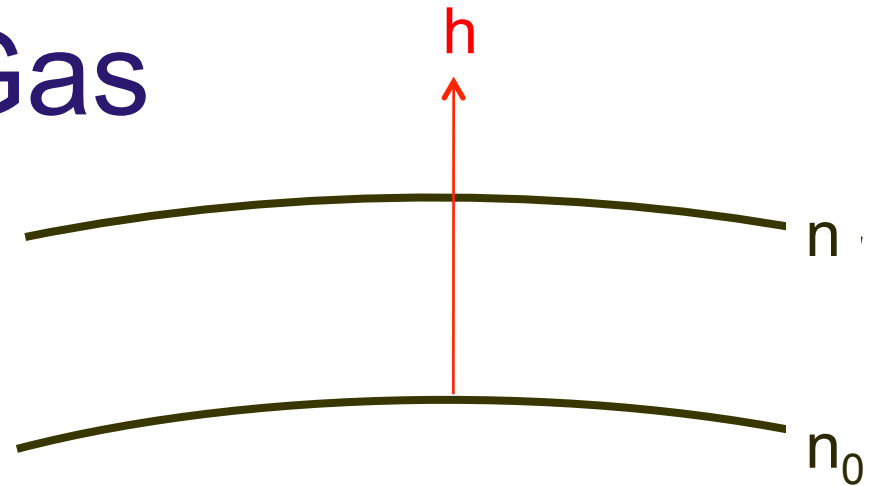
- Free electrons in a solid are similar to charged atoms in a gas
- Statistical mechanics of quantum theory is required
- Boltzmann's law – probability of finding molecules in a given spatial arrangement varies exponentially with the negative of potential energy of the arrangement divided by KT

$$n = (\text{constant}) \exp\left(-\frac{\text{P.E.}}{K_B T}\right)$$

Applications – Gas

In atmosphere P.E. = mgh

$$n = n_0 \exp\left(-\frac{mgh}{k_B T}\right)$$



m =mass

g =acceleration due to gravity

h =height

n =particle density at height h

n_0 =particle density at height $h=0$

Exponential decrease in density with height in the atmosphere

Applications – Electrons

Semiconductor P.E. = Band-gap

We therefore expect something like -

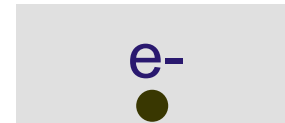
$$n_i = (\text{constant}) \exp\left(-\frac{E_g}{k_B T}\right)$$

In reality

$$n_i = (\text{constant}) \exp\left(-\frac{E_g}{2k_B T}\right)$$

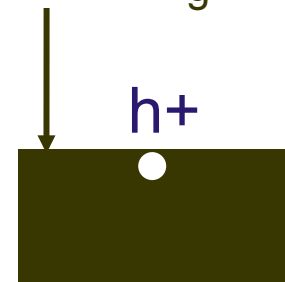
n_i shows exponential;
Increase with temperature
Decrease with band-gap

Conduction
Band

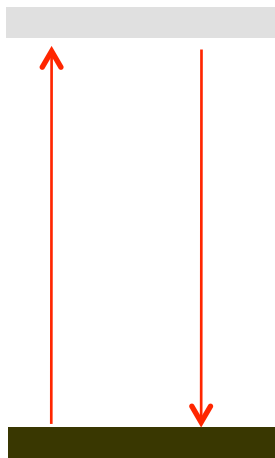


Band-gap = E_g

Valence
Band



Transition Between States



General Principle

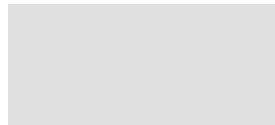
Transition rate, R , between two states is number of transitions per second

(We usually think of this as being per unit volume)

$$R \propto (\# \text{ candidates with enough energy}) \times (\# \text{ empty final states})$$

Thermal Generation

Conduction
Band



candidates with sufficient energy =
#initial states x Boltzmann factor

Boltzmann factor is related to Fermi –
levels not band edge

Valence
Band



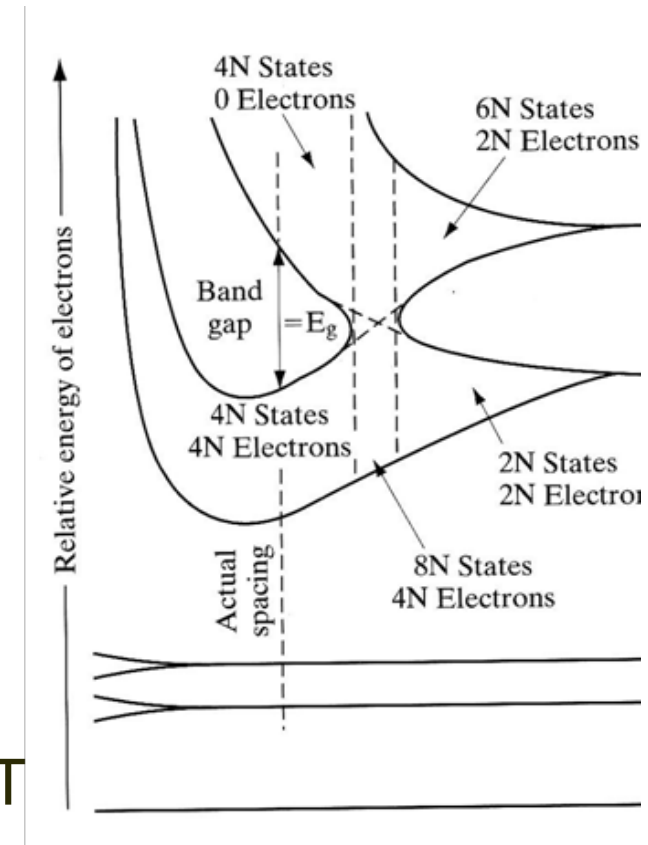
Density of electrons and holes related
to $E_g/2$

$$G \propto (\text{\#initial states}) \times \exp\left(-\frac{E_g}{2K_B T}\right) \times (\text{\#final states})$$

Full n_i equation

$$n_i = C T^{3/2} \exp\left(-\frac{E_g}{2K_B T}\right)$$

A new term - $T^{3/2}$ appeared !
Due to density of states changing with T



$$G \propto (\text{\#initial states}) \times \exp\left(-\frac{E_g}{2K_B T}\right) \times (\text{\#final states})$$

However, main temperature effect is the exponential part

Recombination

- From slide 7 – for recombination of electrons and hole

$R \propto (\# \text{ candidates with enough energy}) \times (\# \text{ empty final states})$

$$R \propto n p$$

$$R = B n p$$

- Where B is the (Einstein) recombination constant
 - Characteristic of different semiconductors
 - Independent of doping, n, p

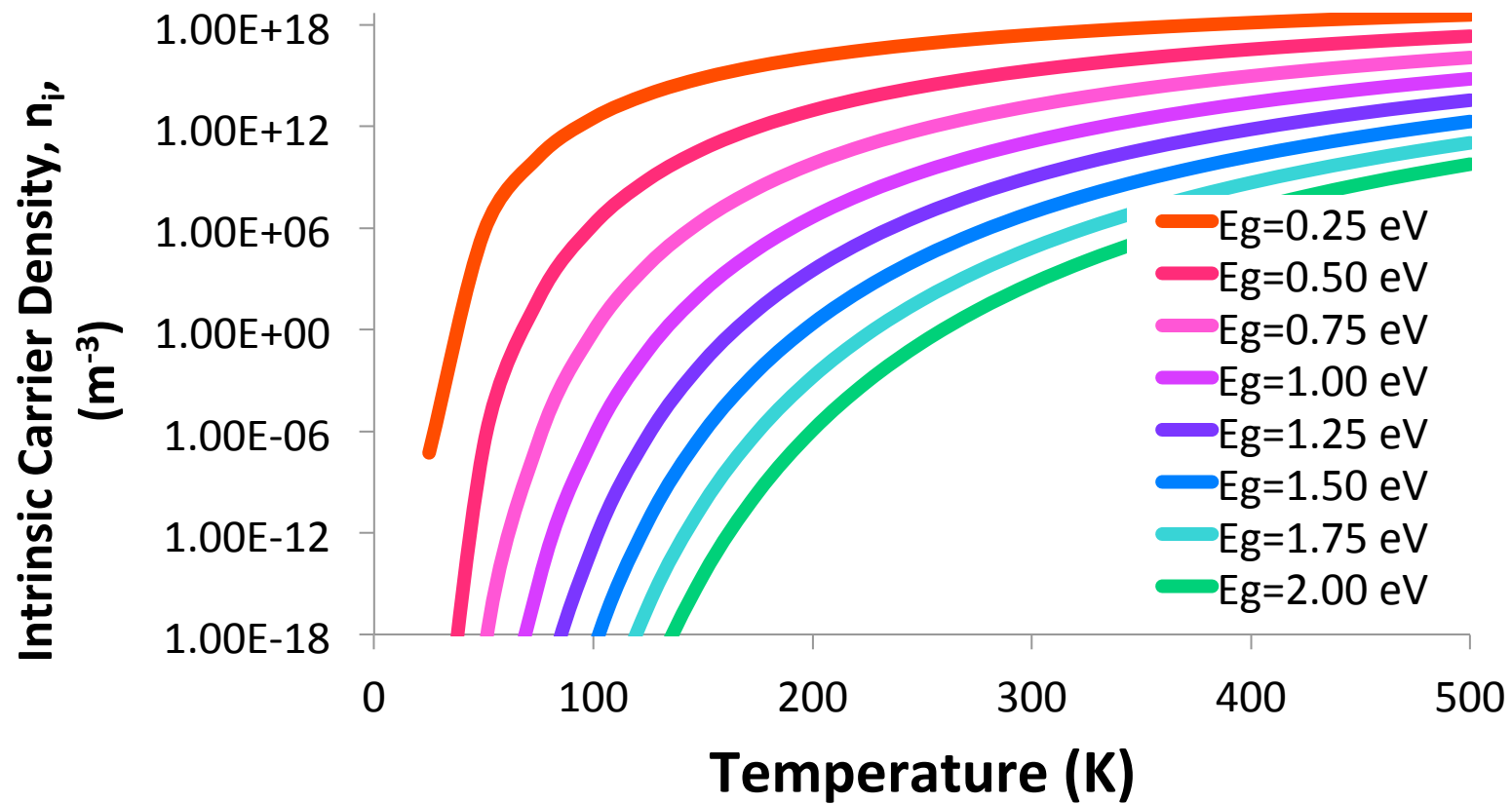
Equilibrium ($G=R$)

- Intrinsic Semiconductor

$$G = R = B n_i p_i = B n_i^2 \quad \text{As } n_i = p_i$$

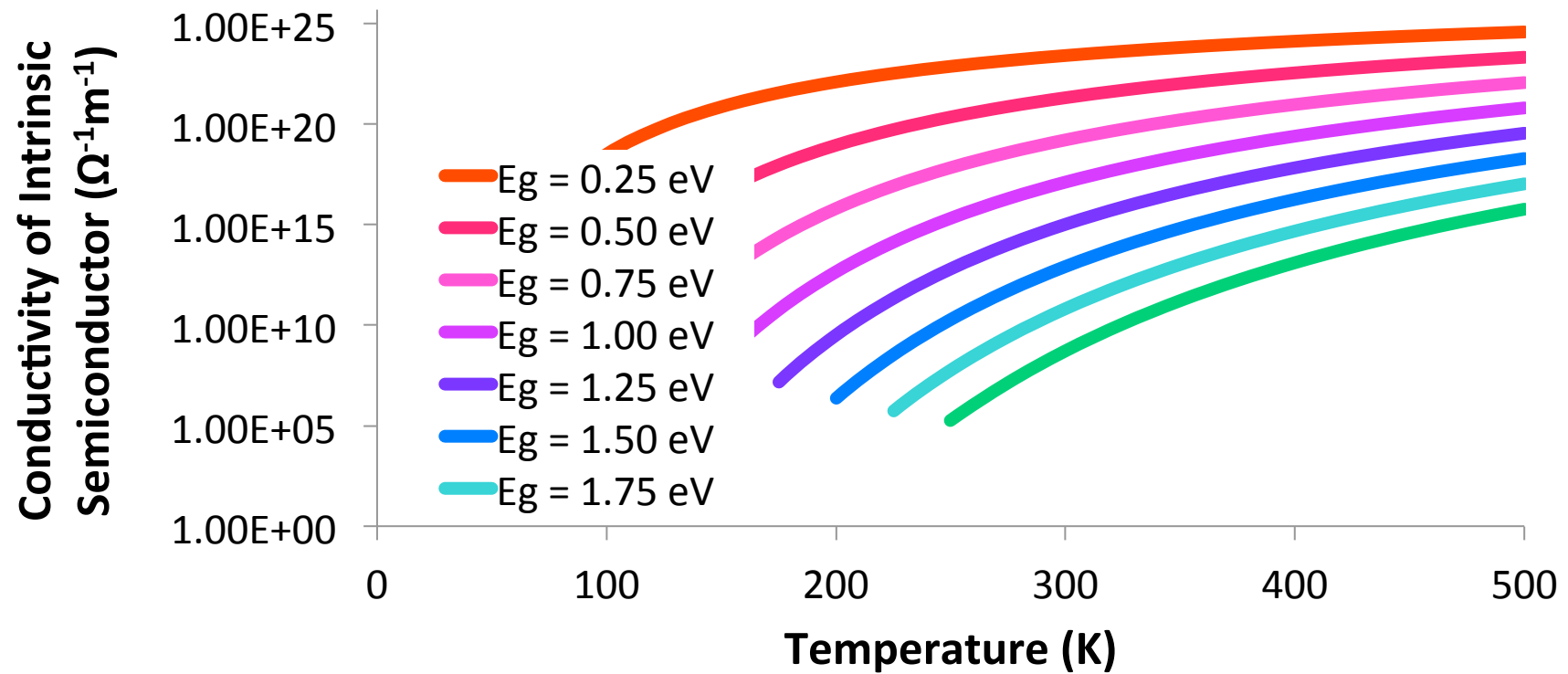
This will be very useful later - when we dope our semiconductors

How big is n_i ?





σ - Intrinsic Semiconductors



Summary

- The Boltzmann function has been introduced and applied to a semiconductor - intrinsic carrier density can be determined
- The transition between states is governed by the number of candidates with sufficient energy and the number of empty states
- Using this we can develop a fuller description for the intrinsic carrier density has been discussed
- Recombination of carriers is proportional to the electron density and hole density
- At equilibrium thermal generation and recombination rates are equal
- The effect of temperature and band-gap on intrinsic carrier density and conductivity has been explored – huge variations can be obtained through band-gap and temperature changes of intrinsic semiconductors