

Solutions to Tutorial Problem Sheet 7  
Week 9

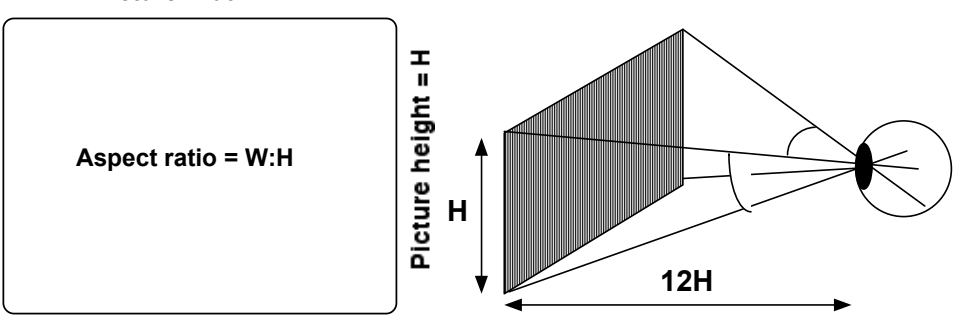
(Q.11)

- (i) Estimate the resolution (in pixels (picture elements) of a static display

Picture width = W

Aspect ratio = W:H

Picture height = H



Vertical angle subtended on eye =  $H / 12H = 1/12$  radians = 4.8 degrees  
Horizontal angle subtended on eye =  $(1/12) * (4/3) = 1/9$  radians = 6.4 degree

Spatial cut-off frequency = 60 cycles per degree

Therefore, No of cycles per picture height = 288  
No of cycles per picture width = 384

Using the Nyquist limit,

Pixels per picture height =  $288 \times 2 = 576$   
Pixels per picture width =  $384 \times 2 = 768$   
Spatial resolution is  $768 \times 576$

- (ii) Estimate the computer memory requirements (in bits) to hold (a) one monochrome screen, and (b) one full colour screen.

(a) Monochrome levels = 100

Solve  $2^N = 100$  to get  $N = 7$  bits per pixel

Therefore, total bits for a screen (a frame) =  $576 \times 768 \times 7 = 3,096,576$  bits

(b) Different colour levels = 50000 – usually represents as 2 chroma spectral bands.

Solve  $2^N = 50000$  to get  $N = 16$  bits per pixel.

In total  $16 + 7 = 23$  bits per pixel

Therefore, total bits for a screen (a frame) =  $576 \times 768 \times 23 = 10,174,464$  bits

- (iii) Estimate the total memory requirements to store one hour of video

The flicker rate is 70Hz. That means

Considering the Nyquist limit we should sample 140 frames per second.

$$\begin{aligned}\text{Totals bits per second} &= \text{total bits per frame} * \text{frames per second} \\ &= 10,174,464 \text{ bits/frame} * 140 \text{ frames/second} \\ &= 10,174,464 \times 140\end{aligned}$$

$$\begin{aligned}\text{Total bits per one hour} &= 10,174,464 * 140 * 60 * 60 \\ &= 5.1279 \times 10^{12} \text{ bits}\end{aligned}$$

$$\begin{aligned}(\text{divide by } 2^{30} \times 8 \text{ to convert to G Bytes}) \\ &= 597 \text{ Gbytes}\end{aligned}$$

- (iv) How do the above estimates compare with the actual screen resolution of practical displays and the total memory capacity of a DVD disc? Comment on your answers.

SDTV actual resolution 788\*576 @25 frames per second interlaced with 24 bits per pixel colour.

A CD-ROM can store 850 Mbytes

A single-layer DVD can store about 4.5 Gbytes.

A standard size of a hard disc in a PC is about 100-200 Gbytes

- (v) If the available bandwidth is premium and the Nyquist limit can be relaxed, revisit (i) and (iii) and define the new spatial and temporal resolutions. What is the new data rate?

If the Nyquist limit is relaxed we can exploit the CRT display mechanisms to reduce the bandwidth by reducing the spatial resolution and the frame rate.

Revisiting (i)

$$\text{Number of active lines using the Kell factor of 0.7} \quad \text{lines} = 288 / 0.7 = 411$$

$$\text{Therefore, active pixels per line} = 411 * 4/3 = 548$$

$$\text{Spatial Resolution} = 548 \times 411$$

Revisiting (iii)

The flicker rate is 70Hz. That means 70 fields per second of interlaced video is sufficient. In other words, 70 fields per second are equivalent to 35 frames per second.

The number of bits per pixel is still 23.

Now we can compute the new data rate:

$$= \text{bits/pixel} \times \text{pixels/line} \times \text{lines/frame} \times \text{frames/sec}$$

$$= 23 \times 548 \times 411 \times 35$$

$$= 181,308,540 \text{ bits/sec}$$

for one hour

=  $181,308,540 \times 60 \times 60$  bits/sec (Now divide by  $2^{30} \times 8$  to convert to G Bytes)

= 76 Gbytes.

Data rate can be further reduced by Chrominance sub-sampling and of course by compression.

For example by using 4:2:2 we need only 7 bit for luminance + 16/2 bits for chrominance. (4:2:2 results in  $W \times H/2$  resolution)

Therefore we only need an equivalent of 15 bits/pixel for 4:2:2.

In 4:2:0, the chrominance resolution is  $W/2 \times H/2$ . That means they only need 16/4 bits for chrominance data. Therefore the total equivalent bits per pixel is  $7+4 = 11$  bits/pixel. You can approximately halve the data rate ( $11 \sim 23/2$ ) by using 4:2:0.