

Properties of Fourier Transform

| Property | Aperiodic signal, $x(t)$ | Fourier Transform, $X(\omega)$ |
|------------------------------|--|--|
| Linearity | $ax_1(t) + bx_2(t)$ | $aX_1(\omega) + bX_2(\omega)$ |
| Time Shifting | $x(t - t_o)$ | $e^{-j\omega t_o} X(\omega)$ |
| Frequency Shifting | $e^{j\omega_o t} x(t)$ | $X(\omega - \omega_o)$ |
| Time Scaling | $x(at)$ | $\frac{1}{a} X\left(\frac{\omega}{a}\right)$ |
| Differentiation in Time | $\frac{dx(t)}{dt}$ | $j\omega X(\omega)$ |
| Differentiation in Frequency | $tx(t)$ | $j \frac{dX(\omega)}{d\omega}$ |
| Integration in time | $\int_{-\infty}^t x(\tau) d\tau$ | $\frac{X(\omega)}{j\omega} + \pi X(0) \delta(\omega)$ |
| Convolution | $x(t) * h(t)$ | $X(\omega) \cdot H(\omega)$ |
| Multiplication in time | $x(t) \cdot h(t)$ | $\frac{1}{2\pi} \int_{-\infty}^{\infty} X(\lambda) H(\omega - \lambda) d\lambda$ |
| Parseval's Theorem | $E = \int_{-\infty}^{\infty} x(t) ^2 dt = \frac{1}{2\pi} \int_{-\infty}^{\infty} X(\omega) ^2 d\omega$ | |