ANSWERS TO NUMERICAL QUESTIONS (2003-2004)

1(c) Plane spacing
$$d_{hk1} = a_0 / \sqrt{(h^2 + k^2 + l^2)}$$

For (220)
$$d_{220} = 0.5646 / \sqrt{(4+4+0)} nm$$
$$= 0.1996 nm$$

For (310)
$$d_{310} = 0.5646/\sqrt{(9+1+0)}$$
$$= 0.1785 \text{nm}$$

For (311)
$$d_{311} = 0.5646/\sqrt{(9+1+1)}$$
$$= 0.1702 \text{nm}$$

For (422)
$$d_{422} = 0.5646/\sqrt{(16+4+4)}$$
$$= 0.1152 \text{nm}$$

(d) Angle between planes
$$(h_1k_1l_1)$$
 and $(h_2k_2l_2)$ is given by
$$\cos^{-1}[(h_1h_2+k_1k_2+l_1l_2)/\sqrt{((h_1^2+k_1^2+l_1^2)(h_2^2+k_2^2+l_2^2))}]$$

$$(001) \wedge (111) = \cos^{-1}\left[1/\sqrt{3}\right] = 54.7^{\circ}$$

$$(001) \land (111) = \cos^{-1}[1/\sqrt{3}] = 54.7^{\circ}$$

 $(011) \land (311) = \cos^{-1}[2/\sqrt{22}] = 64.8^{\circ}$

(e)
$$[121] \cdot [1\bar{1}1] = 0$$
 then (121) is perpendicular to (1 $\bar{1}1$)
$$[\bar{1}10] \cdot [1\bar{1}3] = 1$$
 then ($\bar{1}10$) is not perpendicular to (1 $\bar{1}3$)
$$[\bar{1}00] \cdot [0\bar{1}3] = 0$$
 then ($\bar{1}00$) is perpendicular to (0 $\bar{1}3$)

4(b) Diffusion coefficient (D) =
$$D_0 \exp -[E_A/kT]$$

At 1120°C (1393K)
$$D = 0.76 \text{ x exp} - [3.46/(8.62 \text{ x } 10^{-5} \text{ x } 1373)] \text{ cm}^2/\text{s}$$

= 1.53 x 10⁻¹³ cm²/s

For 60s
$$2\sqrt{(Dt)} = 2\sqrt{(1.53 \times 10^{-13} \times 60)} \text{ cm}$$
$$= 6.06 \times 10^{-6} \text{ cm}$$
$$= 0.06 \mu\text{m}$$

Then, autodoping is not a problem.