O2 (2-j2) $\Gamma = \sqrt{2^2 + 2^2} = \sqrt{8} = 2.83$ $\phi = tan^{-1} \frac{-2}{2} = -45^{\circ}$ 2.83/-45

 $(3+18) \qquad r = \sqrt{3^2+8^2} = \sqrt{73} = 8.54 \quad \phi = \tan^{-1}\frac{8}{3} = 69.4^{\circ}.$ $8.54 \cdot 169.4$

 $(-5+13) \quad \Gamma = \sqrt{5^2+3^2} = \sqrt{34} = 5.83 \quad \emptyset = \tan^{-1} \frac{3}{-5} = -31$ angle angle required area so angle w.r.t. positive $\text{calculated} = \frac{1}{5} \text{ angle required} \quad \text{area} = 180^{\circ} + (-31^{\circ}) = 149^{\circ}$

5.83<u>[14</u>9

(-4-j4) $\Gamma = 4\sqrt{1+1} = 5.66$ $\emptyset = tam^{-1} - 4 = 45^{\circ}$ -4 tangke tangke

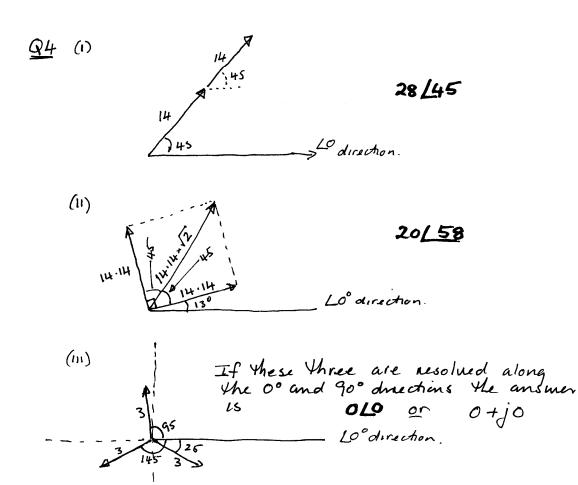
(2-j2)(3+j8) = 22+j10 $r = \sqrt{584} = 24.2$ $\phi = 24.4$ °

24-2/24-4

check using first two. (2.83/-45) × (8.54/69.4) = 2.83 × 8.54 / (-45+69.4) = 24.2/24.4

$$(-5+j3)-(-4-j4)=-1+j7$$
 $r=7.1$ $\phi=\tan^{-1}\frac{7}{4}=-81.9$
calculated $+\frac{7}{4}$ required this angle is in the negative real angle angle required = $180+(-81.9)$
 -1 $= 98.1$

Q3
$$6L45 = 6\cos 45 + 6j\sin 45 = 4.2 + j4.2$$
.
 $50/-170 = 50\cos(-170) + 50j\sin(-170) = -49.2 - j8.7$
 $4/105 = 4\cos 105 + 4j\sin 105 = -1 + j3.9$
 $3/-90 = 3\cos(-90) + 3j\sin(-90) = 0 - 3j$
 $(5/-30)(6/120) = 30/90 = 0 + j30$
 $3/15 + 3/135 + 3/-105 = 2.90 + j0.78 - 2.12 + 2.12j$
 $-0.78 - 2.9j = 0 + j0$



Q5 (1) The impedance of the components is

$$\frac{V}{I} = \frac{280/150}{11/140} = \frac{280}{11} 10 = 25.46/10$$

25.46/10 = 25.1 + j4.42

Since the phase of V. w.r.t. I is positive the circuit is inductive and since the phase is less than 90° these must be surstance involved So the series combination is L+R.

(11) The impedance of a series L-R combination 15 Z=R+JWL

and this must be equal to the impedance calculated from the given V + I

$$R + JWL = 25.1 + J4.42$$

$$R = 25.1 J$$

$$WL = 4.42 \quad \text{or} \quad L = \frac{4.42}{2.71.f} = \frac{4.42}{800}$$

$$= 5.5 \text{ mH}$$

(111) The peak value of current is 11 A and this flows through R

$$\frac{1}{2} P_{Diss} = \frac{Ip}{2} \times R = \frac{121}{2} \times 25.1 = \frac{1.52 \text{ kW}}{2}$$
mean squared value

$$\frac{Q6}{|Z|} = \frac{230}{10} = \sqrt{2^2 + W^2L^2}$$

$$\left(\frac{230}{10}\right)^2 = 529 = 4 + W^2L^2$$

$$L^2 = \frac{529 - 4}{W^2} = \frac{525}{(2.\Pi.50)^2} = 5.32 \times 10^{-3}$$

$$\therefore L = 73 \text{ mH}.$$

Q7
$$|Z| = 110 = \sqrt{47^2 + \frac{1}{W^2c^2}} = \sqrt{47^2 + \chi_e^2}$$

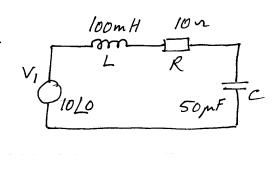
 $110^2 - 47^2 = \chi_c^2 = 9.89 \times 10^3$
 $\therefore \chi_c = 99.5 \text{ Jz}$.
 $\chi_c = \frac{1}{2\pi fc} \therefore C = \frac{1}{2\pi f. \chi_c} = 16\mu F$

$$Q = -tam^{-1} \frac{x_c}{R} = -tam^{-1} \frac{99.5}{47}$$

$$= 64.7^{\circ}$$
In this case the current leads the voltage so the Ixc phase of I w.r.t. V is
$$\frac{64.7^{\circ}}{64.7^{\circ}}$$

Q8 at 50 Hz
$$X_L = j2\pi fL = j31.4$$
 $X_C = \frac{1}{j2\pi fC} = -j63.7$

at 150 Hz $X_L = j94.2$
 $X_C = -j21.2$



(i) for 50Hz,
$$10+j0 = I[j31\cdot4+10-j63\cdot7]$$

$$I = \frac{10L0}{10-j32\cdot3} = \frac{10L0}{33\cdot8L-72\cdot8} = \frac{0\cdot3L73^{\circ}}{33\cdot8L-72\cdot8}$$

$$V_{c} = IX_{c} = -j63\cdot7\left(0\cdot3L73\right)$$

$$= (63\cdot7L-90)\left(0\cdot3L73\right)$$

$$= 18\cdot8L-17$$

(ii) for 150 Hz
$$10 + j0 = I[j94.2 + 10 - j21.2]$$

 $= I[10 + j73] = I[73.7/82]$
 $\therefore I = \frac{10 \angle 0}{73.7/82} = \frac{0.14 \angle -82}{73.7/82}$

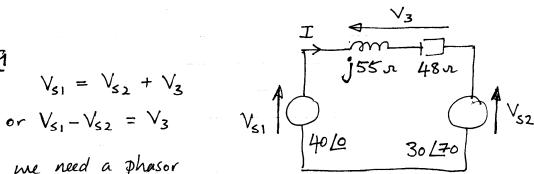
$$V_{c} = IX_{c} = (0.14 L - 82)(0 - j21.2)$$

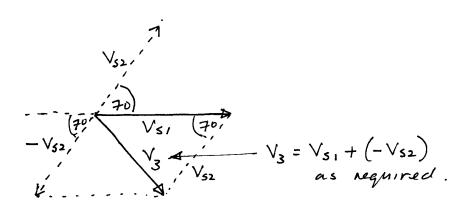
$$= (0.14 L - 82)(21.2 L - 90)$$

$$= 2.9 L - 172$$

$$Qq$$
 $V_{s_1} = V_{s_2} + V_3$
or $V_{s_1} - V_{s_2} = V_3$

me need a phasor dragram to represent this vector equation...





using the cosine rule ...

$$V_3^2 = V_{S_1}^2 + V_{S_2}^2 - 2V_{S_1}V_{S_2} \cos 70$$

where all Vs are the modul; of the appropriate quantity

$$V_3^2 = 1600 + 900 - 2 \times 1200 \times 0.342$$

$$= 2500 - 821 = 1679 V^2$$

$$V_3 = 41 V$$

(11)
$$40\underline{10} = 40+j0$$

 $30\underline{170} = 10.3+j28.2$

(iii)
$$I = \frac{40 \cancel{10} - 30 \cancel{170}}{\cancel{7}} = \frac{40 + j0 - 10 \cdot 3 - j28 \cdot 2}{48 + j55}$$
$$= \frac{29 \cdot 7 - j28 \cdot 2}{48 + j55} = \frac{(29 \cdot 7 - j28 \cdot 2)(48 - j55)}{48^2 + 55^2}$$
$$= -0.024 - j0.561$$

An phases are measured with respect to Vs1.

Q10 (1) Total Z seen by

Sowce is

$$Z_T = \frac{V_3}{I} = \frac{50/45}{2.5/-15}$$
 $= 20/60$
 V_3
 V_3
 V_4
 V_5
 V_5

ZI is also equal to the series circuit

$$Z_{T} = j8 + 5 + Z$$

$$\therefore 20/60 = j8 + 5 + Z = (10 + j17.3)$$

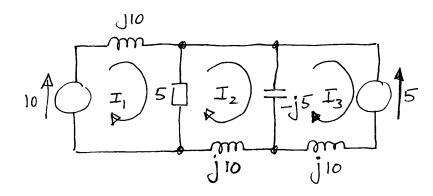
$$\therefore Z = 10 + j17.3 - j8 - 5$$

$$= 5 + j9.3 = 10.6/61.7$$

- (ii) Z has a real part + α + j term so the circuit is inductive and could consist of a resistance R = 5x in series with an inductional $X_L = j9.3 x$.
- (III) If the source phase is modified to 5010, all the other phases of voltages + currents are reduced by 45° so I = 1.51-60

But Z depends only on the components and hence remains unchanged at Z = 5 + j9.3.

Q11



loop
$$I_1$$
: $10 = j10 I_1 + 5(I_1 - I_2)$
 $2 = j2I_1 + I_1 - I_2$
 $2 = I_1(1+j2) - I_2$

loop
$$I_2$$
 $5(I_2-I_1) + j 10 I_2 - j 5(I_2-I_3) = 0$
 $I_1 - I_1 + 2j I_2 - j I_2 + j I_3 = 0$
 $I_2(i+j) + j I_3 - I_1 = 0$

loop
$$I_3$$
 5+ $j_10 I_3 - j_5 (I_3 - I_2) = 0$
 $1 + j_2 I_3 - j_3 + j_2 = 0$
 $1 + j_3 + j_2 = 0$ 3

sub 3 into 2
$$I_{2}(1+j) - (1+jI_{2}) - I_{1} = 0$$

$$I_{2}+jI_{2}-1-jI_{2}-I_{1}=0$$

$$I_{2}-I_{1}-1=0$$
(4)

sub
$$\oplus$$
 mto \bigcirc
 $2 = I_1(1+2j) - I_1 - 1$
 $2 = I_1 + 2jI_1 - I_1 - 1$
 $3 = 2jI_1$ or $I_1 = -1.5j$

sub I, into (1)

$$2 = -1.5j(1+2j) - I_2$$

 $2 = -1.5j + 3 - I_2$

$$-1+1.5j = -I_2$$
 or $I_2 = 1-1.5j$

sub I₂ Into 3

$$1+jI_3+j(1-1.5j)=0$$
 $1+jI_3+j+1.5=0$
 $2.5+j=-I_3=-j2.5+1$

or $I_3=-1+j2.5$

Power delivered to cet =
$$10 \times real I_1 + 5 \times real (-I_3)$$

= $0 + 5$
= $5W$.