

Tutorial 1

1. How is the unit step function $u(t)$ related to (i) $\delta(t)$ and (ii) ramp function $r(t)$?

2. For a signal $x(t) = 3u(t) - u(t-2)$, sketch and label

(i) $x(t)$ (ii) $\frac{dx(t)}{dt}$ (iii) $x(2t)$ (iv) $x(t/2)$ (v) $x(1-t)$

3. For $x(t) = u(t+2) - 2u(t) + u(t-1)$, sketch and label

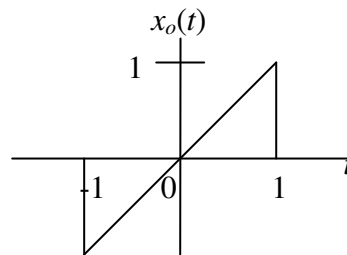
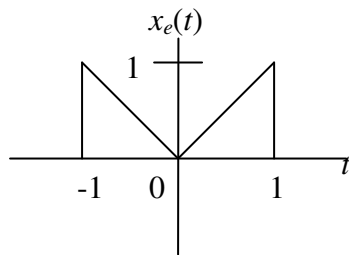
(i) $x(t)$ (ii) $\int_{-\infty}^t x(\tau) d\tau$

4. For $x(t) = \delta(t+3) - 2\delta(t-3)$, sketch and label

(i) $x(t)$ (ii) $\int_{-\infty}^t x(\tau) d\tau$

5. Sketch and label $x(t) = e^{-t}u(t) + e^{-t}u(t-2) + e^{t-4}u(t-4)$.

6. Find the signal that has an even and an odd component shown below.



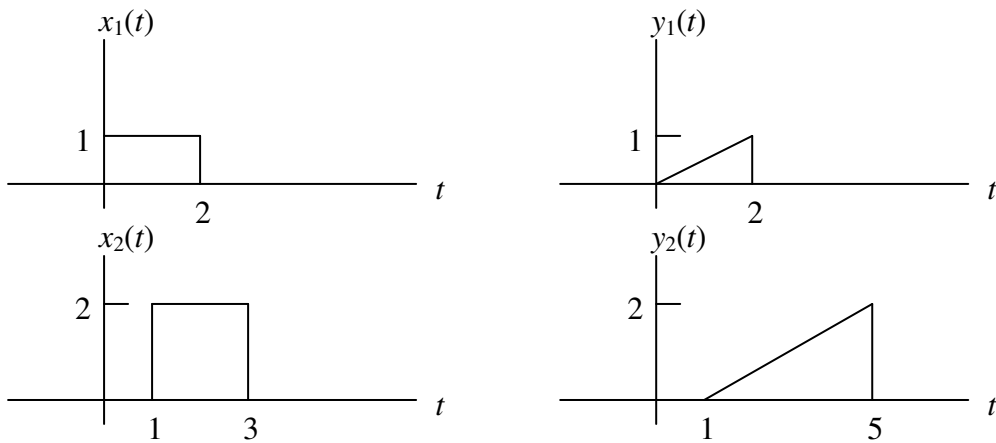
7. Consider a sinusoidal signal $x(t) = A\cos(\omega t)$. Determine the average value, the average power and the root mean square of $x(t)$.

8. Are the following systems with or without memory, causal or noncausal?

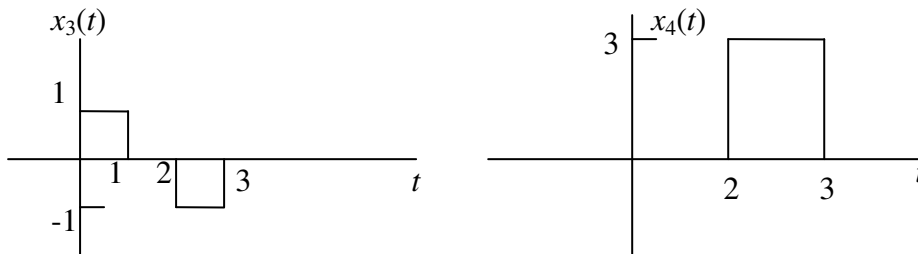
(i) $y(t) = 2u(t)$ (ii) $y(t) = \sin(u(t))$ (iii) $y(t) = \sin(u(t+1))$ (iv) $y(t) = e^{t-2} \cdot u(t-2)$

9. Is the system represented by $y(t) = 1/x(t)$ linear and time-invariant?

10. Consider a linear system with an input-output pairs shown below.



(i) Is the system time invariant? Can we compute the response to the inputs $x_3(t)$ and $x_4(t)$?



(ii) If $y_1(t)$ is the response of another system that is linear time-invariant when the input is $x_1(t)$, find the system response to a unit step function.