where 
$$\tilde{R} = \omega \sqrt{L^{*}C^{*}} \sqrt{1-j} \frac{G^{*}}{\omega C^{*}}$$
with  $\omega = \omega \int \sqrt{L^{*}C^{*}} \sqrt{1-j} \frac{G^{*}}{\omega C^{*}}$ 
 $\omega = \omega \int \sqrt{L^{*}C^{*}} \sqrt{1-j} \frac{G^{*}}{\omega C^{*}}$ 

## . case: weak absorption: occusion

Use 
$$\sqrt{1-jx} = 1 - \frac{1}{2}jx$$

$$\frac{1}{2} \approx \omega \sqrt{L^*C^*} - j \frac{\sigma}{2} \sqrt{\frac{\rho \circ \rho_r}{\varepsilon_0 \varepsilon_r}} = \frac{1}{2} \frac{1}{\varepsilon_0 \varepsilon_r} = \frac{1}{2} \frac{1}{\varepsilon_0 \varepsilon_r}$$

$$\frac{1}{2} \frac{1}{\varepsilon_0 \varepsilon_r} = \frac{1}{2} \frac{1}{\varepsilon_0$$

$$E = E_0 \underbrace{e_7}_{i} \underbrace{e_j(\omega t - k_0 x)}_{i} \underbrace{e^{-\beta x}}_{i}$$

$$\underbrace{H} = H_0 \underbrace{e_1}_{i} \underbrace{e_j(\omega k - k_0 x)}_{i} \underbrace{e^{-\beta x}}_{i}$$

$$\underbrace{S = E_x H}_{i} \quad \text{with} \quad S = EH_x \underbrace{e^{-2\beta x}}_{i}$$

## 2. case: stronj absorption: 0 >> WESE

$$= \sqrt{\frac{\omega \sigma \nu_{o} p_{r}}{2}} \quad (1-j) = \frac{1}{5} \quad (1-j)$$

$$E = E_0 e_7 e$$

$$E = E_0 e_7$$

Note of the becomes very small at high frequencies; i.e. the power (current) travels only close to the surface in a conductor (skin effect).

numerical examples: for copper (Cu), 0 = 6.10 (Scm)-1 @ 50 Hz > 5 = \\ \frac{2}{2\overline{1}\tau \sigma \cdot \pop\_1} = 9 mm but e IMHz: 5 = 70 pm

@ 306Hz: 8 = 0.4 pm

for sea water, 0 = 4 Sv/m, Er=80 @ 100 MHZ

> power penetration is half of this , i.e. ~ lom

= communication with sub-marines only works at lower frequencies 10-200 kHz, where of is much bigger! 

	material	٤٠	pr
	air	1	1
	AL	ı	1
didadrica /	paper	2.3	1
	∫:0 <sub>ℓ</sub>	3.9	1
	Htor	52	1
	8:03 / NP 201	>40	, 1
myretica	ferrite	0	16-600
	mu-metal	1	50,000
	99.95% pure Fe	1	200,000

examples:

glass, light (visible, e.g. red light with 
$$\lambda = 600 \text{ nm}$$
):

->  $\sigma = 10^{-16} \text{ Sv/m}$ ,  $\varepsilon_r = 5$ ,  $\omega = 2\pi f = 2\pi \frac{c}{\lambda} = 3.10^{15} \text{ Hz}$ 

=>  $\frac{\sigma}{\omega \varepsilon_0 \varepsilon_0} = 7.5 \cdot 10^{-21} \ll 1$  it weakly absorbing

copper, weak X-rays (
$$\lambda = 10 \text{ nm}$$
):

 $T = 6.10^{\frac{1}{2}} \text{ Sv/m}$ ,  $E_r = 1$ ,  $\omega = \lambda \pi f = \lambda \pi \frac{c}{\lambda} \approx 2.10^{\frac{17}{2}} \text{ Hz}$ 
 $T = \frac{\sigma}{\omega \varepsilon_0 \varepsilon_r} \approx 36$  331 is strongly absorbing

## complex permittivity and absorption

re-write with complex permittivity

and we E=Ee j(wt-Tx), i.e. 
$$\frac{\partial E}{\partial t} = j\omega E$$

compare real parts:  $E_r' = E_r$  describes unal relationship between field & flux

compare imaginary parts:

Ex = - \frac{\sigma}{\sigma} devibes absorption

due to finite conductivity

If we write for the refractive index in complex notation

$$\Rightarrow \quad \begin{cases} \varepsilon_r^1 = n^{12} - \chi^2 \\ \varepsilon_r^4 = 2n^1 \chi \end{cases}$$

=> Link between dielectric and optical properties.