

Automata, Computability, and Complexity

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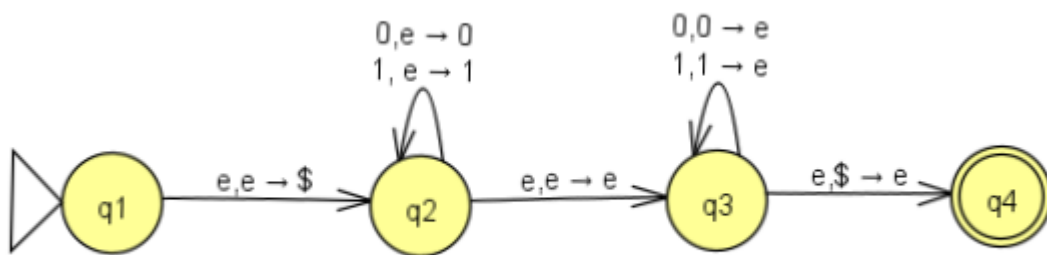
SHEET #5:

Exercise 1 :

a)

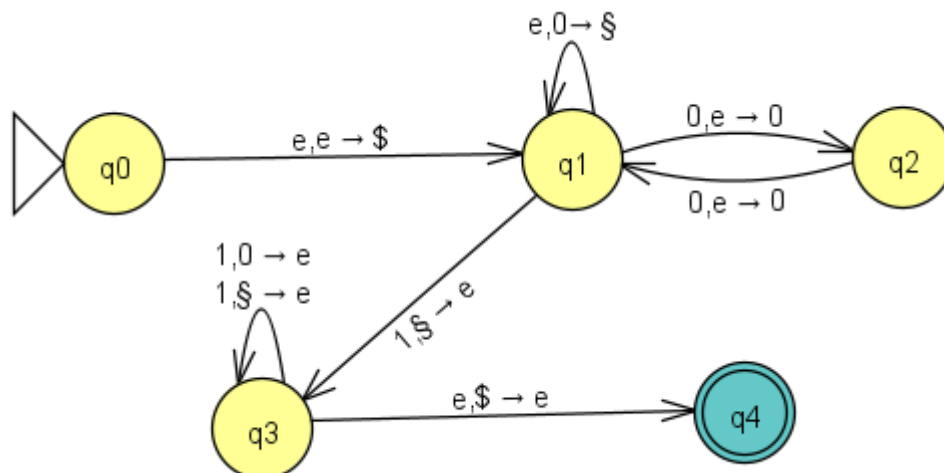
$$M = (\{q_1, q_2, q_3, q_4\}, \{0, 1\}, \{0, 1, \$\}, \delta, q_1, \{q_1, q_4\})$$

The STD:



b)

$$M = (\{q_0, q_1, q_2, q_3\}, \{0, 1\}, \{0, 1, \$, \$\}, \delta, q_0, \{q_4\})$$



Exercise 2:

a) The language described by M1 is:

with $\Sigma = \{a, b, c\}$ $L1 = \{a^x b^y c^z \text{ with } x+y=z \text{ and } x, y, z \in \mathbb{N}\}$

b) The language described by M2 is:

with $\Sigma = \{0, 1\}$ $L1 = \{w \mid w \text{ is either the empty string or a string that start with 0 and has as many 0 as 1 with at no time more 1s than 0s}\}$

Exercise 3:

a) We find from the mPDA M that:

$S \rightarrow TT \mid e$

$T \rightarrow 1T0 \mid e$

b)

$S \Rightarrow TT$

$S \Rightarrow (1T0)(1T0)$

$S \Rightarrow (1(1T0)0)(1(1T0)0)$

$S \Rightarrow (11(e)00)(11(1T0)00)$

$S \Rightarrow (1100)(11(1(e)0)00)$

$S \Rightarrow 1100111000$

Exercise 4:

a) Mahdi Ouchrahou