

[illegible]

Database System Concept (CSE 3103)

Lecture 06-Day 02

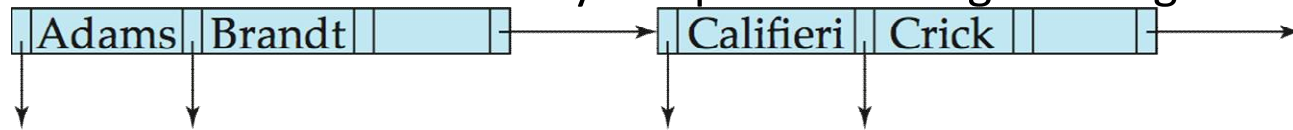
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Updates on B⁺-Trees: Insertion

1. Find the leaf node in which the search-key value would appear
2. If the search-key value is already present in the leaf node
 1. Add record to the file
 2. If necessary add a pointer to the bucket.
3. If the search-key value is not present, then
 1. add the record to the main file (and create a bucket if necessary)
 2. If there is room in the leaf node, insert (key-value, pointer) pair in the leaf node
 3. Otherwise, split the node (along with the new (key-value, pointer) entry) as discussed in the next slide.

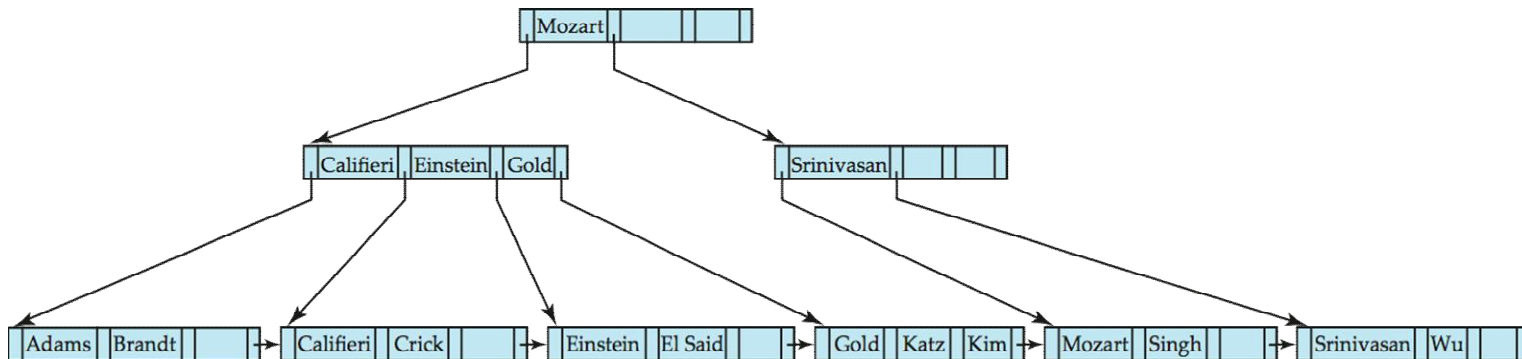
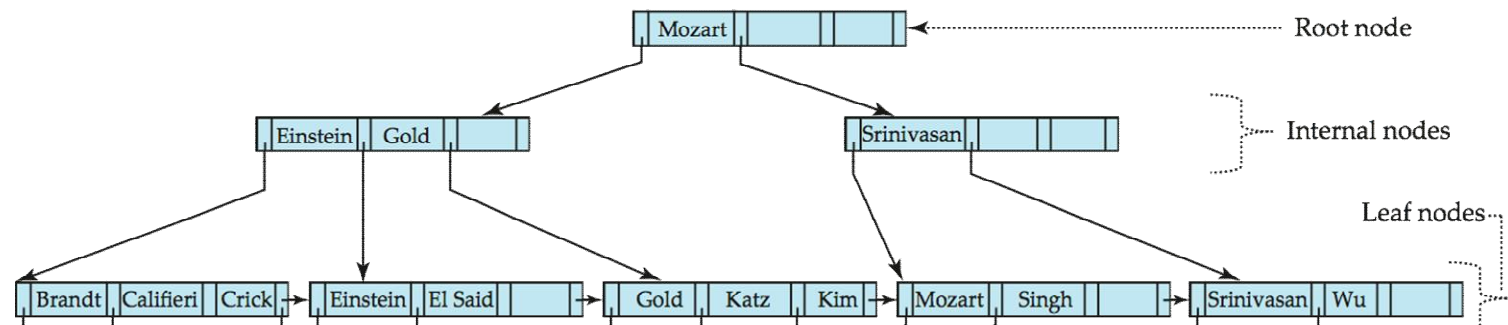
Updates on B⁺-Trees: Insertion (Cont.)

- Splitting a leaf node:
 - take the n (search-key value, pointer) pairs (including the one being inserted) in sorted order. Place the first $\lceil n/2 \rceil$ in the original node, and the rest in a new node.
 - let the new node be p , and let k be the least key value in p . Insert (k,p) in the parent of the node being split.
 - If the parent is full, split it and **propagate** the split further up.
- Splitting of nodes proceeds upwards till a node that is not full is found.
 - In the worst case the root node may be split increasing the height of the tree by 1.



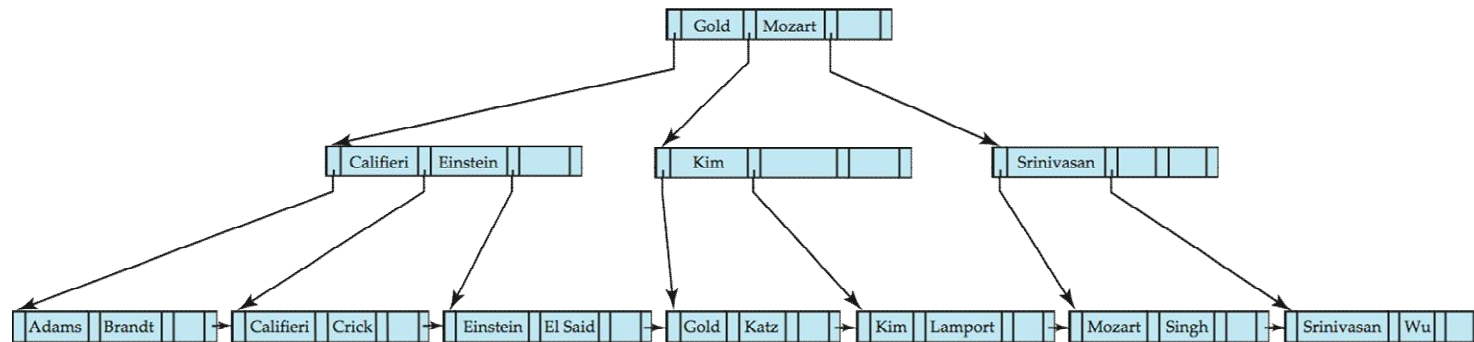
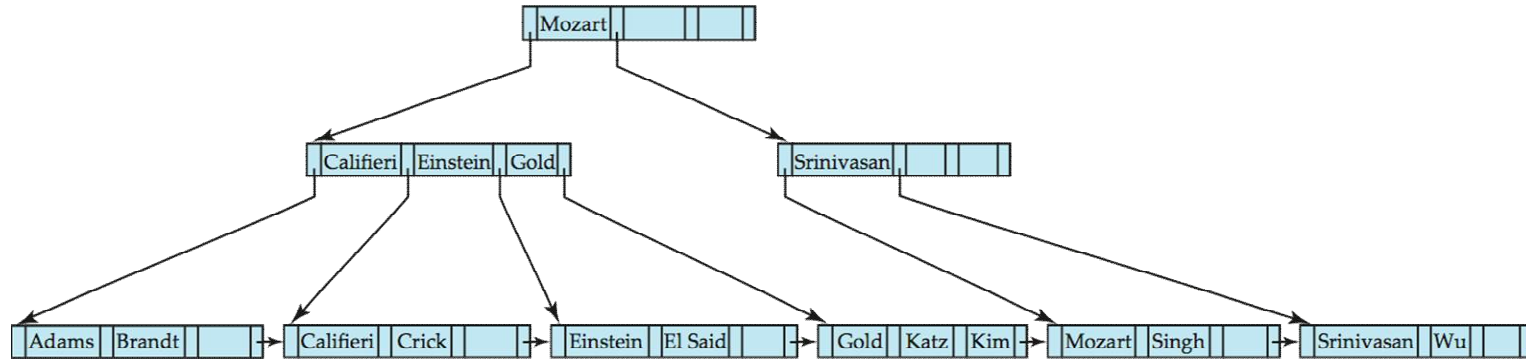
Result of splitting node containing Brandt, Califieri and Crick on inserting Adams
Next step: insert entry with (Califieri, pointer-to-new-node) into parent

B⁺-Tree Insertion



B⁺-Tree before and after insertion of “Adams”

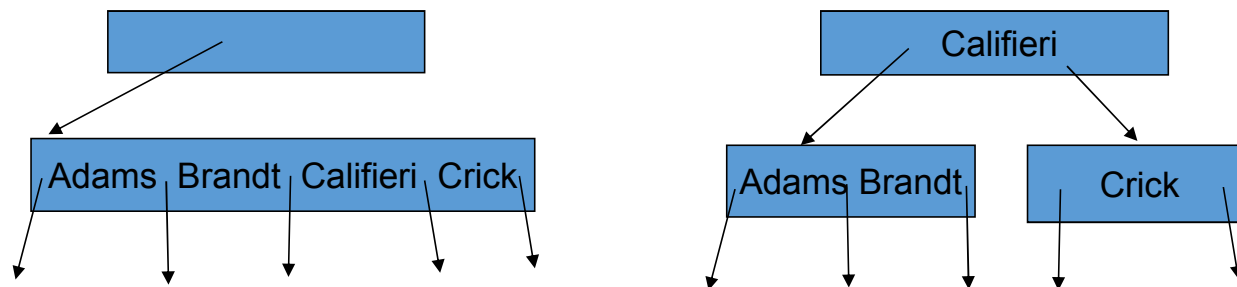
B⁺-Tree Insertion



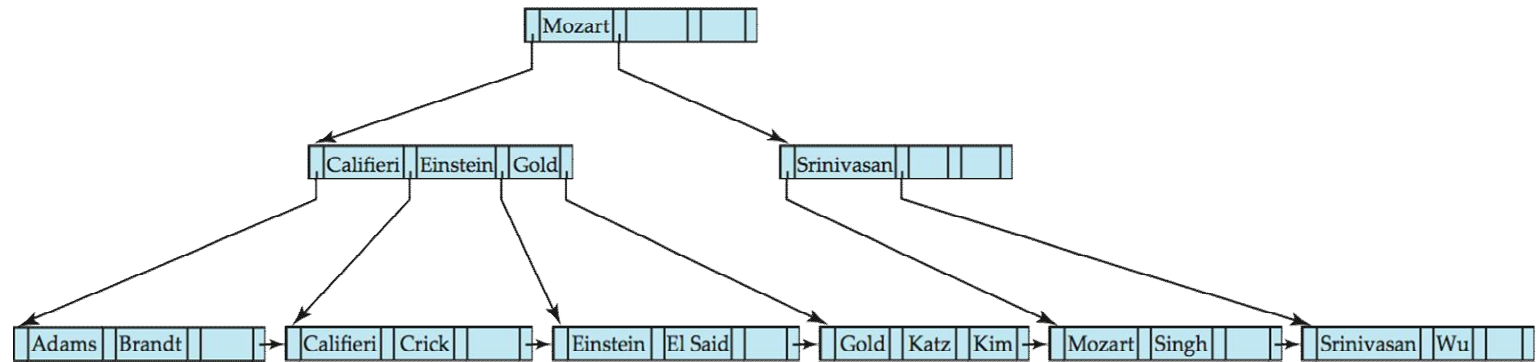
B⁺-Tree before and after insertion of "Lampport"

Insertion in B⁺-Trees (Cont.)

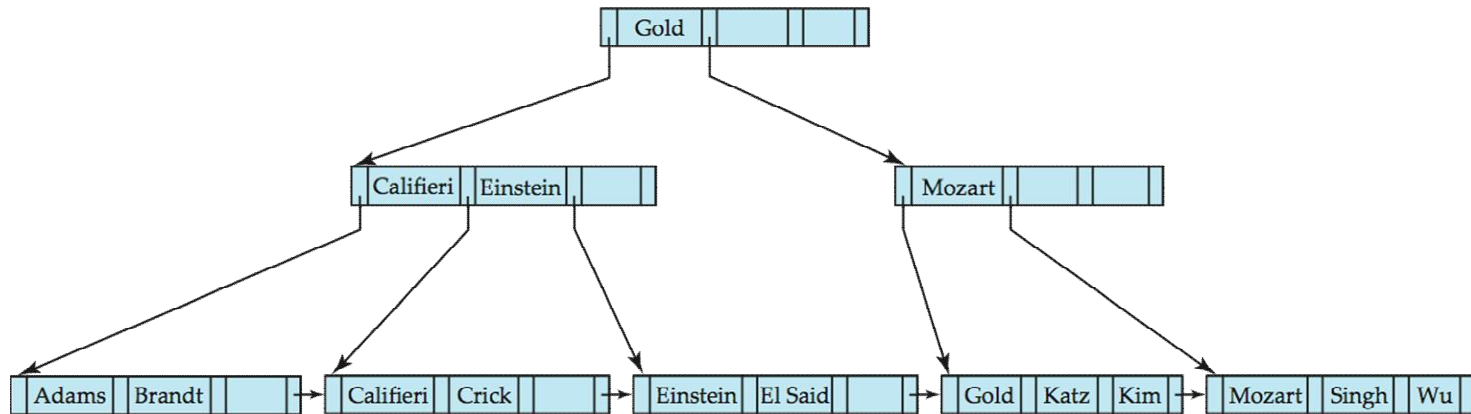
- Splitting a non-leaf node: when inserting (k,p) into an already full internal node N
 - Copy N to an in-memory area M with space for n+1 pointers and n keys
 - Insert (k,p) into M
 - Copy $P_1, K_1, \dots, K_{\lceil n/2 \rceil - 1}, P_{\lceil n/2 \rceil}$ from M back into node N
 - Copy $P_{\lceil n/2 \rceil + 1}, K_{\lceil n/2 \rceil + 1}, \dots, K_n, P_{n+1}$ from M into newly allocated node N'
 - Insert $(K_{\lceil n/2 \rceil}, N')$ into parent N
- **Read pseudocode in book!**



Examples of B⁺-Tree Deletion

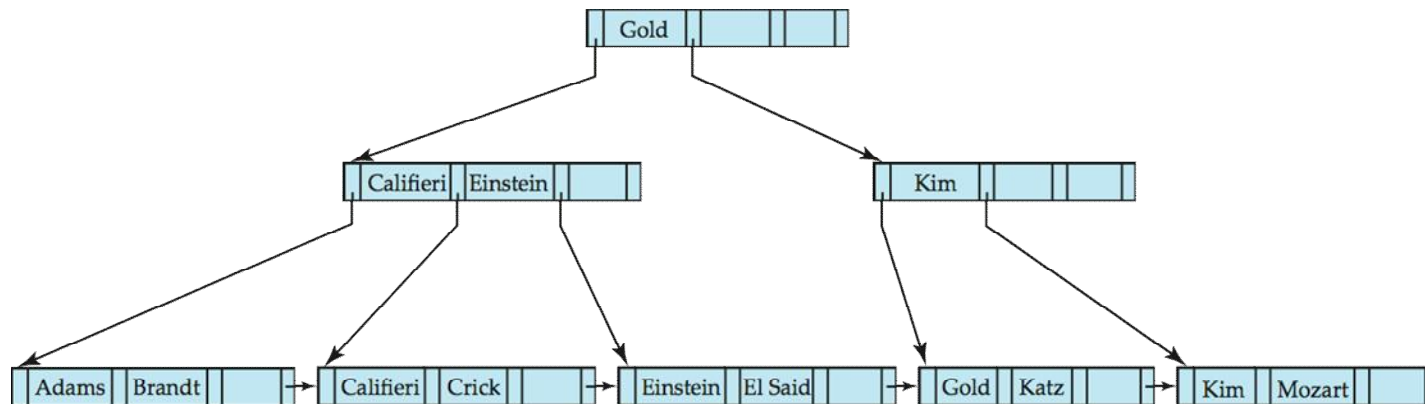


Before and after deleting “Srinivasan”



- Deleting “Srinivasan” causes merging of under-full leaves

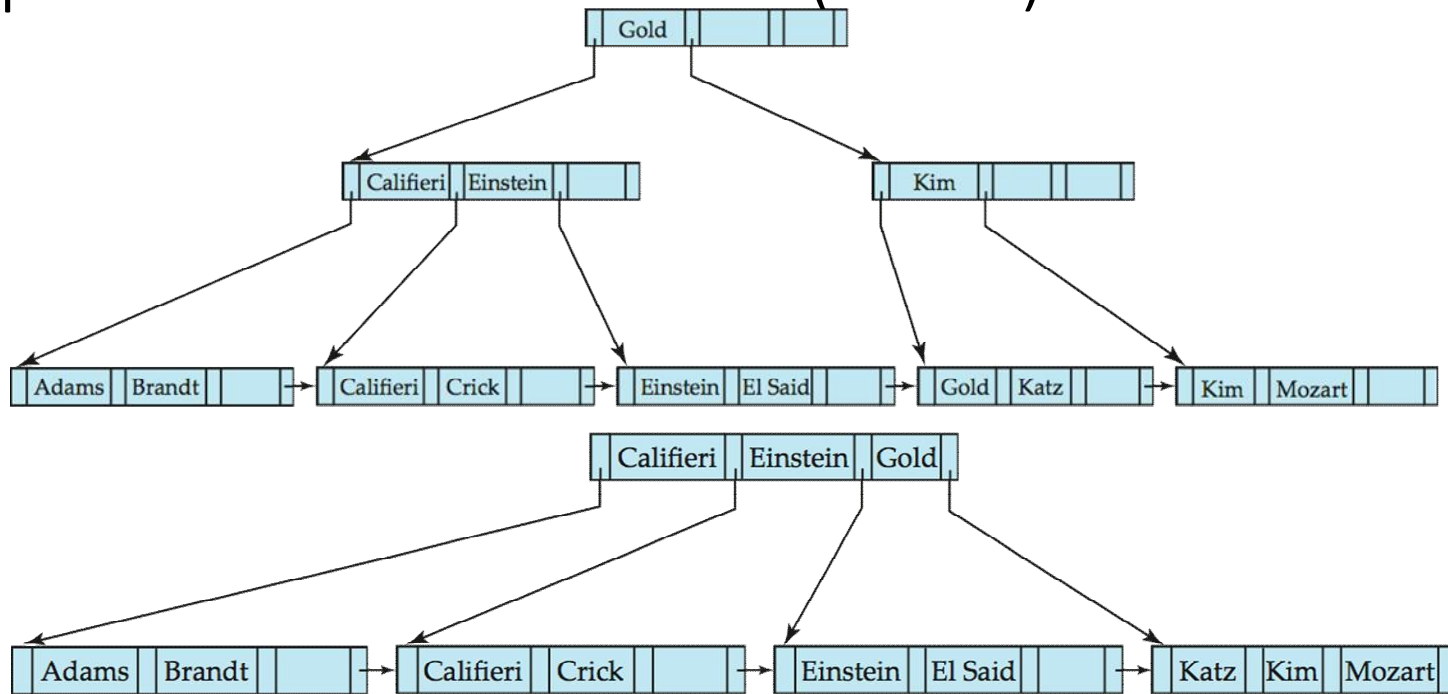
Examples of B⁺-Tree Deletion (Cont.)



Deletion of “Singh” and “Wu” from result of previous example

- Leaf containing Singh and Wu became underfull, and borrowed a value Kim from its left sibling
- Search-key value in the parent changes as a result

Example of B⁺-tree Deletion (Cont.)



Before and after deletion of “Gold” from earlier example

- Node with Gold and Katz became underfull, and was merged with its sibling
- Parent node becomes underfull, and is merged with its sibling
 - Value separating two nodes (at the parent) is pulled down when merging
- Root node then has only one child, and is deleted

Updates on B⁺-Trees: Deletion

- Find the record to be deleted, and remove it from the main file and from the bucket (if present)
- Remove (search-key value, pointer) from the leaf node if there is no bucket or if the bucket has become empty
- If the node has too few entries due to the removal, and the entries in the node and a sibling fit into a single node, then *merge siblings*:
 - Insert all the search-key values in the two nodes into a single node (the one on the left), and delete the other node.
 - Delete the pair (K_{i-1}, P_i) , where P_i is the pointer to the deleted node, from its parent, recursively using the above procedure.

Updates on B⁺-Trees: Deletion

- Otherwise, if the node has too few entries due to the removal, but the entries in the node and a sibling do not fit into a single node, then **redistribute pointers**:
 - Redistribute the pointers between the node and a sibling such that both have more than the minimum number of entries.
 - Update the corresponding search-key value in the parent of the node.
- The node deletions may cascade upwards till a node which has $\lceil n/2 \rceil$ or more pointers is found.
- If the root node has only one pointer after deletion, it is deleted and the sole child becomes the root.