

Semester 01:-

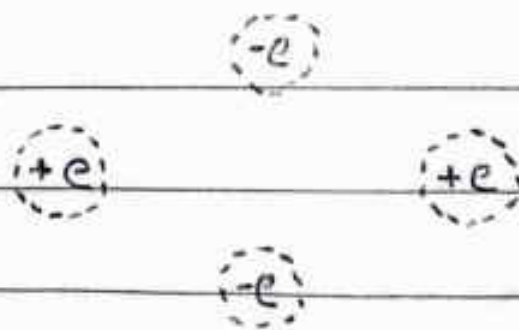
QNo18:-

Calculate Electric Potential due to quadrupole?

Answer:-

The two electric dipoles arranged in such a way that they almost cancel electric effects of each other at distant points is called Quadrupole.

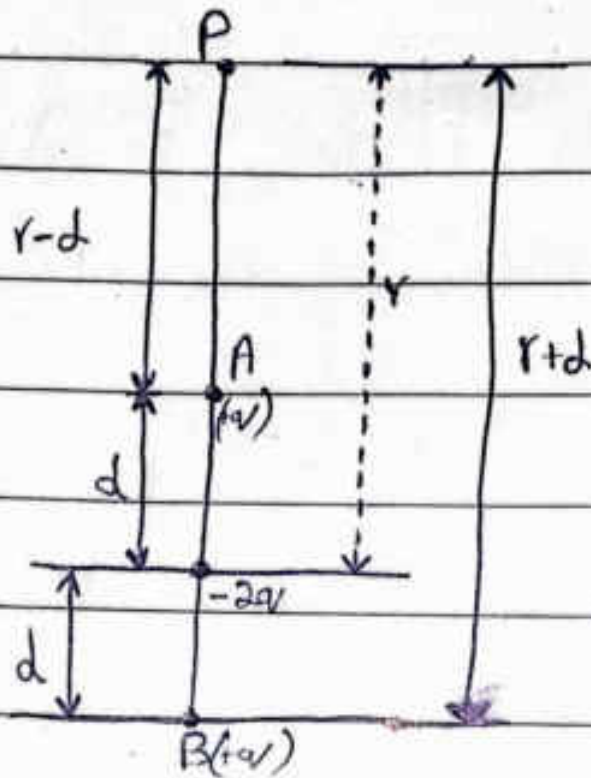
Diagrams:-



An elementary quadrupole can be represented as two dipoles oriented antiparallel. The most important uses of quadrupole is the characterization of nuclei.

Electric Potential due to Quadrupole:-

Diagram:-



Explanation:-

Consider two charges each of value $-q$ are placed at origin on x -axis.

Now place $+q$ charge at point A having distance ' d ' from ' $-2q$ '.

Similarly place an other charge $(+q)$ at point B having distance ' d ' from ' $-2q$ '.

Now take a point P on z-axis having distance 'r' from $-2q$ and (diameter) distance $(r+d)$ from $+q$ charges at B.

The electric potential at P due to $+q$ at A is:

$$V_1 = \frac{Kq}{r-d}$$

Similarly due to $+q$ at B:

$$V_2 = \frac{Kq}{r+d}$$

due to $-2q$ charge:

$$V_3 = \frac{K(-2q)}{r}$$

The total electric potential is:

$$V = V_1 + V_2 + V_3$$

$$V = \frac{Kq}{r-d} + \frac{Kq}{r+d} - \frac{2Kq}{r}$$

$$V = Kq \left(\frac{1}{r-d} + \frac{1}{r+d} - \frac{2}{r} \right)$$

$$V = Kq \left(\frac{r^2 + d^2 + r^2 - d^2 - 2(r^2 - d^2)}{r(r-d)(r+d)} \right)$$

$$V = Kq \left(\frac{\cancel{2r^2} - \cancel{2r^2} + 2d^2}{r(r^2 - d^2)} \right)$$

$$V = \frac{Kq(2d^2)}{r(r^2 - d^2)}$$

$$r(r^2 - d^2)$$

$$V = \frac{K(2qd^2)}{r^3 \left(1 - \frac{d^2}{r^2} \right)}$$

$$\left\{ \begin{array}{l} \because P = qd \\ Q = 2qd^2 \end{array} \right\}$$

$$V = \frac{KQ}{r^3} \left(1 - \frac{d^2}{r^2} \right)^{-1}$$

By Binomial :-

$$V = \frac{KQ}{r^3} \left(1 + (-1) \left(\frac{-d^2}{r^2} \right) + \dots \right)$$

The term $\left(\frac{-d^2}{r^2} \right) = 0$ because $r \gg d$

$$\boxed{V = \frac{KQ}{r^3}}$$

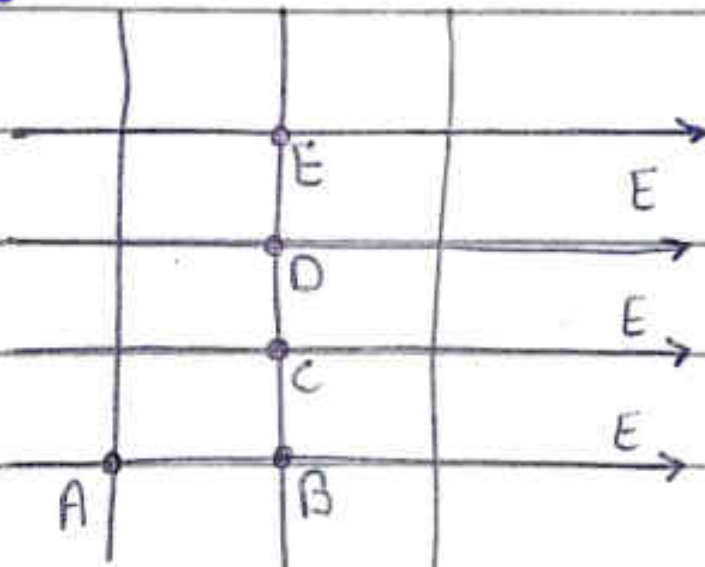
Topic:-

Equipotential Surfaces:-

The family of surfaces that connect points having same value of the electric potential are called equipotential surfaces.

Due to Uniform field:-

Diagram:-



Explanation:-

Consider uniform electric field indicated by horizontal electric lines of force. The perpendicular dashed lines are cross-section of equipotential surface.

Take two points having distance l .

$$\Delta V = - \int_a^b E \cdot ds$$

$$\Delta V = -EL$$

Potential difference b/w B and C:

Electric potential at B is $V_B = \frac{Kq}{r_B}$

Electric potential at C is $V_C = \frac{Kq}{r_C}$

$$\Delta V = V_B - V_C$$

$$V_B - V_C = \frac{Kq}{r_B} - \frac{Kq}{r_C} \quad \left\{ \because r_B = r_C \right\}$$

$$V_B - V_C = \frac{Kq}{r_B} - \frac{Kq}{r_B}$$

$$V_B - V_C = 0$$

$$\boxed{V_B = V_C}$$

Since $\Delta V = -\frac{W_{BC}}{q} = 0$, So $W_{BC} = 0$

Hence no work is done by electric field when q is moved from B to C.

(ii) Due to positive point charge:-

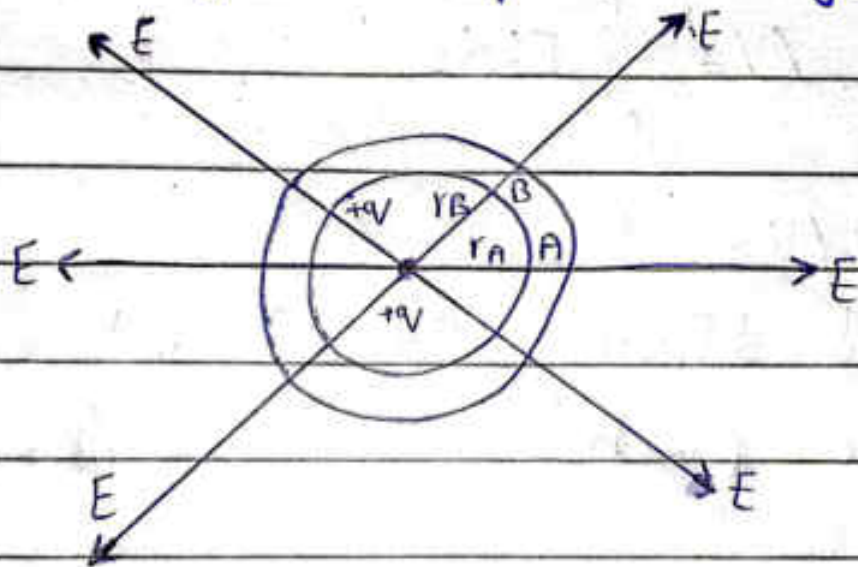


Diagram:-

In this way all the points on the line containing points A, B, C etc have same potential. The surface passing through these points are called equipotential surface.

Consider a $+q$ charge is placed at the center of sphere. The electric field is along ~~radius~~ direction.

Potential difference b/w A and B.

$$V_A - V_B = Kq \left(\frac{1}{r_A} - \frac{1}{r_B} \right)$$

when points A and B lies on the surface of same sphere $r_A = r_B$

In this case:-

$$V_A - V_B = Kq \left(\frac{1}{r_A} - \frac{1}{r_A} \right)$$

$$V_A - V_B = 0$$

$$\boxed{V_A = V_B}$$

It means all points at a given radius have the same potential.

Therefore, the equipotential surface of a given charge from a family of concentric sphere.

For a dipole, the equipotential surfaces are more complicated.